

**Meeting August 26, 2024**  
**Forward and inverse modeling of wave propagation**  
**combining classical and machine learning approaches**

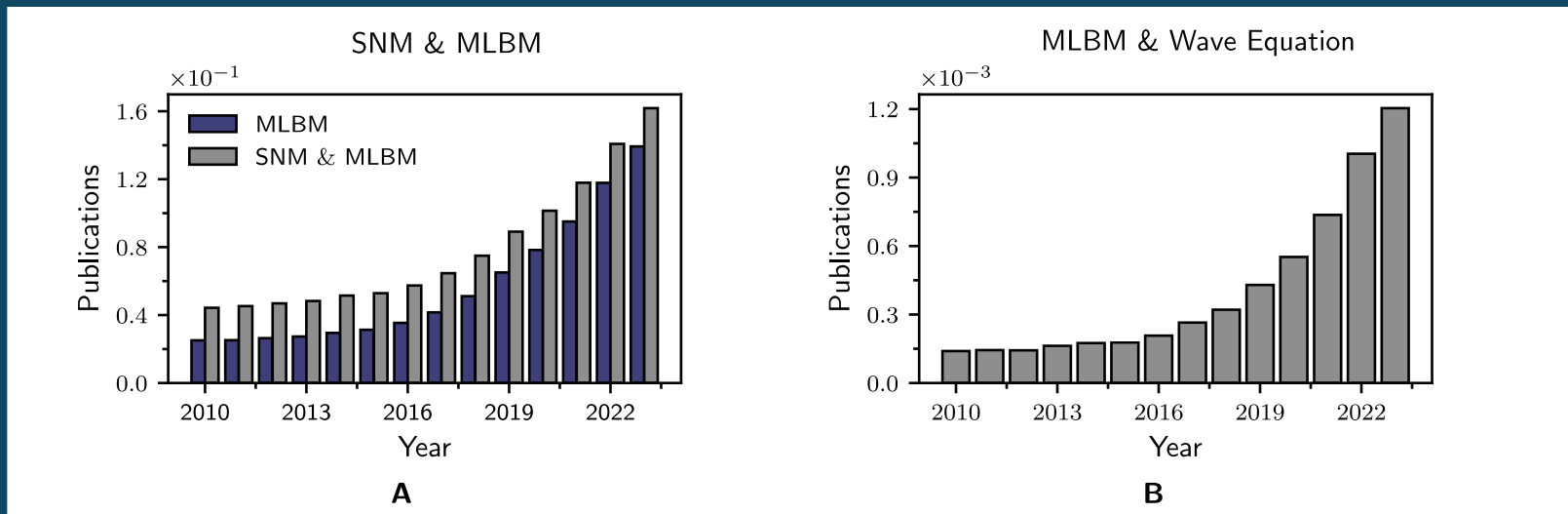
**Student:** Oscar Andrés Rincón Cardéño  
**Advisors:** Nicolas Guarín Zapata and Silvana Montoya

Applied Mechanics research group  
Universidad EAFIT



# Introduction

The growth of literature related to machine learning and wave propagation modeling is shown.



Machine learning-based methods (MLBM) and standard numerical methods (SNM) (A), as well as MLBM specifically associated with wave propagation modeling (B).

## Possible causes

- Hardware
  - GPU
  - Storage
- Available data
- Open-source packages
  - Tensorflow
  - PyTorch
  - JAX

# Research Question

What machine learning techniques have been applied to model the wave equation in computational seismology?

Forward Problem

Inverse problem

Surrogate models



MLBM & SNM

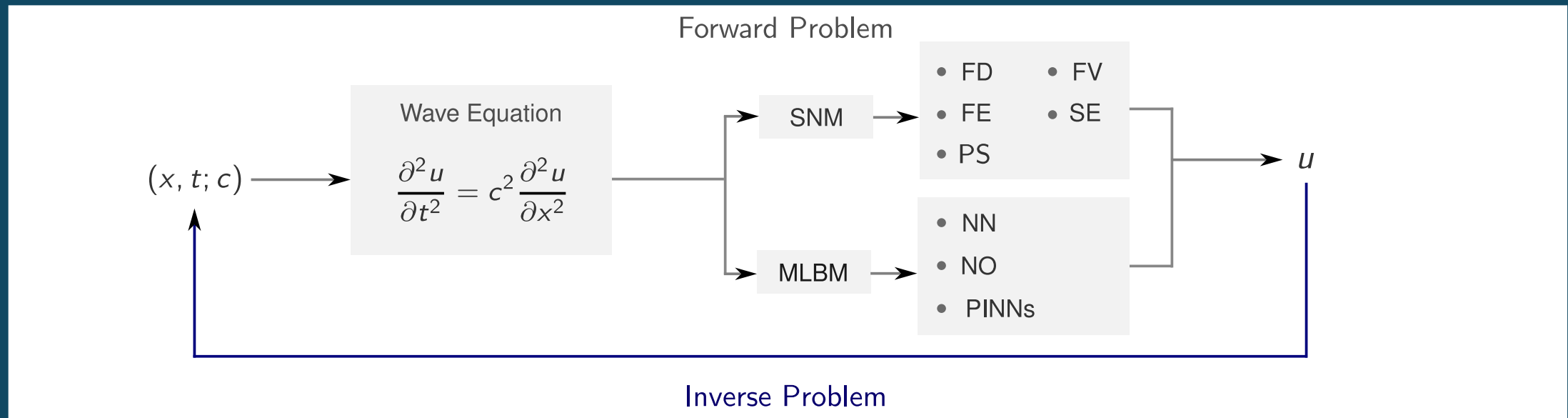
# Justification

**In principle, machine learning can offer a promising balance between computational cost and accuracy.**

## **Given the rapid growth of the field:**

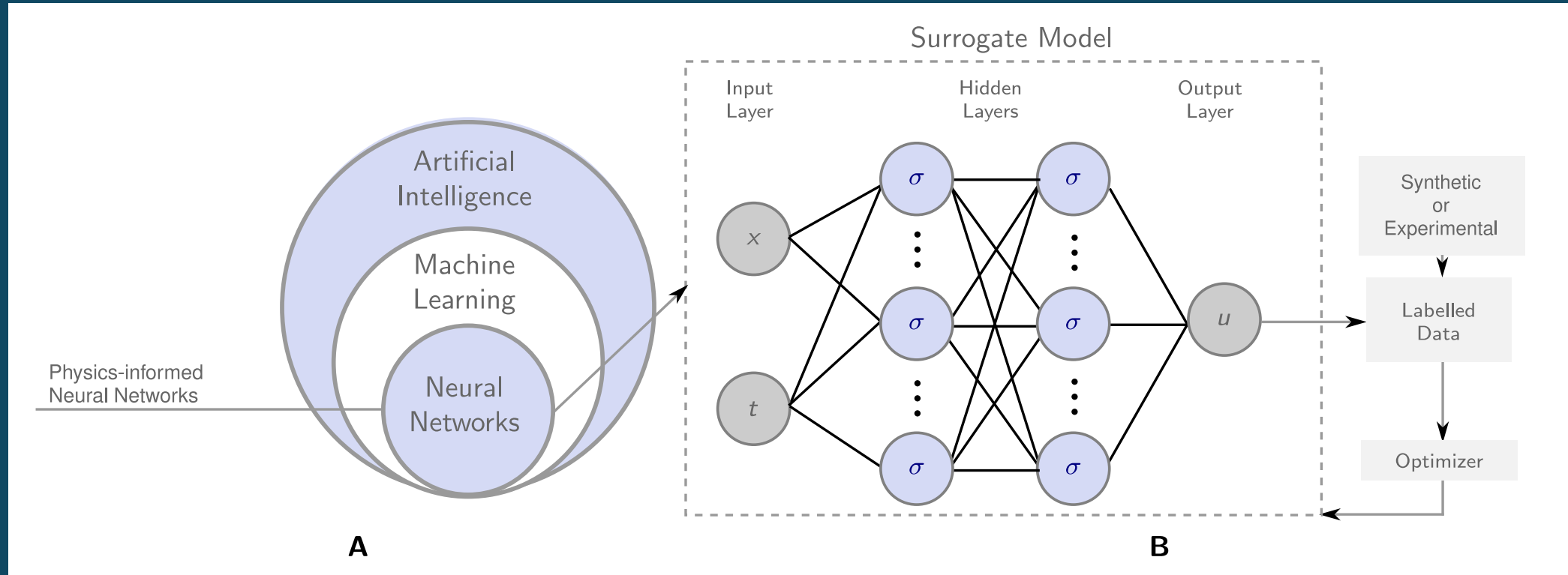
1. Uncertainty about what machine learning based methods have been applied and demonstrated to be an efficient complement or alternative to standard numerical methods.
2. Already proposed methods may still haven't been fully explored in the context of seismic wave propagation modeling.

# Modeling of Wave Propagation



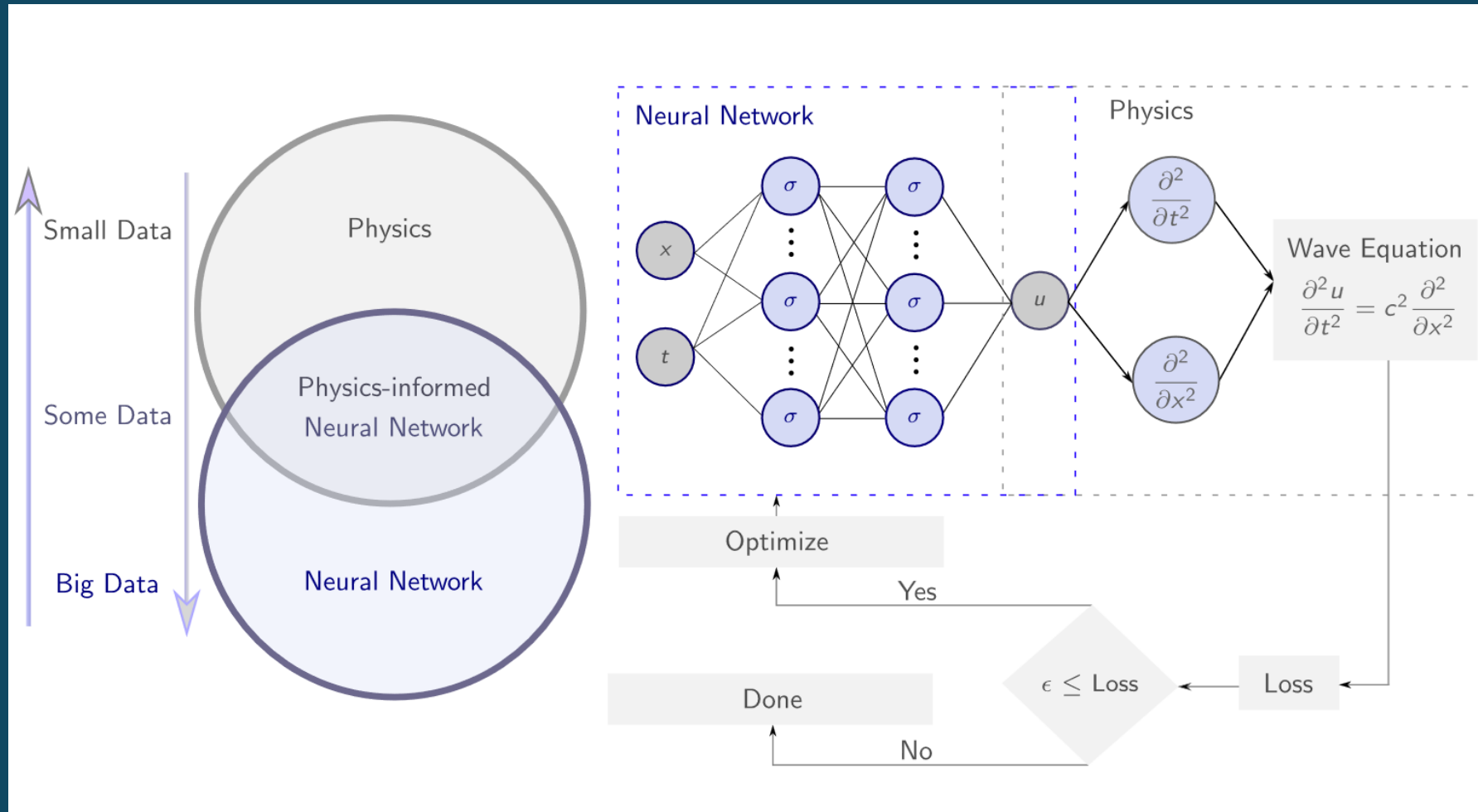
Scheme of the forward and inverse problems encountered in solving partial differential equations. In the forward scenario, the inputs  $(x, t; c)$  are employed to characterize a model across PDEs.

# Machine learning Based Methods



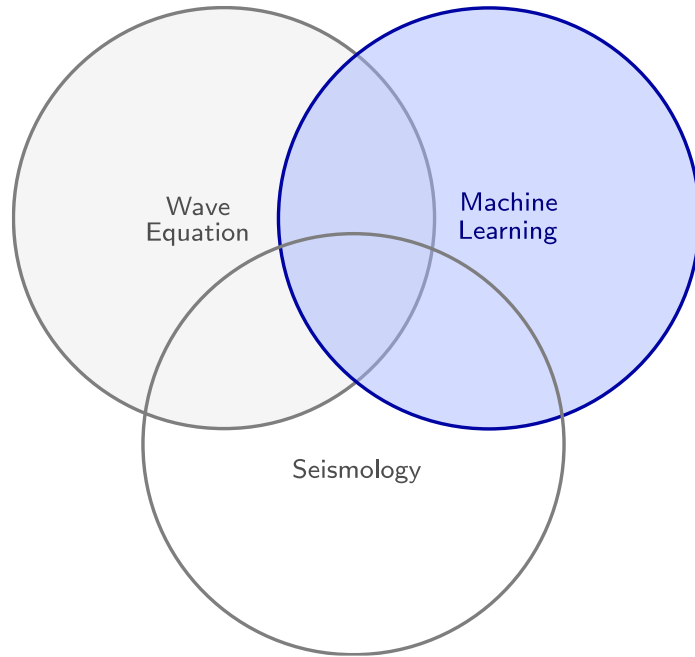
Artificial Intelligence subsets and artificial neural networks. (A) Deep learning as a subset of machine learning and artificial intelligence and (B) basic architecture of artificial neural networks.

# Machine learning Based Methods



Physics-informed neural networks scheme applied to the wave equation.

# Applications



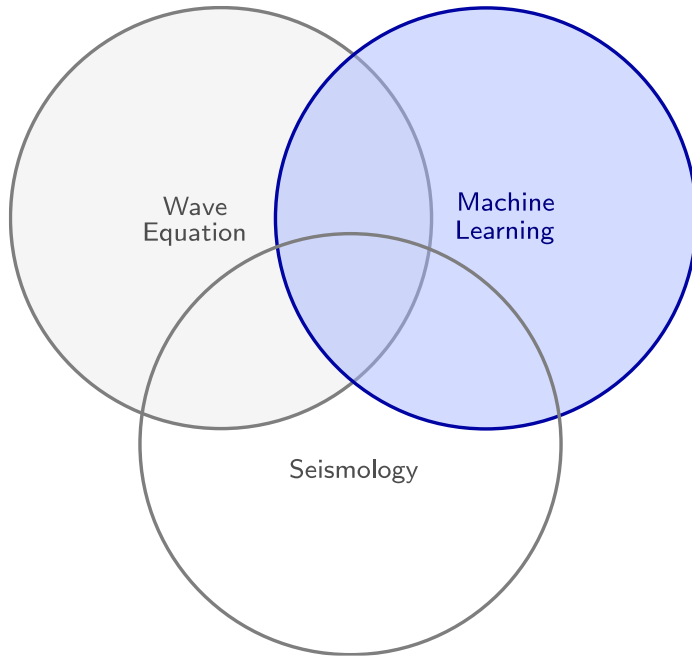
## Inclusion criteria

### We considered studies that:

- Machine learning methods applied to computational seismology.
- Incorporate descriptions of physical phenomena through partial differential equations.
- Reported a quantitative or supported qualitative comparison of the implemented model's computational efficiency relative to standard numerical methods.
- Are applied to solve inverse problems.



# Applications



## Exclusion criteria

### We not considered studies that:

- Did not provide a comparison at all.
- Compared their results only to other machine learning methods.
- Focused on accuracy comparisons without addressing computational times were also excluded.
- Are outside the scope of computational seismology.

## Query

("machine learning" OR "deep learning" OR "neural networks") AND ("seismic" OR "seismology") AND "wave equation" AND (modeling OR modelling OR model OR simulation)

## Search strategy

