### In [1]:

```
import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
from sklearn import linear_model
from sklearn.neighbors import KNeighborsClassifier
from sklearn.tree import DecisionTreeClassifier
from sklearn.naive_bayes import GaussianNB
from sklearn.svm import SVC
from sklearn import metrics
from sklearn.cluster import KMeans, DBSCAN
import seaborn as sns
import matplotlib.pyplot as plt
from plotly.figure_factory._county_choropleth import create_choropleth
```

## In [2]:

```
# Load data
data = pd.read_csv("merged_train.csv")
data.head()
```

# Out[2]:

	State	County	FIPS	Total Population	Percent White, not Hispanic or Latino	Percent Black, not Hispanic or Latino	Percent Hispanic or Latino	Percent Foreign Born	Percen Femal
0	AZ	apache	4001	72346	18.571863	0.486551	5.947806	1.719515	50.59851
1	AZ	cochise	4003	128177	56.299492	3.714395	34.403208	11.458374	49.069646
2	AZ	coconino	4005	138064	54.619597	1.342855	13.711033	4.825298	50.581614
3	AZ	gila	4007	53179	63.222325	0.552850	18.548675	4.249798	50.296170
4	AZ	graham	4009	37529	51.461536	1.811932	32.097844	4.385942	46.313518
4									<b>&gt;</b>

### In [3]:

```
# task 1
# Partition dataset into training, validation sets using holdout method 75/25 split

# Xvariables has all the names except for State, County, FIPS, Party, Democratic, Republican
# Yvariables has Party, Democratic', Republican
Yvariables = ['Party', 'Democratic', 'Republican']

Xvariables = ['Total Population', 'Percent White, not Hispanic or Latino', 'Percent B lack, not Hispanic or Latino', 'Percent Hispanic or Latino', 'Percent Foreign Born', 'Pe rcent Female', 'Percent Age 29 and Under', 'Percent Age 65 and Older', 'Median Household Income', 'Percent Unemployed', 'Percent Less than High School Degree', 'Percent Less than Bachelor\'s Degree', 'Percent Rural']

X_train, X_val, Y_train, Y_val = train_test_split(data[Xvariables], data[Yvariables], test_size = 0.25, random_state = 1)

X_train.head()
```

### Out[3]:

		Total Population	Percent White, not Hispanic or Latino	Percent Black, not Hispanic or Latino	Percent Hispanic or Latino	Percent Foreign Born	Percent Female	Percent Age 29 and Under	Perc Age and O
•	943	15919	91.940449	5.207614	1.432251	1.300333	51.077329	31.660280	23.902
	853	76	72.368421	0.000000	15.789474	11.842105	47.368421	11.842105	25.000
	578	60878	95.579684	0.877164	1.404448	1.342028	50.962581	40.464536	16.324
	1035	54562	95.484037	1.268282	1.414904	1.611011	50.500348	32.005792	20.301
	822	54217	85.327480	0.673221	11.634727	3.225925	50.709187	32.939853	23.861

## In [4]:

```
# task 2
# standardize the training and validation sets by using X_train as the scalar and app
lying to the training and validation sets
scaler = StandardScaler()
scaler.fit(X_train) # find the mean and standard diviation for the columns in X_train
x_train_scaled = scaler.transform(X_train) # scales X_train using the results from fi
t method
x_val_scaled = scaler.transform(X_val) # scales X_val using the results from fit met
hod
x_train_scaled
```

### Out[4]:

```
# task 3
# predict democratic votes using 2 predictors
model = linear model.LinearRegression()
fitted model = model.fit(X=X train[['Percent Foreign Born', 'Median Household Income'
]],y=Y train['Democratic'])
predicted = fitted model.predict(X train[['Percent Foreign Born','Median Household In
come']])
print (predicted)
# Evaluate linear regression model using 2 predictors on democratic votes
X train dummy = pd.get dummies(X train, drop first = True)
X_val_dummy = pd.get_dummies(X_val, drop_first = True)
model = linear model.LinearRegression().fit(X = X train dummy[['Percent Foreign Born'
, 'Median Household Income']], y = Y_train['Democratic'])
score_val = model.score(X = X_val_dummy[['Percent Foreign Born', 'Median Household In
come']], y = Y val['Democratic']) # R squared (validation)
print(score val)
# Evaluate LASSO regression model on democratic votes
model = linear model.Lasso(alpha = 1).fit(X = X train dummy, y = Y train['Democratic'
1)
score val = model.score(X = X val dummy, y = Y val['Democratic']) # R squared (valida
tion)
print(score val)
# predict republican votes using 2 predictors
model = linear model.LinearRegression()
fitted model = model.fit(X=X train[['Percent Foreign Born', 'Median Household Income'
]],v=Y train['Republican'])
predicted = fitted model.predict(X train[['Percent Foreign Born', 'Median Household I
ncome']])
print (predicted)
# Evaluate linear regression model using 2 predictors on republican votes
X_train_dummy = pd.get_dummies(X_train, drop_first = True)
X val dummy = pd.get dummies(X val, drop first = True)
model = linear_model.LinearRegression().fit(X = X_train_dummy[['Percent Foreign Born'
, 'Median Household Income']], y = Y_train['Republican'])
score val = model.score(X = X val dummy[['Percent Foreign Born', 'Median Household In
come']], y = Y_val['Republican']) # R squared (validation)
print(score val)
# Evaluate LASSO regression model on republican votes
model = linear_model.Lasso(alpha = 1).fit(X = X_train_dummy, y = Y_train['Republican'
score val = model.score(X = X val dummy, y = Y val['Republican']) # R squared (valida
tion)
print(score val)
# it seems like lasso regression is better
```

```
[-8.64500143e+02
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                                  2.55502563e+03 -7.71882399e+02
 2.37294394e+04
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 2.14776256e+04
                 3.91440958e+04
                                  8.14666662e+03
                                                  4.34302414e+04
                                                  1.39796986e+04
2.88984861e+04
                 3.43119672e+04
                                  1.92063954e+04
1.97934732e+03
                 1.50266817e+04
                                  3.31604409e+04 -3.71529297e+03
2.35133532e+04
                 6.83121426e+04
                                  3.65679698e+03 -1.62531038e+03
                                  1.44977410e+04
                                                  2.43431691e+04
7.03811130e+03
                 1.74141808e+04
 2.59699968e+04
                 3.28988519e+03
                                  5.20489721e+04
                                                  1.16296643e+04
2.77358371e+04
                 4.31558592e+04
                                  5.78911733e+03
                                                  2.92159385e+03
 1.94502662e+04
                 1.07694150e+04
                                  2.31889541e+04
                                                  6.97362498e+02
 3.25594383e+03 -1.54101094e+03
                                  1.12976435e+04
                                                  4.15183116e+04
-3.00810052e+03
                 2.98277407e+04
                                  1.23259628e+04
                                                  4.38972512e+04
8.81394484e+02
                 1.13401874e+03
                                  1.07062295e+03
                                                  7.58732971e+04
```

```
1.52495606e+04
                 2.40094951e+04
                                  1.49124368e+04
                                                  1.12441837e+04
                 9.95437558e+03
                                                  4.52259634e+04
5.55829867e+04
                                  6.69190873e+04
 2.16997465e+04
                 1.71840041e+04
                                  1.00401237e+04
                                                  3.32201592e+03
 2.73025250e+03 -4.65536337e+03
                                  2.74508295e+04
                                                  2.28511900e+03
-7.59952385e+02
                 4.32440602e+02
                                  4.11157888e+04
                                                  2.56900266e+04
3.37714540e+04
                 9.14908473e+03
                                  1.98624561e+04
                                                  3.47491799e+04
-2.27683603e+03
                 6.07365043e+02
                                  9.94758672e+04
                                                  1.78386837e+04
1.34245563e+04
                 1.26347426e+04
                                  2.05709602e+04 -1.59761594e+03
3.86647372e+04
                 2.22129220e+04
                                  2.24746751e+04
                                                  2.78999002e+00
 1.43110942e+04
                 3.15046968e+04
                                  8.23616685e+03 -1.43132550e+03
9.38338647e+03
                 7.29574080e+03
                                  3.39891318e+04
                                                  3.15801327e+04
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                                  4.07216305e+03
                                                  1.57484685e+04
7.08334673e+03
                 1.65562853e+04
                                  1.78147503e+04
                                                  4.18819746e+04
                                  1.55995206e+04
                                                  1.14337857e+04
4.67002384e+04
                 1.30223506e+04
-1.18810127e+03
                 6.12858718e+04
                                  9.20379078e+03
                                                  1.65128125e+04
8.54309092e+03
                 8.14359412e+01
                                  1.52139772e+04
                                                  3.20022777e+04
-1.39738966e+03
                                  2.96772038e+04 -7.84672471e+03
                 1.45016850e+03
4.01464120e+04
                 2.05777968e+04
                                  1.44074858e+04 -2.37677290e+02
8.88125475e+04
                 1.22572670e+04
                                  7.61922105e+03
                                                  2.60380738e+04
1.16084769e+04
                 8.65509616e+03
                                  3.07262874e+03 -1.27634136e+03
4.26099315e+03
                 3.37311325e+04
                                  6.29970216e+04
                                                  4.52626814e+04
1.75210206e+04
                 3.25476423e+03
                                  4.19919401e+03
                                                  2.27949439e+04
1.42433241e+04
                 4.73944138e+03
                                  2.10146242e+03
                                                  1.37688662e+04
9.29510144e+03
                 1.55975150e+04
                                  1.79653607e+04
                                                  1.79572555e+04
                                                  7.66778514e+04
1.33499949e+04
                 1.78896986e+04
                                  1.88809141e+04
 3.97654589e+04
                 2.51678672e+02
                                  2.46575296e+04
                                                  9.89696185e+03
 3.28908018e+04
                 1.78906261e+04
                                  2.62207483e+04
                                                  8.10740271e+03
 2.79653793e+04
                 2.59997114e+04
                                                  3.16434847e+04
                                  7.83892638e+03
1.52838598e+04
                 1.28706142e+04
                                  8.40569621e+03
                                                  2.51396284e+04
 2.66218594e+04
                 9.48691488e+03
                                  5.88152588e+03
                                                  2.22016128e+04
 2.83097006e+03
                 1.11359618e+05
                                  2.36324857e+04
                                                  1.74166522e+03
 1.06404794e+04 -4.73789079e+03
                                  5.18587730e+04
                                                  1.64142040e+04
 2.78476971e+04
                 1.16079268e+05
                                  5.80678263e+03 -1.61418442e+03
 3.87041838e+04
                 3.71264921e+02
                                  1.35940162e+04
                                                  1.98360906e+04
6.00262587e+03
                 3.22161314e+04
                                  2.70075879e+04
                                                  5.00452794e+02
                                                  2.21619188e+04
 5.51068300e+03
                 3.40809271e+03 -7.64824818e+03
 1.16476579e+04
                 8.01683478e+03
                                  2.77731087e+04
                                                  2.77003191e+04
8.74093014e+04
                 6.25655221e+03
                                  1.59064001e+04
                                                  2.24093197e+04
 5.34555722e+04 -1.37567664e+03
                                  5.82749384e+04
                                                  2.89814835e+04
4.94334485e+04
                 8.27565351e+03
                                  9.11751346e+03
                                                  2.78560055e+04
1.04468571e+04
                 1.32621563e+04
                                  4.05075454e+04
                                                  3.69074156e+04
 3.24263500e+03
                 1.25659734e+04
                                  2.79814742e+04
                                                  1.11875616e+04
 3.73787480e+04 -4.57983688e+03
                                  1.11878324e+04
                                                  5.35706862e+03
9.20808161e+04 -1.12354739e+03
                                  1.26755177e+04
                                                  1.16007298e+05
4.03912708e+02
                 1.06043969e+04
                                                  5.67153984e+04
                                  2.40730889e+04
 2.43302808e+04
                 2.58244164e+04
                                  2.86046697e+04
                                                  7.79277166e+03
1.43588511e+04
                 4.85040598e+04 -9.10737935e+02
                                                  1.33063719e+04
                                                  1.96742372e+04
                 2.86053742e+04 -4.77427789e+03
4.83777841e+03
2.07959825e+04
                 4.38650102e+03 -3.51582144e+02
                                                  9.46150206e+03
7.28990183e+04
                 1.97370431e+04
                                  6.01367118e+04
                                                  2.26979114e+03
 3.24262788e+04
                 2.53428204e+04
                                  2.11934424e+04
                                                  6.44267284e+03
4.76226315e+04
                 3.65127731e+03
                                  8.56724369e+03
                                                  3.72881651e+04
-4.48289886e+03 -8.79956690e+02
                                  5.07728258e+04
                                                  1.33717377e+04
 1.06678680e+04
                 4.02463939e+03
                                  6.39254674e+03
                                                  2.21632822e+04
```

```
5.61871848e+03
                 1.60748808e+03
                                  4.84278189e+04
                                                  4.31296041e+04
-1.72826187e+03
                 1.41198623e+04
                                  1.40751287e+04
                                                  1.71240988e+04
1.27011934e+04
                 5.70405623e+03
                                  3.56997398e+04
                                                  1.52864760e+04
4.69411759e+04 -1.31097281e+03
                                  3.86837561e+04
                                                  3.01295068e+04
 2.24980774e+04
                 9.95777029e+03
                                  2.53753872e+04
                                                  1.76067615e+04
 1.67792151e+04
                 5.79879775e+04
                                  4.47224419e+04
                                                  3.93260252e+04
1.58921727e+04
                 1.38054544e+05
                                  5.91585285e+01
                                                  1.26052041e+05
 3.56394572e+03
                 2.69963893e+04
                                  2.94214843e+03
                                                  2.14120635e+04
1.91443378e+04
                 3.48804534e+03
                                  1.95023357e+04
                                                  3.23039037e+04
4.18259525e+02
                 1.43749511e+04
                                  3.71586617e+04
                                                  3.94679953e+04
 3.90470836e+03
                 1.86717660e+03
                                  1.26957719e+04
                                                  3.24012301e+04
                                                  2.80042344e+04
8.07964431e+02
                 4.10395171e+04
                                  2.14635601e+04
 1.15159212e+04
                 3.73151831e+03
                                  1.18829112e+04
                                                  5.60239277e+04
                 1.72491491e+04
                                                  1.20486233e+05
1.27122183e+04
                                  3.36109676e+04
-6.36672080e+03 -3.84164690e+03
                                  3.87752319e+04
                                                  2.11921118e+04
7.38467843e+02
                 1.53275076e+04
                                  9.25274477e+03
                                                  1.91704256e+03
                                                  2.98977559e+04
2.96135455e+04
                 2.37180713e+04
                                  2.67784511e+04
7.99141528e+03
                                  1.54927381e+05
                                                  1.75306554e+03
                 3.03958886e+04
 7.48074239e+03
                 6.64665604e+04
                                  7.40008459e+03
                                                  1.63168566e+04
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                 2.73060736e+03
                                  4.09385939e+03
                                                  9.46488441e+02
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                 2.27635892e+04
                                  1.41811025e+04
                                                  1.48217044e+04
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                                                  6.07125595e+04
4.30009262e+04
2.78115743e+03 -3.28688614e+03
                                  1.40712453e+05
                                                  1.28109841e+04
4.43985074e+04
                 5.28129454e+04
                                  7.39041069e+04
                                                  6.01237756e+04
                 8.99599031e+03
                                  1.97993832e+04
                                                  8.45997251e+03
6.48528255e+04
 2.32193074e+04
                 1.22125211e+04
                                  7.66548584e+03
                                                  2.08938759e+04
 1.79799660e+04
                 1.42697711e+04
                                  6.78776099e+04 -3.69306946e+03
 1.60094457e+04
                 2.17435874e+04
                                  4.06514706e+04
                                                  1.57939054e+04
2.98261171e+03
                 7.19189452e+03
                                  1.28213741e+04
                                                  1.73683187e+04
4.24876261e+04
                 1.15159213e+04
                                  1.34889011e+03
                                                  9.05555520e+04
 1.82991078e+04 -5.31910150e+02
                                  6.16933909e+03
                                                  1.71359353e+04
 1.84788893e+04
                 8.49435142e+03
                                  1.29938945e+04
                                                  6.62348198e+03
4.19282971e+04
                 2.92091118e+04
                                                  9.98182817e+03
                                  8.86128835e+03
2.03193068e+04
                 3.88817318e+04
                                  1.45409870e+04 -8.42224749e+03
7.01075783e+03
                 4.27320789e+03
                                  1.19727588e+04
                                                  1.04705140e+05
                 1.20489739e+04 -2.21968977e+03
 3.14936793e+04
                                                  1.52018605e+03
 1.34301949e+04 -1.77993369e+03
                                  3.01192374e+03
                                                  6.46996774e+04
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                                  9.39563525e+03
                                                  1.41259393e+04
 3.58505662e+04
                 9.47725154e+03
                                  1.08983011e+04
                                                  4.24261974e+04
2.38813639e+03
                 2.03009246e+04
                                  1.11036997e+04
                                                  1.39657186e+04
6.03989467e+03
                 5.06089685e+03
                                  1.38480320e+04 -1.02075315e+04
4.42799492e+03
                 2.01052847e+04
                                  2.07481032e+04
                                                  2.96151934e+04
5.97951048e+03 -1.10051265e+03 -2.58511707e+02
                                                  1.89799616e+04
 1.75560211e+04
                 1.89268955e+04
                                  6.57645266e+02
                                                  3.06570293e+04
                                  1.57116681e+04
                                                  1.36794224e+04
-4.96899356e+03
                 3.27193036e+04
5.64564984e+04
                 9.86812669e+03
                                  1.20659471e+03
                                                  4.93413233e+03
4.56010809e+04
                 3.36795432e+04
                                  4.69496441e+04
                                                  2.20751102e+04
                 1.29187238e+04
5.16702323e+02
                                  3.33323246e+04
                                                  9.65466730e+03
-2.18927706e+03
                 1.81316236e+04
                                  8.72428968e+03
                                                  8.71263124e+01
2.40775220e+04
                 2.91007223e+04
                                  9.62449795e+03
                                                  4.22546667e+03
 1.43765450e+04
                 2.78646733e+04
                                  9.54461942e+02
                                                  3.28147124e+03
1.99753721e+04
                 8.13201149e+03
                                  4.94953746e+04
                                                  9.07781172e+04
-6.64557897e+03
                 2.41301759e+04
                                  1.94837004e+04
                                                 -1.64763723e+03
6.84909589e+03
                 5.94764872e+04
                                  2.34507478e+04
                                                  1.67142739e+04
```

```
3.89791957e+03 3.34834509e+04 1.49313832e+04 -9.64453227e+01
 5.50381374e+03 -7.31643828e+03 -4.52877618e+01 1.63256772e+04
 6.49019790e+03 2.64321880e+04 1.37258533e+04 1.52082323e+04
 4.02338876e+04 2.34236170e+04 5.59983816e+02 1.47516333e+04
  1.28210450e+04 4.10697011e+03 1.00603773e+04 3.39278102e+04
 1.67930916e+04 1.95661104e+04 1.44483893e+04 -1.99029206e+03
 9.69282945e+04 1.24709397e+05
                                1.26283823e+04 3.15138298e+04
 2.11933549e+04 2.58337471e+04 5.20200066e+04 7.52093596e+04
 6.55578323e+04 2.03669530e+04 1.45052353e+04 2.01528210e+04
 1.30341427e+04 -2.11085983e+03 2.42152419e+04 1.47806699e+04
 1.35239743e+04 4.91520712e+04 6.73185702e+03 1.20966399e+04
  3.11453809e+04 5.06364999e+03 1.74765990e+04 7.88053980e+03
 1.75193751e+04 3.32218538e+04 1.61389251e+04 2.96711954e+04
 2.34644078e+04 5.78060844e+03 1.19050224e+04 2.17994292e+03
 1.06904502e+04 1.05320707e+04 3.60058763e+04 -2.59283471e+03
 6.99270447e+03 8.56403453e+03 3.72680123e+04 7.44263799e+04
 2.54025605e+04 3.37042801e+04 4.66566866e+04 6.78089773e+03
 1.18199468e+04 4.22190208e+04 2.41112373e+04 6.62278595e+03
  3.14997815e+03 1.65416820e+04 7.52705550e+03 1.10479978e+04]
0.12344379156818297
0.8328536880997107
```

# In [6]:

```
# task 4
# Partitioning the data into training and validation using only variables that are st
ronger predictors
X = ['Percent White, not Hispanic or Latino', 'Percent Black, not Hispanic or Latino'
, 'Percent Hispanic or Latino', 'Percent Age 29 and Under', 'Percent Age 65 and Olde
r', 'Percent Less than High School Degree', 'Percent Less than Bachelor\'s Degree',
'Percent Rural']
Y = ['Party']
X_train_class, X_val_class, Y_train_class, Y_val_class = train_test_split(data[X], da
ta[Y], test_size=0.25, random_state=0)
scaler.fit(X_train_class)
x_train_scaled_class = scaler.transform(X_train_class)
x_val_scaled_class = scaler.transform(X_val_class)
```

## In [7]:

```
# task 4 - continuation
# Build a classification model to classify each county as Democratic or Republican
# kNN classifier
classifier = KNeighborsClassifier(n_neighbors=5, weights='uniform')
classifier.fit(x_train_scaled_class, Y_train_class.values.ravel())
```

#### Out[7]:

# In [8]:

```
y_pred_class = classifier.predict(x_val_scaled_class)
```

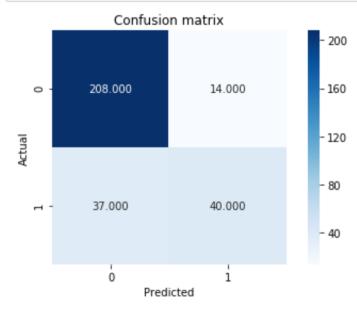
# In [9]:

```
conf_matrix = metrics.confusion_matrix(Y_val_class, y_pred_class)
print(conf_matrix)
```

```
[[208 14]
[ 37 40]]
```

# In [10]:

```
sns.heatmap(conf_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Confusion matrix')
plt.tight_layout()
```



## In [23]:

```
accuracy = metrics.accuracy_score(Y_val_class, y_pred_class)
error = 1 - accuracy
precision = metrics.precision_score(Y_val_class, y_pred_class, average=None)
recall = metrics.recall_score(Y_val_class, y_pred_class, average=None)
F1_score = metrics.f1_score(Y_val_class, y_pred_class, average=None)
print("Results of kNN classifier\n")
print("Accuracy: " + str(accuracy) + "\n" + "Error: " + str(error) + "\n" + "Precision: " + str(precision) + "\n" + "Recall: " + str(recall) + "\n" + "F1 score: " + str(F1_score))
```

Results of kNN classifier

Accuracy: 0.8394648829431438 Error: 0.1605351170568562

Precision: [0.84251969 0.82222222] Recall: [0.96396396 0.48051948] F1 score: [0.89915966 0.60655738]

## In [24]:

```
# task 4 - continuation
# SVM Classifier
classifier = SVC(kernel='rbf')
classifier.fit(x_train_scaled_class, Y_train_class.values.ravel())
svm_class = classifier
```

# In [25]:

```
y_pred_class = classifier.predict(x_val_scaled_class)
```

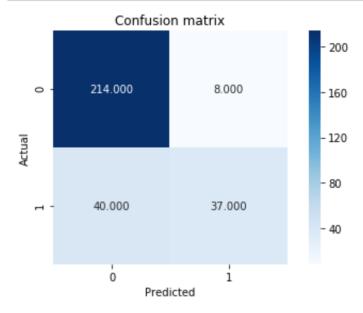
#### In [26]:

```
conf_matrix = metrics.confusion_matrix(Y_val_class, y_pred_class)
print(conf_matrix)
```

```
[[214 8]
[ 40 37]]
```

#### In [27]:

```
sns.heatmap(conf_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Confusion matrix')
plt.tight_layout()
```



# In [28]:

```
accuracy = metrics.accuracy_score(Y_val_class, y_pred_class)
error = 1 - accuracy
precision = metrics.precision_score(Y_val_class, y_pred_class, average=None)
recall = metrics.recall_score(Y_val_class, y_pred_class, average=None)
F1_score = metrics.f1_score(Y_val_class, y_pred_class, average=None)
print("Results of SVM classifier\n")
print("Accuracy: " + str(accuracy) + "\n" + "Error: " + str(error) + "\n" + "Precision: " + str(precision) + "\n" + "Recall: " + str(recall) + "\n" + "F1 score: " + str(F1_score))
```

#### Results of SVM classifier

Accuracy: 0.8394648829431438 Error: 0.1605351170568562

Precision: [0.84251969 0.82222222]
Recall: [0.96396396 0.48051948]
F1 score: [0.89915966 0.60655738]

```
In [29]:
```

```
# task 4
# Decision trees
classifier = DecisionTreeClassifier(criterion="entropy", random_state=0)
classifier.fit(x_train_scaled_class, Y_train_class.values.ravel())
```

## Out[29]:

## In [30]:

```
# Number of nodes in the decision tree
print("Number of nodes in the decision tree: " + str(len(classifier.tree_.__getstate_
_()['nodes'])))
```

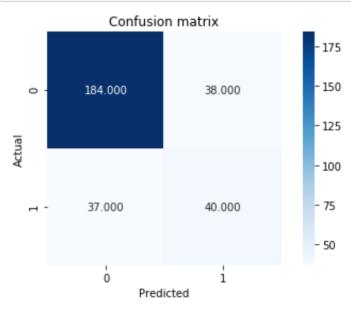
Number of nodes in the decision tree: 227

### In [31]:

```
y_pred_class = classifier.predict(x_val_scaled_class)
```

# In [32]:

```
conf_matrix = metrics.confusion_matrix(Y_val_class, y_pred_class)
sns.heatmap(conf_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Confusion matrix')
plt.tight_layout()
```



```
In [33]:
```

```
accuracy = metrics.accuracy_score(Y_val_class, y_pred_class)
error = 1 - accuracy
precision = metrics.precision_score(Y_val_class, y_pred_class, average=None)
recall = metrics.recall_score(Y_val_class, y_pred_class, average=None)
F1_score = metrics.f1_score(Y_val_class, y_pred_class, average=None)
print("Results of Decision trees classifier\n")
print("Accuracy: " + str(accuracy) + "\n" + "Error: " + str(error) + "\n" + "Precision: " + str(precision) + "\n" + "Recall: " + str(recall) + "\n" + "F1 score: " + str(F1_score))
```

Results of Decision trees classifier

Accuracy: 0.7491638795986622 Error: 0.25083612040133785

Precision: [0.83257919 0.51282051] Recall: [0.82882883 0.51948052] F1 score: [0.83069977 0.51612903]

## In [34]:

```
# task 4
# Naives Bayes Classifier
classifier = GaussianNB()
classifier.fit(x_train_scaled_class, Y_train_class.values.ravel())
```

#### Out[34]:

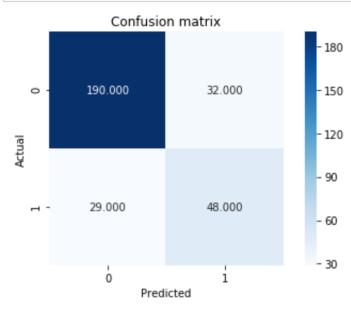
GaussianNB(priors=None, var\_smoothing=1e-09)

#### In [35]:

```
y_pred_class = classifier.predict(x_val_scaled_class)
```

# In [36]:

```
conf_matrix = metrics.confusion_matrix(Y_val_class, y_pred_class)
sns.heatmap(conf_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Confusion matrix')
plt.tight_layout()
```



## In [37]:

```
accuracy = metrics.accuracy_score(Y_val_class, y_pred_class)
error = 1 - accuracy
precision = metrics.precision_score(Y_val_class, y_pred_class, average=None)
recall = metrics.recall_score(Y_val_class, y_pred_class, average=None)
F1_score = metrics.f1_score(Y_val_class, y_pred_class, average=None)
print("Results of Naive Bayes classifier\n")
print("Accuracy: " + str(accuracy) + "\n" + "Error: " + str(error) + "\n" + "Precision: " + str(precision) + "\n" + "Recall: " + str(recall) + "\n" + "F1 score: " + str(F1_score))
```

Results of Naive Bayes classifier

Accuracy: 0.7959866220735786 Error: 0.20401337792642138 Precision: [0.86757991 0.6 ] Recall: [0.85585586 0.62337662] F1 score: [0.861678 0.61146497]

#### In [38]:

# SVM Classifier has the highest accuracy among all the 4 classification methods for the selected predictors.

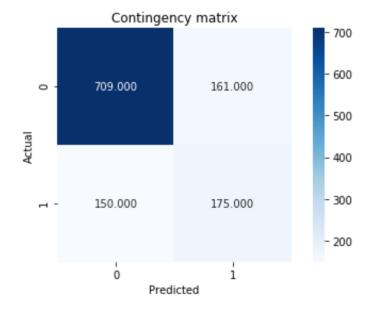
### In [39]:

# Task 5 Start Kmeans 2 clusters all vars

#### In [40]:

```
X = ['Total Population', 'Percent White, not Hispanic or Latino', 'Percent Black, not
Hispanic or Latino', 'Percent Hispanic or Latino', 'Percent Foreign Born', 'Percent Fema
le', 'Percent Age 29 and Under', 'Percent Age 65 and Older', 'Median Household Income',
'Percent Unemployed', 'Percent Less than High School Degree', 'Percent Less than Bachel
or\'s Degree','Percent Rural']
Y = ['Party']
train class = data[X]
lables = data[Y].to_numpy().reshape(-1)
scaler = StandardScaler()
scaler.fit(train_class)
train_scaled_class = scaler.transform(train_class)
clustering = KMeans(n clusters=2, init='random', random state=0).fit(train scaled cla
clusters = clustering.labels_
cont matrix = metrics.cluster.contingency matrix(lables, clusters)
sns.heatmap(cont matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Contingency matrix')
plt.tight_layout()
adjusted rand index = metrics.adjusted rand score(lables, clusters)
silhouette coefficient = np.average(metrics.silhouette samples(train scaled class, cl
usters, metric='euclidean'))
print([adjusted rand index, silhouette coefficient])
```

## [0.19751656022671712, 0.30700290833697047]



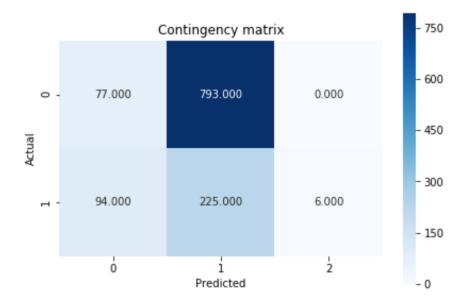
## In [41]:

```
# DB Scan eps = 2 min_samples = 5
clustering = DBSCAN(eps=2,min_samples=5,metric='euclidean').fit(train_scaled_class)
clusters = clustering.labels_

cont_matrix = metrics.cluster.contingency_matrix(lables, clusters)
sns.heatmap(cont_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Contingency matrix')
plt.tight_layout()

adjusted_rand_index = metrics.adjusted_rand_score(lables, clusters)
silhouette_coefficient = np.average(metrics.silhouette_samples(train_scaled_class, clusters, metric='euclidean'))
print([adjusted_rand_index, silhouette_coefficient])
```

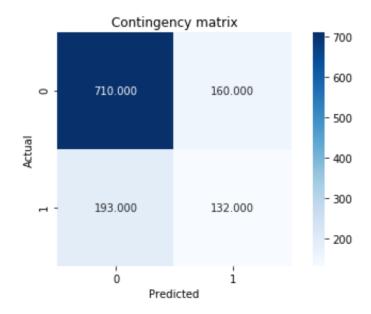
## [0.1577583255755803, 0.31265113101181913]



## In [42]:

```
# Percent White, not Hispanic or Latino', 'Percent Black, not Hispanic or Latino', 'Pe
rcent Hispanic or Latino', 'Percent Foreign Born'
# Kmeans init = 'k-means++' n init = 15
X = ['Percent White, not Hispanic or Latino', 'Percent Black, not Hispanic or Latino'
, 'Percent Hispanic or Latino', 'Percent Foreign Born']
Y = ['Party']
train_class = data[X]
lables = data[Y].to numpy().reshape(-1)
scaler = StandardScaler()
scaler.fit(train class)
train_scaled_class = scaler.transform(train_class)
clustering = KMeans(n_clusters=2, n_init= 15, init='k-means++', random_state=0).fit(t
rain scaled class)
clusters = clustering.labels_
cont matrix = metrics.cluster.contingency matrix(lables, clusters)
sns.heatmap(cont_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Contingency matrix')
plt.tight_layout()
adjusted rand index = metrics.adjusted rand score(lables, clusters)
silhouette coefficient = np.average(metrics.silhouette samples(train scaled class, cl
usters, metric='euclidean'))
print([adjusted rand index, silhouette coefficient])
```

## [0.11911877926404817, 0.5818101112791731]



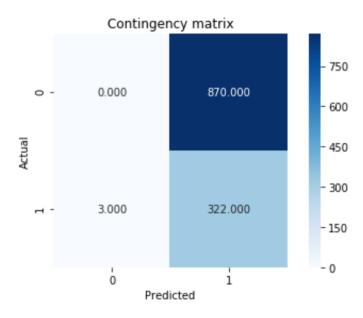
# In [43]:

```
# DB Scan eps = 2 min samples = 8
clustering = DBSCAN(eps=2,min_samples=8,metric='euclidean').fit(train_scaled_class)
clusters = clustering.labels_

cont_matrix = metrics.cluster.contingency_matrix(lables, clusters)
sns.heatmap(cont_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Contingency matrix')
plt.tight_layout()

adjusted_rand_index = metrics.adjusted_rand_score(lables, clusters)
silhouette_coefficient = np.average(metrics.silhouette_samples(train_scaled_class, clusters, metric='euclidean'))
print([adjusted_rand_index, silhouette_coefficient])
```

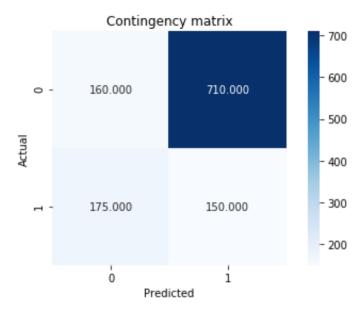
# [0.008414453628750557, 0.7233179178571693]



### In [44]:

```
# 'Total Population', 'Percent White, not Hispanic or Latino', 'Percent Black, not Hi
spanic or Latino', 'Percent Hispanic or Latino', 'Percent Foreign Born', 'Percent Femal
e', 'Percent Age 29 and Under', 'Percent Age 65 and Older', 'Median Household Income', 'P
ercent Unemployed', 'Percent Less than High School Degree', 'Percent Less than Bachelor
\'s Degree', 'Percent Rural'
# Kmeans init = 'k-means++' n init = 15
X = ['Total Population', 'Percent White, not Hispanic or Latino', 'Percent Black, not
Hispanic or Latino', 'Percent Hispanic or Latino', 'Percent Foreign Born', 'Percent Fema
le', 'Percent Age 29 and Under', 'Percent Age 65 and Older', 'Median Household Income',
'Percent Unemployed', 'Percent Less than High School Degree', 'Percent Less than Bachel
or\'s Degree', 'Percent Rural']
train class = data[X]
lables = data[Y].to_numpy().reshape(-1)
scaler = StandardScaler()
scaler.fit(train class)
train_scaled_class = scaler.transform(train_class)
clustering = KMeans(n clusters=2, n init= 15, init='k-means++', random state=0).fit(t
rain scaled class)
clusters = clustering.labels
cont matrix = metrics.cluster.contingency matrix(lables, clusters)
sns.heatmap(cont matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Contingency matrix')
plt.tight layout()
adjusted rand index = metrics.adjusted rand score(lables, clusters)
silhouette_coefficient = np.average(metrics.silhouette_samples(train_scaled_class, cl
usters, metric='euclidean'))
print([adjusted_rand_index, silhouette_coefficient])
```

# [0.19893799165776016, 0.30691597445230206]



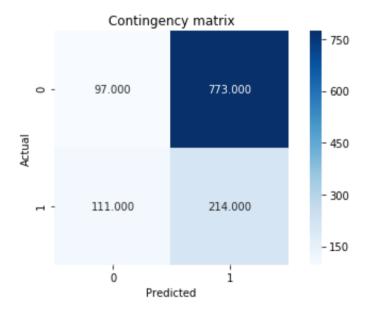
# In [45]:

```
# DB Scan eps =2 min samples =8
clustering = DBSCAN(eps=2,min_samples=8,metric='euclidean').fit(train_scaled_class)
clusters = clustering.labels_

cont_matrix = metrics.cluster.contingency_matrix(lables, clusters)
sns.heatmap(cont_matrix, annot = True, fmt = ".3f", square = True, cmap = plt.cm.Blue
s)
plt.ylabel('Actual')
plt.xlabel('Predicted')
plt.title('Contingency matrix')
plt.tight_layout()

adjusted_rand_index = metrics.adjusted_rand_score(lables, clusters)
silhouette_coefficient = np.average(metrics.silhouette_samples(train_scaled_class, clusters, metric='euclidean'))
print([adjusted_rand_index, silhouette_coefficient])
```

## [0.15489854564128577, 0.3468850007721493]



# In [46]:

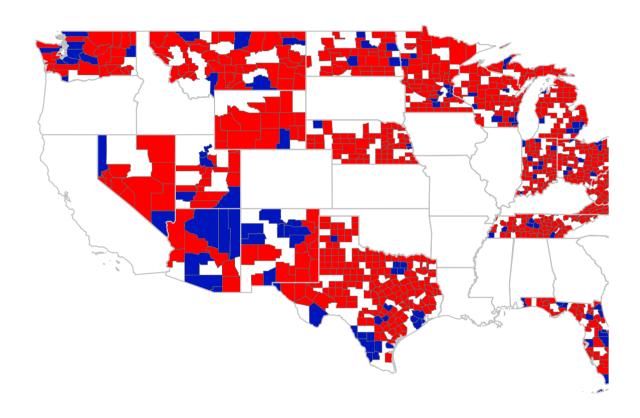
```
# task 6
X = ['Percent White, not Hispanic or Latino', 'Percent Black, not Hispanic or Latino'
, 'Percent Hispanic or Latino', 'Percent Age 29 and Under', 'Percent Age 65 and Olde
r', 'Percent Less than High School Degree', 'Percent Less than Bachelor\'s Degree',
'Percent Rural']
_data = data[X]
_fips = data[['FIPS']]
scaler = StandardScaler()
scaler.fit(_data)
scaled_data = scaler.transform(_data)
party = svm_class.predict(scaled_data).tolist()
fips = _fips.values
colorscale = ["#ff0000","#0015bc"]
fig = create_choropleth(fips=fips, values=party, colorscale=colorscale, county_outlin
e={'color': 'rgb(105,105,105)', 'width': 0.25}, state outline={'color': 'rgb(192,192,
192)','width': 1})
fig.layout.template = None
fig.show()
```

//anaconda3/lib/python3.7/site-packages/pandas/core/frame.py:6692: Futur
eWarning:

Sorting because non-concatenation axis is not aligned. A future version of pandas will change to not sort by default.

To accept the future behavior, pass 'sort=False'.

To retain the current behavior and silence the warning, pass 'sort=Tru e'.



### In [48]:

```
# task 7
test data = pd.read csv("demographics test.csv")
scaler.fit(X train)
x test scaled = scaler.transform(test data[Xvariables])
model = linear_model.Lasso(alpha=1).fit(X=X_train_dummy, y=Y_train['Democratic'])
dem predicted = model.predict(x test scaled)
dem_predicted = dem_predicted.astype(int)
model = linear_model.Lasso(alpha=1).fit(X=X_train_dummy, y=Y_train['Republican'])
rep_predicted = model.predict(x_test_scaled)
rep predicted = rep predicted.astype(int)
class test = test_data.iloc[:, [4, 5, 6, 9, 10, 13, 14, 15]]
scaler.fit(class test)
class test scaled = scaler.transform(class test)
test pred = svm class.predict(class test scaled)
a = np.array([test_data['State'], test_data['County'], dem_predicted, rep_predicted,
test pred1)
a = np.column stack(a)
np.savetxt("output.csv", a, delimiter=',', header="State,County,Democratic,Republica")
n,Party", fmt="%s", comments="")
# the output of this task is stored in the file 'output.csv'
```