## Quiz 1-Linear Regression with Multiple Variables

## QUES1.

Suppose *m*=4 students have taken some class, and the class had a midterm exam and a final exam. You have collected a dataset of their scores on the two exams, which is as follows:

midterm exam	(midterm exam)^2	final exam
89	7921	96
72	5184	74
94	8836	87
69	4761	78

You'd like to use polynomial regression to predict a student's final exam score from their midterm exam score. Concretely, suppose you want to fit a model of the form  $h_{\theta}(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 \text{, where } x_1 \text{ is the midterm score and x_2 is (midterm score)^2}.$  Further, you plan to use both feature scaling (dividing by the "max-min", or range, of a feature) and mean normalization.

What is the normalized feature  $x_2^{(4)}$ ? (Hint: midterm = 69, final = 78 is training example 4.) Please round off your answer to two decimal places and enter in the text box below.

## **Answer:**

mean = (7921+5184+8836+4761)/4 = 6675.5deviation = 8836-4761 = 4075normalized x2(4) = (4761-6675.5)/4075 = -0.50

**Ques2.** You run gradient descent for 15 iterations with  $\alpha$ =0.3 and compute J( $\theta$ ) after each iteration. You find that the value of J( $\theta$ ) decreases quickly then levels off. Based on this, which of the following conclusions seems most plausible? **Answer**:  $\alpha$ =0.3 is an effective choice of learning rate.

**Ques3**. Suppose you have m = 28 training examples with n = 4 features (excluding the additional all-ones feature for the intercept term, which you should add). The normal equation is theta =  $(X^T X)^{-1} X^T y\theta$ . For the given values of m and n, what are the dimensions of  $\theta$ , X, and y in this equation? **Answer:** X is  $28 \times 5$ , y is  $28 \times 1$ ,  $\theta$  is  $5 \times 1$ 

**Ques4.** Suppose you have a dataset with m = 1000000 examples and n = 200000 features for each example. You want to use multivariate linear regression to fit the parameters  $\theta$  to our data. Should you prefer gradient descent or the normal equation?

**Answer:** Gradient descent, since  $(X^T X)^{-1}$  will be very slow to compute in the normal equation.

**Ques5.** Which of the following are reasons for using feature scaling? **Answer:** It speeds up gradient descent by making it require fewer iterations to get to a good solution.