Rotations of Conic Sections

Classify each conic section.

1)
$$-u^2 + 2uv - v^2 + \sqrt{2} \cdot u + \sqrt{2} \cdot v = 0$$

2)
$$37u^2 + 70uv + 37v^2 - 72 = 0$$

3)
$$u^2 - 14uv + v^2 - 120 = 0$$

4)
$$13u^2 + 10uv + 13v^2 - 288 = 0$$

Transform each equation from the xy-plane to the rotated uv-plane. The uv-plane's angle of rotation is provided.

5)
$$x^2 + y = 0$$
, $\theta = 60^\circ$

6)
$$x^2 + 4y^2 - 36 = 0$$
, $\theta = 30^\circ$

7)
$$\frac{x^2}{16} + \frac{y^2}{36} = 1$$
, $\theta = 30^\circ$

8)
$$\frac{x^2}{16} - \frac{y^2}{16} = 1$$
, $\theta = 45^\circ$

Eliminate the cross-product term by determining an angle of rotation between 0° and 90° and transforming the equation from the xy-plane to the rotated uv-plane.

9)
$$37x^2 + 42\sqrt{3} \cdot xy + 79y^2 - 400 = 0$$

10)
$$11x^2 + 10\sqrt{3} \cdot xy + y^2 - 64 = 0$$