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1  ┌────────────────────────── MODULE VectorClocks ───────────────────────────┐
2  EXTENDS Integers
3  CONSTANTS Procs, MAX

6  --algorithm VectorClocks
7  variables
8     $msgs = [p \in Procs \mapsto [q \in Procs \mapsto 0]]$ ; defined as Vector Clock

10 define
11   returns the maximum value for each element of two vectors
12    $Max(v1, v2) \triangleq [p \in Procs \mapsto \text{IF } v1[p] > v2[p] \text{ THEN } v1[p] \text{ ELSE } v2[p]]$ 
13   increments by 1 the 'e' element of the vector 'v'
14    $Increment(e, v) \triangleq [p \in Procs \mapsto \text{IF } p = e \text{ THEN } v[p] + 1 \text{ ELSE } v[p]]$ 
15 end define ;

17 fair process VectorClock  $\in Procs$ 
18 variables
19    $vc = [p \in Procs \mapsto 0]$  Initially all clocks are zero
20 begin Main:
21   while  $vc[self] < MAX$  do
22     either Receive: increments local clock and calcs maximum of two clocks
23        $vc := Increment(self, Max(vc, msgs[self]))$ ;
24     or Send: increments local clock and sends it to another process
25        $vc[self] := vc[self] + 1$ ;
26       with  $p \in Procs \setminus \{self\}$  do send  $vc$  to 'p' via  $msgs[p]$ 
27          $msgs[p] := vc$ ;
28       end with ;
29     end either ;
30   end while ;
31 end process ;

33 end algorithm ;

35 BEGIN TRANSLATION
36 VARIABLES  $msgs, pc$ 

38 define statement
39    $Max(v1, v2) \triangleq [p \in Procs \mapsto \text{IF } v1[p] > v2[p] \text{ THEN } v1[p] \text{ ELSE } v2[p]]$ 

41    $Increment(e, v) \triangleq [p \in Procs \mapsto \text{IF } p = e \text{ THEN } v[p] + 1 \text{ ELSE } v[p]]$ 

43   VARIABLE  $vc$ 

45   vars  $\triangleq \langle msgs, pc, vc \rangle$ 

47    $ProcSet \triangleq (Procs)$ 

49   Init  $\triangleq$  Global variables
50      $\wedge msgs = [p \in Procs \mapsto [q \in Procs \mapsto 0]]$ 

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51      Process VectorClock
52       $\wedge vc = [self \in Procs \mapsto [p \in Procs \mapsto 0]]$ 
53       $\wedge pc = [self \in ProcSet \mapsto \text{"Main"}]$ 

55      Main(self)  $\triangleq$   $\wedge pc[self] = \text{"Main"}$ 
56                   $\wedge$  IF  $vc[self][self] < MAX$ 
57                      THEN  $\wedge \vee \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"Receive"}]$ 
58                           $\vee \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"Send"}]$ 
59                      ELSE  $\wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"Done"}]$ 
60                   $\wedge$  UNCHANGED  $\langle msgs, vc \rangle$ 

62      Receive(self)  $\triangleq$   $\wedge pc[self] = \text{"Receive"}$ 
63                   $\wedge vc' = [vc \text{ EXCEPT } ![self] = \text{Increment}(self, Max(vc[self], msgs[self]))]$ 
64                   $\wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"Main"}]$ 
65                   $\wedge msgs' = msgs$ 

67      Send(self)  $\triangleq$   $\wedge pc[self] = \text{"Send"}$ 
68                   $\wedge vc' = [vc \text{ EXCEPT } ![self][self] = vc[self][self] + 1]$ 
69                   $\wedge \exists p \in Procs \setminus \{self\} :$ 
70                       $msgs' = [msgs \text{ EXCEPT } ![p] = vc'[self]]$ 
71                   $\wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"Main"}]$ 

73      VectorClock(self)  $\triangleq$  Main(self)  $\vee$  Receive(self)  $\vee$  Send(self)

75      Next  $\triangleq$   $(\exists self \in Procs : VectorClock(self))$ 
76           $\vee$  Disjunct to prevent deadlock on termination
77           $((\forall self \in ProcSet : pc[self] = \text{"Done"}) \wedge \text{UNCHANGED } vars)$ 

79      Spec  $\triangleq$   $\wedge Init \wedge \square [Next]_{vars}$ 
80           $\wedge \forall self \in Procs : WF_{vars}(VectorClock(self))$ 

82      Termination  $\triangleq$   $\diamond (\forall self \in ProcSet : pc[self] = \text{"Done"})$ 

84      END TRANSLATION

86      Boundedness
87      VectorClockOK  $\triangleq$   $(\forall k, l \in Procs : vc[k][k] \geq vc[l][k])$ 

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89      \ * Modification History
      \ * Last modified Sun Nov 25 18:51:00 PST 2018 by ocosta
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