

# Projet\_controle\_qualite

## Contrôle de Qualité

Ousmane LO

27 décembre 2018

- Consignes
- Questions

## Consignes

Les résultats à envoyer avant le 10 janvier.

## Questions

1. Vous devez faire un test adéquat pour chacune des 6 colonnes pour définir la loi des données.
2. Construire des cartes de contrôle sur la moyenne, la variance et l'étendue pour les colonnes 7 à 107.
3. CUMSUM EWMA pour chaque colonne 108 et 109 pour détecter un changement par rapport à une moyenne égale à 2.

Chargeons sous R les données **QualiteOusmane.csv** dans un tibble appelé **ousman**.

```
library(readr)

ousman <- read_csv(file="QualiteOusmane.csv")
```

```
## Parsed with column specification:
## cols(
##   .default = col_double(),
##   X1 = col_integer()
## )
```

```
## See spec(...) for full column specifications.
```

```
ousman
```

```
## # A tibble: 1,000 x 109
##       X1   Date    V2    V3    V4    V5    V6    V7    V8    V9    V10
##   <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1     1  5510.  8664.  8410. 13124.  8030.   32.0  2.88   3.25  2.08  2.49
## 2     2  2836.  8878.  8666. 13137.  2663.   15.0  2.97   1.42  1.42  2.52
## 3     3  5463.  8712.  8664. 13203.  2830.  2894.   2.23   1.60  2.97  1.83
## 4     4 13360.  8588.  8768. 13167.  5841.  1224.   1.83   2.54  1.34  0.961
## 5     5 13686.  8904.  8689. 13110.  7503.   447.   2.37   2.09  2.05  2.88
## 6     6  8372.  8652.  8853. 13116.  6312.   438.   0.828  2.49  2.37  2.67
## 7     7  7103.  8811.  8883. 13172.  8984.  4213.   1.59   2.03  1.48  1.59
## 8     8 12172.  8874.  8764. 13086.  7818.  9070.   1.86   1.53  2.11  2.67
## 9     9  7178.  8798.  8643. 13180.  5389.  6302.   2.20   1.81  1.46  1.18
## 10    10  4953.  9089.  8618. 13157.  3218.  9802.   1.98   2.03  1.64  1.29
## # ... with 990 more rows, and 98 more variables: V11 <dbl>, V12 <dbl>,
## #   V13 <dbl>, V14 <dbl>, V15 <dbl>, V16 <dbl>, V17 <dbl>, V18 <dbl>,
## #   V19 <dbl>, V20 <dbl>, V21 <dbl>, V22 <dbl>, V23 <dbl>, V24 <dbl>,
## #   V25 <dbl>, V26 <dbl>, V27 <dbl>, V28 <dbl>, V29 <dbl>, V30 <dbl>,
## #   V31 <dbl>, V32 <dbl>, V33 <dbl>, V34 <dbl>, V35 <dbl>, V36 <dbl>,
## #   V37 <dbl>, V38 <dbl>, V39 <dbl>, V40 <dbl>, V41 <dbl>, V42 <dbl>,
## #   V43 <dbl>, V44 <dbl>, V45 <dbl>, V46 <dbl>, V47 <dbl>, V48 <dbl>,
## #   V49 <dbl>, V50 <dbl>, V51 <dbl>, V52 <dbl>, V53 <dbl>, V54 <dbl>,
## #   V55 <dbl>, V56 <dbl>, V57 <dbl>, V58 <dbl>, V59 <dbl>, V60 <dbl>,
## #   V61 <dbl>, V62 <dbl>, V63 <dbl>, V64 <dbl>, V65 <dbl>, V66 <dbl>,
## #   V67 <dbl>, V68 <dbl>, V69 <dbl>, V70 <dbl>, V71 <dbl>, V72 <dbl>,
## #   V73 <dbl>, V74 <dbl>, V75 <dbl>, V76 <dbl>, V77 <dbl>, V78 <dbl>,
## #   V79 <dbl>, V80 <dbl>, V81 <dbl>, V82 <dbl>, V83 <dbl>, V84 <dbl>,
## #   V85 <dbl>, V86 <dbl>, V87 <dbl>, V88 <dbl>, V89 <dbl>, V90 <dbl>,
## #   V91 <dbl>, V92 <dbl>, V93 <dbl>, V94 <dbl>, V95 <dbl>, V96 <dbl>,
## #   V97 <dbl>, V98 <dbl>, V99 <dbl>, V100 <dbl>, V101 <dbl>, V102 <dbl>,
## #   V103 <dbl>, V104 <dbl>, V105 <dbl>, V106 <dbl>, V107 <dbl>, V108 <dbl>
```

span style="color:red"> 1) Faisons un **test adéquat** pour chacune des 6 premières colonnes pour définir la loi des données.

a) Test adéquat pour la première variable :

```
library(MASS)
z1 <- ousman$Date
fitdistr(z1, "weibull")
```

```
##       shape      scale
##  2.129726e+00  8.652357e+03
## (5.241165e-02) (1.365680e+02)
```

## TEST POUR Date

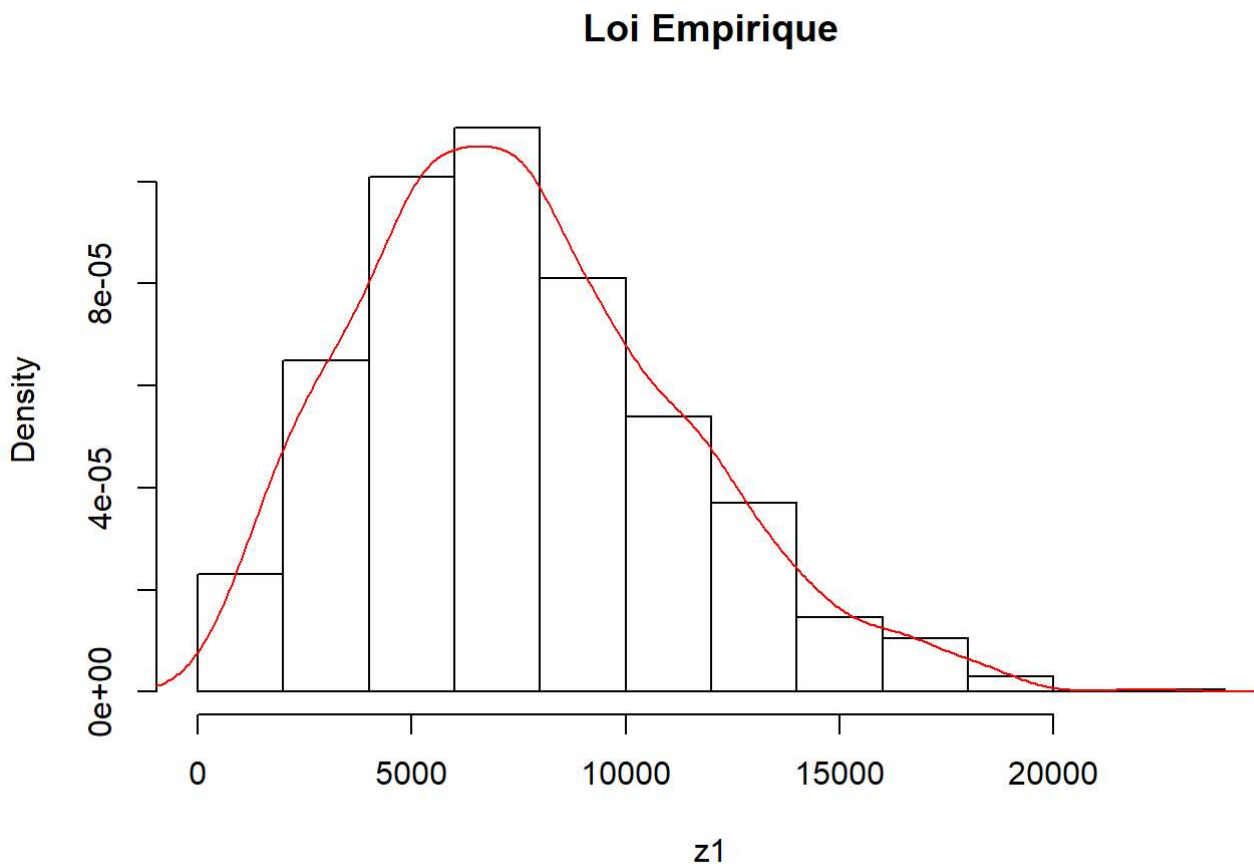
```
## TESTS

## 1) Adequation de la loi Empirique avec une loi weibull
ks.test(z1,"pweibull",shape=2.129726e+00,scale=8.652357e+03 )
```

```
##
## One-sample Kolmogorov-Smirnov test
##
## data:  z1
## D = 0.030589, p-value = 0.3067
## alternative hypothesis: two-sided
```

```
## GRAPHIQUES
```

```
hist(z1, probability=T, main='Loi Empirique')
lines(density(z1), col='red')
```



D'après le test de Kolmogorov Smirnov, la variable aléatoire Date semble suivre une loi de weibull.

b) Test adéquation pour la deuxième variable :

```
library(MASS)
z2 <- ousman$V2
fitdistr(z2, "normal")
```

```
##      mean      sd
## 8760.983742 136.386400
## ( 4.312917) ( 3.049693)
```

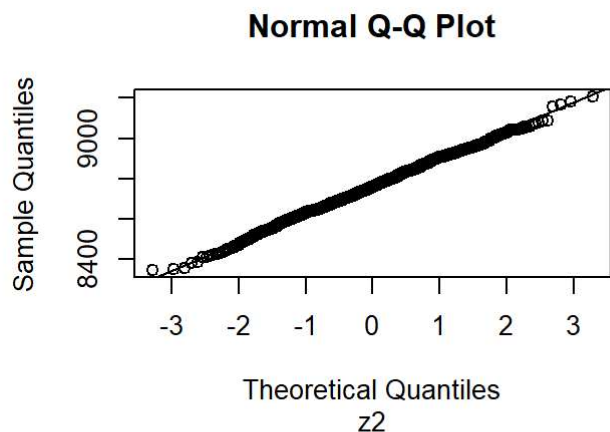
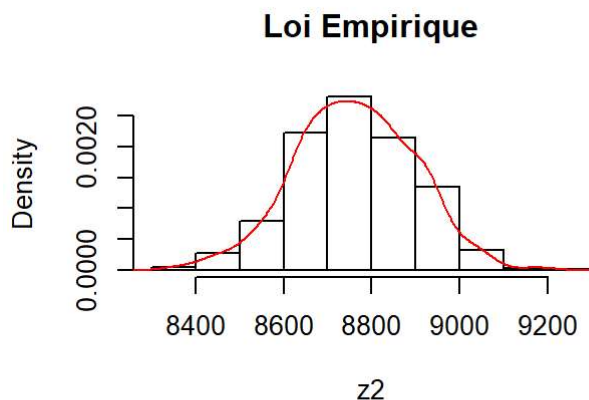
## TEST POUR V2

```
## 1) Adequation de La Loi Empirique avec une Loi normale
ks.test(z2,"pnorm",mean=8760.983742 ,sd=136.386400 )
```

```
##
## One-sample Kolmogorov-Smirnov test
##
## data:  z2
## D = 0.019766, p-value = 0.8295
## alternative hypothesis: two-sided
```

```
## GRAPHIQUES
op <- par(mfrow=c(2,2))
hist(z2, probability=T, main='Loi Empirique')
lines(density(z2), col='red')

## Normale qqplot
qqnorm(z2,sub="z2")
qqline(z2)
par(op)
```



D'après le test de Kolmogorov Smirnov, la variable aléatoire V2 semble suivre une loi normale car la p-value = 0.8295 > 0.05.

c) Test adéquation pour la troisième variable :

```
library(MASS)
z3 <- ousman$V3
fitdistr(z3, "normal")
```

```
##          mean          sd
## 8760.186086    132.250239
## ( 4.182120) ( 2.957205)
```

## TEST POUR V3

```
## 1) Adequation de La Loi Empirique avec une Loi normale
ks.test(z3,"pnorm",mean= 8760.186086 ,sd= 132.250239)
```

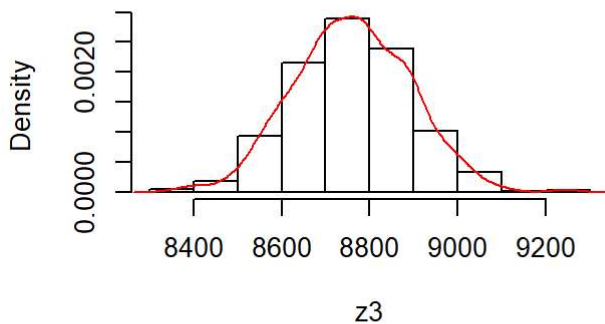
```
##
## One-sample Kolmogorov-Smirnov test
##
## data:  z3
## D = 0.018152, p-value = 0.8967
## alternative hypothesis: two-sided
```

### ## GRAPHIQUES

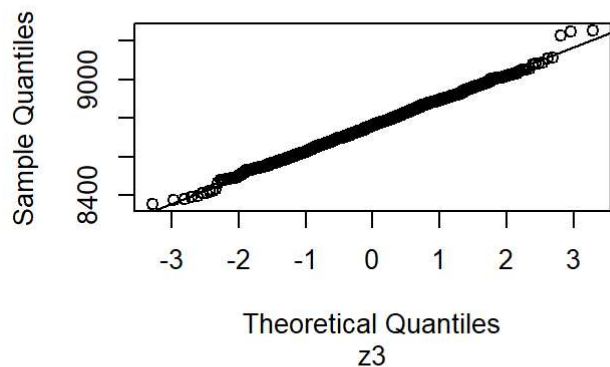
```
op <- par(mfrow=c(2,2))
hist(z3, probability=T, main='Loi Empirique')
lines(density(z3), col='red')

qqnorm(z3,sub="z3")
qqline(z3)
par(op)
```

**Loi Empirique**



**Normal Q-Q Plot**



La variable V3 suit approximativement une loi normale car sa  $p\_value=0.8967>0.05$ .

d) Test adéquation pour la variable V4 :

```
library(MASS)
z4 <- ousman$V4
fitdistr(z4, "normal")
```

```
##           mean           sd
## 1.314039e+04  3.134952e+01
## (9.913589e-01) (7.009966e-01)
```

## TEST POUR V4

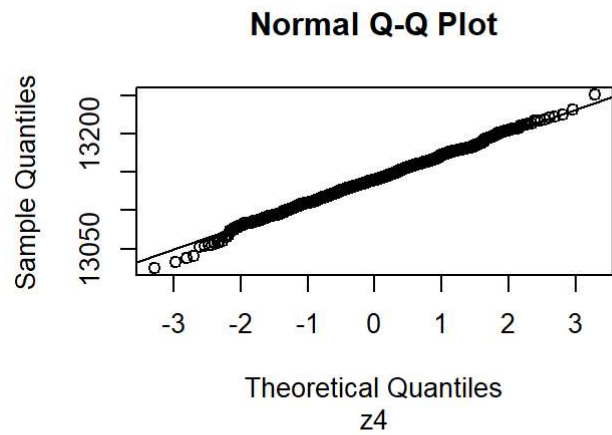
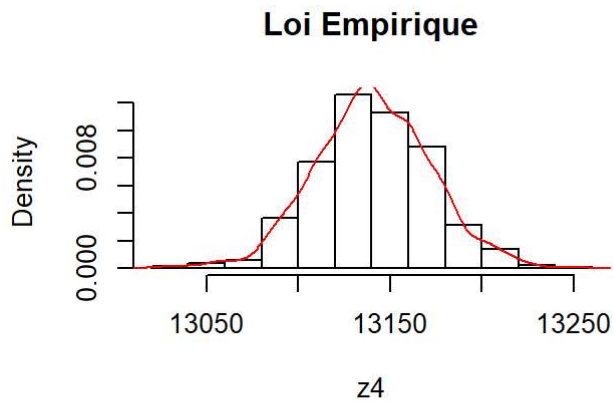
```
## 1) Adequation de la Loi Empirique avec une Loi normale
ks.test(z4,"pnorm",mean= 1.314039e+04 ,sd= 3.134952e+01)
```

```
##
## One-sample Kolmogorov-Smirnov test
##
## data:  z4
## D = 0.018753, p-value = 0.8734
## alternative hypothesis: two-sided
```

```
## GRAPHIQUES

op <- par(mfrow=c(2,2))
hist(z4, probability=T, main='Loi Empirique')
lines(density(z4), col='red')

qqnorm(z4,sub="z4")
qqline(z4)
par(op)
```



La variable V4 ressemble à la distribution d'une loi normale.

e) Test adéquat pour la variable V5 :

```
library(MASS)
z5 <- ousman$V5
fitdistr(z5, "log-normal")
```

```
##      meanlog      sdlog
## 8.68018494 0.50438789
## (0.01595015) (0.01127846)
```

## TEST POUR V5

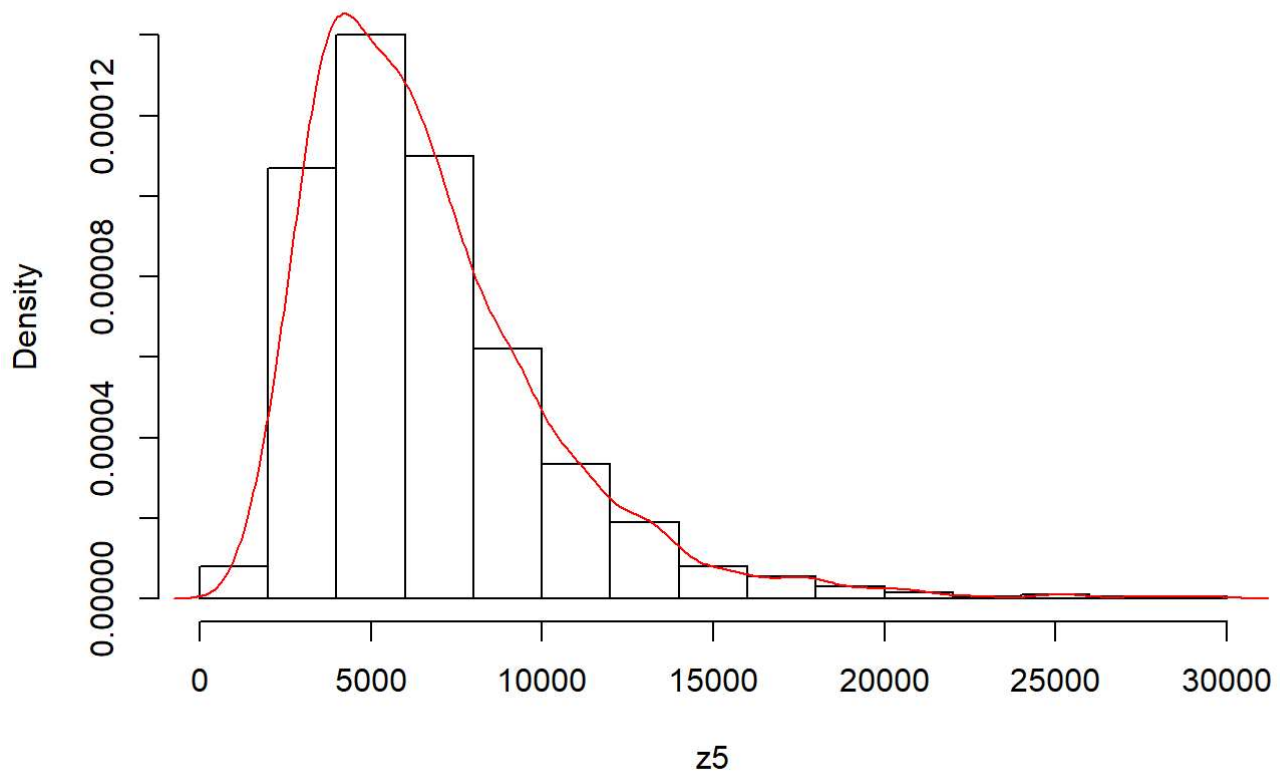
```
## 1) Adequation de la Loi Empirique avec une Loi normale
ks.test(z5, "plnorm", meanlog=8.68018494, sdlog=0.50438789 )
```

```
##
## One-sample Kolmogorov-Smirnov test
##
## data:  z5
## D = 0.017984, p-value = 0.9028
## alternative hypothesis: two-sided
```

```
## GRAPHIQUES
```

```
hist(z5, probability=T, main='Loi Empirique')
lines(density(z5), col='red')
```

## Loi Empirique



On constate que V5 suis une loi log-normale car sa p-value = 0.9028 > 0.05.

e) Test adéquation pour la variable V5 :

```
library(MASS)
z6 <- ousman$V5
fitdistr(z6, "log-normal")
```

```
##      meanlog      sdlog
## 8.68018494 0.50438789
## (0.01595015) (0.01127846)
```

**\*\* TEST POUR V5\*\***

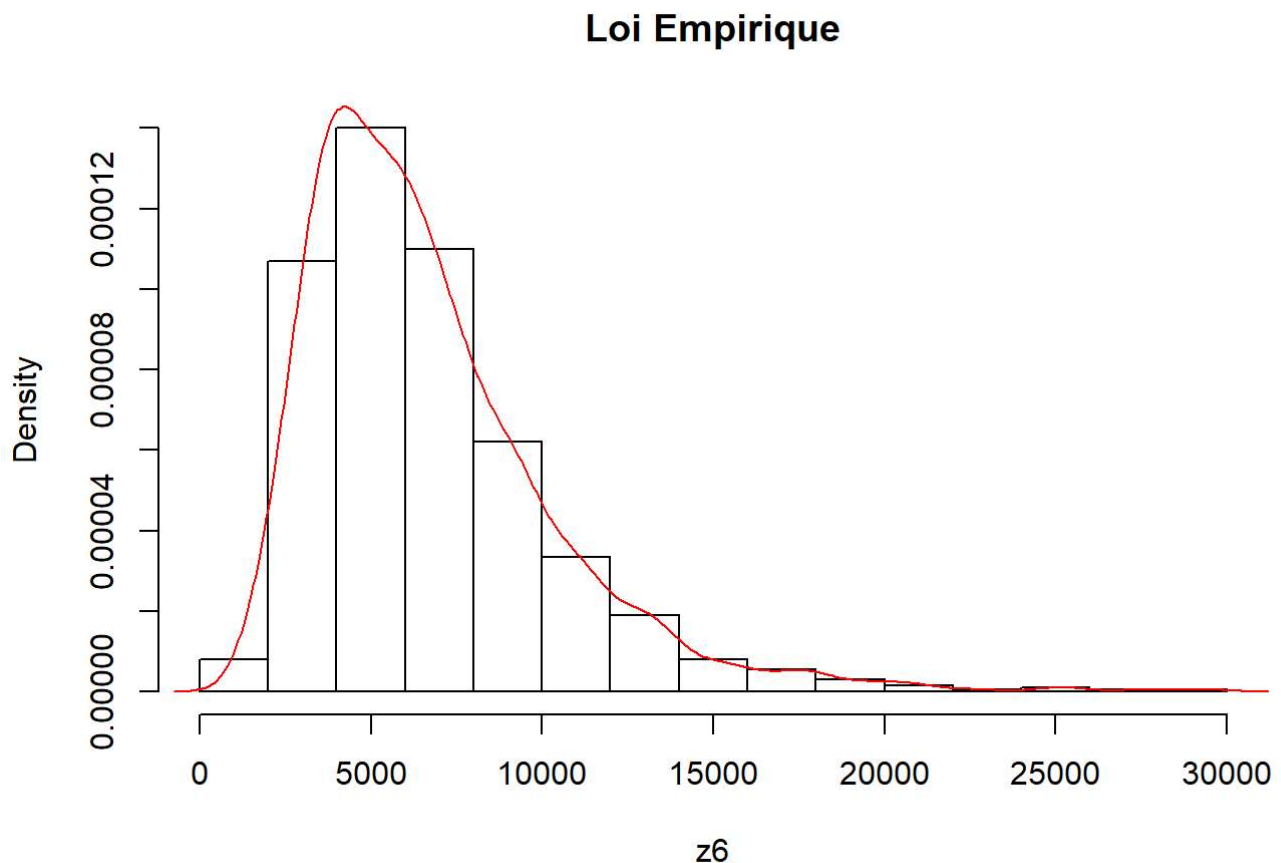
```
## 1) Adequation de La Loi Empirique avec une Loi normale
ks.test(z6,"plnorm",meanlog=8.68018494,sdlog=0.50438789 )
```



```
##
## One-sample Kolmogorov-Smirnov test
##
## data:  z6
## D = 0.017984, p-value = 0.9028
## alternative hypothesis: two-sided
```

```
## GRAPHIQUES
```

```
hist(z6, probability=T, main='Loi Empirique')
lines(density(z6), col='red')
```



La variable aléatoire ressemble à une loi log-normale car sa p-value = 0.9028 > 0.05.

2) Construisons des cartes de controle sur la moyenne, la variance et l'étendu pour les colonnes 7 à 107.

#### Récupération de colonnes 7 à 107

```
ousman_1 <- ousman[, 8:108]
ousman_1
```

```
## # A tibble: 1,000 x 101
##       V7      V8      V9      V10     V11     V12     V13     V14     V15     V16     V17     V18
##   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 2.88   3.25   2.08 2.49   1.79 2.17 2.04 1.82 1.35 2.42 2.45 1.52
## 2 2.97   1.42   1.42 2.52   2.50 2.03 2.27 1.93 2.76 1.35 1.63 2.28
## 3 2.23   1.60   2.97 1.83   1.67 2.39 1.69 2.24 2.31 2.39 1.72 0.925
## 4 1.83   2.54   1.34 0.961 1.88 2.25 2.04 2.17 1.10 3.11 1.86 2.72
## 5 2.37   2.09   2.05 2.88   2.30 1.86 1.62 1.76 1.88 1.92 1.56 1.80
## 6 0.828 2.49   2.37 2.67   2.63 1.92 1.39 1.97 1.60 1.12 1.95 1.62
## 7 1.59   2.03   1.48 1.59   1.96 2.31 2.50 2.63 1.71 1.78 1.92 1.98
## 8 1.86   1.53   2.11 2.67   1.79 2.20 1.77 2.01 2.53 1.87 2.00 2.21
## 9 2.20   1.81   1.46 1.18   1.50 1.56 2.36 2.16 1.49 1.29 1.19 2.24
## 10 1.98   2.03   1.64 1.29   1.31 2.04 1.75 1.92 2.07 1.80 2.28 1.60
## # ... with 990 more rows, and 89 more variables: V19 <dbl>, V20 <dbl>,
## #   V21 <dbl>, V22 <dbl>, V23 <dbl>, V24 <dbl>, V25 <dbl>, V26 <dbl>,
## #   V27 <dbl>, V28 <dbl>, V29 <dbl>, V30 <dbl>, V31 <dbl>, V32 <dbl>,
## #   V33 <dbl>, V34 <dbl>, V35 <dbl>, V36 <dbl>, V37 <dbl>, V38 <dbl>,
## #   V39 <dbl>, V40 <dbl>, V41 <dbl>, V42 <dbl>, V43 <dbl>, V44 <dbl>,
## #   V45 <dbl>, V46 <dbl>, V47 <dbl>, V48 <dbl>, V49 <dbl>, V50 <dbl>,
## #   V51 <dbl>, V52 <dbl>, V53 <dbl>, V54 <dbl>, V55 <dbl>, V56 <dbl>,
## #   V57 <dbl>, V58 <dbl>, V59 <dbl>, V60 <dbl>, V61 <dbl>, V62 <dbl>,
## #   V63 <dbl>, V64 <dbl>, V65 <dbl>, V66 <dbl>, V67 <dbl>, V68 <dbl>,
## #   V69 <dbl>, V70 <dbl>, V71 <dbl>, V72 <dbl>, V73 <dbl>, V74 <dbl>,
## #   V75 <dbl>, V76 <dbl>, V77 <dbl>, V78 <dbl>, V79 <dbl>, V80 <dbl>,
## #   V81 <dbl>, V82 <dbl>, V83 <dbl>, V84 <dbl>, V85 <dbl>, V86 <dbl>,
## #   V87 <dbl>, V88 <dbl>, V89 <dbl>, V90 <dbl>, V91 <dbl>, V92 <dbl>,
## #   V93 <dbl>, V94 <dbl>, V95 <dbl>, V96 <dbl>, V97 <dbl>, V98 <dbl>,
## #   V99 <dbl>, V100 <dbl>, V101 <dbl>, V102 <dbl>, V103 <dbl>, V104 <dbl>,
## #   V105 <dbl>, V106 <dbl>, V107 <dbl>
```

```
length(ousman_1)
```

```
## [1] 101
```

a) Carte de controle sur la moyenne pour les colonnes 7 à 107 :

```
# Construction des cartes
# install.packages("qicharts")
library(qicharts)
```

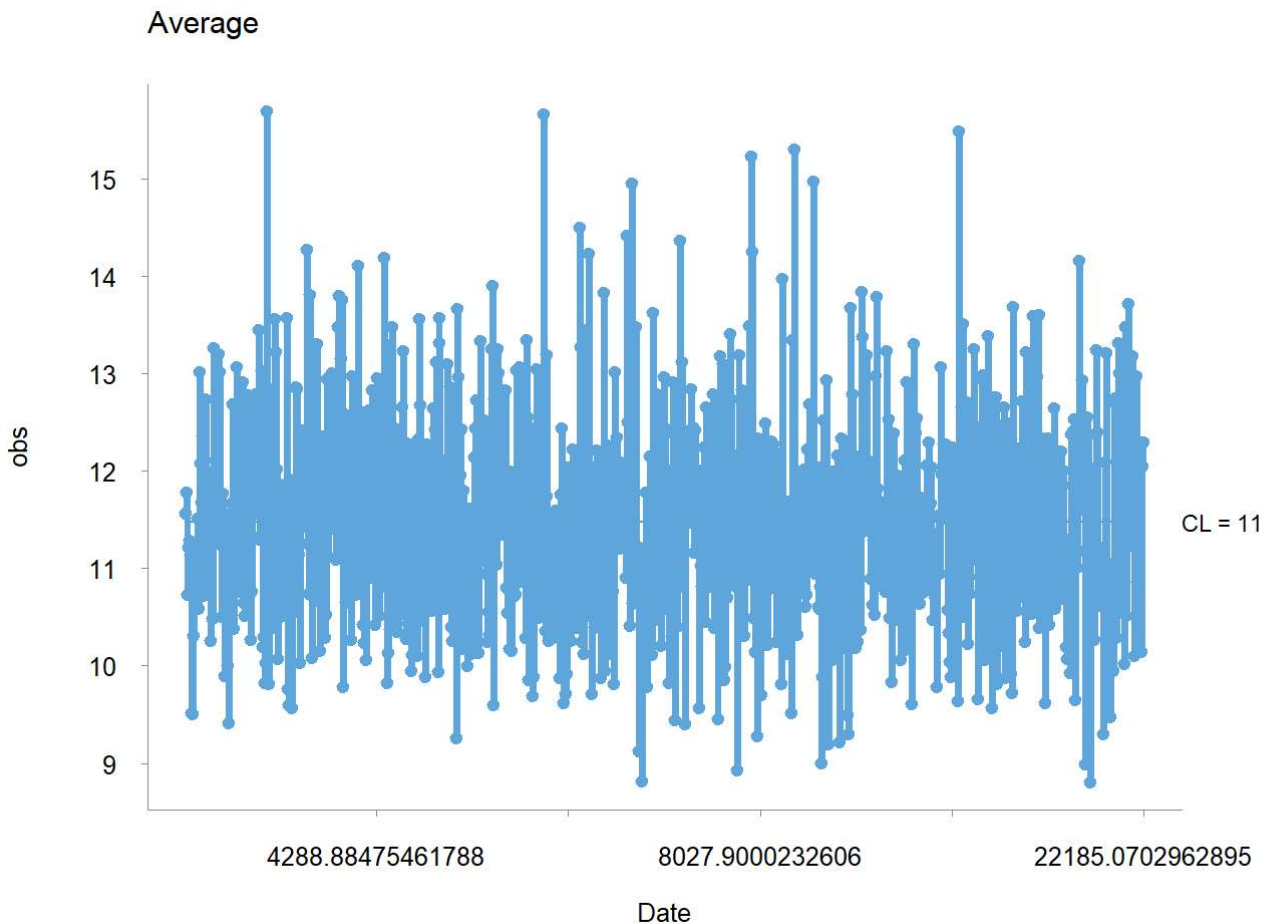
```
## Warning: package 'qicharts' was built under R version 3.5.2
```

```
## qicharts will no longer be maintained. Please consider moving to qicharts2: https://anhoe
j.github.io/qicharts2/.
```

```

data_extract = ousman[8:109]
average = apply(data_extract,1,mean)
control_chart = data.frame(time =ousman$Date , values =average )
qic(values,
  x      = time,
  data   = control_chart,
  chart  = 'xbar',
  main   = 'Average ',
  ylab   = 'obs',
  xlab   = 'Date')

```



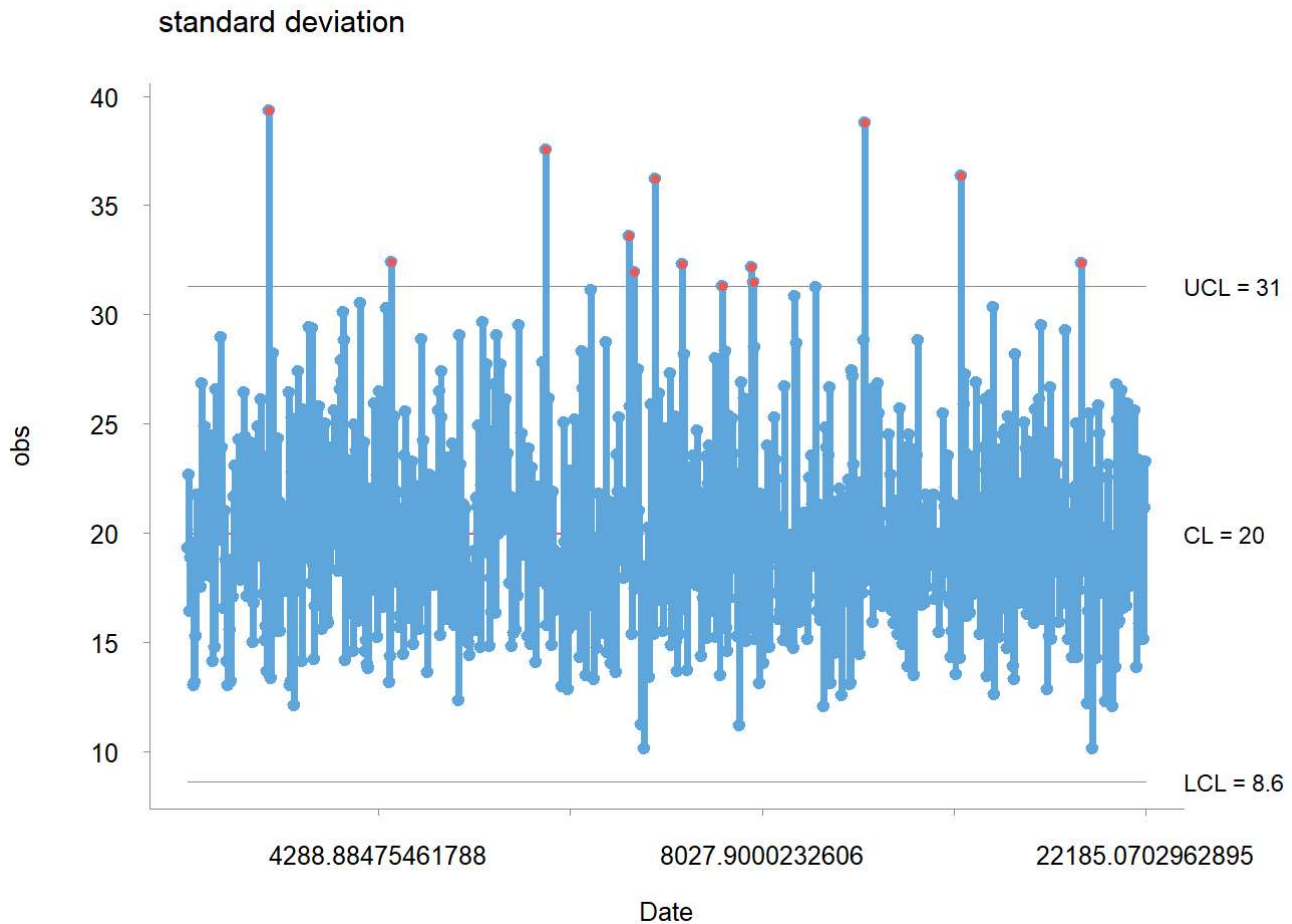
On constate à partir de la carte de controle sur la moyenne obtenue que le processus est **hors controle**.

a) Carte de controle sur la variance pour les colonnes 7 à 107 :

```

# Construction des cartes
# install.packages("qicharts")
library(qicharts)
data_extract = ousman[8:109]
stan_dev = apply(data_extract,1,sd)##### vecteur variance
control_chart = data.frame(time = ousman$Date , values =stan_dev )
qic(values,
  x      = time,
  data   = control_chart,
  chart  = 'i',
  main   = ' standard deviation ',
  ylab   = 'obs',
  xlab   = 'Date')

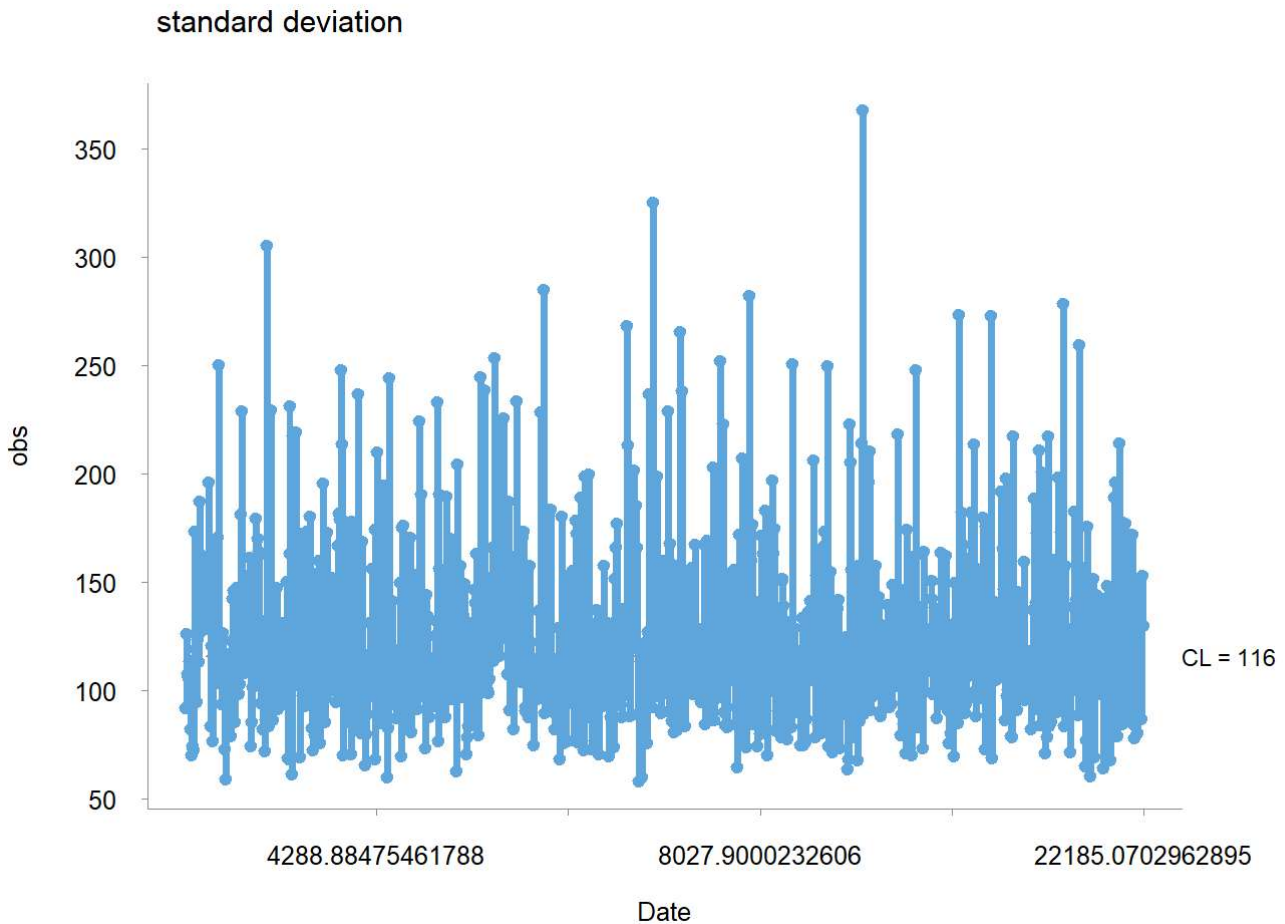
```



On constate à partir de la carte de controle sur la Variance obtenue que le processus est **hors controle**.

c) Carte de controle sur l'étendu pour les colonnes 7 à 107 :

```
# Construction des cartes
# install.packages("qicharts")
library(qicharts)
data_extract = ousman[8:109]
stan_dev = apply(data_extract,1,max) - apply(data_extract,1,min)
control_chart = data.frame(time = ousman$Date , values = stan_dev )
qic(values,
     x      = time,
     data   = control_chart,
     chart  = 'r',
     main   = ' standard deviation ',
     ylab   = 'obs',
     xlab   = 'Date')
```



On constate à partir de la carte de controle sur l'étendu obtenue que le processus est **hors controle**.

3) CUMSUM EWMA pour chaque colonne 108 et 109 pour détecter un changement par rapport à une moyenne égale à 2.

a) CUMSUM EWMA pour la colonne 108 :

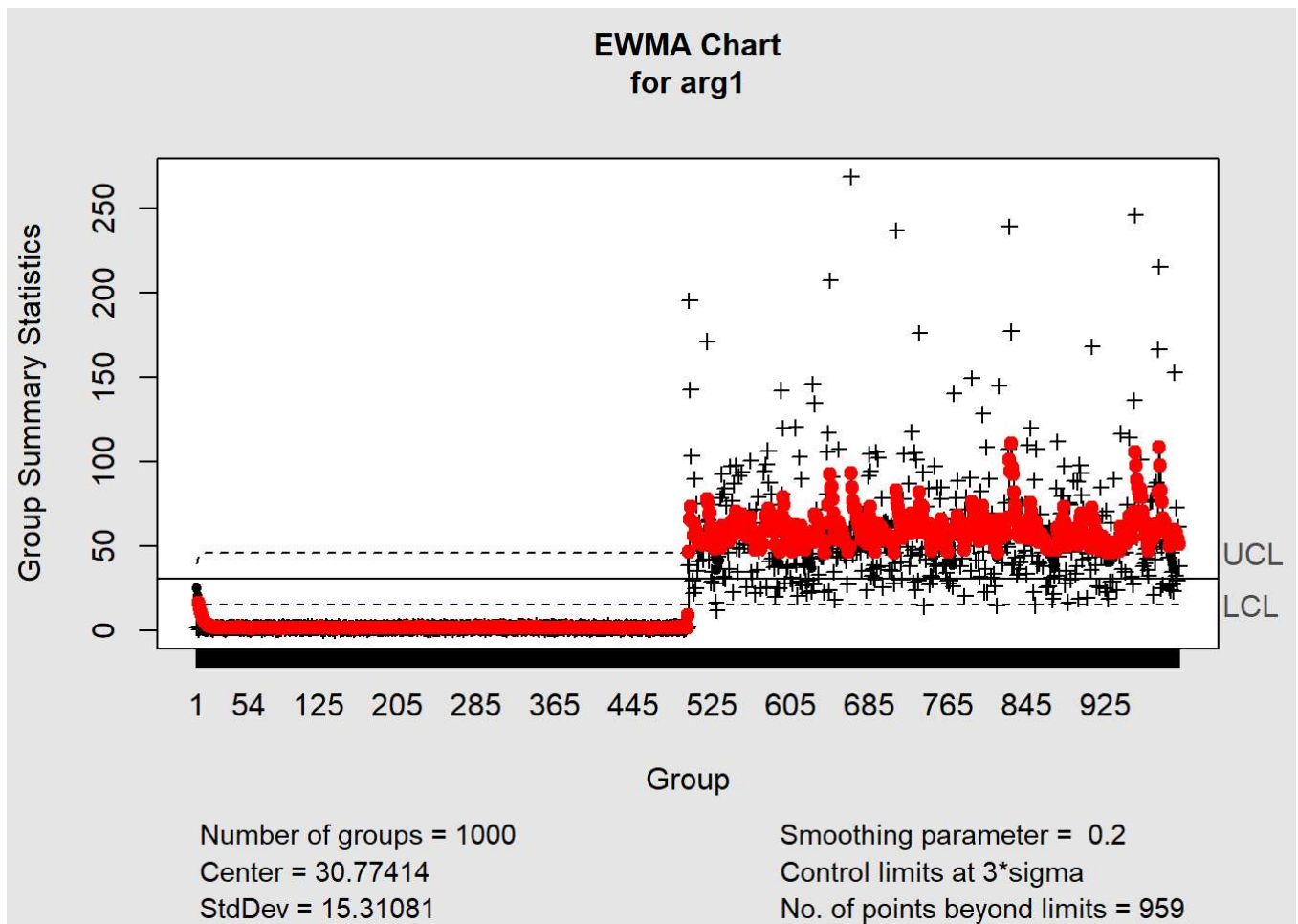
```
# Construction des cartes
#install.packages("qcc")
library(qcc)
```

```
## Warning: package 'qcc' was built under R version 3.5.2
```

```
## Package 'qcc' version 2.7
```

```
## Type 'citation("qcc")' for citing this R package in publications.
```

```
arg1 = ousman$V107
q1 = ewma(arg1, lambda=0.2, nsigmas=3)
```

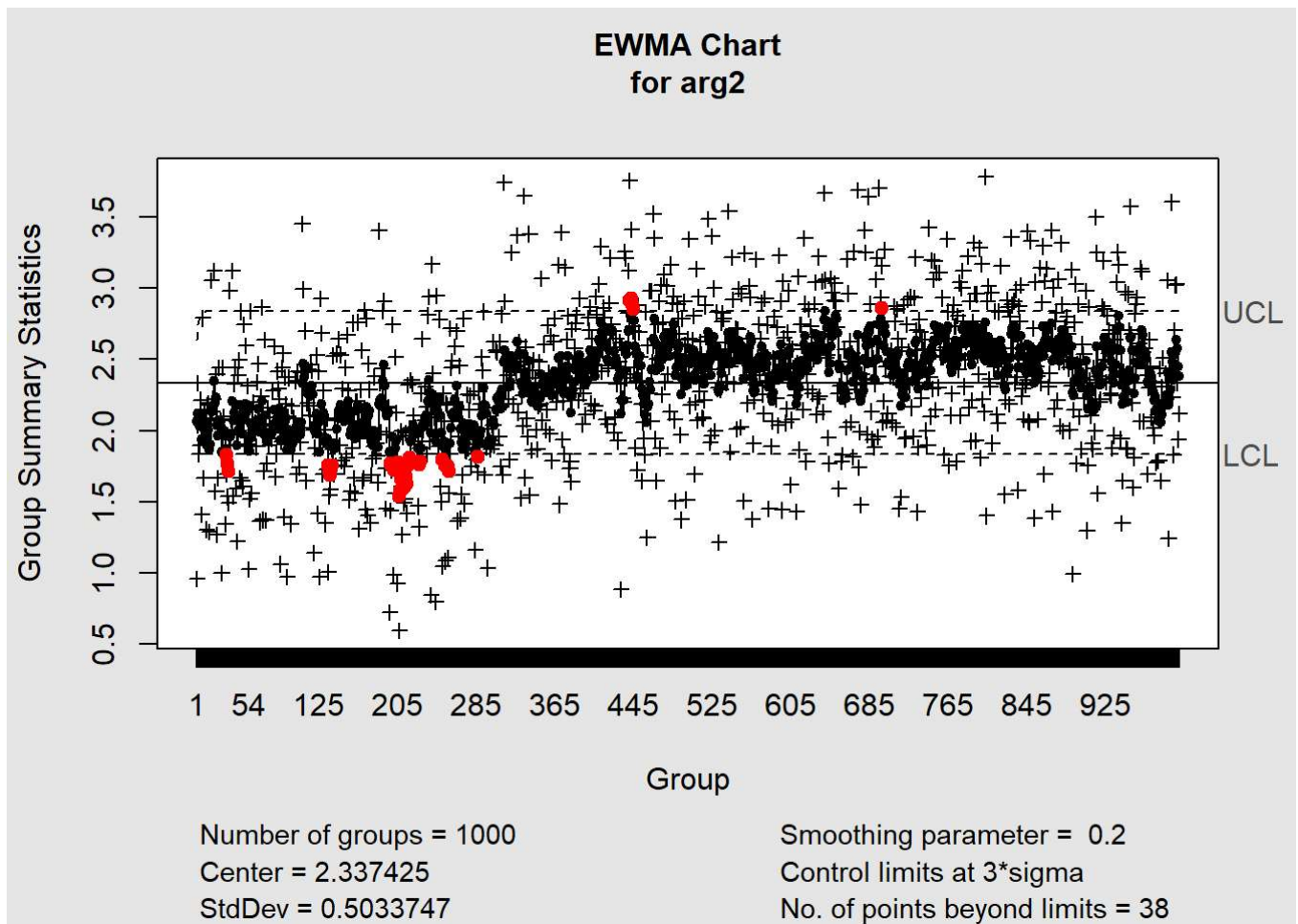


On constate à partir de la carte CUSUM EWMA obtenue que le processus est **hors controle**.

a) CUMSUM EWMA pour la colonne 109 :

```
# Construction des cartes
```

```
library(qcc)
arg2 = ousman$V108
q2 = ewma(arg2, lambda=0.2, nsigmas=3,col="")
```



On constate à partir de la carte CUSUM EWMA obtenue que le processus est **hors controle**.