# TP: is Batman somewhere?

## Oussama Oulkaid

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```
# The environment
library(tidyverse)
library(ggplot2)
library(corrplot)
```

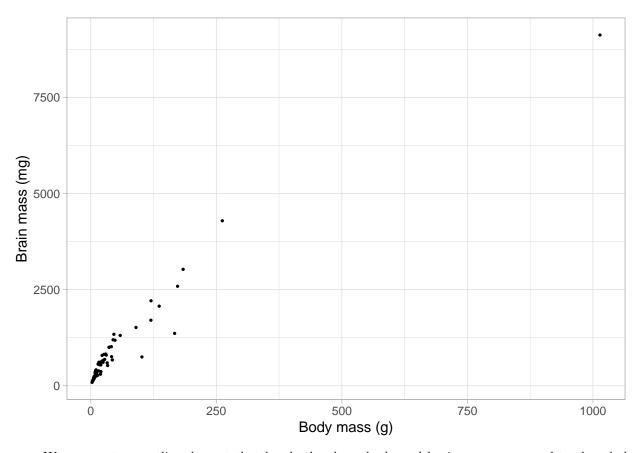
## Dataframe

```
myData <- read.table("bats.csv", sep=";", skip=3, header=T)
names(myData)

## [1] "Species" "Diet" "Clade" "BOW" "BRW" "AUD" "MOB"
## [8] "HIP"</pre>
```

# 2 - Relationship between brain weight and body mass

```
# Focusing only on the phytophagous
phyto = myData[(myData$Diet==1),]
ggplot(myData, aes(x=BOW, y=BRW)) + geom_point(size = 0.5) +
    xlab("Body mass (g)") + ylab("Brain mass (mg)") + theme_light()
```



- We can spot an outlier element that has both a huge body and brain mass compared to the whole distribution.
- We launch the simple linear regression. The estimated model has the following form:  $BRW = \hat{\beta}_1 + \hat{\beta}_2 \times BOW + \epsilon$

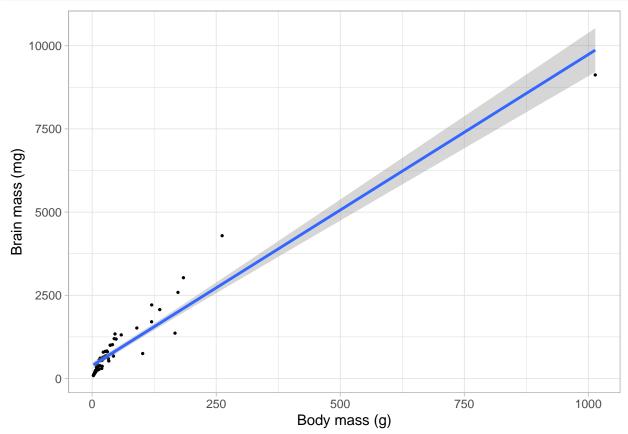
```
# Simple regression model: BRW = b1 + b2*BOW + error
                           BRW = 623.4469 + 8.9999*BOW + error
reg1 = lm(BRW ~ BOW, data=phyto)
summary(reg1)
##
## Call:
## lm(formula = BRW ~ BOW, data = phyto)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
##
   -628.32 -233.94 -65.74
                           158.26 1308.59
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 623.4469
                           81.4762
                                     7.652 3.14e-08 ***
                            0.3972 22.659 < 2e-16 ***
## BOW
                 8.9999
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

## Residual standard error: 396.9 on 27 degrees of freedom
## Multiple R-squared: 0.95, Adjusted R-squared: 0.9482

#### ## F-statistic: 513.4 on 1 and 27 DF, p-value: < 2.2e-16

- From the summary we have the numerical form of the model:  $BRW = 623.4469 + 8.9999 \times BOW + \epsilon$  (where 623.4469 is the estimate of the intercept  $\hat{\beta}_1$ ).
- We also see that the value of the coefficient of determination  $\hat{\beta}_2$  (~9) is significantly different from zero.
- At the end of the row we got three stars, which is the highest level of significance of the variable BOW in the model.
- In addition, the very low p-value (< 2.2e-16) reflects the fact that the variable BOW has a big influence on BRW. Thus, the relationship between brain weight and body mass can be estimated to be linear.
- The H0 hypothesis would be to say that the coefficient  $\hat{\beta}_2$  is null (meaning that BOW has no influence of the value of BRW). This hypothesis is false.
- we draw the regression line:

```
ggplot(myData, aes(x=BOW, y=BRW)) + geom_point(size = 0.5) +
  stat_smooth(method="lm", se=TRUE) +
  xlab("Body mass (g)") + ylab("Brain mass (mg)") + theme_light()
```



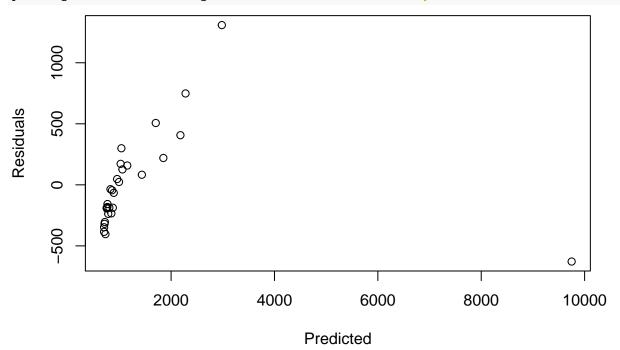
• Analysis of the variance table:

```
anova(reg1)
```

```
## Residuals 27 4253838 157550
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

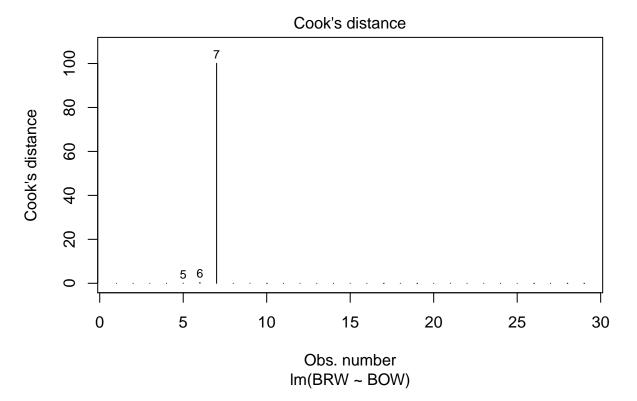
- Additional information in the table: SSE (sum of squares of the error) and SSM (sum of squares of the model).
- The sum of squared residuals is 4253838.
- We draw the graph of the residuals with respect to the predicted values:

plot(reg1\$fitted.values, reg1\$residuals, xlab="Predicted", ylab="Residuals")



- The graph shows that the value of residuals generally increases for higher values of predicted brain weight. At a first glance, we can assume that the outlier element (with a predicted value of brain weight around 1000) caused a deviation in the linear regression model, because the model tries to include all the elements of the dataset.
- The Cook's distance graph shows that the seventh element in the dataset has the largest distance. It corresponds to the outlier previously cited.

plot(reg1, 4) #Cook's distance



• We redo the analysis without this individual and we compare the results obtained:

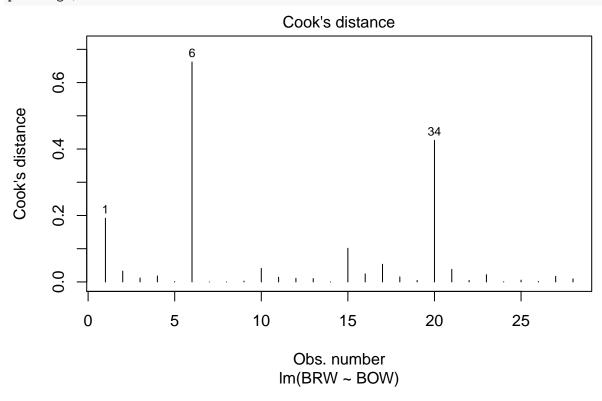
```
which(phyto$BRW>8000)
```

```
## [1] 7
phytobis = phyto[which(phyto$BRW<8000),]</pre>
reg2 = lm(BRW ~ BOW, data=phytobis)
summary(reg2)
##
## Call:
## lm(formula = BRW ~ BOW, data = phytobis)
##
## Residuals:
##
       Min
                1Q
                   Median
                                3Q
                                       Max
  -269.76 -93.33
                      8.73
                           112.93
                                    322.55
##
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
##
  (Intercept) 346.5452
                           35.4920
                                     9.764 3.48e-10 ***
                            0.4285
                                    33.860 < 2e-16 ***
## BOW
                14.5099
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 141.8 on 26 degrees of freedom
## Multiple R-squared: 0.9778, Adjusted R-squared: 0.977
## F-statistic: 1147 on 1 and 26 DF, p-value: < 2.2e-16
```

• Now, we clearly notice an improvement of the relevance of the model; the coefficient of determination is much more significant  $(\hat{\beta}_2)$ . it's value is 14.5099 (was 8.9999 for reg1). This goes along with a decrease of the intercept  $(\hat{\beta}_1)$ .

- Thus, our assumption was valid; removing the outlier from the linear regression model is helpful.
- The Cook's distance corresponding to the new model is:

#### plot(reg2, 4) #Cook's distance



# 3 - Contribution of each part of the brain to the total weight

->

• Pearson tests

```
##
## Pearson's product-moment correlation
##
## data: phyto$BRW and phyto$HIP
## t = 12.91, df = 27, p-value = 4.574e-13
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.8502663 0.9658107
## sample estimates:
## cor
## 0.9276811
```

cor.test(phyto\$BRW, phyto\$MOB)

cor.test(phyto\$BRW, phyto\$HIP)

```
##
## Pearson's product-moment correlation
##
## data: phyto$BRW and phyto$MOB
## t = 9.7964, df = 27, p-value = 2.203e-10
```

```
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
  0.7644185 0.9442114
## sample estimates:
         cor
## 0.8834215
cor.test(phyto$BRW, phyto$AUD)
##
##
    Pearson's product-moment correlation
##
## data: phyto$BRW and phyto$AUD
## t = 3.2338, df = 27, p-value = 0.003215
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
   0.2007495 0.7497021
## sample estimates:
         cor
## 0.5283792
  • between BRW and HIP: the correlation is the highest (p-value = 4.574e-13).
  • between BRW and MOB: the correlation is high (p-value = 2.203e-10).
  • between BRW and AUD: the correlation is lower (p-value = 0.003215).
  • Multiple regression model: BRW = \hat{\beta}_1 + \hat{\beta}_2 \times AUD + \hat{\beta}_3 \times MOB + \hat{\beta}_4 \times HIP + \epsilon
# BRW = b1 + b2*AUD + b3*MOB + b4*HIP + error
# BRW = -312.692 + 47.989*AUD - 2.444*MOB + 15.981*HIP
regm = lm(BRW~AUD+MOB+HIP, data=phytobis)
summary(regm)
##
## Call:
## lm(formula = BRW ~ AUD + MOB + HIP, data = phytobis)
##
## Residuals:
##
       Min
                 1Q Median
                                  3Q
                                          Max
## -268.55 -68.84
                       9.88
                               61.66
                                      375.34
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -312.692
                              76.628
                                      -4.081 0.00043 ***
## AUD
                  47.989
                               6.067
                                        7.910 3.85e-08 ***
## MOB
                  -2.444
                               3.257
                                       -0.750 0.46034
## HIP
                  15.981
                               2.960
                                        5.399 1.52e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 158.5 on 24 degrees of freedom
## Multiple R-squared: 0.9744, Adjusted R-squared: 0.9712
## F-statistic: 304.5 on 3 and 24 DF, p-value: < 2.2e-16
  • The numerical model: BRW = -312.692 + 47.989 \times AUD - 2.444 \times MOB + 15.981 \times HIP + \epsilon
```

• The p-value is very small. We can tell that the variable BRW is influenced by the AUD and HIP. MOB on the other hand seems to not have a significant coefficient  $(\hat{\beta}_3)$  compared to  $(\hat{\beta}_2 \text{ and } \hat{\beta}_4)$ .

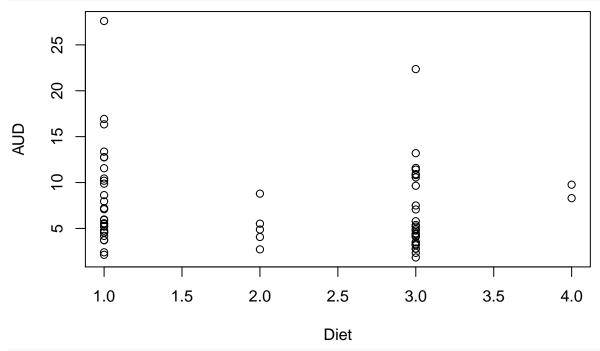
```
anova(regm)
## Analysis of Variance Table
##
## Response: BRW
##
             Df
                  Sum Sq Mean Sq F value
## AUD
                6817133 6817133 271.210 1.397e-14 ***
              1
              1 15409397 15409397 613.040 < 2.2e-16 ***
## MOB
## HIP
                  732653
                           732653 29.148 1.519e-05 ***
              1
## Residuals 24
                  603265
                            25136
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
  • We run the following function:
reg0 = lm(BRW ~ 1, data = phyto)
step(reg0, scope=BRW~AUD + MOB + HIP, direction="forward")
## Start: AIC=433.88
## BRW ~ 1
##
          Df Sum of Sq
                            RSS
                                    AIC
## + HIP
           1
             73272731 11869487 378.74
## + MOB
              66447848 18694370 391.92
           1
## + AUD
           1 23770396 61371823 426.39
## <none>
                       85142218 433.88
##
## Step: AIC=378.74
## BRW ~ HIP
##
                                   AIC
##
          Df Sum of Sq
                            RSS
## + MOB
           1
               2846939
                        9022548 372.79
## + AUD
           1
               2013783 9855704 375.35
## <none>
                       11869487 378.74
##
## Step: AIC=372.79
## BRW ~ HIP + MOB
##
          Df Sum of Sq
##
                           RSS
                                   AIC
## + AUD
               1910121 7112426 367.89
## <none>
                       9022548 372.79
##
## Step: AIC=367.89
## BRW ~ HIP + MOB + AUD
##
## Call:
## lm(formula = BRW ~ HIP + MOB + AUD, data = phyto)
##
## Coefficients:
## (Intercept)
                        HIP
                                      MOB
                                                   AUD
##
      -1003.95
                      44.35
                                   -29.24
                                                 52.82
```

• The purpose of this function is to start from a linear regression model (reg0 in this case) and perform some analysis by adding at each time a new variable. It seems that the variables are added in a specific order such that the variable with the highest p-value is added first, and so on.

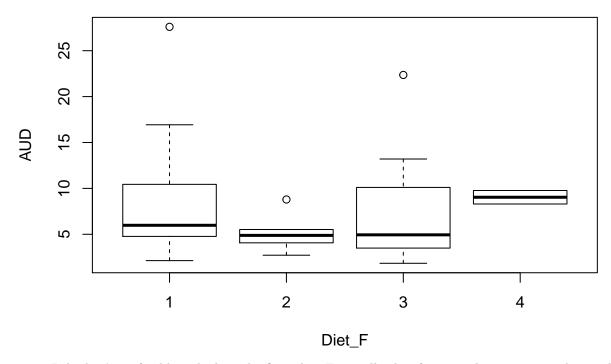
- "The AIC is designed to find the model that explains the most variation in the data, while penalizing for models that use an excessive number of parameters.. The lower the AIC, the better the model fit." (source: https://www.statology.org/aic-in-r/)
- If we consider this definition, we can assume that the multivariate model (BRW~AUD + MOB + HIP) fits better.

## 4 - Link between volume of the auditory part and diet

myData\$Diet\_F = as.factor(myData\$Diet)
with(myData, plot(AUD~Diet))



with(myData, plot(AUD~Diet\_F))



- I think it's preferable to look at the first plot. Especially that for some diet categories the number of samples is not representative (2 and 4). So looking only at the factors graph would be misleading.
- Regression analysis:

## Response: AUD

```
lm = lm(AUD~Diet_F, data=myData)
summary(lm)
##
## Call:
## lm(formula = AUD ~ Diet_F, data = myData)
## Residuals:
##
              1Q Median
                            3Q
## -6.179 -3.226 -1.341 2.530 19.291
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 8.3093
                            0.9040
                                     9.192 5.48e-13 ***
                                    -1.321
## Diet_F2
                -3.1133
                            2.3573
                                               0.192
                                               0.227
## Diet_F3
                -1.5886
                            1.3019
                                    -1.220
## Diet_F4
                 0.7257
                            3.5591
                                     0.204
                                               0.839
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.868 on 59 degrees of freedom
## Multiple R-squared: 0.04512,
                                    Adjusted R-squared:
## F-statistic: 0.9293 on 3 and 59 DF, p-value: 0.4323
anova(lm)
## Analysis of Variance Table
```

```
## Diet_F 3 66.07 22.023 0.9293 0.4323 ## Residuals 59 1398.26 23.699
```

• Conclusion: there is no correlation between the auditory brain volume and diet; the sum of squared residuals is way more large than the sum of squares of the model. In addition, the corresponding p-value is relatively high.