

Figure 5.9 The probability function of the Poisson distribution with $\lambda = 4$ and the binomial approximation with the same mean, for various choices of n.

We seek $P(X \ge 3)$ and it is clearly much easier to find the probability of the complementary event. Thus, we find

$$P(X \ge 3) = 1 - P(X < 3) = 1 - P(X = 0) - P(X = 1) - P(X = 2)$$

$$= 1 - {4500 \choose 0} (0.0001)^{0} (0.9999)^{4500} - {4500 \choose 1} (0.0001)^{1} (0.9999)^{4500-1}$$

$$- {4500 \choose 2} (0.0001)^{2} (0.9999)^{4500-2}$$

$$= 1 - 0.6376 - 0.2870 - 0.0646 = 0.010874.$$

However, the required probability may also be found by applying the Poisson approximation to the binomial. The Poisson parameter in this case is

$$\lambda = np = 4500 \cdot (0.0001) = 0.45.$$