

## A TLA+ and PLUSCAL Overview

Some koans and exercises

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OSOCO

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Introduction

TLA\* and PLUSCAL Semantics

### About PlusCal

- Developed by Lamport in 2009 to make TLA<sup>+</sup> more accessible to programmers.
- PLUSCAL provides a pseucode-like structure on top of TLA+.
- · Adds additional syntax: assignments and labels.
- PLUSCAL is language that compiles down to TLA\*.

## Spec layout

```
---- 1 MODULE example 2 ----
EXTENDS Integers 3
(* --algorithm wire ◀
    variables 6
        people = { "bob", "alice" },
        acc = [ alice | -> 5, bob | -> 5 ];
    begin 6
        skip;
    end algorithm; 4 *)
==== 0
```

## Spec layout

- TLA<sup>+</sup> specs must start with at least four at each side of MODULE and four = at the end.
- 2 The module name must be the same as filename.
- **3** EXTENDS is the import keyword.
- ◆ (\*...\*) is the block comment. PLUSCAL spec starts with--algorithm <name> and ends with end algorithm.
- **6** Initialization of variables.
- **6** Where the algorithm is implemented.

### Basic values

### Four basic values in TLA+:

String Must be written en double quotes.

Integer Floats are not supported.

Boolean Written as TRUE and FALSE.

Model value A kind of symbol value.

# Standard operators

Operator	Meaning	Example
x = y	Equals	>> 1 = 2 FALSE
x /= y	Not Equals	>> 1 /= 2 TRUF
x /\ y	And	>> TRUE /\ FALSE FALSE
x \/ y	Or	>> TRUE \/ FALSE
~X	Not	>> ~TRUE FALSE
x := y	Assignment	PlusCal only

## **Arithmetic Operators**

- If you EXTENDS Integers get the arithmetic operators: +, -, % and \*.
- Decimal division is not supported, only the integer division: \div.
- You also get the range operator .. where a..b is the set {a, a+1, ..., b-1, b}.

# **Complex Types**

### TLA\* has four complex types:

- · Sets.
- · Tuples or sequences.
- · Structures.
- Functions.

#### Sets

### Sets

Unordered collections of elements of the same type.

```
{1, 2, 42}
{{TRUE}, {FALSE, TRUE}, {}}
```

# **Set Operators**

Operator	Meaning	Example
x \in set	Is member of	>> 1 \in 13 TRUE
x \notin set	Is not member of	>> 1 \notin 12 FALSE
set1 \subseteq set2	Is subset of	>> {1, 2} \subseteq {1, 2, 3} TRUE
set1 \union set2	Union	>> {1, 2} \union (23) {1, 2, 3}
set1 \intersect set2	Intersection	>> {1, 2} \intersect (23) {2}
set1 \ set2	Difference	>> {1, 2} \ (23) {1}
Cardinality(set)	Cardinality (requires EXTENDS FiniteSets)	>> Cardinality({1, 2}) 2

### **Set Transformations**

```
Filter sets
{x \in set: conditional}

>> {x \in 1..3: x > 2}
{3}
```

### Map sets

```
{expression: x \in \text{set}}
```

```
>> \{x * 3: x \in 1..3\} {3, 6, 9}
```

# **Tuples or Sequences**

### **Tuples or Sequences**

Ordered collections of elements with the index starting at 1.

```
tuple := <<1, TRUE, {1, 2}>>;
>> tuple[1]
1
>> tuple[3]
{1, 2}
```

# **Sequence Operators**

If you **EXTENDS** Sequences you get the following additional operators:

Example
>> Head(<<1, 2>>
>> Tail(<<1, 2, 3>>
<<2, 3>> >> Append(<<1, 2>>, 3
<<1, 2, 3>> >> <<1, 2>> \o <<3>>>
<<1, 2, 3>>

### Structures or Structs

#### Structures or Structs

A map of strings to values.

# Assignments

Assign an existing variable to a value with :=.

#### Rule of thumb

If it's the first time you're using the variable, = is initialization. Every other time, = is equality and := is assignment.

#### assert

#### assert

assert TRUE does nothing, assert FALSE raises an error.

In order to use assertions you need to add EXTENDS TLC to the spec.

## skip

- · A no-op.
- To fill parts of the spec that we haven't filled out yet or conditionals that don't update anything.

```
if condition1 then
  body1
elsif condition2 then
  body2
else
  body3
end if;
```

# while loop

```
while condition do
  body
end while;
```

To avoid duplications in your specs you can add macros before the begin of the algorithm:

```
macro name(arg1, arg2) begin
  \* macro's body
end macro;

begin
  name(x, y);
end algorithm;
```

#### **Macros limitations**

You can place assignments, assertions, and if statements in macros, but not while loops. You also cannot assign to any variable more than once.

# Multiple Starting States i

We need a way to specify not just one setup, but an entire space of setups to check our specifications.

# Multiple Starting States ii

We initialize variables with =, but we can also initialize them with \in.

TLC will try running the algorithm with any possible element in the set:

```
(* --algorithm in
variables x \in 1..3};

begin
  assert x < 3;
end algorithm; *)</pre>
```

# Multiple Starting States iii

#### **BOOLEAN** set

TLA\* defines BOOLEAN as the set {TRUE, FALSE}. This can be useful if you have a variable isReady \in BOOLEAN.

# Multiple Starting States iv

### **SUBSET**

**SUBSET** is the power set, or the set of all subsets.

```
>> SUBSET 1..2 {{}, {1}, {2}, {1, 2}}
```

# Multiple Starting States v

#### \X

**set1** \X **set2** is the set of all tuples where the first element is in set1 and the second element in set2.

```
>> (1..2) \X BOOLEAN {<<1, TRUE>>, <<2, TRUE>>, <<2, FALSE>>}
```

# Multiple Starting States vi

### [key: set]

If  $x \in [key: set]$ , then x is an structure where the value of key is an element in set.

```
>> [a: (1..2), b: BOOLEAN]
{[a |-> 1, b |-> TRUE], [a |-> 2, b |-> TRUE],
    [a |-> 1, b |-> FALSE], [a |-> 2, b |-> FALSE]}
```

## Beware of state explosion i

```
variables
  capacity = [trash |-> 10, recycle |-> 10],
  items = <<
     [type |-> "trash", size |-> 5],
     [type |-> "recycle", size |-> 3],
     [type |-> "recycle", size |-> 4],
     [type |-> "trash", size |-> 2]
  >>;
```

# Beware of state explosion ii

```
variables
  capacity \in [trash: 1..10, recycle: 1..10],
  item \in [type: {"trash", "recycle"}, size: 1..6],
  items \in item \X item \X item;
```

1 state vs.  $10x10x(2x6)^4 = 2,073,600$  states

# Simulating Nondeterminism i

For single process algorithms **PLUSCAL** provides two constructs to simulate nondeterminism:

# Simulating Nondeterminism ii

```
either
  /* branch 1
or
  /* branch 2
/* ...
or
  /* branch n
end either;
```

- · TLC will check all branches.
- No way to make one branch more likely than others.
- If all branches are macro-valid, we can place an either inside a macro.

# Simulating Nondeterminism iii

There are two ways to use the with statement:

- The former creates a temporary variable, the second is nondeterministic.
- TLC will check what happens to all possible assignments of var to elements of set.
- with follows macro rules: no double assignments and no while loops.
- · You can place with statements inside macros.

**PLUSCAL Koans** 

Test the Water

Workshop of Spec Writing



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