

1. Consider the `customers.csv` datafile. This file contains information related to customers' activity on a company website. Below are the description of the variables.

- **ID**: customer ID
- **Visit_Time**: The number of visits to the company's website in a given month.
- **Average_Expense**: The average amount of money that the customer has spend.
- **Sex**: gender of the customer (0: female, 1: male).
- **Age**: age of the customer.

In Python, answer the following:

- (a) (3 points) Using the `pandas` library, read the csv file and create a data-frame called `customers`.
- (b) (3 points) Using the appropriate Python commands, remove the `ID` variable.
- (c) (5 points) Using the appropriate standardization formula, put all the variables on the same scale.
Hint: Notice that `Sex` is a 0-1 variable.
- (d) (8 points) Using the silhouette score, estimate the number of cluster for this dataset. Consider 2 to 20 clusters. Make sure to use `n_init = 20`.
- (e) (6 points) Using the `cmeans` function from the `skfuzzy.cluster` library, cluster the customers into the number of clusters estimated from part (d).
- (f) (10 points) Change the likelihoods to cluster labels using 70% as threshold. Describe each of the clusters from part (d).