

69361

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I have completed this assignment individually, without support from anyone else.
I hereby accept that only the below listed sources are approved to be used during this assignment:

(i) Course textbook,

(ii) All material that is made available to me by the professor (e.g., via Blackboard for this course, course website, email from professor/TA),

(iii) Notes taken by me during lectures.

I have not used, accessed or taken any unpermitted information from any other source. Hence, all effort belongs to me.



Pseudo Code:

```
func (array[ ][ ], int row, int lowerbound, int upperbound) {  
    if row is equal to n for nxn matrix:  
        return 0  
  
    if upperbound is equal to lowerbound:  
        midpoint = lowerbound +  $\frac{upperbound - lowerbound}{2}$   
        if array[row][midpoint] is char 'a':  
            lowerbound will be midpoint + 1  
            return func(array[ ][ ], row, lowerbound, upperbound)  
        else:  
            upperbound will be midpoint  
            return func(array[ ][ ], row, lowerbound, upperbound)  
  
    go to next row  
    return lowerbound + func(array[ ][ ], row, = n-1upperbound, = 0lowerbound)
```

in same row

```
count(char[][] mat) {
```

```
    int result = 0;
```

```
    if n=1 for n x n matrix:
```

```
        if mat[0][0] is char 'a':
```

```
            result = 1
```

```
        Otherwise:
```

```
            result = func(mat, 0, 0, (n-1))
```

```
    return result
```


Complexity analysis

1) Time

For each row the algorithm's complexity is the same as binary search. For a $n \times n$ matrix, the complexity of each row is $O(\log n)$. There are n rows so the overall complexity is $n \cdot O(\log n)$. Hence the time complexity is $O(n \log n)$.

For each row \rightarrow binary search algorithm

$$T(1) = 2$$

$$T(n) = 2 + T(n/2) = 2 + (2 + T(n/4)) = 4 + (2 + T(n/8))$$

$$= 2k + T\left(\frac{n}{2^k}\right)$$

$$n = 2^k \quad k = \log n$$

$$2 \log n = O(\log n)$$

2) Space

array $\rightarrow N \times N \times 1$ byte

row $\rightarrow 4$ bytes

lowerbound $\rightarrow 4$ bytes

upperbound $\rightarrow 4$ bytes

midpoint $\rightarrow 4$ bytes

Auxillary space $\rightarrow 4$ bytes

$$+ \frac{(N^2 + 20 \text{ bytes}) \times N \log N (\text{recursion})}{}$$

$$= N^3 \log N + 20 \times N \log N$$

$$= O(N^3 \log N)$$