Recurrent Neural Networks and Sentence Representations

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Overview and Objectives. In this homework, we'll get more familiar with LSTMs by doing a bit of math, interacting with simple versions in toy settings, and then move on to developing a full pipeline for part-of-speech tagging in English with a Bidirectional LSTM.

How to Do This Assignment. The assignment walks you through completing the provided skeleton code and analyzing some of the results. Anything requiring you to do something is marked as a "Task" and has associated points listed with it. You are expected to turn in both your code and a write-up answering any task that requested written responses. Submit a zip file containing your completed skeleton code and a PDF of your write-up to Canvas.

Advice. Start early. Students will need to become familiar with pytorch for this and future assignments. Extra time may be needed to get used to working remotely on the GPU cluster here. You can also use GPU-enabled runtimes in Colab colab.research.google.com.

Demystifying Recurrent Neural Networks [5pt]

1.1 Hand Designing A Network for Parity

Consider a univariate LSTM defined given the following equations. We refer to this model as univariate because all inputs, outputs, and weights are scalars. $\sigma(\cdot)$ is a sigmoid activation.

$$i_t = \sigma(w_{ix}x_t + w_{ih}h_{t-1} + b_i) \tag{1}$$

$$f_t = \sigma(w_{fx}x_t + w_{fh}h_{t-1} + b_f) \tag{2}$$

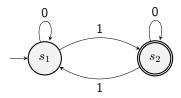
$$o_t = \sigma(w_{ox}x_t + w_{oh}h_{t-1} + b_o) \tag{3}$$

$$g_t = \tanh(w_{qx}x_t + w_{qh}h_{t-1} + b_q) \tag{4}$$

$$c_t = f_t c_{t-1} + i_t g_t (5)$$

$$h_t = o_t \tanh(c_t) \tag{6}$$

To ground this complicated looking model, we will consider a simple sequence classification problem – parity of binary strings. Given an arbitrarily-long binary string $b \in \{0,1\}^*$, classify whether it has an even or odd number of ones. For example all these strings have an even parity – " ", 0000, 101101 – and these an odd parity – 1, 0011001, 00011100. Below is a simple DFA¹ that accepts strings with odd parity at the accepting state s_2 . As it only has two states, it seems solving the parity classification problem only requires storing 1 bit of information in memory.



Another way to think about this computation is as a recursive application of XOR over time. If the parity up to element t-1 is 1 (odd) and we see a 1 for element t, the updated parity is 1 XOR 1=0 (even). Likewise, if at time t+1 we observe another 1, 0 XOR 1=1. In other words, PARITY(X,t)=X[t] XOR PARITY(X,t-1) and PARITY(X,t)=0 by definition. This sounds like the sort of operation we can do with an LSTM!

 $^{^{1} \}verb|https://en.wikipedia.org/wiki/Deterministic_finite_automaton$

TASK 1.1 [5 pt] Manually find weights and biases for the univariate LSTM defined above such that the final hidden state will be greater than or equal to 0.5 for odd parity strings and less than 0.5 for even parity. The parameters you must provide values for are w_{ix} , w_{ih} , b_i , w_{fx} , w_{fh} , b_f , w_{ox} , w_{oh} , b_o , w_{gx} , w_{gh} , b_g and are all scalars. The LSTM will take one bit of the string (0 or 1) as input x at each time step. A tester is set up in univariate_tester.py where you can enter your weights and check performance.

Hints: Some of the weights will likely be zero. Others may be large. Scale matters, larger weights will saturate the activation functions. Also note that A XOR B can be written as (A OR B) AND (A NAND B). Work backwards and try to find where this sort of two-term structure could be implemented.

Through this exercise, we've shown that a 1-dimensional LSTM is sufficient to solve parity of binary strings of arbitrary length. In the next section, we'll try to actually train an LSTM for this task. Hint: It may be harder than you think.

2 Learning to Copy Finite State Machines [10pt]

Let's probe LSTMs a bit by making them mimic simple finite state machines. The rest of this assignment will work within the PyTorch deep learning framework. You'll need to install PyTorch in your development environment.

2.1 Parity: Examining Generalization To Longer Sequences

First, lets try to train an LSTM to perform the parity task we just did manually. The driver_parity.py file provide skeleton code for these experiments including a parity dataset shown below. During training, it generates all binary strings of length 0 to max_length. At inference, it generates all binary strings of length max_length.

```
class Parity(Dataset):
      def __init__(self,split="train", max_length=4):
   if split=="train":
3
           self.data = []
           for i in range(1, max_length+1):
6
             self.data += [torch.FloatTensor(seq) for seq in itertools.product
       ([0,1], repeat=i)]
         else:
           self.data = [torch.FloatTensor(seq) for seq in itertools.product
9
       ([0,1], repeat=max_length)]
10
       def __len__(self):
           return len(self.data)
12
13
14
      def __getitem__(self, idx):
           x = self.data[idx]
15
           y = x.sum() \% 2
           return x,y
17
```

Listing 2: Parity Dataset

To train our network, we can build a DataLoader from our Parity dataset (see below). However, our dataset contains strings of variable length so we need to pass a custom function to our data loader describing how to combine elements in a sampled batch together.

```
train = Parity(split='train', max_length=max_length)
train_loader = DataLoader(train, batch_size=B, shuffle=True,
collate_fn=pad_collate)
```

Listing 3: Data loader

Our pad_collate function puts all the elements of a batch in a $B \times T_{\text{max}}$ tensor for inputs and a B tensor for outputs where T_{max} is the largest length in the batch. Shorter sequences are zero-padded. A batch of inputs looks like:

Listing 4: Example input for a batc

The architecture I used

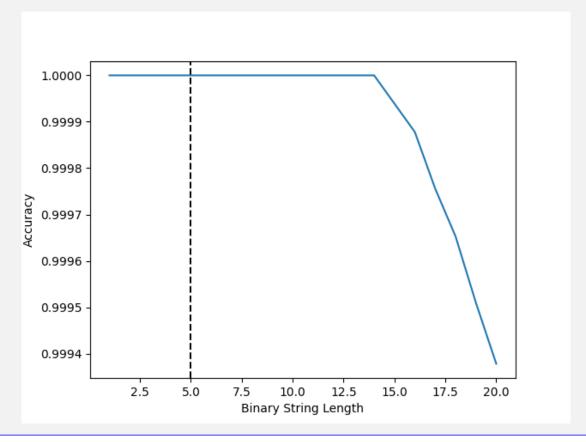
TASK 2.1 [5 pt] Implement the ParityLSTM class in driver_parity.py. Your model's forward function should process the batch of binary input strings and output a $B \times 2$ tensor y where $y_{b,0}$ is the score for the b^{th} element of the batch having an even parity and $y_{b,1}$ for odd parity. You may use any PyTorch-defined LSTM functions. Larger hidden state sizes will make for easier training in my experiments. Running driver_parity.py will train your model and output per-epoch training loss and accuracy. A correctly-implemented model should approach 100% accuracy on the training set. In your write-up for this question, describe any architectural choices you made.

Hint: Efficiently processing batches with variable input lengths requires some bookkeeping or else the LSTM will continue to process the padding for shorter sequences along with the content of longer ones. See pack padded sequence and pad packed sequence documentation in PyTorch.

The architecture that I used was as LSTM followed by a linear transformation. I used varying hidden dimension sizes in the LSTM and got optimal performance with a hidden dimension size of 64 (more on that in Task 2.3). The LSTM in Pytorch was configured with only one layer as performance degraded with more than 2 layers.

TASK 2.2 [1 pt] driver_parity.py also evaluates your trained model on binary sequences of length 0 to 20 and saves a corresponding plot of accuracy vs. length. Include this plot in your write-up and describe the trend you observe. Why might the model behave this way?

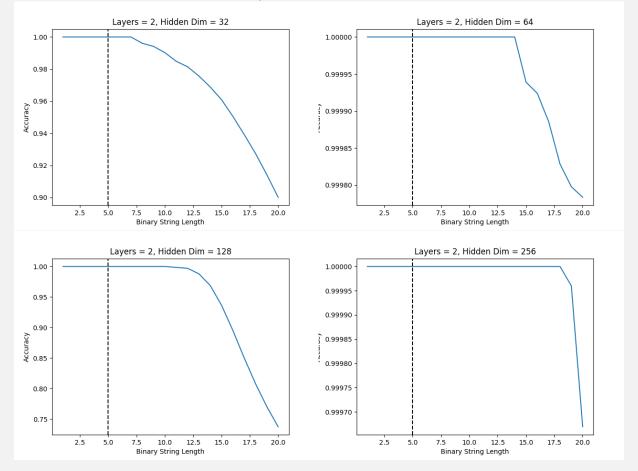
The plot below shows the performance for a single layer LSTM with 64 hidden dimensions. The model is perfect to 15 digits and nearly perfect to 20 digits (performance degrades less than one percent). The reason for the slight drop-off is that 20 digits is starting to push the limits of its memory, but the near perfrect performance is still acceptable.



TASK 2.3 [3 pt] We know from 1.1 that even a univariate LSTM (one with a scalar hidden state) can theoretically solve this problem. Run a few (3-4) experiments with different hidden state sizes, what is the smallest size for which you can still train to fit this dataset? Feel free to adjust any of the hyper-parameters in the optimization in the train_model function if you want. Describe any trends you saw in training or the generalization experiment as you reduced the model capacity.

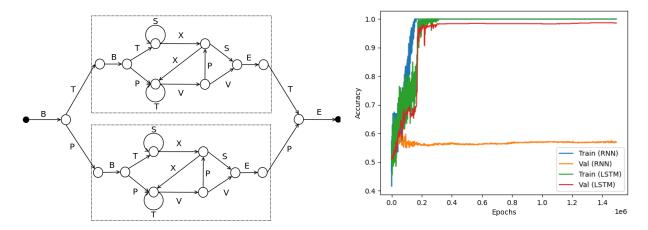
Note: In developing this assignment, I never successfully got it down to a hidden dimension of 1. Lower dimensional settings tended to be sensitive to batch size and learning rate. Don't spend all night tuning this unless you've finished the rest of the assignment and have nothing better to do.

For these experiments, I increased the number of layers in the LSTM from one to two. The performance of a single layer was 'too good' and could achieve perfect or near perfect results, so I wanted to see some variation in results with different hidden dimensions. There are four plots below, with hidden dimensions of 32, 64, 128, and 256. Interestingly, the performance significantly increased from 32 to 64 but fell off sharply at 128 and then returned to near perfect with 256 hidden dimensions. The trend would be more obvious if the plots were consolidated into one, but I did not have time to rework the infrastructure, so they remain as separate plots. My takeaway from this is that hidden dimension size is yet another hyperparamter than can be tuned for performance and a trend in one direction may not continue indefinitely (as was seen in the drastic performance changes from 64 to 128 to 256).



2.2 Embedded Reber Grammars: Thinking About Memory

Next we turn to recognizing an Embedded Reber Grammar (ERG). An ERG generation diagram is shown below. To generate an ERG string, start from the leftmost black node and sample any outgoing edge (only B in this case) and write down the letter of that edge. Repeat this process from the new node until reaching the right-most black node through the edge labelled E. So BTBTSSXSETE is a valid ERG string. Notice that the sub-networks in dashed boxes are identical for the upper and lower branch. These are the Reber Grammars that are embedded in this larger grammar. To make longer strings, the dashed boxes can be repeated k times (E edge returns to start) before exiting to the T/P edges headed towards the terminal node on the right.



The plot on the right shows train and validation accuracy over training for an LSTM and vanila RNN on the task of identifying ERG strings with k=4. An example string from this grammar is BTBTXSEBTXSEBPVVEBTXXVVETE. Breaking it out, its easy to see the structure – BT BTXSE BTXSE BPVVE BTXXVVE TE – as a prefix, four repeated Reber Grammar strings, and a suffix. The dataset contained 50% positives samples, 25% negative with a random perturbation of one character, and 25% negatives with the second-to-last letter perturbed. In this setting, the vanilla RNN model overfit to the training set given sufficient time, but failed to generalize. In contrast, the LSTM model generalized well to the test set.

▶ TASK 2.4 [1 pt] It has been demonstrated that vanilla RNNs have a hard time learning to classify whether a string was generated by an ERG or not. LSTMs on the other hand seem to work fine. Based on the structure of the problem and what you know about recurrent networks, why might this be the case?

The vanilla RNN is unable to generalize because of its lack of memory compared to the LSTM. The grammar is setup so that the second to last letter depends on the second letter (both must either be a T or P to be valid strings). To adequately categorize an input string, the RNN would need to have both characters in memory at the same time, but vanilla RNNs are unable to do this, hence their poor performance on validation data.

Part-of-Speech Tagging [15pt]

Now lets get to work on a real problem – part-of-speech tagging in English. This is a many-to-many sequence problem where each word in an input must be labelled with a corresponding part-of-speech tag. The goal of this section will be to train a bidirectional LSTM model for this task. Unlike in the previous sections, no skeleton code will be provided and students are responsible for building the whole pipeline including text processing, data loading, model design, training, and evaluation. Feel free to use any libraries you wish to accomplish this.

We will be using the Universal Dependencies² English Part-Of-Speech (UDPOS) benchmark. The easiest way to load this dataset is through the torchtext module. The code below loads the dataset and prints out an example.

 $^{^2 \}rm https://universal dependencies.org/$

Listing 5: Loading the UD En POS benchmark

```
> visualizeSentenceWithTags(vars(train_data.examples[997]))

Token POS Tag

they PRON
are AUX
doing VERB
it PRON
deliberately ADV
10. PUNCT
```

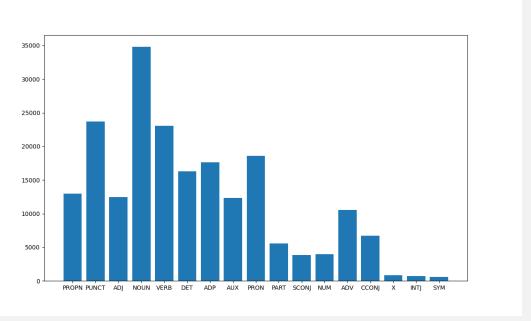
Listing 6: Visualizing a sentence and its associated list of tags.

Notice that there is a train, validation, and test split of the dataset. We should only evaluate on test once when we are completely done tuning our model on validation and are looking to report final results.

► TASK 3.1 [2 pt] The first step for any machine learning problem is to get familiar with the dataset. Read through random samples of the dataset and summarize what topics it seems to cover. Also look at the relationship between words and part-of-speech tags — what text preprocessing would be appropriate or inappropriate for this dataset? Produce a histogram of part-of-speech tags in the dataset — is it balanced between all tags? What word-level accuracy would a simple baseline that picked the majority label achieve?

The topics seem to focus on new stories, particularly about conflict in the Middle East. The content seemed to cover both the actual articles, including recounts and interviews but also some comments by readers of the articles.

A histogram of the tags can be seen here:



As you can see, the dominating part of speech is noun, followed by punctuation and verbs. When the counts of nouns are simplified/condensed with other nouns (proper nonns, pronouns), this accounts for nearly a third of the entries.

You will need to get the dataset into a form that we can use in a model – i.e. numeralized batches of sequences and their labels. Simple examples of dataset classes and dataloaders that rely on our Vocabulary code from last assignment have been demonstrated in lecture. Another option is to look into the torchtext.data APIs which can flexibly handle text datasets like this one and take care of tokenization / numeralization with less effort – provided you spend the time learning the API. Either way is fine for this assignment.

The next step is to implement your model and the training routine. The lectures and other skeleton code in this assignment should provide a good starting point for these. If you run into trouble, printing out the shapes of tensors and reading the PyTorch documentation can be very helpful. A useful development strategy is to operate only on a single batch at first – if your model can't quickly fit the batch, something is wrong. Once you get a basic model running, you'll want to tune parameters and network structure to achieve good validation accuracy.

TASK 3.2 [10 pt] Create a file driver_udpos.py that implements and trains a bidirectional LSTM model on this dataset with cross entropy loss. The BiLSTM should predict an output distribution over the POS tags for each token in a sentence. In your written report, produce a graph of training and validation loss over the course of training. Your model should be able to achieve >70% per-word accuracy fairly easily.

To achieve stronger performance, you will likely need to tune hyper-parameters or model architecture to achieve lower validation loss. Using pretrained word vectors will likely help as well. You may also wish to employ early-stopping – regularly saving the weights of your model during training and then selecting the saved model with the lowest validation loss. In your report, describe any impactful decisions during this process. Importantly – DO NOT EVALUATE ON TEST DURING THIS TUNING PROCESS.

Once you are done finetuning, evaluate on the test split of the data and report the per-word accuracy.

I made some progress on the LSTMTagger module but had some issues with training. My accuracy calculation was not correct and I ran out of time/energy before the deadline. I was utlimately unable to train/validate the LSTM, but turning in my progress. I will attend office hours to debug issues and find where I mis-stepped.

▶ TASK 3.3 [3 pt] Implement a function tag_sentence(sentence, model) that processes an input sentence (a string) into a sequence of POS tokens. This will require you to tokenize/numeralize the sentence, pass it through your network, and then print the result. Use this function to tag the following sentences:

The old man the boat.

The complex houses married and single soldiers and their families.

The man who hunts ducks out on weekends.