ECON 121: Problem Set #8

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Problem 1

You have \$100 to invest and are wondering where to put it. You are considering whether to buy your favorite stock (B) or put it in your couch (C), either decision occurring today. You know the stock price today, conveniently enough \$100 per share, but you don't know the stock price tomorrow. For simplicity, it could either be double (\$200) or nothing (\$0), with the probability of double being p, and the probability of nothing being $1 - p$. If you invest in your couch you get your \$100 back tomorrow. Your discount factor is δ, and you are risk neutral (i.e. your payoffs only depend on time discounting and money.)

1. Draw the complete game tree, with nature and player 1.

2. At what level of p should you buy you favorite stock?

3. Why doesn't δ affect part (b)?

4. Suppose p is greater than you answer in part (b). Martha Stewart knows what the stok price is going to be tomorrow, and offers to sell this information to you. You trust that she knows and is being honest because her written offer is finely hand-crafted using everyday houshold items. Assuming you only concern is making money and discounting for time (instead of moral quams), or going to prison), how much would you be willing to pay for this information?

Problem 2

There was an old game show called "Let's Make a Deal" hosted by Monty Hall. In it was a game where a prize was hidden behind one of three doors, and behind the other two doors were goats. The contestant initially chose a door; then Monty Hall would open one of the doors the contestant did not pick to reveal a goat. Then the contestant had the option to stay with the door he chose or switch to the other un-opened door.
Suppose you are playing this game, the "prize" is worth \$10,000, and a goat is worth nothing. Since it's random anyway, you already chose door A (the decision is "sunk" and is not part of the game directly). The game starts as nature randomly determines where the prize is (1/3 chance for any of the three doors); then Monty Hall selects one of doors B or C that has a goat (also a move by nature); then you choose to Stay at door A or to Switch to the unopened door. Finally, the outcome is resolved – either you find a goat or the prize behind the door you finally selected.
If both B and C have a goat, Monty flips a coin (50/50 chance) to determine which one to open. If either B or C have the car, there is only one available door Monty can open, so he opens that one.
Now, we draw the complete game tree; I detail it in several steps to try and help you

1. Draw the first mover, Nature, picking which door has the prize, A,B,or C. Make sure to include probabilities!

2. Draw the second mover, Nature (again!). picking which door to open - B or C. If it's a degenerate lottery, you don't have to actlly draw a new branch of the tree. But when it isn't a degenerate lottery, you actually have to draw out the branches of the decision tree and think about what is happening.

3. Draw the third and final mover, the player (you), picking either to Stay at door A or Switch to the only other door available.

4. Finally, list the payoffs at each terminal node. It's either \$10,000 if the player's decision led to the prize, or \$0if it didn't