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- What's next? My research goals.

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- High-level idea:
  - Evaluate programs in compile-time, while making the most out of known inputs and definitions.
    - Definitions of used functions.
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    - When branching, propagate learned information through branches and make use of that information while compiling branches.

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- High-level idea: (contd)
  - Evaluate programs in compile-time, while making the most out of known inputs and definitions.
    - Most of the time the goal is to generate more efficient programs.
      - (but see Klyuchnikov and Romanenko [2010] for a different use of supercompilation)

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- This optimizes in the sense that: If we have a programs  $\mathcal{P}_1$  and  $\mathcal{P}_2$ , and  $\mathcal{P}_1 \Downarrow v$  in N steps and  $\mathcal{P}_2 \Downarrow v$  in M steps, we consider  $\mathcal{P}_2$  optimized if M < N.

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- An approximation. It's very unlikely that all of the rules have same costs.

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mapOfMap f g = (.) (map f) (map g)
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When we get stuck, we keep evaluating sub-expressions.

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h1 f g = (\f1 -> \f2 -> \a -> f1 (f2 a))

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\beta-reduction (twice):
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h7 f g a = case (case a of
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                    h1 : t1 -> g h1 : map g t1) of
                      -> []
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At this point we consider all branches, let's start with first one:

```
case [] of
  [] -> []
h0 : t0 -> f h0 : map f t0
```

Known case reduction evaluates this to it's final form, and we update our expression to:

```
h9 f g a = case a of

[] -> []

h1 : t1 -> case (g h1 : map g t1) of

[] -> []

h0 : t0 -> f h0 : map f t0
```

Since h0 and t0 are linear in the RHS of the second branch, we can just do substitution, without introducing lets:

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```
h10 f g a = case a of

[] -> []

h1 : t1 -> f (g h1) : map f (map g t1)
```

4 D > 4 P > 4 B > 4 B > B 9 9 P

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We can't do anything about this, all names are free. We consider the second sub-term.

map f (map g t1)

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■ No linearity restriction. (in the linear case they would do similar things – see Sørensen et al. [1994] for a comparison)

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Some of the important differences are:

- No linearity restriction. (in the linear case they would do similar things – see Sørensen et al. [1994] for a comparison)
- We do generalization. (not demonstrated here)

# Operations of a supercompiler - Driving

We evaluated the program, and while doing that we were careful with previously evaluated terms: Driving.

When we're stuck because the expression we do pattern matching on couldn't take any more steps, we evaluated branches:

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This is called splitting.

We need to "compare" current expression with our history of expressions, to prevent loops, and generate optimized functions.

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```

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Matching, returns all the necessary information to replace current expression with a function call to optimized function.

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reverse_acc (h : t) acc = reverse_acc t (h : acc)
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. . .
h5 1st =
  case 1st of
    [] -> []
    h1 : t1 ->
      case (reverse_acc t1 (h1 : [])) of
        [] -> []
        h0 : t0 -> reverse_acc t0 (h0 : [])
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h_ lst = ... reverse_acc t1 (h1 : []) ...
. . .
h_ lst = ... reverse_acc t2 (h2 : h1 : []) ...
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What to do after stopping like this is another story. (see Bolingbroke [2013])

Each one has tricky problems.

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- Example: (from Bolingbroke [2013])

```
let n = fib 100
    b = n + 1
    c = n + 2
in (b, c)
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let map = ...
    ys = map f zs
    xs = map g ys
in Just xs
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- Jonsson [201?] focuses on compilation performance, and reports <3 seconds for all the small programs from nofib.

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- Problems and current solutions are documented nicely.
- We don't have any solutions that work well on all programs.
- We don't have a usable implementation.

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# GHC Plugin API

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- No need to merge anything to GHC(in theory).
- But... GHC API feels like exposed internals rather than an API.

 No easy ways to do most basic stuff: Moving terms around(substitutions), known-case reduction, case-of-case, etc. (all done in some parts of Core-to-Core passes, need to reverse engineer)

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- No easy way to annotate Core syntax. Duplicating the syntax means duplicating huge amounts of code.
- Working on Core hard: Invariants are encoded as partial functions without any helpful error messages – if we're lucky, there's a NOTE.
- Some things are not clear. (Types are first-class, but can I use them wherever I want? The definition allows this)

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Ideally we need all the definitions in a module in it's .hi file.

Idea: Use -fexpose-all-unfoldings all the time, distribute base with this option.

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  - Work on some of the obvious improvements, like parallelizing the matcher.
  - I'm open for more ideas!

#### References I

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