

Numpy Basics

Overview

NumPy is the foundational package for numerical computing in Python. It provides the ndarray, a fast and space-efficient multidimensional array, along with capabilities for vectorized computation, broadcasting, mathematical operations, file I/O, and linear algebra.

Creating Arrays

Arrays are created using functions like `np.array`, `np.zeros`, `np.ones`, and `np.arange`.

```
import numpy as np
arr1 = np.array([1, 2, 3])
arr2 = np.zeros((2, 3))
arr3 = np.arange(10)
```

→ [1, 2, 3]
→ [0 0 0]
→ [0 0 0]

→ [0, 1, 2, 3, ..., 8, 9]

Table: Array Creation Functions

Function	Description
array	Convert input data to ndarray
arange	Similar to range but returns an array
zeros, ones	Create arrays filled with 0s or 1s
empty	Create array <u>without initializing entries</u>
eye, identity	Create identity matrices

np.ones((2,3))
→ [1 1 1]
→ [1 1 1]

np.eye(2) → [1 0]
→ [0 1]

Data Types (dtype)

NumPy supports several data types, which can be set using the `dtype` parameter.

```
arr = np.array([1.5, 2.3, 3.1], dtype=np.float32)
```

↑ ↑ ↑
X = np.array([1, 2, 3], dtype=np.int32)

Type	Description
<u>int32</u> , <u>int64</u>	Integer types
<u>float32</u> , <u>float64</u>	Floating point
<u>bool</u>	Boolean
<u>object</u>	Generic Python objects

"one" ← dtype

Array Operations and Indexing

Vectorized operations eliminate the need for explicit loops.

```
arr = np.array([1, 2, 3]) ✓
arr * 2 # array([2, 4, 6])
```

$\text{np.array}([1, 2, 3]) + \text{np.array}([4, 5, 6])$
 $\rightarrow \text{np.array}([5, 7, 9])$

Indexing and slicing:

```
arr = np.arange(10)
arr[5:8] = 100 # modifies elements at indices 5, 6, 7
```

$[0, 1, 2, 3, \dots, 8, 9]$

$\rightarrow [0, 1, 2, 3, 100, 100, 100, 8, 9]$

Boolean Indexing

Boolean indexing allows you to filter or select data from an array using boolean conditions. It is a powerful feature for subsetting arrays without the need for loops. Example: selecting rows based on a condition.

```
names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])
data = np.random.randn(7, 4) # 7x4 matrix of standard normal values

# Get rows where names == 'Bob'
data[names == 'Bob']
```

7 rows
4 columns

\rightarrow TRUE FALSE FALSE TRUE FALSE FALSE FALSE

Fancy Indexing

Fancy indexing allows indexing using arrays of integers. It creates copies rather than views, and supports powerful reordering and extraction capabilities. Example, reassign values

```
arr = np.empty((8, 4)) ✓
for i in range(8):
    arr[i] = i
```

$\text{arr} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \\ 2 & 2 & 2 & 2 \\ \vdots & \vdots & \vdots & \vdots \\ 7 & 7 & 7 & 7 \end{bmatrix}_{8 \times 4}$

$\begin{bmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \\ (2,0) & (2,1) & (2,2) \end{bmatrix}_{3 \times 3}$

Using negative indices:

`arr[[-1, -3]]`

Selecting multiple elements (advanced):

`arr = np.arange(32).reshape((8, 4))`

Select elements at (1, 0), (5, 3), and (7, 1)

`arr[[1, 5, 7], [0, 3, 1]]`

Transposing

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}^T \rightarrow \begin{bmatrix} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{bmatrix}$$

Transposing is a special form of reshaping that similarly returns a view on the underlying data without copying anything.

`arr.T` # Transpose

Universal Functions (ufuncs)

Universal functions (ufuncs) are vectorized wrappers for simple functions. They perform element-wise operations and are much faster than Python loops.

Unary ufuncs

Operate on a single array.

$$[-1, 2.5, -2, 4] \rightarrow \text{np.abs}([-1, 2.5, -2, 4])$$

$$\hookrightarrow [1, 2.5, 2, 4]$$

Function	Description
<code>np.abs</code> , <code>np.fabs</code>	Absolute value
<code>np.sqrt</code>	Square root
<code>np.square</code>	Element-wise square
<code>np.exp</code>	Exponential
<code>np.log</code> , <code>np.log10</code>	Natural / base-10 logarithm
<code>np.sign</code>	Sign of number (+1, 0, -1)

Table 1: Common unary ufuncs

`arr = np.array([1, 2, 3, -4])`
`np.sqrt(np.abs(arr))` # Safe square root

$$\hookrightarrow [1, 2, 3, 4]$$

$$\hookrightarrow [1, \sqrt{2}, \sqrt{3}, 2]$$

Binary ufuncs

Operate on two arrays (or array and scalar).









Function	Description
 np.add	Addition
 np.subtract	Subtraction
 np.multiply	Multiplication
 np.divide	Division
 np.maximum	Element-wise maximum
 np.minimum	Element-wise minimum
 np.mod	Modulo operation

Table 2: Common binary ufuncs

Example: element-wise operations




```

x = np.array([1, 2, 3]) ✓
y = np.array([4, 5, 6]) ✓ ✓ ✓
np.maximum(x, y) # array([4, 5, 6])
  
```


Performance

Ufuncs are implemented in C, enabling fast execution without explicit Python loops. This makes them ideal for large-scale numerical computation. Comparison with loop:



```

# Slower with loop
result = [math.sqrt(abs(x)) for x in arr]
  
```



```

# Faster with ufunc
np.sqrt(np.abs(arr))
  
```

import math

absolute value

fix