Simulates vs Real World Data

```
library(dplyr)
library(broom)
library(ggplot2)
library(patchwork)
library(sandwich)
library(lmtest)
```

1. Simulated Data

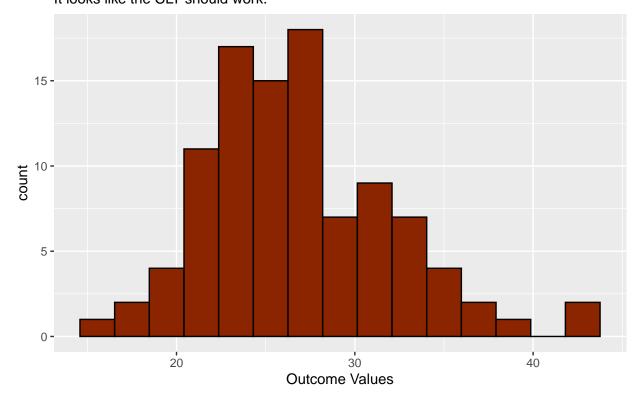
For this question, we are going to create data, and then estimate models on this simulated data. This allows us to effectively know the population parameters that we are trying to estimate. Consequently, we can reason about how well our models are doing.

d <- create_homoskedastic_data(n=100)</pre>

1. Data Exploration

```
outcome_histogram <- d %>%
  ggplot() + # fill in the rest of this chunk to create a plot
  aes(x = y) +
  geom_histogram(bins = 15, fill = "orangered4", color = "black") +
  labs(
    x = "Outcome Values",
    title = "Histogram of Outcomes",
    subtitle = "It looks like the CLT should work."
  )
  outcome_histogram
```

Histogram of Outcomes It looks like the CLT should work.



This distribution looks reasonably well behaved. Because we have more than 30 data points, I think that the CLT should work, and this data will satisfy the assumptions necessary for the large-sample model to produce consistent estimates.

The only two OLS assumptions are (i) iid data which is satisfied by problem setup; and (ii) reasonably well-behaved data so that the CLT works. These are both met in this data. 1. Estimate two models, called $model_1$ and $model_2$ that have the following form (The only difference is that the second model has squared x3):

$$Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \epsilon \tag{1}$$

$$Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3^2 + \epsilon \tag{2}$$

```
model_1 <- lm(y ~ x1 + x2 + x3, data = d)
model_2 <- lm(y ~ x1 + x2 + I(x3^2), data = d)

calculate_msr <- function(model) {
    # This function takes a model, and uses the `resid` function
    # together with the definition of the mse to produce
    # the MEAN of the squared errors.

msr <- mean(resid(model)^2)

return(msr)
}
calculate_msr(model_1)</pre>
```

[1] 2.611361

```
calculate_msr(model_2)
```

[1] 0.9054898

The second model is doing a better job, the model that has the correctly specified x_3^2 term is fitting better. It has a lower MSE.

```
# ?broom::augment # if you would like to view the documentation
d_model_1 <- augment(model_1)
d_model_2 <- augment(model_2)

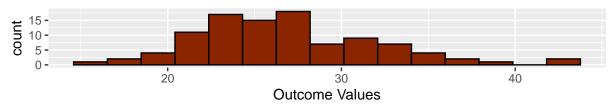
model_1_residuals_histogram <- d_model_1 %>%
    ggplot() +
    aes(x = .resid) +
    geom_histogram(bins = 20, fill = "chartreuse3", color = "black") +
    labs(title = 'Model 1 Residuals')

model_2_residuals_histogram <- d_model_2 %>%
    ggplot() +
    aes(x = .fitted - y) +
    geom_histogram(bins = 20, fill = "lightblue2", color = "black") +
    labs(title = 'Model 2 Residuals')
outcome_histogram /
    model_1_residuals_histogram /
```

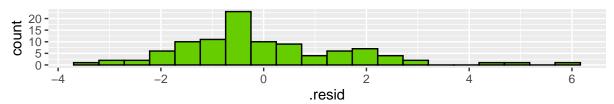
Histogram of Outcomes

model_2_residuals_histogram

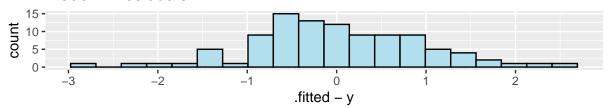
It looks like the CLT should work.



Model 1 Residuals



Model 2 Residuals



One thing that I notice right away is that both of the models have much smaller variance in the residuals than in the outcome overall. This is good! It means that the model is working to predict outcomes. The other thing that I notice is that the residuals seem to be centered at zero, while the outcome is not. This is a guarantee that comes from Theorem 4.1.5, and something that I

was hoping to see in this data.

Finally, I notice that when I compare Model 2 residudls to Model 1 residuals, there seems to be lower variance/dispersion in the Model 2 residuals. We saw this above, when we calculated the MSE for the two models, but this is anothe way to see this result: Although we have a guarantee that each of these etimates are the BLP given a certain set of data, the model that more closely matches the underlying form of the data will be able to predict with smaller residuals.

Beause the question asked: Mean of Y: 26.8076811 Mean of Model 1 residuals: $-5.7021556 \times 10^{-15}$ Mean of Model 2 residuals: $7.5850251 \times 10^{-15}$

2. Real-World Data

"Can timely reminders *nudge* people toward increased savings?" Dean Karlan, Margaret McConnell, Sendhil Mullainathan, and Jonathan Zinnman published a paper in 2016 examining just this question. In this research, the authors recruited people living in Peru, Bolivia, and the Philippines to be a part of an experiment. Among those recruited, a randomly selected subset were sent SMS messages while others were not sent these messages. The authors compare savings rates between these two groups using OLS regressions.

A. Read the data

Read in the data using the following code.

```
d <- haven::read_dta(file = 'analysis_dataallcountries.dta')
glimpse(d)</pre>
```

```
## Rows: 13,560
## Columns: 62
## $ motivo
                            <chr> "COMPRA DE TERRENO", "OTROS", "EMERGENCIA~
                            ## $ depart
## $ quant saved
                            <dbl> 13.09080, 39.27240, 294.54300, 58.90860, ~
## $ age
                            <dbl> 28, 0, 0, 0, 0, 43, 52, 52, 34, 46, 0, 26~
## $ saved_formal
                            <dbl> 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 1,~
## $ incentive
                            ## $ female
                            <dbl> 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 0, 1, 1, 1,~
## $ married
                            <dbl> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1,~
## $ highschool_completed
                            <dbl> 0, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, -
## $ reached_b4goal
                            <dbl> 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 1, -
## $ bolivia
                            ## $ rem_any
                            <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1,~
## $ provincia
                            <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 0,~
## $ wealthy
                            <dbl> 0, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, ~
## $ puzzle_ica
                            <dbl> 0, 0, 0, 0, 1, 1, 1, 0, 0, 1, 1, 1, 0, 0,~
## $ foto
                            <dbl> 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, ~
                            <dbl> 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, ~
## $ rem_motive
## $ peru
                            <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 0,~
## $ branch
                            <dbl> 0, 0, 0, 0, 0, 0, 0, 0, 3, 0, 0, 0, 3,~
## $ marketer
                            <dbl> 0, 0, 0, 0, 0, 0, 0, 0, 3, 0, 0, 0, 0, 2,~
## $ joint
                            <dbl> 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, ~
## $ joint_single
                            ## $ dc
                            <dbl> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1,~
## $ highint
## $ rewardint
                            ## $ missing_inc
                            <dbl> NA, NA, NA, NA, NA, NA, NA, NA, O, NA, NA~
## $ inc_7d
                            <dbl> 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, ~
```

```
## $ hyperbolic
                        ## $ missing_savamt
                        <dbl> NA, NA, NA, NA, NA, NA, NA, NA, O, NA, NA~
## $ missing havesaved
                        <dbl> NA, NA, NA, NA, NA, NA, NA, NA, O, NA, NA~
                        ## $ missing_savedwhere
## $ missing_savwhynot
                        <dbl> NA, NA, NA, NA, NA, NA, NA, NA, NA, NA~
                        <dbl> NA, NA, NA, NA, NA, NA, NA, NA, O, NA, NA~
## $ missing satisfied
                        <dbl> NA, NA, NA, NA, NA, NA, NA, NA, O, NA, NA~
## $ missing satisfy
                        <dbl> NA, NA, NA, NA, NA, NA, NA, NA, O, NA, NA~
## $ missing_regretspend
## $ saved asmuch
                        <dbl> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, ~
## $ spent_b4isaved
                        <dbl> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, ~
## $ philippines
                        <dbl> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1,~
                        <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 3, 1, 1, 1, 1, 3,~
## $ country
## $ late_rem_any
                        <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 0, 0, 1,~
                        <dbl> 2.645522, 3.695666, 5.688814, 4.092820, 4~
## $ log_quant_saved
                        <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0,~
## $ rem_any_peru
## $ rem_any_phil
                        <dbl> 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 1,~
                        ## $ rem_any_boli
## $ missing female
                        <dbl> 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 1, 0, 1, 0,~
## $ missing_age
## $ missing_married
                        ## $ missing saved formal
                        ## $ missing_inc_7d
                        ## $ missing wealthy
## $ missing_hyperbolic
                        ## $ missing_saved_asmuch
## $ missing_spent_b4isaved
                        ## $ missing_number_account
                        ## $ ivhquant_saved
                        <dbl> 3.266513, 4.363831, 6.378575, 4.769207, 5~
## $ logalt_quant_saved
                        <dbl> 2.572673, 3.670777, 5.685459, 4.076157, 4~
## $ gain_rem
                        <dbl> 0, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1,~
## $ loss_rem
                        <dbl> 1, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, ~
## $ noincentive
                        <dbl> 1, 0, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, ~
## $ rem_no_motive
## $ masterid
                        <dbl> 1246, 2229, 1490, 943, 1922, 1931, 212, 2~
```

B. F-test

One of the requirements of a data science experiment is that treatment be randomly assigned to experimental units. One method of assessing whether treatment was randomly assigned is to try and predict the treatment assignment. Here's the intuition: because treatment was assigned at random, it should not be possible to predict something random with other data.

The specifics of the testing method utilize an F-test. Here is how:

- First estimates a model that regresses treatment using only a regression intercept, $Y \sim \beta_0 + \epsilon_{short}$. In lm(), you can estimate this by writing lm(outcome_variable ~ 1), where outcome_variable is the outcome that you're actually testing.
- Then estimates a model that regresses treatment using all data available on hand, $Y \sim \beta_0 + \beta_1 x_1 + \cdots + \beta_k x_k + \epsilon_{long}$.

To test whether the long model has explained more of the variance in Y than the short model, we conduct an F-test for the long- vs. short-models.

The null hypothesis is that there is no difference in the residual sum of squares between the two models. That is, the longmodel with the additional estimates will not perform any better than

the short model where these estimates are restricted to be zero.

If the p-value for an F-test were to be lower than 0.05, I would reject the null hypothesis.

- c. Using variables that indicate:
- d. sex (as noted in the codebook);
- ii. age:

##

- iii. high school completion;
- iv. wealth:
- v. marriage status;
- vi. previous formal savings (saved_formal, which isn't in the codebook);
- vii. weekly income;
- viii. meeting savings goals (saved_asmuch)
- ix. and, spend before saving

F-test to evaluate whether there is evidence to call into question whether respondents in the *Philippines* were randomly assigned to receive any reminder (rem_any). To do so we filter/subset the data to include only individuals who live in the Philippines, and then estimate a long- and a short- model.

```
short_model <- lm(rem_any ~ 1, data = d[d$country == 3,])</pre>
long_model <- lm(rem_any ~ female + age + highschool_completed + wealthy +</pre>
                   married + saved_formal + inc_7d + saved_asmuch +
                   spent_b4isaved, data = d[d$country == 3,])
anova(long_model, short_model, test = 'F')
## Analysis of Variance Table
##
## Model 1: rem any ~ female + age + highschool completed + wealthy + married +
       saved_formal + inc_7d + saved_asmuch + spent_b4isaved
```

Model 2: rem_any ~ 1 Res.Df RSS Df Sum of Sq F Pr(>F) 1399 204.95 ## 1 ## 2 1408 206.93 -9 -1.9763 1.4989 0.1429

I fail to reject the null hypothesis because the p-value for this test is larger than the criteria I set set for rejecting.

At stake was whether the randomization was conducted correctly. Because I fail to reject the null hypothesis for this F-test, I ultimately conclude that there is no evidence that this randomization was performed incorrectly. Notice, that this doesn't necessarily mean that it was conducted correctly, just that there isn't any evidence that it was done improperly.

C. Reproduce OLS regression estimates

First, we reproduce the OLS regression estimates

In Section 3.1 of the included paper, the authors describe the OLS model that they estimate:

$$Y_i = \alpha + \beta R_i + \gamma Z_i + \epsilon_i$$

For the upper right panel that you are estimating, the outcome, Y_i is a binary indicator for whether the individual met their savings goal.

The indicator R_i is a binary indicator for whether the individual was assigned to receive a reminder. And, Z_i are additional features: a categorical variable for the country, and a binary indicator for whether the individual was recruited by a marketer. In the model labeled (3) only Y, R and Z are used in the regression. In the model labeled (4) these variables are used, but so too are the other variables that you previously used in the F-test.

One of the difficulties of this data is that the outcome is a binary indicator for whether the individual met (or did not meet) their commitments. At first blush, this doesn't seem like it meets the requirements of the large-sample model – after all, a bernoulli RV is *certainly* not normally distributed. But, in the large sample there is actually no requirement that the data be normally distributed. Only, that it is sampled iid and that the CLT might work. > In section 2 of this paper the authors note that individuals were recruited via door-to-door canvassing in the Phillippines; in Peru individuals were recruited via TV and radio ads; and in Bolivia the product was again marketed on TV and radio ads.

And so, we have a rather careful statment that we have to make about this data. On the one hand, the people who are influenced by this marketing, and thereby come to the bank, are probabilty not either (a) independent – they might come with family members or friends, or see the ads at a bar; and (b) nor identically distributed to the rest of the population who do not come to the bank to sign up.

However, because of the random assignment into treatment conditions we have an iid sample, within a subset of the population. Namely, within the population who come to the bank to sign up for a savings product. b. The authors have concluded that they can conduct these regressions.

```
model_pooled_no_covariates <- lm(</pre>
  reached_b4goal ~ rem_any + highint + rewardint + joint +
   dc + joint_single + factor(country),
  data = d
model_pooled_with_covariates <- lm(</pre>
  reached_b4goal ~ rem_any + highint + rewardint + joint +
    dc + joint single +
   female + age + highschool_completed + wealthy + married +
    saved_formal + inc_7d + saved_asmuch + spent_b4isaved +
   missing_female + missing_age + missing_highschool_completed +
   missing married + missing saved asmuch + missing spent b4isaved +
   factor(depart) + factor(provincia) + factor(marketer) + factor(branch) +
    factor(country),
  data = d
stargazer::stargazer(
  model_pooled_with_covariates, model_pooled_no_covariates,
  omit = c('depart', 'provincia', 'marketer', 'branch', 'country'),
  omit.labels = c(
    'Department Fixed Effects', 'Province Fixed Effects',
    'Marketer Fixed Effects', 'Branch Fixed Effects',
    'Country Fixed Effects'),
  single.row = TRUE,
  type = 'latex')
```

% Table created by stargazer v.5.2.2 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu % Date and time: Thu, Jan 13, 2022 - 16:53:53

```
calculate_msr(model_pooled_no_covariates)
```

```
## [1] 0.2305645
calculate_msr(model_pooled_with_covariates)
## [1] 0.219986
```

Table 1:

	(1)	(2)
rem_any	$0.032^{***} (0.009)$	$0.032^{***} (0.009)$
highint	$-0.010 \ (0.031)$	$-0.002 \ (0.031)$
rewardint	$0.044 \ (0.031)$	$0.046 \; (0.032)$
joint	0.0005 (0.031)	$0.004 \ (0.032)$
dc	$0.011 \ (0.029)$	$0.012\ (0.030)$
joint_single	-0.038(0.030)	-0.035 (0.031)
female	0.016*(0.009)	
age	$0.002^{***} (0.0004)$	
highschool_completed	-0.038***(0.010)	
wealthy	-0.033*(0.017)	
married	$0.018 \ (0.013)$	
saved_formal	-0.026**(0.012)	
inc_7d	$0.0001 \ (0.0002)$	
saved asmuch	-0.030(0.037)	
spent b4isaved	-0.0001(0.034)	
missing_female	$0.004 \ (0.145)$	
missing_age	$0.099^{**}(0.039)$	
missing highschool completed	-0.109(0.480)	
missing_married	$0.038\ (0.131)^{'}$	
missing_saved_asmuch	-0.084(0.083)	
missing_spent_b4isaved	,	
Constant	$0.250^{***} (0.088)$	$0.663^{***} (0.012)$
Department Fixed Effects	Yes	No
Province Fixed Effects	Yes	No
Marketer Fixed Effects	Yes	No
Branch Fixed Effects	Yes	No
Country Fixed Effects	Yes	Yes
Observations	13,560	13,560
R^2	0.110	0.067
Adjusted R^2	0.106	0.067
Residual Std. Error	0.470 (df = 13503)	0.480 (df = 13551)
F Statistic	$29.782^{***} (df = 56; 13503)$	$121.900^{***} (df = 8; 1355)$
Note:	29.102 (di = 90 ; 13903)	*p<0.1; **p<0.05; ***p<

```
anova(model_pooled_with_covariates, model_pooled_no_covariates, test = 'F')
## Analysis of Variance Table
##
## Model 1: reached_b4goal ~ rem_any + highint + rewardint + joint + dc +
##
       joint_single + female + age + highschool_completed + wealthy +
##
       married + saved_formal + inc_7d + saved_asmuch + spent_b4isaved +
##
       missing_female + missing_age + missing_highschool_completed +
##
       missing_married + missing_saved_asmuch + missing_spent_b4isaved +
##
       factor(depart) + factor(provincia) + factor(marketer) + factor(branch) +
##
       factor(country)
## Model 2: reached_b4goal ~ rem_any + highint + rewardint + joint + dc +
       joint_single + factor(country)
##
     Res.Df
               RSS Df Sum of Sq
                                            Pr(>F)
##
## 1 13503 2983.0
## 2 13551 3126.4 -48
                         -143.44 13.528 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
    Including these extra "baseline" covariates is useful at improving the model performance. The
    null hypothesis is that there is not difference in the RSS of the two models; a null hypothesis
    that I would reject if the p-value were lower than 0.05 for an F-test. Here, the p-value is lower
    than 0.05, and so I reject. This means, that the additional covariates are improving the model
    performance. The authors report that they used Huber-White standard errors. That is to say,
    they used robust standard errors. Use the function vcovHC - the variance-covariance matrix that
    is heteroskedastic consistent - from the sandwich package, together with the coeftest function
    from the lmtest package to print a table for each of these regressions.
coeftest(model_pooled_no_covariates, vcov. = vcovHC(model_pooled_no_covariates, type = 'HC1'))
##
## t test of coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
##
                     ## (Intercept)
                     0.0318551 0.0091531
                                            3.4802 0.0005025 ***
## rem anv
## highint
                    -0.0016874 0.0256233
                                          -0.0659 0.9474939
## rewardint
                     0.0461544 0.0269002
                                            1.7158 0.0862280 .
## joint
                     0.0036252 0.0273634
                                             0.1325 0.8946029
## dc
                     0.0119754 0.0250280
                                            0.4785 0.6323148
                    -0.0354484 0.0255492 -1.3875 0.1653255
## joint_single
## factor(country)2 -0.1143957 0.0107312 -10.6601 < 2.2e-16 ***
## factor(country)3 -0.4870514 0.0261962 -18.5924 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
coeftest(model_pooled_with_covariates, vcov. = vcovHC(model_pooled_with_covariates, type = 'HC1'))[1:16
                                        Std. Error
##
                             Estimate
                                                         t value
                                                                     Pr(>|t|)
## (Intercept)
                         2.498270e-01 0.0672883049
                                                     3.712784240 2.058162e-04
## rem any
                         3.183629e-02 0.0089423905 3.560154798 3.719099e-04
## highint
                        -9.970223e-03 0.0256875905 -0.388133816 6.979231e-01
## rewardint
                         4.358375e-02 0.0268423804 1.623691624 1.044650e-01
## joint
                         4.820782e-04 0.0273952056 0.017597173 9.859605e-01
## dc
                         1.080298e-02 0.0249442351 0.433085133 6.649598e-01
                        -3.773627e-02 0.0254452916 -1.483035342 1.380884e-01
## joint_single
```

```
## female
                         1.579625e-02 0.0086248161 1.831488053 6.704975e-02
                         1.737994e-03 0.0003594338 4.835364702 1.343665e-06
## age
## highschool completed -3.769042e-02 0.0096628562 -3.900546853 9.644067e-05
## wealthy
                        -3.257150e-02 0.0162773598 -2.001030857 4.540904e-02
## married
                         1.771074e-02 0.0132454866 1.337115295 1.812075e-01
## saved formal
                        -2.565272e-02 0.0115623416 -2.218644370 2.652749e-02
## inc 7d
                         8.667443e-05 0.0001693684 0.511751018 6.088336e-01
## saved asmuch
                        -3.031777e-02 0.0318521013 -0.951829370 3.412006e-01
## spent b4isaved
                        -1.141808e-04 0.0289497825 -0.003944099 9.968531e-01
```

For each of the tests, the null hypothesis is that the coefficient = 0. The alternative hypothesis is that the coefficient does **not** equal zero (<.05).

Individuals who were randomly assigned to receive a reminder message were 3.2 percentage points more likely to meet their savings goals than those who were not assigned to receive such messages. This effect is statistically significant. Because these reminder messages were experimentally assigned, it is very, very easy to satisfy the "ceteris peribus" nature of the interpretation of this coefficient. For every year older was a participant, they are 0.0012, or 0.12 percentage points, more likely to meet their commitments. Compared to someone who is 18, someone who is 68 (i.e. 50 years older) is about 6 percentage points more likely to meet their savings goal. However, this requires a really strong assumption that these two individuals are otherwise identical in terms of their covariate profiles. i. Interpret the meaning of the coefficient estimated on highschool_completed.

The rather crass interpretation is that there is no evidence that completing highschool has any effect on meeting one's savings goals. To state this more precisely, for two individuals with the same covariate profile, the model predicts that someone who has completed highschool will be 0.002 more likely to meet their savings goal than someone who has not completed highschool. This result is not statistically significant.