

CREATING A UNIVERSAL INFORMATION LANGUAGE

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ABSTRACT. Welkin is a formalized programming language to store information. We introduce its use cases and rigorously define its syntax and semantics. From there, we introduce the bootstrap, making Welkin completely self-contained under a meta-theory based on combinators, equivalent to a provably minimal fragment of arithmetic.

CONTENTS

1. Introduction	1
2. Motivating Example	4
2.1. Scenario 1: Relating Distinct Representations	5
2.2. Scenario 2: Distinguishing Referants	5
3. Foundations	5
3.1. Words	5
3.2. Arithmetic	6
4. Syntax	6
4.1. Encoding	6
4.2. Strings	7
4.3. Grammar	7
4.4. Proof of LL(1) Membership	7
5. Semantics	8
5.1. ASTs	8
5.2. Representations	8
5.3. Truth Management	9
5.4. Universal Systems	9
6. Information Organization	10
6.1. Impossible Classes	10
6.2. Efficient Querying	11
7. Bootstrap	11
8. Conclusion	11
References	12

1. INTRODUCTION

Information Management (IM) is an open area of research as a result of the depth and breadth of disciplines. In terms of depth, many areas are often specialized, requiring an immense understanding of the broader concepts involved and nomenclature used. This specialization is evident in the sciences, as explored in [FG13], [CF14]. Additionally, in terms of breadth, creating common representations shared across sub-disciplines can be difficult. For example, mathematics has extremely diverse disciplines, and connecting these areas is an open problem in scalability [Car+21]. Moreover, creating a standardized form across communities is challenging. In other subjects, like the social sciences, there are no standard terms [Arc+06], and in the humanities, representing certain artifacts as data is involved [Har+20]. More broadly, IM *itself* is divided from distinct approaches that lack interoperability [AJ23]. Certain frameworks equate IM to Knowledge Management (KM) and assert that information

must be true [Edw22]. These problems, in both faithfully and broadly storing information, demonstrate the enormous task of effective IM.

In response to these challenges, several solutions have been proposed, but none have been fully successful. In the sciences, a group of researchers created the Findable Accessible Interoperable Resuable (FAIR) guidelines [Wil+16]. Instead of providing a concrete specification or implementation, FAIR provides best practices for storing scientific information. However, multiple papers have outlined problems with these overarching principles, including missing checks on data quality [Gui+25], missing expressiveness for ethics frameworks [Car+21], and severe ambiguities that affect implementations [Jac+20]. Along with the sciences, there are several projects for storing mathematical information (see [CF09] for more details). Older proposals, including the QED Manifesto [KR16] and the Module system for Mathematical Theories (MMT), aimed to be more general and have seen limited success. More centralized systems, like `mathlib` in the Lean proof assistant [The20], have seen adoption but do not give equal coverage nor are interoperable with other systems. Beyond more “hard” fields, IM in the humanities has few models, including an adaption of FAIR [Har+20] and discipline specific, linked databases in the PARNTHEOS project [Hed+19]. Each of these proposals, even within specific fields, fail to accommodate for all of the mentioned challenges.

In addition to domain specific proposals, there are approaches for general IM which still fail to resolve all issues. One prominent example is Burgin’s theory of information [Bur09] that comprehensively includes many separate areas for IM, including the complexity-based Algorithmic Information Theory (AIT), through a free parameter called an “infological system”, which encompasses domain specific terminology and concepts. In contrast to other approaches, Burgin’s generalized theory is flexible and enables greater coverage of different kinds of information [Mik23]. Despite this coverage Burgin does not closely tie the free parameter with his formal analysis of AIT, making it unclear how to use this in a practical implementation. Broad frameworks for IM, along with the specific proposals, have severe shortcomings, highlighting major obstacles for IM.

This thesis introduces a language to resolve these issues. I call this language **Welkin**, based on an old German word meaning cloud [Dic25]. The core result of this thesis is proving that Welkin satisfies three goals: is **universal**, **scalable**, and **standardized**. For details, see Table 1. The core idea is to generalize Burgin’s free parameter and enable arbitrary representations in the theory, controlled by a computable system. The notion of representation builds on Peirce’s semiotics, or the study of the relationship between a symbol, the object it represents, and the interpreter or interpretation that provides it that meaning [Atk23]. Moreover, to address queries on the validity of truth, we use a relative notion that includes a context managed by a formal system. Truth can then be determined on an individual basis, providing flexibility to any discipline. The focus then shifts to the usefulness of representations based on a topological notion of how “foldable” a structure is, which we call **coherency**. This approach is inspired by coherentism, a philosophical position that states truth is determined in comparison to other truths. [Bra23]. We incorporate ideas from coherentism to identify which representations identify their corresponding objects, and we define information as an invariant under these coherent representations. We include definitions on a *working* basis as what is most practical, not an epistemological stance that can be further

clarified in truth systems. Additionally, we keep the theory as simple as possible to make scalability and standardization straight-forward.

Goal 1	Universality	The language must enable any user created parameters, whose symbolic representation is accepted a computable function. Every computable function must be definable in the language.
Goal 2	Scalability	The database must appropriately scale to broad representations of information. Local queries must be efficient. Certificates must be available to prove cases where optimal representations have been achieved.
Goal 3	Standardization	The language needs a rigorous and formal specification. Moreover, the bootstrap must be formalized, as well as an abstract machine model. The grammar and bootstrap must be fixed to ensure complete forwards and backwards compatibility.

TABLE 1. Goals for the Welkin language.

This thesis is organized according to Table 2.

Section 2	Motivating Example	Introduces a high-level example, with geographic maps, to explain the core concept in Welkin.
Section 3	Foundations	Explains the meta-theory.
Section 4	Syntax	Provides the grammar and proof that it is unambiguous.
Section 5	Semantics	Explains how ASTs are validated and processed. Develops representations and coherency, and connects these to a working definition of information.
Section 6	Information Organization	Develops a Greedy algorithm to locally optimize information. Creates a certificate that demonstrates when a representation is optimal relative to the current information database.
Section 7	Bootstrap	Bootstraps the language.
Section 8	Conclusion	Concludes with possible applications, particularly in programming languages and broader academic knowledge management.

TABLE 2. Organization for the thesis.

2. MOTIVATING EXAMPLE

We illustrate Welkin with a motivating example: geographic maps.

Fix some landscape L . A map provides a representation to guide travelers in L , usually through coordinates and directions. Some common elements include landmarks, paths, and regions.

There are two major problems in creating “good” representations:

- 1) Between two representations, how can we tell they represent the same entity?
- 2) Given a representation that represents some referant, how can we distinguish from other possible referants?

In the context of maps, we can make these problems more concrete:

- 1) Consider two maps M, M' . How can we tell whether some landmark O in M represents the same entity as O' in M' ?
- 2) Consider a map M , and suppose there are landscapes L, L' . With the goal to have M represent L , how does M distinguish between L and L' ?

2.1. Scenario 1: Relating Distinct Representations.

2.2. Scenario 2: Distinguishing Referants.

This overarching example demonstrates how two sources communicate about some entity, or how a source's representation can distinguish between two entities.

3. FOUNDATIONS

To introduce our foundations, we need to ensure the language is *expressive* enough. As an information language, the core design is to mechanize the storage and retrieval of information, so we generally say that this must be processed as a computable function, which is a well established notion. Thus, at the very least, we must express all computable function; this is shown in Theorem 5.4.5.

However, we need more than computable functions: we seek *clarity* in concepts. We need to include meaning into the symbols, so we at least need representations. This encompasses partial computable functions as well by modelling non-termination as a unit, as well as Input/Output mechanisms.

Given these two components, managing information with computable functions and including representations, we argue that Welkin precisely captures anything *representable by a computable representation*. Practically, we impose defining things based on *restrictions*. As a justification, suppose we abstractly consider representing *anything*. The problem is, this is an open concept, and we may easily miss certain notions. We could also say there are *no* restrictions, but this, too, is similarly problematic. But the least *practical* restriction is precisely having representations accepted by a computable function. This provides a best of both worlds: the flexibility for any (reasonable) concept, and guarantees mechanically feasible operations on representations.

Now, a key component of this argument, as well as our truth management system, is proving *true* things about computable functions. We develop the machinery through Welkin's meta-theory. We keep this section self-contained with explicit alphabets and explicit recursive definitions. For simplicity, we will use the notation a_0, \dots, a_n for a finite list of items. We will revisit the notion "finite" more rigorously in Section 7.

TODO: Prove the claim for partial computable functions and IO!

3.1. Words.

Definition 3.1.0. The **alphabet of binary words** is $\mathcal{A}_{\text{bword}} ::= \text{bit} \mid . \mid w$, where $\text{bit} ::= 0 \mid 1$. A **binary word** is defined recursively: the symbols 0 or 1 are strings, or if w is a string, then so are $w.0$ and $w.1$. We set concatenation to be right-associative, i.e., $(w.w').w'' = w.(w'.w'')$, and safely abbreviate $w.w'$ as ww' . We write $w \in \text{bword}$ to denote that w is a binary word.

For simplicity, we extend the alphabet to include two common bases: decimal and hexadecimal.

Definition 3.1.1. The **alphabet of words** $\mathcal{A}_{\text{word}} ::= \mathcal{A}_{\text{bword}} + \mathcal{A}_{\text{dec}} + \mathcal{A}_{\text{hex}}$, where:

- $\mathcal{A}_{\text{dec}} ::= 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$
- $\mathcal{A}_{\text{hex}} ::= A \mid B \mid C \mid D \mid E \mid F$

A **word** is a concatenation of either only binary digits, only decimal digits, or hexadecimal digits. Each of these are denoted with different prefixes: decimal has none, binary uses $0b$, and hexadecimal uses $0x$.

Using binary words simplifies the bootstrap, so while these digits are included, they are *defined* in terms of binary words, see Section 7. Additionally, we will frequently use **bytes**, which are eight bits, or equivalently two hexadecimal digits.

3.2. Arithmetic.

4. SYNTAX

Now, the base encoding for Welkin is in US-ASCII, formally defined below.

4.1. Encoding.

Definition 4.1.0. US-ASCII consists of 256 symbols, listed in Table 3.

Dec.	Hex.	Glyph	Dec.	Hex.	Glyph	Dec.	Hex.	Glyph	Dec.	Hex.	Glyph
0	00	NUL	32	20	Space	64	40	@	96	60	`
1	01	SOH	33	21	!	65	41	A	97	61	a
2	02	STX	34	22	"	66	42	B	98	62	b
3	03	ETX	35	23	#	67	43	C	99	63	c
4	04	EOT	36	24	\$	68	44	D	100	64	d
5	05	ENQ	37	25	%	69	45	E	101	65	e
6	06	ACK	38	26	&	70	46	F	102	66	f
7	07	BEL	39	27	'	71	47	G	103	67	g
8	08	BS	40	28	(72	48	H	104	68	h
9	09	HT	41	29)	73	49	I	105	69	i
10	0A	LF	42	2A	*	74	4A	J	106	6A	j
11	0B	VT	43	2B	+	75	4B	K	107	6B	k
12	0C	FF	44	2C	,	76	4C	L	108	6C	l
13	0D	CR	45	2D	-	77	4D	M	109	6D	m
14	0E	SO	46	2E	.	78	4E	N	110	6E	n
15	0F	SI	47	2F	/	79	4F	O	111	6F	o
16	10	DLE	48	30	0	80	50	P	112	70	p
17	11	DC1	49	31	1	81	51	Q	113	71	q
18	12	DC2	50	32	2	82	52	R	114	72	r
19	13	DC3	51	33	3	83	53	S	115	73	s
20	14	DC4	52	34	4	84	54	T	116	74	t
21	15	NAK	53	35	5	85	55	U	117	75	u
22	16	SYN	54	36	6	86	56	V	118	76	v
23	17	ETB	55	37	7	87	57	W	119	77	w
24	18	CAN	56	38	8	88	58	X	120	78	x
25	19	EM	57	39	9	89	59	Y	121	79	y
26	1A	SUB	58	3A	:	90	5A	Z	122	7A	z
27	1B	ESC	59	3B	;	91	5B	[123	7B	{
28	1C	FS	60	3C	<	92	5C	\	124	7C	
29	1D	GS	61	3D	=	93	5D]	125	7D	}
30	1E	RS	62	3E	>	94	5E	^	126	7E	~
31	1F	US	63	3F	?	95	5F	_	127	7F	DEL

TABLE 3. US-ASCII codes and glyphs.

4.2. Strings.

We reserve the term **string** when a word is explicitly enclosed in delimiters, namely single or double quotes. The precise definition is involved, due to including quotes within a string, which are called “escaped quotes”. To detect escaped quotes, we use our fixed set of characters (see Table 3).

Definition 4.2.1. A **single-quoted string** is defined recursively.

The definition of double-quoted string is analogous.

4.3. Grammar.

Definition 4.3.2. Backus-Naur Form (BNF) consists of productions. Writing $r := a_1 \mid \dots \mid a_n$ is shorthand for the rules $r := a_1, \dots, r := a_n$. A **derivation** is a sequence of steps, recursively defined by starting with the empty derivation, and if d is a derivation and s is a step, then $d.s$ is a derivation. We write $\alpha \Rightarrow^* \beta$ if there is a derivation from α to β .

Now, we formalize an unambiguous form of EBNF for our use case.

Welkin’s grammar is displayed in Listing 1, inspired by a minimal, C-style syntax. Note that the empty string is not accepted, but is instead represented by the string `{}`.

```
start ::= (term ",")* term
term  ::= arc | graph | base
arc   ::= (term "-" term "->")+ term
       | (term "<-" term "-")+ term
       | (term "-" term "-")+ term
graph ::= unit? { term* }
base  ::= unit | string
unit  ::= int
```

TODO: Ensure this is actually LL(1)! Probably need to massage some productions.

LISTING 1. The grammar for Welkin, shown in BNF notation (see Definition 4.3.5). The terminals `int` and `string` are defined in Definition 3.1.2 and Definition 4.2.4, respectively

4.4. Proof of LL(1) Membership.

We now prove that the Welkin language is unambiguous by showing it is LL(1), a rich class of grammars that can be efficiently parsed. For more details, please consult [Aho+06].

Definition 4.4.3. Let G be a grammar.

Definition 4.4.4. A grammar is LL(1) if, given two distinct productions α, β :

-
-
- If $\beta \Rightarrow^* \epsilon \dots$

Theorem 4.4.5. Welkin’s grammar is LL(1). Hence, this grammar is unambiguous, i.e., every string accepted by the language has exactly one derivation.

Proof. Consider the corresponding LL(1) table...

□

5. SEMANTICS

This section describes how ASTs are processed and validated. We postpone information organization to Section 6.

5.1. ASTs.

- Semantics on ASTs
 - Terms: graphs
 - For ease of use, include a null node that is the root of the tree. This represents the module itself.

5.2. Representations.

Now we develop the formal framework to discuss information in terms of units, enabling a complete mechanization of Welkin’s meta-theory. To keep this section self-contained, we explicitly provide all recursive definitions.

Definition 5.2.0. The **alphabet of units** is $\mathcal{A}_{\text{unit}} = u \mid \mathcal{A}_{\text{word}}$. A **unit ID** is combination of symbols u_w , where $w \in \text{word}$.

Definition 5.2.1. A **free parameter** is a parameter given an associated ID. No further restrictions are imposed.

We now define representations recursively, using unit IDs and free parameters as the base case.

Definition 5.2.2. Units are recursively defined:

- **Base case:** IDs and free parameters are units.
- **Recursive step:**
 - **Parts::** if u_1, \dots, u_n are finitely many units, then so is their combination $\{u_1, \dots, u_n\}$. A combination defined without a provided ID is called an **anonymous unit**.
 - **Representations:** If u, w, v are units, so is $v \rightarrow u$. We say v **represents** u . or conversely, u is **represented by** v .

Key equalities:

- $u.\{\} = u$. Acts as a sort of $*$ operator from other languages.
 - To use one level up: $.u$
- $\left(u \xrightarrow{v} w\right) \in x \Leftrightarrow x(u) \xrightarrow{x(v)} x(w)$, where $x(u)$ is $x.u$ if $u \in x$ or u otherwise.

Example 5.2.3. Consider a house with a dog, a cat, and a person. We can represent the house as unit house, the dog as unit dog, the cat by unit cat, and the person by unit person. In our Welkin file, we add, `house { dog, cat, person }`. The person has an internal concept of pet and uses it to represent both the dog and cat, which we write as `person { animal --> dog, animal --> cat }`, under the scope of house.

Parts of units are denoted as $u.u'$. Scoping is included to provide namespaces. Moreover, parts enable **interpretations**. We write $u \xrightarrow{v} u'$ in case $u, v, (u \rightarrow v) \in u'$, so u represents v **via** u' . In this case, we say u' is a **context** to $u \rightarrow v$. Note that unlabeled representations can have multiple contexts.

Example 5.2.4. Consider the recursive definition of a binary tree: either it is a null (leaf) node, or it contains two nodes, left and right. We can model this as follows:

- First, create units for each of the notions: $\text{tree} \{ \text{null}, \text{left}, \text{right} \}$.
- Next, we write, $\text{tree} \{ \text{null} \rightarrow .\text{tree}, .\text{tree} \rightarrow \text{left}, .\text{tree} \rightarrow \text{right}, \{ .\text{left}, .\text{right} \} \rightarrow .\text{tree} \}$. Notice that we refer to the *namespace*, thereby enabling recursion. By our scoping rules, writing tree would be a *new* unit.
- To impose that the left subtree is *distinct* from the right one, we can use symbols.

An important idea in this example is that the abstraction could be defined *first*, or a concrete model could. For this reason, the choice of how entities are represented is flexible.

Definition 5.2.5. A unit u is **non-trivial** if it is non-empty and does not contain all relations. A unit u is **coherent relative to a context** u' if $u + u'$, the union of these units, is non-trivial.

Remark 5.2.6. This definition is a natural generalization of consistency in first-order logic. We will frequently rely on this result throughout the thesis.

Theorem 5.2.7. A representation is preserves information modulo \equiv iff the representation modulo \equiv is coherent.

Remark 5.2.8. This theorem enables truth management via specific contexts, specified as units. The task of finding core truths is then free, left open to flexibility accommodate for any truth management.

5.3. Truth Management.

Welkin manages truth through a flexible interface, grounded in the true properties on computable functions. The term “properties on computable functions” needs to be carefully defined. Do we only restrict this to a well established theory of arithmetic, like Peano Arithmetic, or permit larger notions, like infinite ordinals like ZFC?

...

Corollary 5.3.9. Any truth management system representable by computable functions can be represented in Welkin.

5.4. Universal Systems.

Inspired by [Mes12], we prove that scoping is strictly more expressive than without.

Lemma 5.4.10. Representations with interpretations are undefinable in terms of unlabeled representations.

Proof. It suffices to note that representing partial computable functions requires combinations. But every transformation under unlabeled representations does not preserve these conditions, hence, representations with interpretations are not definable. \square

Theorem 5.4.11. Any computable function and its trace under a given string can be represented by units. (TODO: make more precise.)

Proof. We prove there is a natural embedding from the lambda calculus into our meta-theory, using two parts:

- $\lambda x.f$ is represented as $\{x \rightarrow f\}$.

TODO: Come up with a term for “observations representable by computable

TODO: TODO: define the generalization to Padoa’s Method clearer.

- $f.g$ is represented as the combination of units, or $\{f, g\}$.

Thus, any λ -term can be represented in the meta-theory, completing the proof. \square

Note that there are multiple ways to prove Theorem 5.4.5, infinitely in fact. This motivates the following definition.

Definition 5.4.12. A universal representation system (URS) is a unit that can represent any representation.

Theorem 5.4.13. *A unit is a universal representation system if and only if it can represent any partial computable function. Moreover, any universal representation system can represent any universal representation system. In particular, representing itself is called **reflection**.*

TODO: Make this more precise and complete proof.

The term *universal* is specifically for expressing *representations* symbolically. The free parameter still needs to be included and is an additional feature on top of partial computable functions. However, the *management* of these symbols is done entirely with partial computable functions.

The next section discusses the issue of *managing* the infinitely many choices for URSs.

6. INFORMATION ORGANIZATION

- Main question: **which** universal system to choose? Is this practical?
 - What is a suitable criterion for a base theory?
 - Recall aim: want to mechanically store systems for a database
 - * What if possible performance degradation? Will we get stuck if we start with one architecture? Will we have to adjust later?
 - * Aim is to ensure architecture is completely flexible and can automatically adapt
 - * One key metric: ability to store as many systems coherently as possible, i.e., store as much information as possible
 - Main problem: Blum's speedup theorem
 - * Briefly generalize this for slate logic
 - * Show that no single way to completely organize systems based on a computable metric.
- This is part of the need for new search techniques!
- * Want to separate search from storage though, but we want to improve stored results **with** new results. This forms the idea behind the database architecture: have a simple way to store results that automatically gets better with new techniques/results.
 - * Need explicit proofs for this! Not sure how to store certificates...

6.1. Impossible Classes.

The reason to restrict our transformations is two-fold. First, we need to ensure we can *verify* them efficiently. Determining whether a morphism between two formal systems exist can be reduced to the Halting problem, and is therefore not practical for defining

an optimal formal system. Second, if we include those transformations that we *can* effectively check, no optimal formal system exists.

Theorem 6.1.0. *With respect to the class of all computable transformations that can be computably verified, there is no optimal formal system.*

6.2. Efficient Querying.

Instead of making proofs most efficient as is, we want to support finding optimal representations. But we want to do this from an efficiently queryable system, which is the most optimal.

7. BOOTSTRAP

- Provided in bootstrap.welkin file or similar. Main module is welkin, which needs to:
 - Provide slates, so inductive definition of binary strings + variables
 - Explain combinators
 - Explain the basics of universal systems. This is very important!
 - * Can elide proofs IF there is enough information content.
 - * TODO: figure out how proofs might work in this setting
 - Provides syntax and semantics of Welkin itself
- This thesis: will prove that the AST generated from this file is correct AND that it does, with a suitable interperation bootstrap itself.
- Explain how slates expand the envelope for implementations, BUT ensures that the final product, the syntax + semantics checkers and the information organization, can be externally seen!

8. CONCLUSION

- Review of thesis
 - Developed slate logic + bi-translation with FOL
 - Developed locally optimal organizational technique that can improve based on annotations/certificates
 - Introduced the language, with a straightforward graph syntax and semantics
 - Builds upon the last section
 - Bootstrapped standard + used coherency condition
- Significance
 - Backwards AND forwards compatbile standard that bootstraps itself. Easy for implementations!
 - Applications to any human subject
 - * Sciences
 - * Liberal arts
 - * Economics
 - * Etc.
- Future work
 - Programming language semantics + synthesis

- * Incorporate broader aspects + intent of users! ESSENTIAL for new programming languages to be able to discuss pragmatics in some way!
- * Also reproducible AND executable specifications, though creating an engine to execute these is far beyond the scope of the thesis
- Organizing large corpuses of human text
- Numerous applications to AI and improving results
 - * Emphasize role of symbol grounding problem in AI

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