## safeAI | checking logical models

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#### 1 WEEK 8 ASSIGNMENTS

#### **Defining Concurrent Epistemic Game Structures**

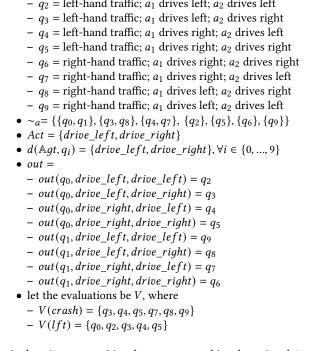
Consider a CEGS  $M_{chicken}$ , where (Agt, St, Act, d, out) is a concurrent game structure, and  $\sim_a$  are indistinguishability relations over St, one per agent in Aqt. We can now define the CEGS as a tuple

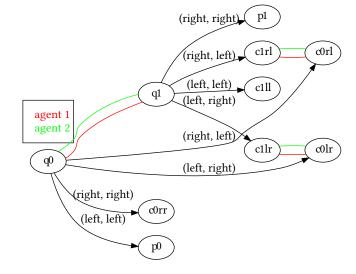
$$M_{chicken} = (\mathbb{A}qt, St, \sim_a | a \in \mathbb{A}qt, Act, d, out)$$
 (1)

, where

- $Aqt = \{a_1, a_2\}$
- - $-q_0 =$ left-hand traffic
  - $-q_1$  = right-hand traffic
  - $-q_2$  = left-hand traffic;  $a_1$  drives left;  $a_2$  drives left

As there is no propositional argument matching the action *drive\_right*, we are evaluating  $q_6$  implicitly.





#### Validating Concurrent Epistemic Game Structures through Memoryless Strategies

For the defined CEGS  $M_{chicken}$  in 1.1, it is **untrue** that under the independent combination of ATL semantics with epistemic semantics (no uniform strategies requirement) agent  $a_1$  has a memoryless strategy in  $q_0$  to enforce  $\neg crash$  in the next state  $(\langle \langle 1 \rangle \rangle X \neg crash)$ .

This is because in  $q_0$ , the only way not to crash is for both agents to take action drive left. Agent  $a_1$  cannot force this protocol alone, agent  $a_2$  needs to adhere to it as well.

### Validating Concurrent Epistemic Game Structures through Indistinguishability

For the defined CEGS  $M_{chicken}$  in 1.1, it is **untrue** that under ATL<sub>ir</sub>,  $M_{chicken}, q_0 \models_{ir} \langle \langle 1 \rangle \rangle X \neg crash \text{ holds.}$ 

This is because agent  $a_1$  does not know whether it is in  $q_0$  or  $q_1$ . Therefore it does not know whether the action to take is *drive\_left* or drive\_right. Even more, if agent a1 would choose the correct action (drive\_left), agent 2 can still cause a crash by executing drive\_right.

#### 1.4 Validating Concurrent Epistemic Game Structures through Memoryless Strategies

For the defined CEGS  $M_{chicken}$  in 1.1, it is **true** that under the independent combination of ATL semantics with epistemic semantics (no uniform strategies requirement), both agents together have a memoryless strategy in  $q_0$  to enforce  $\neg crash$  in the next state, namely  $s_{a_1}(q_0) = drive\_left$ .

This is because there is a strategy in  $q_0$  which leads to a state with  $\neg crash$  from both agents' perspective. To make it a complete strategy in the formal sense, we would need a strategy that also covers state  $q_1$ . Then, the strategy becomes  $s_i(q_0) = drive\_left \ \forall i \in \{1, 2\}$ ;  $s_i(q_1) = drive \ right \ \forall i \in \{1, 2\}.$ 

# 1.5 Validating Concurrent Epistemic Game Structures through Indistinguishability

For the defined CEGS  $M_{chicken}$  in 1.1, it is **true** that under ATL $_{ir}$ ,  $M_{chicken}$ ,  $q_0 \models_{ir} \langle \langle 1, 2 \rangle \rangle X \neg crash$  holds.

This is because agents do not know whether they are in  $q_0$  or  $q_1$ . Therefore, they do not know whether the action to take is  $drive\_left$  or  $drive\_right$ , not being able to create a uniform strategy.

# 1.6 Validating Concurrent Epistemic Game Structures through Knowledge

For the defined CEGS  $M_{chicken}$  in 1.1, it is **true** that under the independent combination of ATL semantics with epistemic semantics

(no uniform strategies requirement), both agents together know that they have a memoryless strategy in  $q_0$  to enforce  $\neg crash$  in the next state  $(K_1\langle\langle 1,2\rangle\rangle X \neg crash \wedge K_2\langle\langle 1,2\rangle\rangle X \neg crash)$ .

This is because the only state indistinguishable for both agents from  $q_0$  is  $q_1$ . For  $q \in \{q_0, q_1\}$ , it holds that  $M_{chicken}, q \models \langle \langle 1, 2 \rangle \rangle X \neg crash$ , using the following strategy  $s_i(q_0) = drive\_left \ \forall i \in \{1, 2\}$ ;  $s_i(q_1) = drive\_right \ \forall i \in \{1, 2\}$ .

1.7 7

1.8 8

1.9 9

1.10 10