$$L(\lbrace N_{\varpi}^{\rm SS,obs}\rbrace | \lbrace \xi(\eta, p_{\rm T})\rbrace) = \prod_{\varpi} \mathcal{P}\left(N_{\varpi}^{\rm SS,obs} | w_{\rm flip}(\xi(\eta_1, p_{\rm T,1}), \xi(\eta_2, p_{\rm T,2})) \times N_{\varpi}^{\rm OS+SS,obs}\right)$$

$$\tag{1}$$

$$\begin{pmatrix} n_{\rm T} \\ n_{\rm L} \end{pmatrix} = \begin{pmatrix} \varepsilon_r & \varepsilon_f \\ 1 - \varepsilon_r & 1 - \varepsilon_f \end{pmatrix} \begin{pmatrix} n_{\rm R} \\ n_{\rm F} \end{pmatrix}$$

$$\varepsilon_f = \frac{n_{\rm signal}^{\rm data} - n_{\rm signal}^{\rm MC}}{n_{\rm baseline}^{\rm data} - n_{\rm baseline}^{\rm MC}}$$

$$\varepsilon_r = \frac{n_{\rm signal}^{\rm data}}{n_{\rm baseline}^{\rm data} - n_{\rm baseline}^{\rm BKG}}$$

$$\varepsilon_r = \frac{n_{\rm baseline}^{\rm data} - n_{\rm baseline}^{\rm BKG}}{n_{\rm baseline}^{\rm data} - n_{\rm baseline}^{\rm BKG}}$$
(2)

| $10 < p_{\rm T} < 12$ | $12 < p_{\rm T} < 14$ | $14 < p_{\rm T} < 17$ | $17 < p_{\rm T} < 20$ |
|--------------------------|--------------------------|--------------------------|--------------------------|
| $0.10 \pm 0.01 \pm 0.00$ | $0.10 \pm 0.01 \pm 0.01$ | $0.12 \pm 0.01 \pm 0.01$ | $0.08 \pm 0.02 \pm 0.00$ |
| $20 < p_{\rm T} < 25$ | $25 < p_{\rm T} < 30$ | $30 < p_{\rm T} < 40$ | $40 > p_{\rm T}$ |
| $0.07 \pm 0.02 \pm 0.01$ | $0.11 \pm 0.03 \pm 0.01$ | $0.20 \pm 0.07 \pm 0.03$ | $0.25 \pm 0.10 \pm 0.05$ |

Table 1: Electron fake rate measured in data and the associated statistical uncertainty. The systematic uncertainty originating from the subtraction of "backgrounds" with only prompt leptons is also displayed.

| $10 < p_{\rm T} < 12 \; {\rm GeV}$ | | $12 < p_{\rm T} < 14$ | |
|------------------------------------|--------------------------|---------------------------------|--------------------------|
| $ \eta < 2.3$ | $ \eta > 2.3$ | $ \eta < 2.3$ | $ \eta > 2.3$ |
| $0.14 \pm 0.01 \pm 0.00$ | $0.22 \pm 0.05 \pm 0.00$ | $0.11 \pm 0.01 \pm 0.00$ | $0.24 \pm 0.06 \pm 0.00$ |
| $14 < p_{\rm T} < 17$ | | $17 < p_{\rm T} < 20 { m ~GeV}$ | |
| $ \eta < 2.3$ | $ \eta > 2.3$ | $ \eta < 2.3$ | $ \eta > 2.3$ |
| $0.12 \pm 0.01 \pm 0.00$ | $0.09 \pm 0.05 \pm 0.00$ | $0.09 \pm 0.01 \pm 0.00$ | $0.21 \pm 0.07 \pm 0.00$ |
| $20 < p_{\rm T} < 30$ | $30 < p_{\rm T} < 40$ | $40 < p_{\rm T} < 60$ | $p_{\rm T} > 60$ |
| $0.07 \pm 0.02 \pm 0.00$ | $0.12 \pm 0.05 \pm 0.01$ | $0.16 \pm 0.09 \pm 0.04$ | $0.49 \pm 0.10 \pm 0.07$ |

Table 2: Muon fake rate measured in data and the associated statistical uncertainty. The systematic uncertainty originating from the subtraction of "backgrounds" with only prompt leptons is also displayed.