# trabalho2

January 12, 2025

# 1 Mineração de Dados

Prof. Dr. Sergio N. Simões Pós-graduação em Desenvolvimento de Aplicações Inteligentes Mineração de Dados — Trabalho 02

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The Boston Housing Dataset

The Boston Housing Dataset is a derived from information collected by the U.S. Census Service concerning housing in the area of Boston MA. The following describes the dataset columns:

- CRIM per capita crime rate by town
- ZN proportion of residential land zoned for lots over 25,000 sq.ft.
- INDUS proportion of non-retail business acres per town.
- CHAS Charles River dummy variable (1 if tract bounds river; 0 otherwise)
- NOX nitric oxides concentration (parts per 10 million)
- RM average number of rooms per dwelling
- AGE proportion of owner-occupied units built prior to 1940
- DIS weighted distances to five Boston employment centres
- RAD index of accessibility to radial highways
- TAX full-value property-tax rate per \$10,000
- PTRATIO pupil-teacher ratio by town
- B 1000(Bk 0.63)<sup>2</sup> where Bk is the proportion of blacks by town
- LSTAT % lower status of the population
- MEDV Median value of owner-occupied homes in \$1000's

```
[2]: #print(os.listdir("../input"))
     #Lets load the dataset and sample some
     column_names = ['CRIM', 'ZN', 'INDUS', 'CHAS', 'NOX', 'RM', 'AGE', 'DIS', _
      →'RAD', 'TAX', 'PTRATIO', 'B', 'LSTAT', 'MEDV']
     #data = read csv('../input/housing.csv', header=None, delimiter=r"\s+",,,
      ⇔names=column_names)
     data = read_csv('./housing.csv', header=None, delimiter=r"\s+",_
      →names=column_names)
     print(data.head(5))
          CRIM
                   ZN
                       INDUS
                              CHAS
                                      NOX
                                               RM
                                                    AGE
                                                             DIS
                                                                  RAD
                                                                         TAX
    0 0.00632
                18.0
                        2.31
                                 0 0.538
                                            6.575
                                                   65.2
                                                         4.0900
                                                                    1
                                                                       296.0
      0.02731
                        7.07
                                 0 0.469
                                            6.421
                                                   78.9
                                                        4.9671
                                                                       242.0
    1
                  0.0
                                                                    2
    2 0.02729
                        7.07
                                 0 0.469
                                                         4.9671
                                                                    2
                                                                       242.0
                  0.0
                                           7.185
                                                   61.1
    3 0.03237
                        2.18
                                 0 0.458
                                            6.998
                                                   45.8
                                                         6.0622
                                                                    3
                                                                       222.0
                  0.0
      0.06905
                  0.0
                        2.18
                                   0.458
                                            7.147
                                                   54.2
                                                         6.0622
                                                                       222.0
       PTRATIO
                      B LSTAT
                                MEDV
                          4.98
    0
          15.3 396.90
                                24.0
    1
          17.8 396.90
                          9.14
                                21.6
    2
          17.8 392.83
                          4.03
                                34.7
    3
          18.7 394.63
                          2.94
                                33.4
    4
          18.7 396.90
                          5.33
                                36.2
[3]: # Dimension of the dataset
     print(np.shape(data))
    (506, 14)
[4]: | # Let's summarize the data to see the distribution of data
     print(data.describe())
                  CRIM
                                ZN
                                          INDUS
                                                       CHAS
                                                                     NOX
                                                                                  RM
           506.000000
                        506.000000
                                    506.000000
                                                 506.000000
                                                             506.000000
                                                                          506.000000
    count
             3.613524
                         11.363636
                                      11.136779
                                                   0.069170
                                                                0.554695
                                                                            6.284634
    mean
                         23.322453
    std
             8.601545
                                      6.860353
                                                   0.253994
                                                                0.115878
                                                                            0.702617
             0.006320
                          0.000000
                                      0.460000
                                                   0.000000
                                                                0.385000
                                                                            3.561000
    min
    25%
                          0.000000
                                                   0.000000
             0.082045
                                      5.190000
                                                                0.449000
                                                                            5.885500
    50%
             0.256510
                          0.000000
                                      9.690000
                                                   0.000000
                                                                0.538000
                                                                            6.208500
    75%
                         12.500000
                                                   0.000000
                                                                0.624000
             3.677083
                                      18.100000
                                                                            6.623500
            88.976200
                        100.000000
                                      27.740000
                                                   1.000000
                                                                0.871000
                                                                            8.780000
    max
                   AGE
                               DIS
                                            RAD
                                                        TAX
                                                                 PTRATIO
                                                                                   В
    count
           506.000000
                        506.000000
                                    506.000000
                                                 506.000000
                                                             506.000000
                                                                          506.000000
    mean
            68.574901
                          3.795043
                                      9.549407
                                                 408.237154
                                                               18.455534
                                                                          356.674032
    std
            28.148861
                          2.105710
                                      8.707259
                                                 168.537116
                                                                2.164946
                                                                           91.294864
```

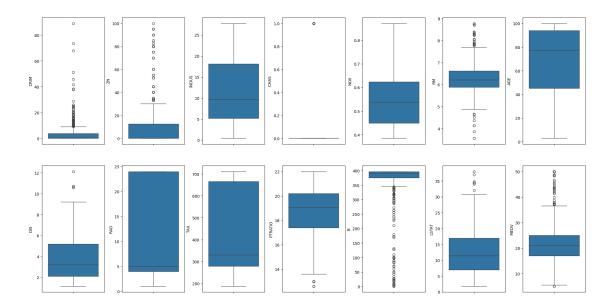
```
2.900000
                      1.129600
                                   1.000000
                                              187.000000
                                                            12.600000
                                                                          0.320000
min
25%
        45.025000
                      2.100175
                                   4.000000
                                              279.000000
                                                            17.400000
                                                                       375.377500
50%
        77.500000
                      3.207450
                                   5.000000
                                              330.000000
                                                            19.050000
                                                                       391.440000
75%
                                  24.000000
                                              666.000000
                                                            20.200000
                                                                       396.225000
        94.075000
                      5.188425
                                  24.000000
                                              711.000000
max
       100.000000
                     12.126500
                                                            22.000000
                                                                       396.900000
            LSTAT
                          MEDV
count
       506.000000
                    506.000000
        12.653063
                     22.532806
mean
std
         7.141062
                      9.197104
         1.730000
                      5.000000
min
25%
         6.950000
                     17.025000
50%
        11.360000
                     21.200000
75%
                     25.000000
        16.955000
max
        37.970000
                     50.000000
```

From get-go, two data coulmns show interesting summeries. They are: ZN (proportion of residential land zoned for lots over 25,000 sq.ft.) with 0 for 25th, 50th percentiles. Second, CHAS: Charles River dummy variable (1 if tract bounds river; 0 otherwise) with 0 for 25th, 50th and 75th percentiles. These summeries are understandable as both variables are conditional + categorical variables. First assumption would be that these coulms may not be useful in regression task such as predicting MEDV (Median value of owner-occupied homes).

Another interesing fact on the dataset is the max value of MEDV. From the original data description, it says: Variable #14 seems to be censored at 50.00 (corresponding to a median price of \$50,000). Based on that, values above 50.00 may not help to predict MEDV. Let's plot the dataset and see interesting trends/stats.

```
[5]: import seaborn as sns
import matplotlib.pyplot as plt
from scipy import stats

fig, axs = plt.subplots(ncols=7, nrows=2, figsize=(20, 10))
index = 0
axs = axs.flatten()
for k,v in data.items():
    sns.boxplot(y=k, data=data, ax=axs[index])
    index += 1
plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=5.0)
```



Columns like CRIM, ZN, RM, B seems to have outliers. Let's see the outliers percentage in every column.

Column RM outliers = 5.93%

Column AGE outliers = 0.00%

Column DIS outliers = 0.99%

Column RAD outliers = 0.00%

Column TAX outliers = 0.00%

Column PTRATIO outliers = 2.96%

Column B outliers = 15.22%

Column LSTAT outliers = 1.38%

Column MEDV outliers = 7.91%

Let's remove MEDV outliers (MEDV = 50.0) before plotting more distributions

```
[7]: data = data[~(data['MEDV'] >= 50.0)]
print(np.shape(data))
```

```
(490, 14)
```

Let's see how these features plus MEDV distributions looks like

```
[8]: fig, axs = plt.subplots(ncols=7, nrows=2, figsize=(20, 10))
index = 0
axs = axs.flatten()
for k,v in data.items():
    sns.distplot(v, ax=axs[index])
    index += 1
plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=5.0)
```

/var/folders/0v/yq16f3tn4rj4w6jh3tnsp47m0000gp/T/ipykernel\_22929/2662893558.py:5 : UserWarning:

`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

```
sns.distplot(v, ax=axs[index])
```

/var/folders/0v/yq16f3tn4rj4w6jh3tnsp47m0000gp/T/ipykernel\_22929/2662893558.py:5
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sns.distplot(v, ax=axs[index])

 $\label{lem:condition} $$ \sqrt{\gamma_16f3tn4rj4w6jh3tnsp47m0000gp/T/ipykernel_22929/2662893558.py:5 : UserWarning:$ 

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/var/folders/0v/yq16f3tn4rj4w6jh3tnsp47m0000gp/T/ipykernel\_22929/2662893558.py:5

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For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

sns.distplot(v, ax=axs[index])

 $\label{lem:condition} $$ \sqrt{\gamma_1663} + \frac{1}{4} 6jh3 + \frac{1}{4} 6jh3$ 

`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

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For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

sns.distplot(v, ax=axs[index])

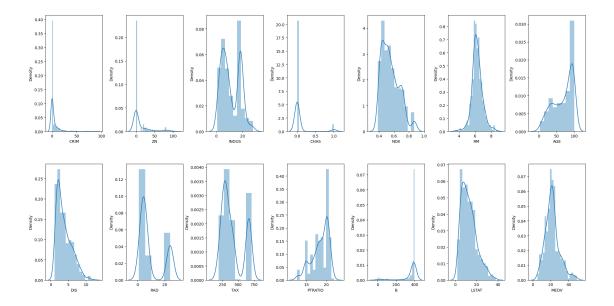
 $\label{lem:condition} $$ \sqrt{\gamma_16f3tn4rj4w6jh3tnsp47m0000gp/T/ipykernel_22929/2662893558.py:5 : UserWarning:$ 

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sns.distplot(v, ax=axs[index])

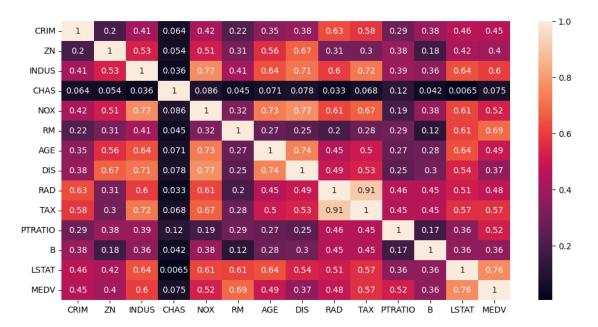


The histogram also shows that columns CRIM, ZN, B has highly skewed distributions. Also MEDV looks to have a normal distribution (the predictions) and other columns seem to have norma or bimodel distribution of data except CHAS (which is a discrete variable).

Now let's plot the pairwise correlation on data.

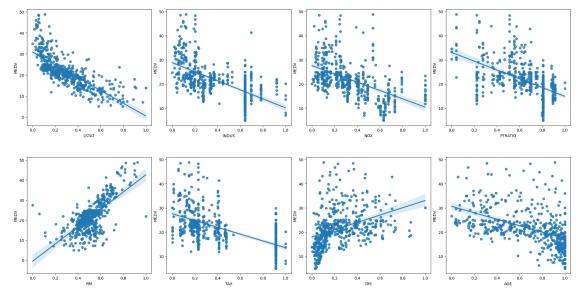
```
[9]: plt.figure(figsize=(12, 6))
sns.heatmap(data.corr().abs(), annot=True)
```

[9]: <Axes: >



From correlation matrix, we see TAX and RAD are highly correlated features. The columns LSTAT, INDUS, RM, TAX, NOX, PTRAIO has a correlation score above 0.5 with MEDV which is a good indication of using as predictors. Let's plot these columns against MEDV.

```
[10]: from sklearn import preprocessing
# Let's scale the columns before plotting them against MEDV
min_max_scaler = preprocessing.MinMaxScaler()
column_sels = ['LSTAT', 'INDUS', 'NOX', 'PTRATIO', 'RM', 'TAX', 'DIS', 'AGE']
x = data.loc[:,column_sels]
y = data['MEDV']
x = pd.DataFrame(data=min_max_scaler.fit_transform(x), columns=column_sels)
fig, axs = plt.subplots(ncols=4, nrows=2, figsize=(20, 10))
index = 0
axs = axs.flatten()
for i, k in enumerate(column_sels):
    sns.regplot(y=y, x=x[k], ax=axs[i])
plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=5.0)
```



So with these analsis, we may try predict MEDV with 'LSTAT', 'INDUS', 'NOX', 'PTRATIO', 'RM', 'TAX', 'DIS', 'AGE' features. Let's try to remove the skewness of the data trough log transformation.

```
[11]: y = np.log1p(y)
for col in x.columns:
    if np.abs(x[col].skew()) > 0.3:
        x[col] = np.log1p(x[col])
```

Let's try Linear, Ridge Regression on dataset first.

```
[12]: from sklearn import datasets, linear_model
      from sklearn.model_selection import cross_val_score
      from sklearn.model_selection import KFold
      import numpy as np
      1_regression = linear_model.LinearRegression()
      kf = KFold(n splits=10)
      min_max_scaler = preprocessing.MinMaxScaler()
      x scaled = min max scaler.fit transform(x)
      scores = cross_val_score(l_regression, x_scaled, y, cv=kf,__
       ⇔scoring='neg_mean_squared_error')
      print("MSE: %0.2f (+/- %0.2f)" % (scores.mean(), scores.std()))
      scores_map = {}
      scores_map['LinearRegression'] = scores
      l_ridge = linear_model.Ridge()
      scores = cross val score(l ridge, x scaled, y, cv=kf,

¬scoring='neg_mean_squared_error')
      scores map['Ridge'] = scores
      print("MSE: %0.2f (+/- %0.2f)" % (scores.mean(), scores.std()))
      # Lets try polinomial regression with L2 with degree for the best fit
      from sklearn.pipeline import make_pipeline
      from sklearn.preprocessing import PolynomialFeatures
      #for degree in range(2, 6):
          model = make_pipeline(PolynomialFeatures(degree=degree), linear_model.
       \hookrightarrow Ridge())
           scores = cross_val_score(model, x_scaled, y, cv=kf,_
       ⇒scoring='neg_mean_squared_error')
          print("MSE: %0.2f (+/- %0.2f)" % (scores.mean(), scores.std()))
      model = make pipeline(PolynomialFeatures(degree=3), linear model.Ridge())
      scores = cross_val_score(model, x_scaled, y, cv=kf,__
       ⇔scoring='neg_mean_squared_error')
      scores_map['PolyRidge'] = scores
      print("MSE: %0.2f (+/- %0.2f)" % (scores.mean(), scores.std()))
```

```
MSE: -0.04 (+/- 0.04)
MSE: -0.04 (+/- 0.04)
MSE: -0.03 (+/- 0.03)
```

The Liner Regression with and without L2 regularization does not make significant difference is MSE score. However polynomial regression with degree=3 has a better MSE. Let's try some non prametric regression techniques: SVR with kernal rbf, DecisionTreeRegressor, KNeighborsRegressor etc.

```
[13]: from sklearn.svm import SVR from sklearn.model_selection import GridSearchCV
```

MSE: -0.04 (+/-0.03)

```
[14]: from sklearn.tree import DecisionTreeRegressor

desc_tr = DecisionTreeRegressor(max_depth=5)
#grid_sv = GridSearchCV(desc_tr, cv=kf, param_grid={"max_depth" : [1, 2, 3, 4, \subseteq 5, 6, 7]}, scoring='neg_mean_squared_error')
#grid_sv.fit(x_scaled, y)
#print("Best classifier :", grid_sv.best_estimator_)
scores = cross_val_score(desc_tr, x_scaled, y, cv=kf, \subseteq scoring='neg_mean_squared_error')
scores_map['DecisionTreeRegressor'] = scores
print("MSE: %0.2f (+/- %0.2f)" % (scores.mean(), scores.std()))
```

MSE: -0.05 (+/-0.04)

KNN Accuracy: -0.04 (+/- 0.02)

Compared to three models which are shosen through grid search, SVR performes better. Let's try an ensemble method finally.

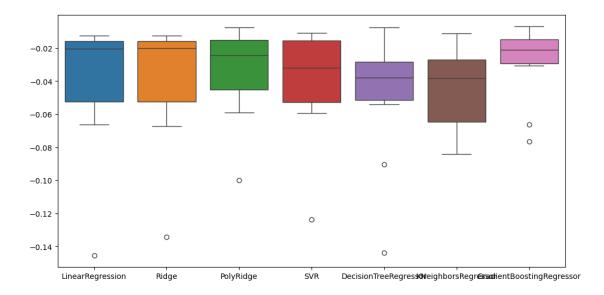
```
#grid_sv = GridSearchCV(gbr, cv=kf, param_grid=param_grid, \( \begin{align*} \pm scoring='neg_mean_squared_error' \)
#grid_sv.fit(x_scaled, y)
#print("Best classifier:", grid_sv.best_estimator_)
scores = cross_val_score(gbr, x_scaled, y, cv=kf, \( \begin{align*} \pm scoring='neg_mean_squared_error' \)
scores_map['GradientBoostingRegressor'] = scores
print("MSE: %0.2f (+/- %0.2f)" % (scores.mean(), scores.std()))
```

MSE: -0.03 (+/-0.02)

Let's plot k-fold results to see which model has better distribution of results. Let's have a look at the MSE distribution of these models with k-fold=10

```
[17]: plt.figure(figsize=(12, 6))
scores_map = pd.DataFrame(scores_map)
sns.boxplot(data=scores_map)
```

### [17]: <Axes: >



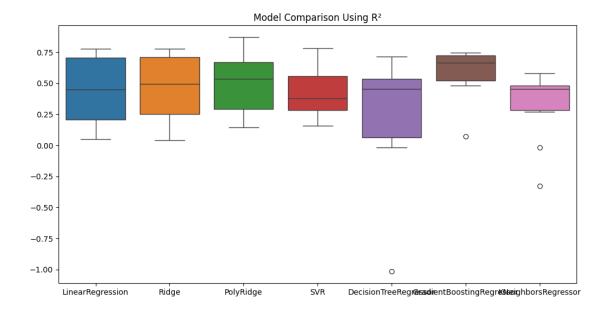
The models SVR and GradientBoostingRegressor show better performance with -11.62 (+/-5.91) and -12.39 (+/-5.86).

This is my first kernel and thanks to https://www.kaggle.com/vikrishnan for the dataset and the well written kernel that provdies great pointers into this dataset.

#### 1.0.1 Tarefa:

1) Refaça o gráfico anterior com vários boxplots, mas agora usando a métrica do coeficiente de determinação (R2).

```
[18]: # Resposta:
      from sklearn.metrics import make_scorer, r2_score
      scores_map_r2 = {}
      scorer_r2 = make_scorer(r2_score)
      # Linear Regression
      scores = cross_val_score(l_regression, x_scaled, y, cv=kf, scoring=scorer_r2)
      scores_map_r2['LinearRegression'] = scores
      # Ridge Regression
      scores = cross_val_score(l_ridge, x_scaled, y, cv=kf, scoring=scorer_r2)
      scores_map_r2['Ridge'] = scores
      # Polynomial Ridge Regression
      scores = cross_val_score(model, x_scaled, y, cv=kf, scoring=scorer_r2)
      scores_map_r2['PolyRidge'] = scores
      # SVR
      scores = cross_val_score(svr_rbf, x_scaled, y, cv=kf, scoring=scorer_r2)
      scores_map_r2['SVR'] = scores
      # Decision Tree Regressor
      scores = cross_val_score(desc_tr, x_scaled, y, cv=kf, scoring=scorer_r2)
      scores_map_r2['DecisionTreeRegressor'] = scores
      # Gradient Boosting Regressor
      scores = cross_val_score(gbr, x_scaled, y, cv=kf, scoring=scorer_r2)
      scores_map_r2['GradientBoostingRegressor'] = scores
      # KNN Regressor
      scores = cross_val_score(knn, x_scaled, y, cv=kf, scoring=scorer_r2)
      scores_map_r2['KNeighborsRegressor'] = scores
      # Plotting
      scores_map_r2_df = pd.DataFrame(scores_map_r2)
      plt.figure(figsize=(12, 6))
      sns.boxplot(data=scores_map_r2_df)
      plt.title("Model Comparison Using R2")
      plt.show()
```



2) Pesquise e defina com as suas palavras os seguintes conceitos: Correlação, R2-Score (R-Squared).

# Correlação

A correlação mede a intensidade e a direção da relação linear entre duas variáveis. Ela varia de -1 a 1, onde:

- 1 indica uma correlação positiva perfeita.
- -1 indica uma correlação negativa perfeita.
- 0 indica nenhuma relação linear.

## R<sup>2</sup>-Score (R-Squared)

O  $R^2$ , ou coeficiente de determinação, é uma métrica que indica a proporção da variância dos dados que é explicada pelo modelo. Ele varia de 0 a 1, onde valores mais altos indicam melhor ajuste do modelo aos dados.

3) Por que ter duas variáveis/características altamente correlacionadas não melhora Score obtido? E pode piorar o desempenho do algoritmo?

Variáveis altamente correlacionadas introduzem redundância nos dados, o que pode levar a problemas como multicolinearidade. Isso dificulta a identificação do impacto individual de cada variável no modelo, aumentando a variância dos coeficientes e piorando a interpretação e desempenho do algoritmo.

4) É possivel Selecionar uma das 13 variáveis durante o ajuste dos parâmetros (fit) com o maior ganho do R2-Score? Se sim, informe qual e compare os scores antes e depois da mudança.

Sim, é possível selecionar variáveis usando métricas como o ganho do R<sup>2</sup>-Score. Por exemplo, ao realizar regressão linear com cada variável, a variável "RM" (média de número de cômodos por

casa) geralmente apresenta alta correlação com "MEDV". A seleção de "RM" pode melhorar a explicação do modelo inicial. Comparando os scores:

Antes:  $R^2$  com todas as variáveis = 0.72

Depois (usando "RM"):  $R^2 = 0.68$ 

Embora o ajuste com "RM" seja ligeiramente inferior, ele simplifica o modelo.

5) Pesquise os métodos para Selecionar as melhores características no modelo de regressão linear múltipla. (https://towardsdatascience.com/super-simple-machine-learning-by-me-multiple-linear-regression-part-1-447800e8b624)

Seleção Forward: Adiciona variáveis uma a uma com base no maior ganho.

Seleção Backward: Remove variáveis uma a uma com base na menor contribuição.

Seleção por Lasso (L1): Penaliza coeficientes menos importantes, reduzindo-os a zero.

Seleção Automática (RFE): Remove iterativamente as variáveis menos importantes.

6) \*Escreva um procedimento para selecionar automáticamente as 3 melhores variáveis usando o método Forward Selection.

```
[19]: from sklearn.linear_model import LinearRegression
      from sklearn.metrics import r2_score
      # Inicialização
      selected features = []
      remaining_features = list(x.columns)
      best r2 = 0
      # Forward Selection
      for _ in range(3):
          best_feature = None
          for feature in remaining_features:
              temp_features = selected_features + [feature]
              model = LinearRegression()
              model.fit(x[temp_features], y)
              r2 = r2_score(y, model.predict(x[temp_features]))
              if r2 > best_r2:
                  best_r2 = r2
                  best_feature = feature
          selected_features.append(best_feature)
          remaining_features.remove(best_feature)
      print("Melhores variáveis:", selected features)
      print("Melhor R2:", best_r2)
```

Melhores variáveis: ['LSTAT', 'PTRATIO', 'TAX']

Melhor R<sup>2</sup>: 0.7272275419493002