

1.

a. For A:

- Maxmin value: 3, by choosing row 2.
- Minmax value: 3, if the opponent chooses column 2.

For B:

- Minmax value: 3, by choosing column 2.
- Maxmin value: 3, if the opponent chooses row 2.

b. Only 5\5 is Pareto efficient

c. Pure Nash equilibria: 5\5 and 3\3.

For A, row 3 is strictly dominated.

For B, column 3 is strictly dominated.

This leaves us with a matrix:

A\B	1	2
1	5\5	1\4
2	4\1	3\3

This gives for A:

$$5p + (1-p) = 4p + 3(1-p)$$

Resulting in $p = 2/3$

The strategy for A is therefore $(2/3, 1/3)$

This gives for B:

$$5x + (1-x) = 4x + 3(1-x)$$

Resulting in $x = 2/3$

The strategy for B is therefore $(2/3, 1/3)$

d. The expected utility for the mixed strategy is the same due to how the game works.

$$2/3 * 2/3 * 5 + 1/3 * 1/3 * 3 = 2.555556$$

e. This is a self-committed utterance, because if the column player believes the utterance the action will indeed be the best for player A

This is not a self-revealing utterance, because if player B does not believe the utterance it will result in a sub-optimal solution for player B. In other words, player A will want player B to believe this statement no matter what because otherwise the player will be put in a lesser utility value. Player A has an incentive to make player B believe the utterance.

f. This is not a self-committed utterance, because column 3 is strictly dominated by the other columns. So, if player A believes player B, player B has every incentive to play a different column.

This is also not a self-revealing utterance, because the utterance will result in row 2 being chosen by player A which creates a scenario with the lowest possible utilities for player B.

2.

a. $G = (\{a, b, c\}, v)$, where

- $v(\emptyset) = 0$
- $v(\{a\}) = 40$, $v(\{b\}) = 25$, $v(\{c\}) = 35$,
- $v(\{a, b\}) = 65$, $v(\{a, c\}) = 75$, $v(\{b, c\}) = 60$, and
- $v(\{a, b, c\}) = 100$

- b. The core of this game is indeed empty. While the efficiency $\sum_{i \in N} x_i = v(N)$ is being met, the stability equations are not being met. These being: $a + b \geq 65$ and $a + c \geq 75$ and $b + c \geq 60$.
- c. As all parties are interchangeable, the correct Shapley values are (33.33, 33.33, 33.33).

3.

- a. Pure, the equilibrium is (r,r,L).
- b. The sub game equilibria are: (r,l,R) and (r,r,L).
- c.

A \ B	L	R
l	2 \ 2	2 \ 2
r, l	5 \ 4	3 \ 6
r, r	4 \ 2	1 \ 0

For player A, (r,l) is a dominant strategy.

For player B, no dominant strategies exist.

4.

- a. Plurality: c
Majority: d
Condorcet: d
Approval: d
Borda: d
- b. d is the winner in this system. This is due to a dropping out first, followed by either b then c or c then b . After this only d remains and is therefore winner.
- c. As said, this will probably not impact any decisions as the order for b and c does not matter.
- d. .
- e. .

5.

- a. .
- b. .