TP: is Batman somewhere?

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December, 2021

```
# The environment
library(tidyverse)
library(ggplot2)
library(corrplot)
```

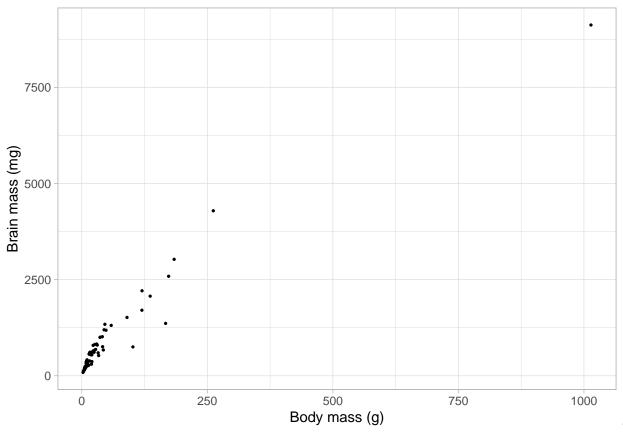
Dataframe

```
myData <- read.table("bats.csv", sep=";", skip=3, header=T)
names(myData)

## [1] "Species" "Diet" "Clade" "BOW" "BRW" "AUD" "MOB"
## [8] "HIP"</pre>
```

2 - Relationship between brain weight and body mass

```
# Focusing only on the phytophagous
phyto = myData[(myData$Diet==1),]
ggplot(myData, aes(x=BOW, y=BRW)) + geom_point(size = 0.5) +
    xlab("Body mass (g)") + ylab("Brain mass (mg)") + theme_light()
```



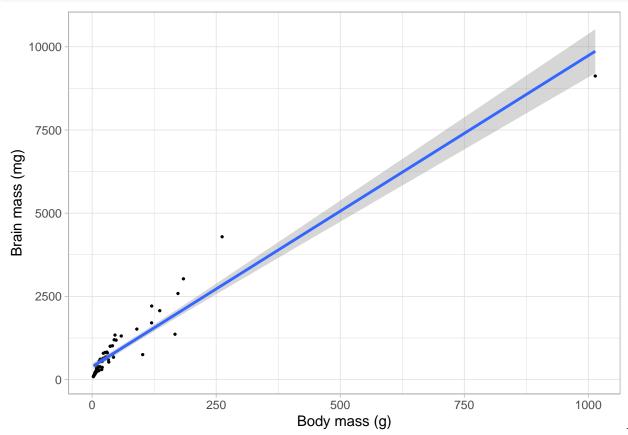
We can spot an outlier element that has both a huge body and brain mass compared to the whole distribution.

• We launch the simple linear regression. The estimated model has the following form: $BRW = \hat{\beta}_1 + \hat{\beta}_2 \times BOW + \epsilon$

```
# Simple regression model: BRW = b1 + b2*BOW + error
                           BRW = 623.4469 + 8.9999*BOW + error
reg1 = lm(BRW ~ BOW, data=phyto)
summary(reg1)
##
## Call:
## lm(formula = BRW ~ BOW, data = phyto)
##
## Residuals:
##
                1Q Median
                                3Q
  -628.32 -233.94 -65.74
                           158.26 1308.59
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
##
  (Intercept) 623.4469
                           81.4762
                                     7.652 3.14e-08 ***
## BOW
                 8.9999
                            0.3972 22.659 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 396.9 on 27 degrees of freedom
## Multiple R-squared: 0.95, Adjusted R-squared: 0.9482
## F-statistic: 513.4 on 1 and 27 DF, p-value: < 2.2e-16
```

- From the summary we have the numerical form of the model: $BRW = 623.4469 + 8.9999 \times BOW + \epsilon$ (where 623.4469 is the estimate of the intercept $\hat{\beta}_1$).
- We also see that the value of the coefficient of determination $\hat{\beta}_2$ (~9) is significantly different from zero.
- At the end of the row we got three stars, which is the highest level of significance of the variable BOW in the model.
- In addition, the very low p-value (< 2.2e-16) reflects the fact that the variable BOW has a big influence on BRW. Thus, the relationship between brain weight and body mass can be estimated to be linear.
- The H0 hypothesis would be to say that the coefficient $\hat{\beta}_2$ is null (meaning that BOW has no influence of the value of BRW). This hypothesis is false.
- we draw the regression line:

```
ggplot(myData, aes(x=BOW, y=BRW)) + geom_point(size = 0.5) +
  stat_smooth(method="lm", se=TRUE) +
  xlab("Body mass (g)") + ylab("Brain mass (mg)") + theme_light()
```



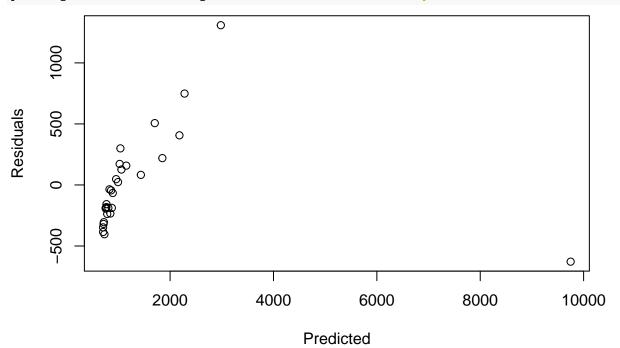
Analysis of the variance table:

```
anova(reg1)
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

- Additional information in the table: SSE (sum of squares of the error) and SSM (sum of squares of the model).
- The sum of squared residuals is 4253838.
- We draw the graph of the residuals with respect to the predicted values:

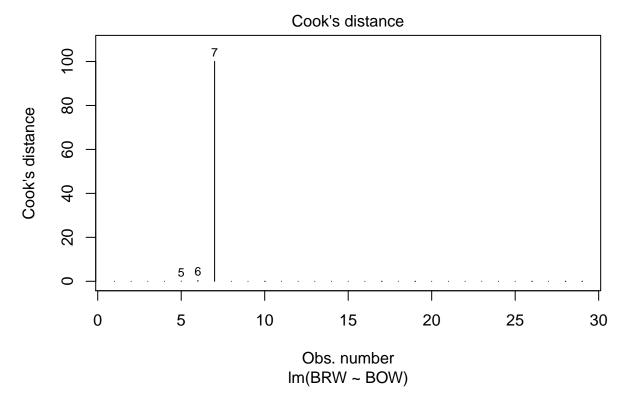
plot(reg1\$fitted.values, reg1\$residuals, xlab="Predicted", ylab="Residuals")



The graph shows that the value of residuals generally increases for higher values of predicted brain weight. At a first glance, we can assume that the outlier element (with a predicted value of brain weight around 1000) caused a deviation in the linear regression model, because the model tries to include all the elements of the dataset.

• The Cook's distance graph shows that the seventh element in the dataset has the largest distance. It corresponds to the outlier previously cited.

plot(reg1, 4) #Cook's distance



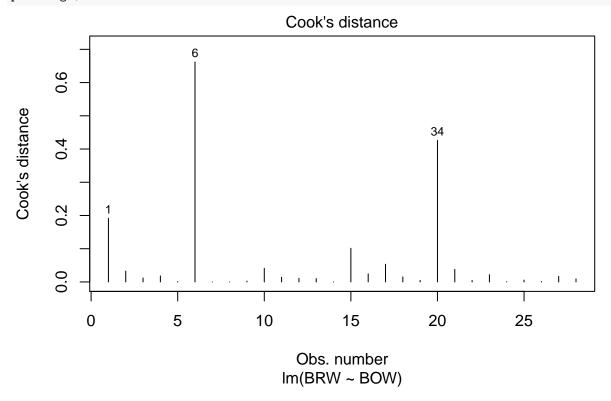
• We redo the analysis without this individual and we compare the results obtained:

```
which(phyto$BRW>8000)
## [1] 7
phytobis = phyto[which(phyto$BRW<8000),]</pre>
reg2 = lm(BRW ~ BOW, data=phytobis)
summary(reg2)
##
## Call:
## lm(formula = BRW ~ BOW, data = phytobis)
##
## Residuals:
##
       Min
                1Q
                   Median
                                3Q
                                       Max
  -269.76 -93.33
                      8.73
                           112.93
                                    322.55
##
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
##
  (Intercept) 346.5452
                           35.4920
                                     9.764 3.48e-10 ***
                            0.4285
                                    33.860 < 2e-16 ***
## BOW
                14.5099
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 141.8 on 26 degrees of freedom
## Multiple R-squared: 0.9778, Adjusted R-squared: 0.977
## F-statistic: 1147 on 1 and 26 DF, p-value: < 2.2e-16
```

• Now, we clearly notice an improvement of the relevance of the model; the coefficient of determination is much more significant $(\hat{\beta}_2)$ is 14.5099 (was 8.9999 for reg1). This goes along with a decrease of the intercept $(\hat{\beta}_1)$.

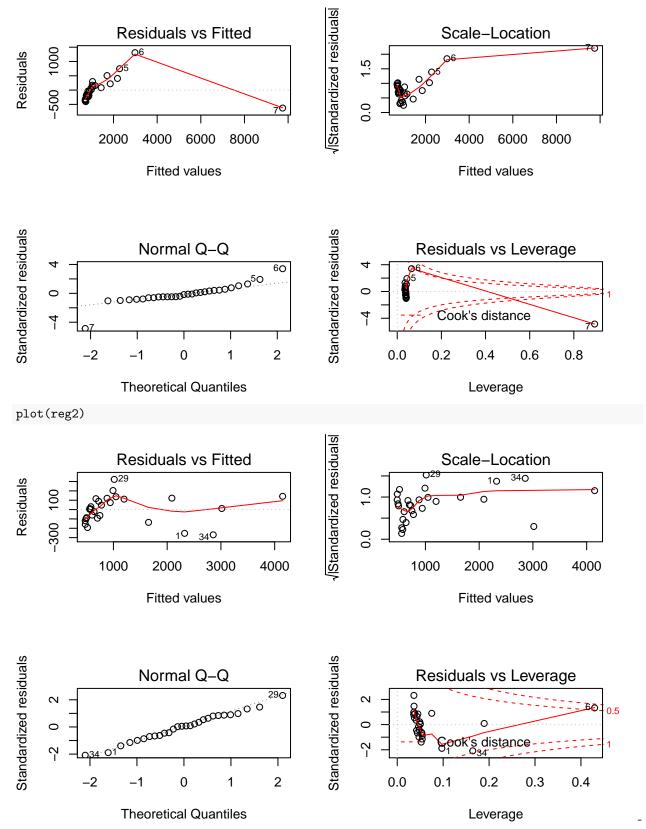
- This, our assumption was valid; removing the outlier from the linear regression model is helpful.
 The Cook's distance corresponding to the new model is:

plot(reg2, 4) #Cook's distance



• Diagnosis of the validity of the linear model approach

```
par(mfcol=c(2,2))
plot(reg1)
```



One advantage is that the second model allows to have a wider view of the distribution of the sample.

3 - Contribution of each part of the brain to the total weight

• Pearson tests cor.test(phyto\$BRW, phyto\$HIP) ## ## Pearson's product-moment correlation ## ## data: phyto\$BRW and phyto\$HIP ## t = 12.91, df = 27, p-value = 4.574e-13 ## alternative hypothesis: true correlation is not equal to 0## 95 percent confidence interval: ## 0.8502663 0.9658107 ## sample estimates: cor ## 0.9276811 cor.test(phyto\$BRW, phyto\$MOB) ## Pearson's product-moment correlation ## ## ## data: phyto\$BRW and phyto\$MOB ## t = 9.7964, df = 27, p-value = 2.203e-10 ## alternative hypothesis: true correlation is not equal to 0 ## 95 percent confidence interval: ## 0.7644185 0.9442114 ## sample estimates: cor ## 0.8834215 cor.test(phyto\$BRW, phyto\$AUD) ## ## Pearson's product-moment correlation ## ## data: phyto\$BRW and phyto\$AUD ## t = 3.2338, df = 27, p-value = 0.003215 ## alternative hypothesis: true correlation is not equal to 0 ## 95 percent confidence interval: ## 0.2007495 0.7497021 ## sample estimates: ## cor ## 0.5283792 • between BRW and HIP: the correlation is the highest (p-value = 4.574e-13). • between BRW and MOB: the correlation is high (p-value = 2.203e-10). • between BRW and AUD: the correlation is lower (p-value = 0.003215). • Multiple regression model: $BRW = \hat{\beta}_1 + \hat{\beta}_2 \times AUD + \hat{\beta}_3 \times MOB + \hat{\beta}_4 \times HIP + \epsilon$

BRW = b1 + b2*AUD + b3*MOB + b4*HIP + error

regm = lm(BRW~AUD+MOB+HIP, data=phytobis)

BRW = -312.692 + 47.989*AUD - 2.444*MOB + 15.981*HIP

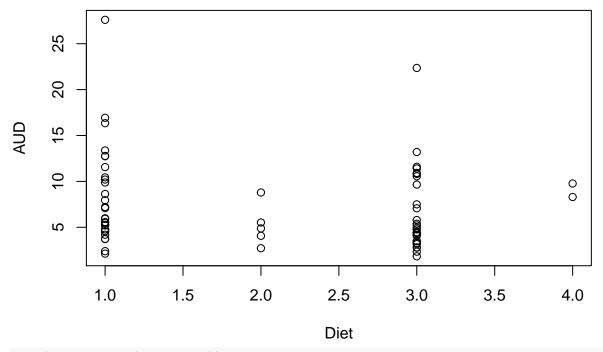
```
summary(regm)
##
## Call:
## lm(formula = BRW ~ AUD + MOB + HIP, data = phytobis)
## Residuals:
##
       Min
                 1Q
                    Median
                                  3Q
                                         Max
                              61.66
## -268.55 -68.84
                       9.88
                                     375.34
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -312.692
                             76.628
                                      -4.081 0.00043 ***
## AUD
                  47.989
                              6.067
                                       7.910 3.85e-08 ***
## MOB
                 -2.444
                              3.257
                                      -0.750 0.46034
## HIP
                 15.981
                              2.960
                                       5.399 1.52e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 158.5 on 24 degrees of freedom
## Multiple R-squared: 0.9744, Adjusted R-squared: 0.9712
## F-statistic: 304.5 on 3 and 24 DF, p-value: < 2.2e-16
  • The numerical model: BRW = -312.692 + 47.989 \times AUD - 2.444 \times MOB + 15.981 \times HIP + \epsilon
  • The p-value is very small. We can tell that the variable BRW is influenced by the AUD and HIP. MOB on
     the other hand seems to not have a significant coefficient (\hat{\beta}_3) compared to (\hat{\beta}_2) and (\hat{\beta}_4).
anova(regm)
## Analysis of Variance Table
##
## Response: BRW
##
             Df
                   Sum Sq Mean Sq F value
                                               Pr(>F)
                  6817133 6817133 271.210 1.397e-14 ***
## AUD
## MOB
               1 15409397 15409397 613.040 < 2.2e-16 ***
## HIP
                   732653
                            732653 29.148 1.519e-05 ***
## Residuals 24
                   603265
                             25136
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
  • We run the following function :
reg0 = lm(BRW ~ 1, data = phyto)
step(reg0, scope=BRW~AUD + MOB + HIP, direction="forward")
## Start: AIC=433.88
## BRW ~ 1
##
          Df Sum of Sq
                             RSS
## + HIP
           1 73272731 11869487 378.74
## + MOB
           1 66447848 18694370 391.92
## + AUD
           1 23770396 61371823 426.39
                        85142218 433.88
## <none>
## Step: AIC=378.74
## BRW ~ HIP
```

```
##
##
                             RSS
                                     AIC
          Df Sum of Sq
## + MOB
                2846939
                         9022548 372.79
## + AUD
                2013783
                         9855704 375.35
##
   <none>
                        11869487 378.74
##
## Step: AIC=372.79
## BRW ~ HIP + MOB
##
                            RSS
                                    AIC
##
          Df Sum of Sq
## + AUD
                1910121 7112426 367.89
                        9022548 372.79
##
   <none>
##
## Step: AIC=367.89
## BRW ~ HIP + MOB + AUD
##
## Call:
## lm(formula = BRW ~ HIP + MOB + AUD, data = phyto)
##
## Coefficients:
   (Intercept)
                                       MOB
                                                     AUD
                         HIP
      -1003.95
##
                       44.35
                                    -29.24
                                                   52.82
```

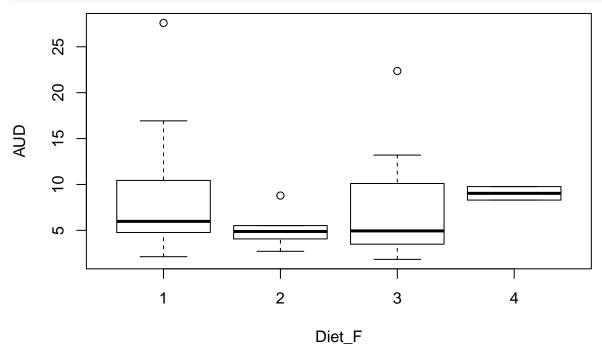
The purpose of this function is to start from a linear regression model (reg0 is this case) and perform some analysis by adding at each time a new variable. It seems that the variables are added in an order such that the variable with the highest p-value is added first, and so on. - "The AIC is designed to find the model that explains the most variation in the data, while penalizing for models that use an excessive number of parameters.. The lower the AIC, the better the model fit." (source: https://www.statology.org/aic-in-r/) - If you consider this definition, we can assume that the multivariate model (BRW~AUD + MOB + HIP) fits better.

4 - Link between volume of the auditory part and diet

```
myData$Diet_F = as.factor(myData$Diet)
with(myData, plot(AUD~Diet))
```



with(myData, plot(AUD~Diet_F))



think it's preferable to look at the first plot. Especially that for some diet categories the number of samples is not representative (2 and 4). So looking only at the factors graph would be misleading.

Ι

• Regression analysis:

```
lm = lm(AUD~Diet_F, data=myData)
summary(lm)
##
```

```
##
## Call:
## lm(formula = AUD ~ Diet_F, data = myData)
```

```
##
## Residuals:
##
      Min
              1Q Median
  -6.179 -3.226 -1.341
                         2.530 19.291
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                                      9.192 5.48e-13 ***
## (Intercept)
                 8.3093
                             0.9040
                                     -1.321
## Diet_F2
                -3.1133
                             2.3573
                                               0.192
## Diet_F3
                -1.5886
                             1.3019
                                     -1.220
                                               0.227
## Diet_F4
                 0.7257
                             3.5591
                                      0.204
                                               0.839
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.868 on 59 degrees of freedom
## Multiple R-squared: 0.04512,
                                     Adjusted R-squared:
## F-statistic: 0.9293 on 3 and 59 DF, p-value: 0.4323
anova(lm)
## Analysis of Variance Table
##
## Response: AUD
##
             Df
                 Sum Sq Mean Sq F value Pr(>F)
## Diet_F
              3
                  66.07
                         22.023 0.9293 0.4323
## Residuals 59 1398.26
                         23.699
```

• Conclusion: there is no correlation between the auditory brain volume and diet; the sum of squared residuals is way more large than the sum of squares of the model. In addition, the corresponding p-value is high, which means that there is no clear correlation linking the auditory brain volume and diet.