

Last name

Name

ID

## Generic Competence EDA

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- *This exercise must be handed in on 09/06/2017 at the **beginning** of the final exam.*
  - *Write your full name and ID.*
  - *Write your answers within the reserved space.*
  - *When giving a reference to a source (book, journal, website, etc.), follow the style "ISO-690 (author-date, English)". You can generate references in this format at:  
[www.citethisforme.com/guides/iso690-author-date-en](http://www.citethisforme.com/guides/iso690-author-date-en)*
  - *When giving an URL, please write **clearly** and use Google URL Shortener:  
<https://goo.gl>*
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(a) Define the complexity class co-NP.

(b) Give the reference of a source where this class is defined.

(c) Show that  $P \subseteq \text{co-NP}$ .

- (d) From the previous exercise and that  $P \subseteq NP$  one can deduce that  $P \subseteq NP \cap \text{co-NP}$ . An important open problem in theoretical Computer Science is whether  $P = NP \cap \text{co-NP}$  or not.

For a long time, a problem from  $NP \cap \text{co-NP}$  that was not known to belong or not to  $P$  (and hence was candidate to refute that  $P = NP \cap \text{co-NP}$ ) was the problem of **PRIMES**: given a natural number (represented by the vector of its digits in binary), to determine whether it is prime or not. Finally however it was shown that this problem belongs to  $P$ .

Give the reference of a source where it is **proved** that **PRIMES** belongs to  $P$ .

- (e) Another important open problem in theoretical Computer Science is whether  $NP = \text{co-NP}$ . If  $NP \neq \text{co-NP}$ , what can we say then about the problem  $P = NP$ ? Justify your answer.