

# Principal component analysis on images

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**DTU Compute** 

#### Based on

M. Turk and A. Pentland. *Face recognition using eigenfaces*. Computer Vision and Pattern Recognition, 1991.

http://compute.dtu.dk/courses/02502





# Principal Component Analysis on images learning objectives

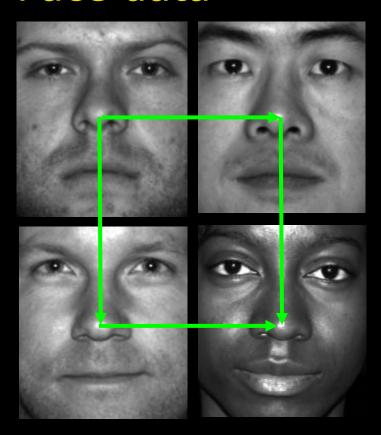
- Construct a column matrix from a single gray scale image
- Construct a data matrix from a set of gray scale images
- Compute and visualize an average image from a set of images
- Compute the principal components of a set of images
- Visualize the principal components computed from a set of images
- Synthesize an image by combining the average image and a linear combination of principal components



2021



#### Face data



- 38 face images
  - 168 x 192 grayscale
- Aligned
  - The anatomy is placed "in the same position in all image"
- Same illumination conditions on the images we use

The Extended Yale Face Database B http://vision.ucsd.edu/~leekc/ExtYaleDatabase/ExtYaleB.html





# Principal component analysis on face images









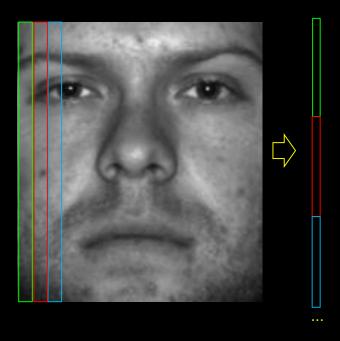
- What is the main variation in face images?
  - The variation of appearance
  - Not the position in the image
  - Not the light conditions
  - Not the direction of the head



**Image Analysis** 



## Putting images into matrices



$$\mathbf{I} = \begin{bmatrix} p_1 \\ p_2 \\ \dots \\ p_m \end{bmatrix}$$

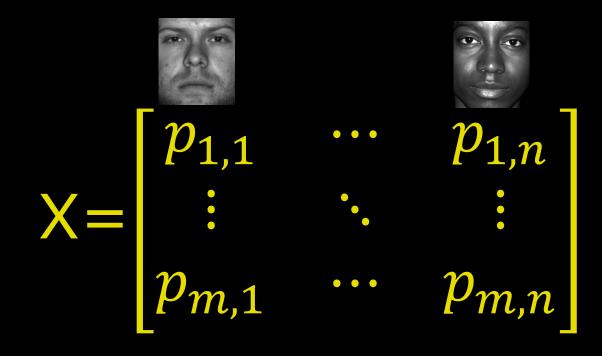
- An image can be made into a column matrix
  - Stack all image columns into one column





### Face images in matrix form

- One column is one face
- n=38 faces
- = m=168x192 = 32256 pixel values per image







### The average face





$$\mathbf{X} = \begin{bmatrix} p_{1,1} & \cdots & p_{1,n} \\ \vdots & \ddots & \vdots \\ p_{m,1} & \cdots & p_{m,n} \end{bmatrix}$$



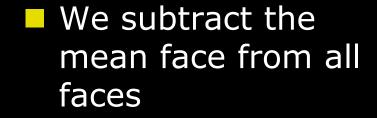
- The average face
  - Average of each row
  - One column
  - Put it back into image shape
- Blurry around the eyes
  - Not perfectly aligned





#### Subtracting the mean face

$$\mathbf{X}' = \begin{bmatrix} p_{1,1} & \cdots & p_{1,n} \\ \vdots & \ddots & \vdots \\ p_{m,1} & \cdots & p_{m,n} \end{bmatrix} - \bar{X}$$



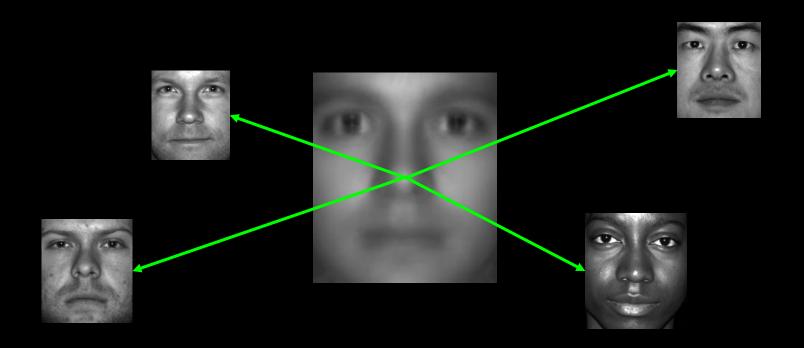






# Analyzing the deviation from the mean face

We want to do the principal component analysis on the deviations from the average face





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## PCA Analysis on face data

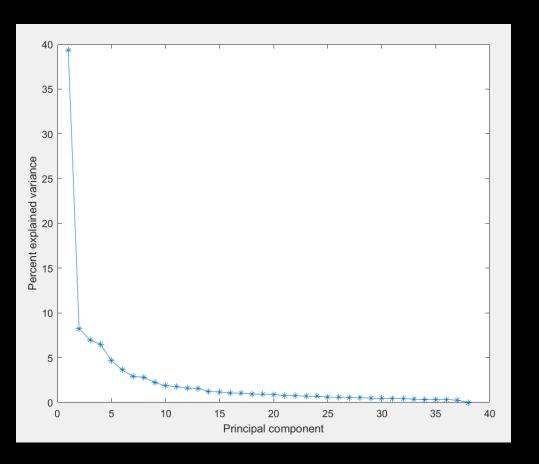
$$\mathbf{X}' = \begin{bmatrix} p_{1,1} & \cdots & p_{1,n} \\ \vdots & \ddots & \vdots \\ p_{m,1} & \cdots & p_{m,n} \end{bmatrix} - \bar{X}$$

- We do the PCA analysis on the X' matrix
- X' is 32256 x 38
- Standard covariance matrix is 32256 x 32256
- Turk and Pentland found a trick:
  - Compute the PCA on the 38 x
    38 matrix instead of the
    32256x32256 matrix
  - Details in the paper
    - Beyond the scope here





#### PCA on faces



- First eigenvector explains 40% of variation
- Second eigenvector explains 8% of variation





#### Visualizing the PCA faces

#### Main deviations from the average face







First PC - 40% of variation







-PC | Average face

+PC

Second PC – 8% of variation

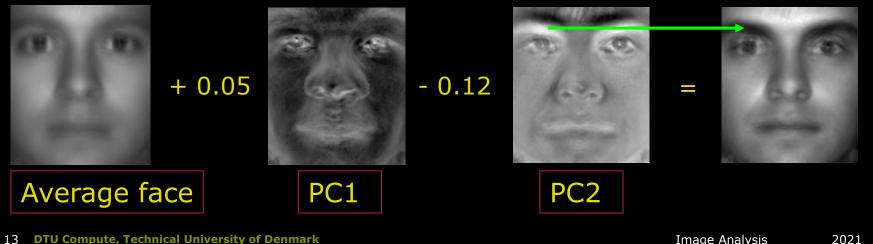
A tool to see major variations – brow lifting





## Synthesizing faces

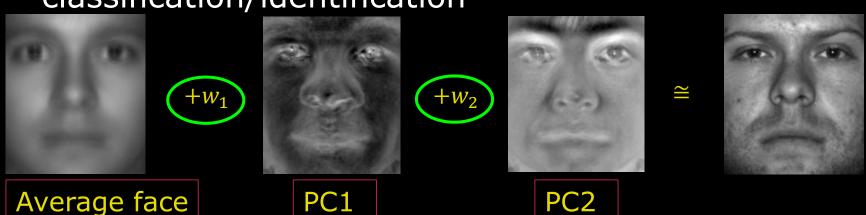
- A new face can be created by combining
  - Average face
  - Linear combination of principal components





#### Decomposing faces

- A given face can be reconstructed using
  - The average face
  - Linear combination of principal components
- Found by projecting the face on the principal components
- The weights can then be used for classification/identification





# Face analysis plus plus?

More examples later in the course

