

ICT

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June 25, 2020

Preface

\LaTeX typesets text as *What You See Is What You Type* compared with *What You See Is What You Get*. It gives finer control over text layout with a host of commands and add-ons. This book firstly demonstrates how \LaTeX supports Chinese typesetting and then moves on to syntax. A bit of ACTeX with Emacs configuration and key bindings are dicussed as well. Gradually, topics from different disciplines (i.e. math and language) are introduced in separate parts.

Priorly, I just planned to learn \LaTeX through trial and error. As it progressed, I found \LaTeX an awesome typesetting tool, creating beautiful text output. Hence, I decided to make it a book containing different parts, covering formal subjects like math, physics, etc. Ultimately, I want to maintain a centralized offline jottings which can be testified by the book title *Miscellanies*.

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Part I

LATEX

Chapter 1

L^AT_EX Resources

1.1 Find References

In part 2 on page 5, we have a simple clarification on how to insert Chinese characters in English articles. We will focus on L^AT_EX itself in this part.

Please find more appropriate at L^AT_EX ctan. Also, please find answers at [1]. You'd better go through the tutorial series [2]. My personal website [3] might give some ideas.

1.2 AUCTeX

1.2.1 Inserting

Have a look at L^AT_EX

1.2.2 L^AT_EX Sources Formating

Use C-c C-q C-s to format L^AT_EX section code. C-c C-q C-p is to format *paragraph* text.

1.2.3 Font Specifiers

Use C-c C-f C-i to insert *italic* text. Similarly, Use C-c C-f C-b to insert *bold* text. Read more at Insert Font Specifiers.

Binding	Function
C-c C-e	insert environment
C-c C-s	insert section
C-c C-m	macro (command)
M-return	another item
C-c C-c	compile L ^A T _E X
C-c C-v	preview output
C-c =	show document layout by RefTeX
C-c C-o C-b	fold the buffer
C-c C-o b	unfold the buffer
C-c C-r	compile selected region
C-c C-b	compile current buffer

Table 1.1: AUCTeX Bindings

C-c C-f C-i	italic
C-c C-f C-b	bold
C-c C-f C-e	emphasize
C-c C-f C-s	slight italic
C-c C-f C-r	roman
C-c C-f C-f	sans
C-c C-f C-d	delete font formating

Chapter 2

汉语

对字体的引用要注意，如果一个字体族 family 有多个变种¹，请引用字体的 postscriptname.

默认情况下， \LaTeX 会把文档里用到的字体子集内嵌到生成的 PDF 里，可以通过命令行 $\text{pdffonts filename.pdf}$ 查询，结果如 A 所示。

此例说明，对应文档内嵌了七个字体子集。 \LaTeX 文档通常只会用到字体文件的部分 code point，所以只需要内嵌使用到的部分即可。每个字体的前面都有一串无规则字母，代表对应字体文件被内嵌的子集。还有一列叫 sub 也说明是否是子集。

2.1 CJK 包

在英文文档里插入少量中文

2.1.1 CJK 和 CJK* 环境

在英文文档里用 CJK 包的 CJK 或 CJK* 环境插入少量汉字。后者会忽略汉字后面的空格，推荐使用。

2.1.2 字体

`bsmi` 字体可能没有，尝试换一个如 `gkai`, `gbsn` 等。

¹如 `regular`, `bold`, `italic` 等。

2.2 xeCJK 更好

xeCJK 在处理细节上更好，关键是可方便设置中英文字体。用 xeCJK 则不需要特殊环境包裹汉字，只需在“导言区”设置好中英文字体即可。

xeCJK 的 `indentfirst` 选项：

```
\usepackage[indentfirst]{xeCJK}
```

已过时，推荐直接用 `indentfirst` 宏包：

```
\usepackage{indentfirst}
```

2.3 fontspec 和 ctex

还有 `fontspec` 和 `ctex` 包可以实现中文输入，更多详情请看 L^AT_EX post.

- `fontspec` sets western or Chinese fonts (i.e. main, sans, serif, bold, italic, and bolditalic).
- `CJK` sets Chinese, Japanese, and Korean fonts, punctuation etc. for TeX engine.
- `xeCJK` similar to `CJK` but for XeTeX engine.
- `CTeX` sets CJK/xecjk document layout.

2.4 中英文空格

我们想要的效果是英文字符前后自动加上空格。xeCJK 则会自动处理，但是效果不是非常好。

CJK 会忽略 T_EX 源码里的空格。用 CJK 宏集里的 `CJKspace` 包，源码里英文后空格会保留，中文后空格依然被 CJK* 压缩。还有一个方法是在需要空格的地方用 `tilde ~`。

2.5 行首缩进

中文习惯每段行首缩进两个汉字。英文有两种缩进格式。默认是每小节的第一段缩进，后面的段不缩进，段间没有空行。另一种是不缩进，每段间留有空行。

本文档只插入少量中文作例子，固保留英文默认缩进方式。如要换成中文缩进，则用 `indentfirst` 包，使每节第一段也缩进，如下：

```
\usepackage{indentfirst}
\setlength{\parindent}{2em}
```

如若换成英文第二种缩进，则用 `parskip` 包，`skip` 表示相临两段之间的间隙大小：

```
\usepackage[parfill]{parskip}
```

也可用相对应的命令实现：

```
\setlength{\parindent}{0pt}
\setlength{\parskip}{1ex plus 0.5ex minus 0.2ex}
```

2.6 局部字体命令

前面提到的方法都是全局生效，有没有类似 `\emph{}` 和 `\textit{}` 这种临时改中文字体的方法呢？

在 `xecjk.tex` 中有如下代码：

```
1 % set new font family
2 \setCJKfamilyfont{zhyaher}{msyh}[
3   Path = fonts/,
4   Extension = .ttf,
5   BoldFont = {*bd}
6 ]
7
8 % create font family command alias
9 \NewDocumentCommand{\yahei}{m}{\setCJKfamily{zhyaher}}
```

Listing 2.1: New font family

根据需求定义一个新的字体族 `family` 名 `zhyaher`，新字体族的引用方法是：

```
1 {\setCJKfamily{zhyaher}{这里输入中文}}
2 % -or-
3 {\setCJKfamily{zhyaher}这里输入中文}
```

Listing 2.2: Inline Chinese fonts

为了方便，我们还定义一个新 `NewDocumentCommand` 命令，便于快速引用。`{\yahei{这是新定义的雅黑字体样例。}}` 的效果如：这是新定义的雅黑字体样例。

特别注意，命令要放在一个 `group` 里，即用 `{}` 围起来，否则从当前位置起，所有中文字体都改了。实际，`fontspec` 提供类似功能，具体请参考 `fontspec` 文档。如：

```
\fontspec{<font name>}[<fontfeatures>] 和 \newfontfamily
```


Chapter 3

L^AT_EX Tutorial

3.1 T_EX Units

mm	millimetre $\approx 1/25$ inch	□
cm	centimetre = 10 mm	□
in	inch = 25.4 mm	□
pt	point $\approx 1/72$ inch $\approx \frac{1}{3}$ mm	□
em	approx width of an ‘M’ in the current font	□
ex	approx height of an ‘x’ in the current font	□

Figure 3.1: T_EX Units

3.2 Special characters

The following 10 characters has special meanings in L^AT_EX.

& % \$ # _ { } ~ ^ \

Outside *verb*, the first 7 should escaped by *backslash*. Of the last three, we use L^AT_EX macros, namely \textasciitilde, \textasciicircum and \textbackslash.

```
1 \& \% \$ \# \_ \{ \} \textasciitilde{} \textasciicircum{} \textbackslash{}
```

Listing 3.1: Special Characters

Specially, L^AT_EX uses tilde ~ as a non-breaking space. You would usually use non-breaking spaces for punctuation marks in some languages, for units and currencies, for initials, etc.

3.3 Text Size

List 3.2 shows available LATEX text size.

```
1 \tiny \scriptsize \small \normalsize \large \Large \LARGE \huge \Huge
```

Listing 3.2: LaTeX Text Size

3.4 verbatim and verb

When to show raw text without LATEX command being executed, use *verbatim* environment or *verb* command. Both have an asterisk alternative like `\begin{verbatim*}` and `\verb*{}`. With extra *, LATEX will typewrite space as `_`.

You can't use `\verb` in other command's parameters. For example, this is not allowed:

```
1 \href{https://tex.stackexchange.com/a/23653}{When should we use
  \verb|\begin{center}| instead of \verb|\begin{centering}|?}
```

Listing 3.3: Illegal verb

Instead, we use `\texttt` and escape special characters¹ like:

```
2 \href{https://tex.stackexchange.com/a/23653}{When should we use
  \texttt{\textbackslash begin\{center\}} instead of \texttt{\textbackslash
  begin\{centering\}}?}
```

Listing 3.4: texttt

3.5 item list

Using lists is quite straightforward and does not require you to add any additional packages. For unordered list, LATEX provides the *itemize* environment and for ordered list there is the *enumarate* environment. With both environments, elements should be declared beginning with `\item` command. We can use M-Enter binding to insert this command automatically.

Take a look at unordered list 3.5:

¹For instance, backslash and {.

```

1 \begin{itemize}
2   \item One
3   \item HKUST
4   \item HUST
5 \end{itemize}

```

- One
- HUST
- HKUST

Here is an ordered list 3.5:

1. Jim
2. Gray
 - This is a
 - nested unordered
 - list within ordered list
3. Who are you?

```

1 \begin{enumerate}
2   \item Jim
3   \item Gray
4     \begin{itemize}
5       \item This is a
6       \item nested unordered
7       \item list within ordered
8       \item list
9     \end{itemize}
10 \item Who are you?
\end{enumerate}

```

3.6 Code listings

Although *verb* and *verbatim* enclose raw text, they don't highlight source code like C, Java etc. This is where *listings* package come into usage.

To insert a code block, use *lstlisting* environment like

```
\begin{lstlisting}[language=bash,caption={Bash},frame=single]
```

Here is an example:

```

1 #!/bin/bash
2 echo 'Hello, world!'

```

Listing 3.5: Bash

Furthermore,

```
\lstinputlisting[language=C,frame=tb,basicstyle=\scriptsize\ttfamily]{helloworld.c}
```

Listing 3.6: Include code file

command includes code source file:

```

1 # include<stdio.h>

```

```

3 int main(void *) {
4     printf("Hello, world!\n");
5     return 0;
}

```

Listing 3.7: C98

This is useful when the code needs updating frequently.

To prevent *lstlisting* from breaking pages, we should wrap it within *minipage* environment as 3.10.

Sometimes, code line is too long to fit page width, leaving tailing part out of page. We could modify *basicstyle* to one of *footnotesize*, *scriptsize* and *tiny*. Check long text line example A. For more options, read Font Size and font size and point (pt) relation.

This is LARGE text while this is Huge.

3.7 Straight Quotes

By default, *listings* typesets both single and double as *back curve ones*.

We should import *textcomp* package and *fontenc* package with T1 option. Then, enable *upquote=true* for code block. Read more at How can I get straight double quotes in listings?

This method, however, is discouraged as *fontenc* would override the whole document L^AT_EX font settings. The underlying cause is *serif(roman)* font. Default roman fonts does not provide straight quotes. We should tell *listings* to use *monospace* font instead by

```
\lstset{basicstyle=\ttfamily}
```

Read more at Consolas: Straight Quotes.

3.8 floating

3.8.1 Figure

First, we import *graphicx* package and then set *graphicspath* in preamble part:

```

1 \usepackage{graphicx}
2 \graphicspath{{figs/}{./}}

```

Listing 3.8: graphicx

graphicx accepts EPS, PDF, PNG or JPEG formats. *graphicspath* defines a list of directories relative to that of *master.tex*. By this means, we can access images anywhere without restriction like `\graphicspath{{.../img/}}`. The trailing slash cannot be omitted.

Then, we use command *includegraphics* like

```
\includegraphics[scale=0.5]{myimg}
\includegraphics[width=.5\linewidth]{myimg}
```

Notice that we do not write figure file extension. Here is the output:



With bare *includegraphics*, if remaining space within current page does not hold the figure, L^AT_EX would start a new page instead, leaving current page partially empty. The method is to wrap it with *figure* environment:

```
1 \begin{figure}[tbp]
2   \centering
3   \includegraphics[width=\textwidth]{Boobs}
4   \caption{Boobs}
5   \label{fig:Boobs}
6 \end{figure}
```

Listing 3.9: Figure Floating

We call this technique as *floating*. Apart from *placement specifier* benefits, we can define *label* and *caption* within *floating* environment. Note that `\label{}` command must come **after** `\caption{}` command since the reference number is generated by `\caption{}`. For details, refer to Why does an environment's label have to appear after the caption?.

The `tbp`² specifies position of floating environment.

²*tbp* is the default *placement specifier*. We could set it to *lhtb*.

Spec	Permission to place the float ...
h	here at the very place in the text where it occurred. This is useful mainly for small floats.
t	at the <i>top</i> of a page
b	at the <i>bottom</i> of a page
p	on a special <i>page</i> containing only floats.
!	without considering most of the internal parameters ^a , which could otherwise stop this float from being placed.

Figure 3.2: Floating Placement Specifiers

Here is a nice boobs example 3.3:



Figure 3.3: boobs

Sometimes, it's necessary to put figures side by side for clear comparasion. We use *subfigure* within *figure* like 3.4. Please be noted that we add non-breakable symbol ~ between *subfigure* to leave some space between figures.

3.8.2 Table

Similarly, we can wrap *tabular* within *table* environment to *float* table 1.1 like 3.10. In the table, \small changes the text size, which is useful when the table has long columns. Check list 3.2 for more text size options.

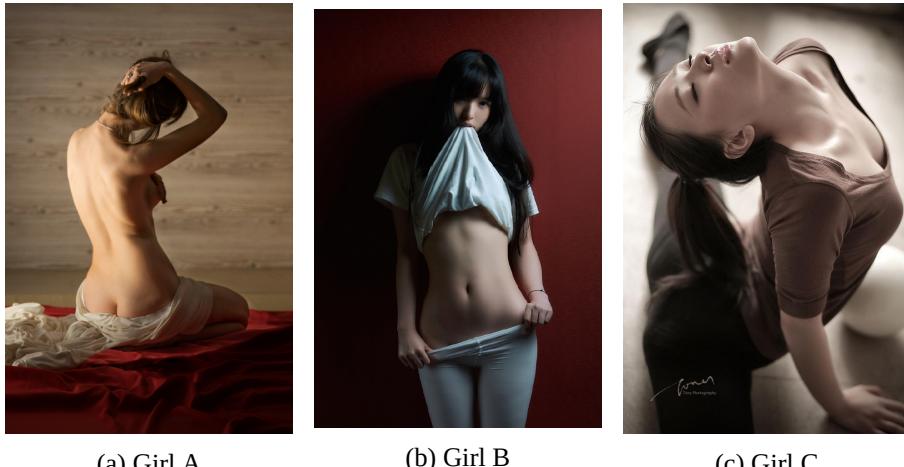


Figure 3.4: Three Girls

```

1 \begin{table}[!htb]
2   \small
3   \centering
4   \begin{tabular}{|l|r|}
5     \hline
6     Binding & Function & \hline \hline
7     \verb|C-c C-e| & insert environment & \hline
8     \verb|C-c C-s| & insert section & \hline
9     \verb|C-c C-m| & macro (command) & \hline
10    \verb|M-return| & another item & \hline
11    \verb|C-c C-c| & compile \LaTeX{} & \hline
12    \verb|C-c C-v| & preview output & \hline
13    \verb|C-c =| & show document layout by RefTeX & \hline
14    \verb|C-c C-o C-b| & fold the buffer & \hline
15    \verb|C-c C-o b| & unfold the buffer & \hline
16  \end{tabular}
17  \caption{AUCTeX Bindings}
18  \label{tab:auctex-bindings}
\end{table}

```

Listing 3.10: Table Floating

In *tabular* environment, we align column texts as *left*, *center* and *right*. What about decimal number cell? Ideally, we want to align numbers at dot, where package *siunitx* plays a role by **S** 3.1 alignment specifier.

```

1 \usepackage[round-mode=places,round-precision=3]{siunitx}

```

Listing 3.11: Decimal Alignment

To make prettier table, we use package *booktabs* which provides *toprule*, *midrule*

and *bottomrule* to override³ dull *hline*.

List 1	Decimal 2	Letter 3
α	β	γ
1	1385.100	a
2	3.067	b
3	87.369	c

Table 3.1: Number Alignment at Dot

To make more complex tables, we can use package *multirow* and *multicolumn* environment respectively.

When typesetting large tables, it is tedious and error-prone which could be avoided by *pgfplotstable* package that generate tables from external .csv file. Programs such as Excel, OpenOffice Calc or even emacs org-mode can export data sheets as .csv files. The *pgfplotstable template A.3* generate table 3.2.

3.8.3 Plot

The *pgfplots* package is a powerful tool, based on *tikz* package, dedicated to create scientific graphs. Similar to *pgfplotstable*, *pgfplots* can read date from .csv file.

Since *pgfplots* is based on *tikz*, the *axis* environment should be enclosed within *tikzpicture* environment. Template A.3 generates plot 3.5.

addplot plots 2D figure, for 3D, we use *addplot3* 3.6.

Besides *pgfplotstable* and *pgfplots*, we could aslo use *tgiz* package or *circuitkiz* to \draw pictures from within your LaTeX document.

³It is not replace!

<i>Ampere</i>	<i>Voltage</i>	<i>Energy</i>
A	V	J
3	5	45
5.303	4.871	136.955

Table 3.2: Table automation from .csv file.

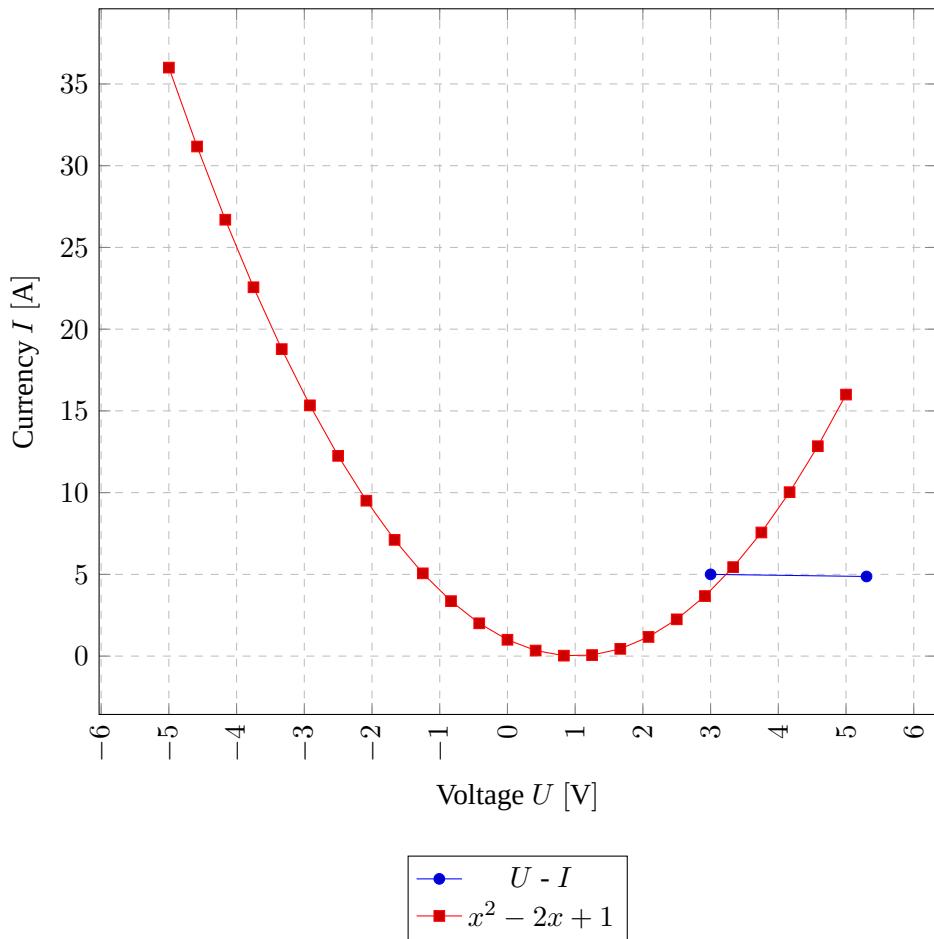


Figure 3.5: pgfplots by table csv file

3.9 center and centering

The main difference between *center* environment and *centering* command is the former leave vertical space before and after it while the later would not.

We usually use `\centering{}` command within a group by curly braces, figure, table, or `\begingroup \centering ... \endgroup` 3.12.

```

1 { \centering{centering require line break by \par, empty line or \\ before closing the group, otherwise text following the group would
3 be centered either.} }\\
}

```

Listing 3.12: centering within braces

centering require line break by `\par`, empty line or `\\\` before closing the group,

Exmple using the mesh parameter

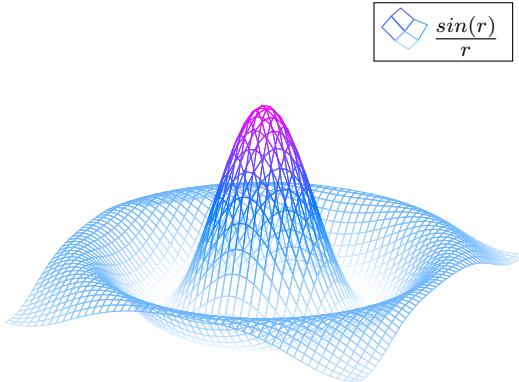


Figure 3.6: pgfplots 3D

otherwise text following the group wound be centered either.

This line is not centered! Check When should we use `\begin{center}` instead of `\centering`? and center vs. centering

3.10 Math Equations

To insert simple inline equation, we wrap it by \$ like `$c^2=a^2+b^2$`: $c^2 = a^2 + b^2$.

For tall or deep inline math expressions or sub expressions, we can enclose them by `\smash` command. This makes LATEX ignore the height of these expressions. This keeps the line spacing even like: $d_{e_{e_p}}$ followed by h^{i^g} .

This is an example without `\smash`. You will find line space is much bigger. A $d_{e_{e_p}}$ expression followed by a h^{i^g} one.

If we want equaton occupy a whole line, then wrap it by double \$\$ or single bracket \[\]. The equation will be centered automatically.

$\$\$(1+x)^n=\sum_{k=0}^n \binom{n}{k} x^k\$\$$

Listing 3.13: Equation in new line

This is the output:

$$(1 + x)^n = \sum_{k=0}^n \binom{n}{k} x^k$$

Let's have another example:

$$A_1 + A_{100}$$

After examining the example above, you are recommended to tune AUCTeX 1.2 configuration a little bit. Enable math mode manually by $\text{C-c } \sim$ or globally into Emacs startup:

```
1 (add-hook 'LaTeX-mode-hook 'LaTeX-math-mode)
```

Listing 3.14: \LaTeX Math Mode

We just prepend ` and type your desired math symbol. AUCTeX automatically completes it. If given a prefix argument C-u , the symbol will be surrounded by dollar signs. For example, if you type $\text{C-u } ` b$, AUCTex will typeset $\$\\beta\$$. Read AUCTex manual Entering Mathematics for more details.

The \$ method by \TeX does provide some basic mathematics features, but it is limited. we should `\usepackage{amsmath}`. What is more, we can `\usepackage{amssymb}` to make math symbols look shiny.

A bit further, we usually want to label and number a equation so that we can refer to it somewhere else. Furthermore, it is better for a long equation to occupy a new line. To do this, enclose equation with *equation* environment like (3.1). Einstein says

$$E = mc^2 \quad (3.1)$$

In order that multiple equations or multiple lines of a single equation align properly at *ampersand &* or we use *align* or *align** instead. (3.10). Each single equation must be separated by *linebreak*

- . The version with asterisk just removes equation numbers.

$$E = mc^2 \quad (3.2)$$

$$F = ma \quad (3.3)$$

We could also use *aligned* environment to achieve the same goal. But, *aligned* should be enclosed within an *equation* environment.

$$\begin{aligned} f(x) &= x^2 \\ \frac{1}{x} &= g(x) \\ F(x) &= \int_b^a \frac{1}{\sqrt[3]{x}} \end{aligned}$$

Compared to *aligned*, *align* and *align** introduce extra space between lines to make the output cleaner. Therefore, irrespective of single equation or multiple equations, we'd better use *align* and/or*align**.

matrix environment must be enclosed by equation marker & or *equation* environment.

```

1 $ 
2 \begin{matrix}
3   1 & 0 \\
4   0 & 1
5 \end{matrix}
$
```

Listing 3.15: Matrix

Similary, matrix breaks line by \\ and & separates columns. Here is a *bmatrix* example:

$$A_{m,n} = \begin{bmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n,1} & a_{n,2} & \cdots & a_{n,n} \end{bmatrix} \quad (3.4)$$

Recall that \$\$ or \[\] let an equation placed on a new line without label. They are equivalent to the \begin{equation*} environment.

3.11 Document Structure

3.12 Boxes

Everything in LATEX is embedded in boxes, from letter to words, *tabular* to *include-graphics*. TeX builds pages by gluing⁴ boxes together according to the default TeX rules, default LATEX rules, or document commands.

Box is of paramount importance to get the base of LATEX typesetting. Boxes are placed relative to other boxes, while visible elements are placed relative to the boxes which contain them.

Let's have a look at letter box illustration 3.7.

\parbox is a box to wrap text into lines and lines are broken into pages.

⁴Squeeze and/or Stretch



Figure 3.7: Letter Box

```
\parbox[pos][height][contentpos]{width}{text}
```

Listing 3.16: parbox box

width is a forced parameter to define box width⁵ This argument can be relative value like `.8\textwidth`, absolute value like `5ex`, or L^AT_EX and T_EX macros like `\width`. Similarly, we set *height* in the same way.

pos selects which *baseline* of text to align with neighbouring box. It can be `center`, `top`, and `bottom`. For details, read the link above. Check 3.8 for real effect.

This is a text line before *parbox* This a text within *parbox*. Please This a tex line
check text box and text align-
ment carefully.

after *parbox*.

contentpos positions the contents of the box within the box which is straightforward. It only takes effect when box is larger than texts it encases.

However, if the *contentpos* is present and not the same as *pos* and *pos* is not `center`, the `\parbox` will align at its borders instead of text baseline 3.9.

This is a text line before *parbox*

This a tex line

This a text within *parbox*. Please
check text box and text align-
ment carefully.

after *parbox*.

We also have *minipage* environment box which is almost identical to `\parbox`. The difference between a *minipage* and a `\parbox` is that you cannot use all commands and environments inside a `\parbox`, while almost anything is possible in a *mini-page*. Hence, without special requirement, we use the later one.

```
1 \begin{minipage}[pos][height][contentpos]{width} text \end{minipage}
```

⁵It is **not** text width.

Listing 3.17: minipage box

Additionally, there are *mbox*, *makebox* and *framebox*.

In order to let multiple boxes stand side by side, we should make sure their *width* in total is less than 1, like 3.5.

3.12.1 input and include

Like other programming language, LATEX supports splitting large document into different parts and importing them individually.

Use `\include{filename}` in the *document body* to insert the contents of another file named *filename.tex*. Note that LATEX will start a new page before processing the material input from *filename.tex*. *include* is commonly used for *chapter* section.

include's sibling command `\includeonly{filename1,filename2,...}` is used in *preamble* part to insert only a subset of *included* files.

Alternatively, `\input{filename}` is allowed in both *preamble* and *body* parts. It does not start a new page like *include* but allow recursive *include* which is impossible for *include*.

No matter which you choose, please omit LATEX file extension *.tex*.

3.12.2 biblatex biber

Generally speaking, *biblatex* and *natbib* are packages that handle LATEX citations in *.tex* source file. However, reference entries are stored separately in external *.bib* file. Hence, we require an intermediate tool to format *.bib* into *.tex* source. That's when we meet *biber* and *bibtex* which are named as *biblatex backend*.

Firstly, we should use *biblatex* package: `\usepackage[backend=biber]{biblatex}` and point out the external *.bib* file to import: `\addbibresource{myref.bib}` in *preamble* part. Do not omit *.bib* extension.

Secondly, in the end of LATEX source (but before `\end{document}`), we print all reference entries: `\printbibliography[heading=bibintotoc]`.

Then, cite as you go. Before that, we should have a look at *.tex* format. The bibliography files must have the standard *bibtex* syntax. Here is a reference entry:

```

1 @article{einstein,
2   author = "Albert Einstein",
3   title = "{Zur Elektrodynamik bewegter K{"o}rper}. ({German})"

```

```

5   [{On} the electrodynamics of moving bodies]",
6   journal = "Annalen der Physik",
7   volume = "322",
8   number = "10",
9   pages = "891--921",
10  year = "1905",
11  DOI = "http://dx.doi.org/10.1002/andp.19053221004",
12  keywords = "physics"
13 }
```

Listing 3.18: BibTeX entry sample

`@article` tells the reference is an article. We also have `@book`, `online` etc. `einstein` is the reference label that we will `cite` with: `\cite{einstein}`.

3.12.3 RefTeX

RefTeX has been bundled and pre-installed with Emacs since version 20.2. We just add to Emacs:

```

1 ; with AUCTeX LaTeX mode
2 (add-hook 'LaTeX-mode-hook 'turn-on-refTeX)
3 ; with Emacs latex mode
4 (add-hook 'latex-mode-hook 'turn-on-refTeX)
```

Listing 3.19: Enable RefTeX

To make cross-reference clickable (i.e. table of contents), use package `hyperref`.

Although `C-c C-m` can prompt for `\cite` command, we'd better use RefTeX instead. RefTeX wraps itself round four LaTeX macros: `\label`, `\ref`, `\cite`, and `\index`, making the process more intelligent.

As mentioned earlier, RefTeX binding `C-c =` displays document layout in a newly created buffer.

To `cite`, we use `C-c [` binding and press `^M`⁶. Afterwards, type a *regular expression* to search reference entries in `.bib` file. Please be noted, there is no completion prompt for *regular expression*.

For reference to objects (i.e. figures) within the document, we use `C-c)`. For details, please visit RefTeX in a Nutshell. RefTeX seems not to support `href` to URLs.

Sometimes, RefTeX cannot find newly created labels, references etc. We should tell it to `refTeX-parse-all` or `refTeX-parse-one` to parse L^AT_EX source files.

⁶It is Enter key or Ctrl and letter 'm', not Emacs Meta Alt key.

<p>This is not a parbox.</p>	<p>This parbox is top aligned. The baseline of the top line in this paragraph lines up with the non-parbox baseline. The top of the parbox doesn't align with anything.</p>
<p>This is not a parbox.</p>	<p>This parbox is bottom aligned. The baseline of the bottom line in this paragraph lines up with the non-parbox baseline. The bottom of the parbox doesn't align with anything.</p>
<p>This is not a parbox.</p>	<p>This parbox is center aligned. Because there are an even number of lines, the imaginary line halfway between the top and bottom baselines line up with the non-parbox baseline. The center of the parbox doesn't align with anything.</p>
<p>This is not a parbox.</p>	<p>This parbox is center aligned. Because there are an odd number of lines, the base line of the middle line in this paragraph lines up with the non-parbox baseline. The center of the parbox doesn't align with anything.</p>

Figure 3.8: parbox baseline alignment

This is not a parbox.

This parbox is top aligned, but its content is center aligned.

This parbox is bottom aligned, but its content is center aligned.

This is not a parbox.

~~This parbox is center aligned, but its content is top aligned.~~

This is not a parbox.

Box center

Figure 3.9: parbox border alignment

Part II

Mathematics

Chapter 4

Combinatorics

Combinatorics, namely *Combinatorial Mathematics*, mainly studies *permutation* and *combination* of a set or multiset.

组合数学里经常要用到**映射**的概念，在后文的描述里，会多次出现**对应**这样的字眼，表示两个集合间元素的映射。通常为了方便分析，把元素、对象的不同用**编号**、**颜色**等标签来表示。

4.1 Set and Multiset

组合数学问题总要对某个集合的元素进行操作，虽然我们通常不需要特别说明。如 10 个人进行全排列，那么对应的集合由这 10 个人组成。

普通集合如：

$$S = \{ a_1, a_2, a_3, \dots, a_n \}, i \in \mathbb{Z} : i \in [1, n]$$

表示有 n 种**不同**元素，并且每种元素只有一个，称 S 为**单重集（合）**。

更一般的，**多重集（合）**：

$$M = \{ n_1 \cdot a_1, n_2 \cdot a_2, \dots, n_k \cdot a_k \}$$

突出元素**种类**，即 a_i 表示第 i 种元素，而 n_i 则表示第 i 种元素的个数。通常元素总个数用 n 表示：

$$n = n_1 + n_2 + \dots + n_k$$

不难发现，单重集是多重集的特例，此时

$$k = n, n_i = 1, i \in \mathbb{Z} : i \in [1, k]$$

如果多重集里每种元素有无限个，则记为：

$$M = \{ \infty \cdot a_1, \infty \cdot a_2, \dots, \infty \cdot a_k \}$$

普通集合和普通排列组合对应，多重集合和多重排列组合对应，这也是在正式介绍排列组合前先说下集合的定义。

排列组合里，集合元素通常都具体化为**不同**颜色小球，组合表示从集合里取小球出来，而排列表示进一步把取出的小球排队，或放进**不同的**盒子里，此时盒子的编号代表队列从头至尾的位置号。

注意符号表示的不同。单重集里 n 既表示元素种类和个数。而多重集用 k 表示元素种数，用 n 和 n_i 表示个数。注意符号表示的习惯：

$$a_i, n_i, k, n, S, M$$

4.2 Counting Principles

加法原理: 设集合 S 可以划分成若干不相交的子集 S_1, S_2, \dots, S_m , 则：

$$|S| = |S_1| + |S_2| + \dots + |S_m|$$

乘法原理: 设集合 S 是序偶 (a, b) 的集合，其中 a 来自于集合 A , b 来自于集合 B . A 中每个元素 a 都要与 B 中每个元素 b 配对。则：

$$|S| = |A| \times |B|$$

减法原理: 设集合 A 是全集 U 的子集，补集¹ $\bar{A} = U \setminus A = \{x \mid x \in U, x \notin A\}$, 则：

$$|A| = |U| - |\bar{A}|$$

除法原理: 设 S 是有限集，被划分为 k 个两两不相交的部分，每部分皆有 m 个元素，则：

$$k = \frac{|S|}{m}$$

后面会发现，很多应用都以单重集的排列、组合为原子操作，再结合计数四原则完成。

¹用 `overline`, `bar`, `complement`, 或 `smallsetminus` 命令表示。后者的好处是同时指明了全集和子集。

4.3 Permutation of Sets

定义：从 n 个元素的单重集合 S 中，取出 r 个元素按次序排成一列，称为 S 的一个 r -排列，记为：

$$P(n, r), P_n^r, A_n^r$$

注意，定义里用 r 表示所取元素个数。

当 $r = n$ 时， S 的 n -排列简称为 S 的排列或 n 个元素的全排列。

从 n 个元素中取 r 个元素的排列的典型例子是从 n 个不同颜色的球中，取出 r 个，放入 r 个不同的盒子里，每盒 1 个，盒子编号就映射成队列位置。显然第 1 个盒子有 n 种球可选，第 2 个盒子有 $n - 1$ 种球可选，……，第 i 个盒子有 $n - (i - 1)$ 种球可选，……，第 r 个盒子有 $n - (r - 1)$ 个球可选。

可以得出

$$A_n^r = n(n - 1) \cdots [n - (i - 1)] \cdots [n - (r - 1)], \quad r \leq n, \quad n, r \in \mathbb{Z}^+$$

定义阶乘 factorial：

$$\begin{aligned} n! &= n \times (n - 1) \times (n - 2) \cdots 2 \times 1 \\ 0! &= 1 \end{aligned}$$

排列组合是没有 0 的情况的，但为了数学定义和计算的完备性，要考虑 0 等情况。其实负数的阶乘也有定义，不过在组合数学里没意义，在此不考虑。后面还会遇到类似形式的定义。那么：

$$\begin{aligned} A_n^r &= \frac{n!}{(n - r)!}, \quad 0 \leq r \leq n \\ A_n^0 &= 1 \\ A_n^n &= n! \end{aligned}$$

排列还分为**直线排列**和**圆排列**。直线排列就是我们常说的排列，圆排列是指把取出的元素排成一个圆形，

上面定义的是**直排列**，**圆排列**定义为取出的元素排成一个圆圈，等于是让直线排列的首尾相连接。从 n 个元素中取出 r 个构成的圆 r -排列数为：

$$A_n^r / r, \quad (1 \leq r \leq n)$$

因为 1 个圆排列从任一位置断开都是一个不同的直排列，也就是说 r 个直排列对应 1 个圆排列，所以要在直排列基础上除以 r . 注意，是除不是乘。特殊的， n 个元素的全圆排列数为 $(n - 1)!$.

圆排列还有一种情况是，可以翻转圆排列，如 n 个不同颜色的珠子串成一条项链。一条项链的一面是一个普通圆排列，但翻转这个项链，它的另一面是一个新圆排列，所以每个可翻转圆排列对应 2 个普通圆排列。因此，**可翻转圆排列数为**

$$\frac{A_n^r}{2 \cdot n}$$

4.4 Combination of Sets

上节讨论了单重集的排列，这节讲单重集的组合。排列和组合的主要区别是**不同元素是否有次序**。组合取出元素堆在一起，而排列在组合的基础上对取出的元素堆进行排队或入盒。

一旦取出，便不再区分组合堆内球的不同。如果取出多个堆，堆间区别是球的个数：堆内无序，堆间也无序。后面多次用到这个原则。

从 S 中取 r 个元素而不进行排序，称为 S 的一个 r -组合，实际就是生成一个 S 的 r 元素子集，可以看成是取出元素堆在一起，没有顺序：组合即组堆，也即生成子集。

组合的对应彩色球问题是从 n 个色彩**不同**的小球中取出 r 个（堆在一起），此时没有放入盒子的操作：只取不入。如果一定要有入盒操作，那么所有的盒子相同，没有编号区分，此时入盒与否没有意义。 r -组合数记为

$$C(n, r), C_n^r, \binom{n}{r}$$

很显然，一个 r -组合可以生成 $r!$ 个排列，所以：

$$\begin{aligned} C_n^r &= \frac{A_n^r}{r!} = \frac{n!}{(n-r)!r!}, \quad r, n \in \mathbb{Z}_0^+ : r \in [0, n] \\ C_n^r &= 0, \quad r > n \\ C_n^0 &= 1 \\ C_n^n &= 1 \\ C_0^0 &= 1 \end{aligned}$$

从上面方程中的特例可以看出，完备性定义对数学计算的意义。阶乘，排列数，组合数的完备性定义主要考虑 $r > n$ 和 $n, r = 0$ 的情况。一般地，我们只考虑 $0 \leq r \leq n$ 的情况。对于 $r, n < 0$ 的情况不在排列组合的讨论范围。在其它计算领域即便碰到，也不难，只要严格按照阶乘的定义计算即可。

由公式：

$$A_n^r = C_n^r r!, \quad r, n \in \mathbb{Z}_0^+ : r \in [0, n]$$

可以得出，除原始定义外，排列操作可看作先取组合，得到一堆元素，再对此堆列队。可以说**排列操作暗含了组合子问题**。简而言之，1个组合对应 $r!$ 个排列，排列数是组合数的 $r!$ 倍。后面更复杂的分配分组问题也遵循此规律。

4.4.1 Combination Formulas

组合数的计算非常重要，因为组合公式是一个很重要的数学工具，如多项式的系数和组合数紧密相联。本小节着重讲组合数的几个公式。

组合数和排列数计算都化成阶乘的计算。不过，当参数很大时，计算阶乘不是件容易的事。但从组合数的原始定义可知：取 r 个元素得到一个子集，余下的就是 $n - r$ 元素的补集，一一对应。也就是说，每取一个 $(n - r)$ -组合就得到一个 r -组合：

$$C_n^r = C_n^{n-r}, \quad r, n \in \mathbb{Z}_0^+ : r \in [0, n]$$

当 r 很大时， $n - r$ 就很小，便于计算。我们还可以想办法降级阶数，让其变得更小：

$$C_n^r = C_{n-1}^r + C_{n-1}^{r-1}$$

由此公式可得出 杨辉三角形，也称 *Pascal* 三角形。

有趣的是让 r 遍历0到 n ，可以看出所有的组合数之和就是集合 S 的幂集的元素个数：

$$\sum_{r=0}^n \binom{n}{r} = 2^n$$

此公式可以用二项式证明：

$$(x + y)^n = \sum_{r=0}^n C_n^r x^r y^{n-r}$$

令 $x, y = 1$ 即可。

更一般地，组合公式的证明**双重计数 double counting** 法：从不同（一般2种）角度对集合计数。更多关于双重计数，看 Double Counting 和 Mod-03 Lec-17 Double counting - Part (2) .

如上面的组合数求和公式，左边表示利用加法原则，以了集元素个数 r 来对 S 的幂集计数。要证明，我们以另外一个角度来计数：利用乘法原则，针对一个元素是否加入子集来计数。 $\forall a_i, 1 \leq i \leq n$ 要么在某个子集里，要么不在，只有两种可能。对 a_i 遍历， a_1 有两种可能， a_2 有两种可能，……， a_n 有两种可能，所以 S 有 $2 \times 2 \times \cdots \times 2 = 2^n$ 个子集。

4.4.2 Application of Combination

现有 n 个管理员管理某保密装置 (Minimum number of locks and keys)。要求任何 $\leq r$ 个管理员都打不开该装置，至少需 $r + 1$ 个。假设该装置有 s 把钥匙，给每个管理员分配其中的 t 把。问题是已知 $n, r, r \leq n$, 求 $s, t, t \leq s$. 并进一步给出该装置的钥匙分配方案。

设管理员集合为：

$$M = \{m_1, m_2, \dots, m_n\}, r \leq n$$

钥匙集合为：

$$K = \{k_1, k_2, \dots, k_s\}, t \leq s$$

先求钥匙数 s . 由描述知，管理员集合 M 的任一 r -组合 (管理员子集) 都不能凑齐 s 把钥匙，可知任一 r -组合至少还缺 1 把钥匙。显然，任两个 r -组合的钥匙不能完全相同，也即不能缺同一把钥匙，否则 $2r$ 个管理员还因缺一个把钥匙而打不开保密装置，而且这样的分配方案没有意义。 M 的 r -组合数是 C_n^r . 所以：

$$s \geq C_n^r$$

从上分析可看出， M 的所有 r 元素子集到 K 的一个单射：每个 r 元素子集的像是它所缺失的那把钥匙。但它不一定是满射，因为 $s \geq C_n^r$ 时，额外的钥匙会被所有的 r -组合所覆盖，这样的钥匙没的原像。其中等号成立的条件是每个 r -组合刚好缺一把钥匙，此时构成一个满射。

再求每个管理员分得的钥匙数 t . M 的任一 $(r + 1)$ 元素子集都能打开装置，说明其中任一管理员可补齐剩下 r 个管理员所缺的那把钥匙。一个管理员 m_l 所参与的 $(r + 1)$ -组合有 C_{n-1}^r 个，所以：

$$t \geq C_{n-1}^r$$

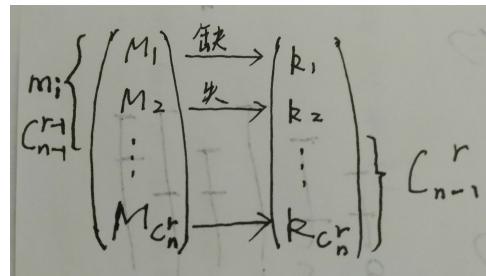
在分析钥匙的分发方案之前，让我们回顾下上面的杨辉三角形，本题已出现公式里两个分项 C_n^r 和 C_{n-1}^r ，只不过后者的意义稍变了。

s 取最小值 C_n^r 时，我们列出 M 的所有 r 元素子集到 K 的满射：

$$f(M_i) = k_j$$

$$\{M_i \mid M_i \text{ is a set of size } r, i = 1, \dots, C_n^r\} \xrightarrow{\text{缺失}} K$$

显然这样的映射有很多种，我们只需选其一，如下图所示：



对于某个管理员 m_l , 他所在 r 元素子集有 C_{n-1}^{r-1} 个, 到此, 杨辉三角形公式里三个分项全部出现。很显然这管理员也缺失了这些 r 元素子集对应的钥匙像, 所以该管理员应分得剩下的 C_{n-1}^r 个钥匙像。针对所有管理员进行类似分配即可。

前面提过, 当 s, t 的不等式不取等号时, 此映射不是满射, 有钥匙没有原像, 此时要求所有的 r -组合都包含这样的钥匙。

现假设 $s = C_n^r + 1$, 此时的分配方案只需在原基础上稍加修改即可: 多出的这枚新钥匙再分配给每个管理员。这样 $t = C_{n-1}^r + 1$. 此设计仍满足保密要求。我们会发现这样的额外钥匙是没有必要的。每个管理员都多了 1 枚同样的钥匙, 起不到额外的安全作用。

分配方案的关键是根据 s 值列出 r 元素子集到钥匙的映射。现给出一个实际的例子。如果 $n = 5, r = 3$, 则 $s = C_5^3 = 10, t = C_4^3 = 4$. 下面给出一个映射。多出的一个钥匙 (编号 11) 是为了说明映射不一定是满射。

$$\begin{aligned}
 123 &\xrightarrow{\text{缺}} 1 \\
 124 &\longrightarrow 2 \\
 125 &\longrightarrow 3 \\
 134 &\longrightarrow 4 \\
 135 &\longrightarrow 5 \\
 145 &\longrightarrow 6 \\
 234 &\longrightarrow 7 \\
 235 &\longrightarrow 8 \\
 245 &\longrightarrow 9 \\
 345 &\longrightarrow 10 \\
 11 &
 \end{aligned}$$

每个管理员参与了 $C_{5-1}^{3-1} = 6$ 个 3 元素子集, 对应到映射图上, 有 6 行。不失一般性, 管理员 m_1 , 参与了前 6 行, 缺失前 6 枚钥匙, 所以分得后 4 枚钥匙 7, 8, 9, 10. 依此类推, 我们可以得出如下分配方案。注意, 该方案考虑到了第 11 枚钥匙。

Managers \ Keys	Keys										
	1	2	3	4	5	6	7	8	9	10	11
1	0	0	0	0	0	0	1	1	1	1	1
2	0	0	0	1	1	1	0	0	0	1	1
3	0	1	1	0	0	1	0	0	1	0	1
4	1	0	1	0	1	0	0	1	0	0	1
5	1	1	0	1	0	0	1	0	0	0	1

Table 4.1: Safe Device

4.5 Permutation of Multiset

排列组合还会考虑所取元素是否**重复**，从而生成（多）重排列和（多）重组合。

前面两节介绍了单重集的排列组合，对应地，多重集也有排列组合，定义和单重集一样，唯一的区别是取出的元素可能有重复。

设多重集 M 为：

$$M = \{ n_1 \cdot a_1, n_2 \cdot a_2, \dots, n_k \cdot a_k \}, \quad \forall i = 1, 2, \dots, k, r \leq n_i$$

或：

$$M = \{ \infty \cdot a_1, \infty \cdot a_2, \dots, \infty \cdot a_k \}$$

由于每种元素的个数超过所取数，所以排列里 r 个元素可能全部来自某一种。

多重集 M 的 r -排列数是：

$$k^r$$

这是很容易理解的，因为队中每个位置都有 k 种可能。

多重集 r -排列对应的彩球模型可以看成**可放回**（可重复）地对单重集取球、排队或入盒。单重集里每个元素可无限重复使用，标记好队列位置后又放回球堆里。当然按照多重集的定义，可以看成是对多重集取球、排队或入盒。如不多于四位的三进制数的个数为 3^4 。对应的多重集是 $M = \{ \infty \cdot 0, \infty \cdot 1, \infty \cdot 2 \}$.

如果 $r = n = \sum_{i=1}^k n_i$ ，则称为 M 的全排列。多重集全排列（也即 n -排列）是对**有限集** M 的**所有**元素（如彩球）进行操作。具体来说，就是对全部 n 个 k 种颜色的球进行排队。

显然此时 r 大于所有的 n_i . M 的全排列数为：

$$\frac{n!}{n_1! n_2! \cdots n_k!}$$

全排列的证明可以先从直觉来分析。 $n!$ 表示所有元素的全排列，但是 a_i 在队列重复了 n_i 次，这此重复实际只表示一种队列，所以除以 $n_i!$ 。如果某个 n_i 等于 1，那么在被除式中是 $1!$ 。

有趣的是，实际证明中，用的是组合思路。第 1 种元素 a_1 要占据队列里的 n_1 个位置，所以有 $C_n^{n_1}$ 种可能，第二种元素要占据剩下 $n - n_1$ 个位置中的 n_2 个，所以有 $C_{n-n_1}^{n_2}$ 种可能，……，依此类推，最后一种元素有 $C_{n_k}^{n_k} = 1$ 种可能：

$$C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k} = \frac{n!}{n_1! n_2! \cdots n_k!}$$

从证明过程可知，当 $k = 2$ 时，多得集的全排列数在数值上等于单重集的组合数 $C_n^{n_1} = C_n^{n_2} = n!/(n_1! n_2!)$ 。如用两面红旗，三面黄旗依次悬挂在一根旗杆上，问可以组成多少种不同的标志？答案是 $5!/(2! 3!) = 10$ 。

下面看一个棋盘的例子。在一个 $k \times k$ 的棋盘上放 k 个车，使得任意两个车之间不能互吃，有多少种方法？棋盘上车全是相同的，没有区别。要想车不互吃，任意两个车的行列值都不同。每行一个车 $a_{1j_1}, a_{2j_2} \cdots a_{kj_k}$ ，只需给不同行的车选列即可，所以方法数是 $k!$ 。

假设是 k 个不同（色）的车呢？保持上面排列不变，现对车的颜色进行调换，有 $k!$ 种，所以方法数是 $k! k!$ 。实际是对车所在的行进行全排列，也即行和列都要全排列。行的全排列负责车的不同，而列的全排列负责车不互吃。

假设是 n_1 个红车， n_2 个蓝车，……， n_k 个黄车，总共 n 个呢？先解决车在行上的全排列： $\frac{n!}{n_1! n_2! \cdots n_k!}$ 。再针对不同的列全排列 $n!$ 。方法数是：

$$\frac{n!}{n_1! n_2! \cdots n_k!} \cdot n!$$

多重集 r -排列要求每种元素个数不少于 r ，若 $\exists t, n_t < r$ ，那么情况变复杂了。这时没有公式计算，要具体针对 n_t 列举分析。如第 t 种元素出 $1, 2, \dots, t$ 个。

例：9 个元素的多重集 $S = 3 \cdot a, 2 \cdot b, 4 \cdot c$ 的 8-排列数为多少？此例中， $r = 8$ 大于 n_i ，所以不能套用公式。 $n = 9$ 只比 r 大 1，所以列队中， a, b, c 之一少出一个元素。如少一个 a 排列数是 $\frac{8!}{2! 2! 4!}$ ，同理可算另两项，再用加法原则：

$$\frac{8!}{2! 2! 4!} + \frac{8!}{3! 1! 4!} + \frac{8!}{3! 2! 3!}$$

4.6 Combination of Multiset

多重集 S 的含有 r 个元素的子多重集就叫做 S 的 r -组合，或表述为取出 r 个元素的堆。和多重集的排列比少了列队操作。

关于多重集的排列问题可以小结如下：

设 $S = \{n_1 \cdot a_1, n_2 \cdot a_2, \dots, n_k \cdot a_k\}$, 且 $n = n_1 + n_2 + \dots + n_k$, 则 S 的 r -排列数 N 满足：

- (1) 若 $r > n$, 则 $N = 0$;
- (2) 若 $r = n$, 则 $N = \frac{n!}{n_1! n_2! \cdots n_k!}$;
- (3) 若 $r < n$, 且对一切 $i = 1, 2, \dots, k$ 有 $n_i \geq r$, 则 S 的 r -排列数是 k^r ;
- (4) 若 $r < n$, 且存在某个 $n_i < r$, 则对 N 没有一般的求解公式, 解法将在后面讨论。

Figure 4.1: Summary on Multiset Permutation

同多重集的组合样, 假设每种元素个数都不小于 r . 方法数即 k 元线性不定方程:

$$r = x_1 + x_2 + \cdots + x_k, \quad x_i \in \mathbb{Z}_0^+, \quad i = 1, 2 \cdots, k$$

的非负整数的解数。非负是表明可能某 x_t 为 0, 此时元素 a_t 没有出现在组合堆里。

计算用 隔板法或 插空法。

可以看成这样, 有 r 个 1 在一行上, 占有 r 位置, 包含首尾共有 $r + 1$ 个空位, 插上 $k - 1$ 个板子。第 i 板子前面的 1 个数是 x_i 的解, 第 $k - 1$ 个板子后面的 1 个数是 x_k 的解。如果某个板 k_t 前没有 1 而是另一个板 (两个板子处在同一空位), 则 x_t 解为 0. 如从

$$| 1 | | 1 1 \cdots 1 1 |$$

看出:

$$x_1 = 0, x_2 = 1, x_3 = 0, x_k = 0$$

非负正整数解的思路是: r 个 1 的位置和 $k - 1$ 的板位置共 $r + (k - 1)$ 个位置, 从中取 r 个作为 1 的位置或取 $k - 1$ 个作为板的位置:

$$C_{r+k-1}^r \quad \text{or} \quad C_{r+k-1}^{k-1}$$

不考虑多重集组合, 单就方程本身来说, 如果是求正整数解呢?

$$r = x_1 + x_2 + \cdots + x_k, \quad x_i \in \mathbb{Z}^+, \quad i = 1, 2 \cdots, k$$

正整数解暗含了 $r \geq k$, 非负解则无此限制。 r 个 1 形中间有 $r - 1$ 个空档, 插入 $k - 1$ 个板, 且每个空档最多一个板, 则解数:

$$C_{r-1}^{k-1}$$

这比非负情况的简单。

实际非负整数解和正整数解之间可以互相转换，形成一个满射，而解个数不变。下面是把非负解转成正整数解的方法，即变量加 1：

$$r + k = (x_1 + 1) + (x_2 + 1) + \cdots + (x_k + 1), \quad x_i \in \mathbb{Z}_0^+, \quad i = 1, 2, \dots, k$$

新方程的解和原方程的解一一对应（满射：减一），这种变换思路很重要。新方程的解是正整数解：

$$C_{r+k-1}^{k-1}$$

把正整数解转成非负解，是把变量减 1。利用转换原理，我们把方程：

$$x_1 + x_2 + x_3 + x_4 = 20, \quad x_1 \geq 3, x_2 \geq 1, x_3 \geq 0, x_4 \geq 5$$

转成非负解形式：

$$(x_1 - 3) + (x_2 - 1) + (x_3 - 0) + (x_4 - 5) = 11, \quad x_1 \geq 3, x_2 \geq 1, x_3 \geq 0, x_4 \geq 5$$

或正整数解形式：

$$(x_1 - 2) + (x_2 - 0) + [x_3 - (-1)] + (x_4 - 4) = 15, \quad x_1 \geq 3, x_2 \geq 1, x_3 \geq 0, x_4 \geq 5$$

后用插板法。

总结：

- 正整数：插板不相临；从中间空槽取 $k - 1$ 。
- 非负整数：插板可相临；从位数取 $k - 1$ 。

4.7 Polynomial

这节谈下多项式和多重集排列、组合之间的联系。多项式：

$$(x_1 + x_2 + \cdots + x_k)^n$$

的 展开式 可写成：

$$\sum_{n_1+n_2+\cdots+n_k=n} \frac{n!}{n_1!n_2!\cdots n_k!} x_1^{n_1} x_2^{n_2} \cdots x_k^{n_k}, \quad n_i \in \mathbb{Z}_0^+ : n_i \in [0, n], \quad i = 0, 1, \dots, k$$

由此可看出，多项式的每项的系数是一个多重集的全排列数 $\frac{n!}{n_1!n_2!\cdots n_k!}$ 。还可算出展开式的项数是多重集组合数 $\binom{n+k-1}{n}$ 。

如果原多项式里 x_i 前还带有系数如 a_i ：

$$(a_1 x_1 + a_2 x_2 + \cdots + a_k x_k)^n$$

则情展开式的系数在多重集全排列数基础上还有乘以对应的原始系数。

如果问多项式的系数之和是多少，只需给所有 x_i 赋值 1 即可：

$$(a_1 + a_2 + \cdots + a_k)^n$$

对于所有 $a_i = 1$ 的情况，则系数和是 k^n .

4.8 Grouping and Distribution

下面是先说分组和分配问题，方法数和多重集全排列数有关。

4.8.1 Distribution as Injection

将 $n = n_1 + n_2 + \cdots + n_k$ 个 **不同的** 球 a_i (单重集) 放到 k 个 **不同的** 对应盒子 b_i 里 (单重集)。 b_1 放 n_1 个， b_2 放 n_2 个，……， b_k 放 n_k 个。如果 $k = n$ ，它就变成单重集的全排列，此时 $n_i = 1$. 简单描述：把 n 个不同色球分成 k 堆 n_i ，依次分配给不同盒子 b_i .

此模型称为**单重集的定向分配**问题。分配强调是分给**不同的**盒子，而定向是说 n_i 映射到 b_i ，每个盒子所分得的**数量固定**，即每堆的球数已经限定。入盒操作相当于组球堆贴标签。

计算过程和多重集全排列的类似，选取 n_1 个 $C_n^{n_1}$ ，再在剩下球里取 n_2 个 $C_{n-n_1}^{n_2}$ ，……

这个取堆顺序是 n_1, n_2, \dots, n_k ，实际按 i 的任何一种排列顺序来取都可以，只要所取之堆放入对应的盒子子即可。如第一次取 n_5 个，相当于给盒子 b_5 取球，那么取出后就放入盒子 b_5 .

计算如下：

$$C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n-k}^{n_k} = \frac{n!}{n_1! n_2! \cdots n_k!}$$

此计算利用了乘法原则。

最后，多重集全排列计算过程是给每种色球找队列位置 (共 n 个)，而上面的模型是给每个盒子 (共 k 个) 选色球。此模型里彩球集合和空盒集合是单重集，但放球后，盒子集合是多重集。每个盒子代表一种元素，里面的球数代表这种元素的个数。

4.8.2 Grouping

定向分配把球堆分给不同但固定的盒子，如取球放入 k 个的相同的盒子里 (盒子没有编号)，此模型称为**单重集的分组**问题。

由于盒子相同，所以有没有入盒操作对结果不影响，所以入盒是一个空操作。所以有的题里，只提到分组，没有入盒操作（如分派给谁）。单重集分组可以看成把取出球堆也堆在一起，形成一个大堆，大堆内元素是小球堆：分组即分堆。

不失一般性，假设按 n_1, n_2, \dots, n_k 的顺序取堆，如果就此打住，那就成了定向分配。到底区别哪？没有去重！

球堆的区别是球个数 n_i 值的大小（球已取完，不再考虑其不同），可能某些堆的球数相等，这些堆算作是相同的堆。

不失一般性，假设 $n_1 = n_2 = n_3$ 这 3 个堆球数相等，它们之间先取谁后取谁没有变化，同理 $n_7 = n_9$ 这 2 个堆的先后也不改变分组操作（没有特殊说明，后面都据此假设）。所以要除掉重复：

$$\frac{C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k}}{3! 2!}$$

对所有的相同数值做类似去重除法即可。做题时，尽量把相同的 n_i 写在一起，好去识别重复。

我们有理由把

$$\{n_1, n_2, \dots, n_k\}$$

看成多重集：这 k 个值分成 l 种，每种里有 t_j , $j = 1, 2, \dots, l$ 个元素，有 $\sum_{j=1}^l t_j = k$. 拿上面的例子来说：

$$\{3 \cdot n_1, 1 \cdot n_4, 1 \cdot n_5, 1 \cdot n_6, 2 \cdot n_7, \dots, 1 \cdot n_k\}$$

所以去重就是除以多重集每种元素个数的阶乘 $t_1! t_2! \cdots t_l!$ ，所以标准表达是：

$$\frac{C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k}}{t_1! t_2! \cdots t_l!}$$

一个特例是，所有 n_i 全相等，表示是平均分组，所以：

$$\frac{C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k}}{k!} = \frac{n!}{k! [(\frac{n}{k})!]^k}$$

再回过头看定向分配，发现可以分解成分组、定向分配 2 步：

$$\frac{C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k}}{3! 2!} \cdot 3! 2!$$

先把不同球数的堆放入对应的盒子。后面乘以 $3!$ 表示 $n_1 = n_2 = n_3$ 这 3 个堆和 b_1, b_2, b_3 间可任意分派。乘以 $2!$ 也是同样的道理。

一句话：**分配问题暗含了分组子问题**。

4.8.3 Distribution without Injection

有定向就有不定向，不定向分配也把球堆分派给不同的盒子，但是没有固定分配关系：球堆 n_i 和盒子 b_j 间没有固定映射关系。把 n 个不同色球分成 k 堆 n_i ，分配给不同盒子 b_j 。此模型称为 **单重集的不定向分配** 问题。

始终记住，盒子的不同、盒子编号代表队列位置。不定向分配分解成分组、不定向分派 2 步：

$$\frac{C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k}}{3! 2!} \cdot k!$$

由于分组里已考虑到重复问题，后面的排列就不再考虑 $3! 2!$ 重复，而应把 $n_1 = n_2 = n_3$ 看作是不同的堆，否则就会多次去重。

不定向分配还可以看成在定向分配基础上对 k 个球堆（数值 n_i ）进行全排列操作，方法数是：

$$C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k} \cdot \text{球堆全排队数}$$

在前节分组问题说到，堆的球数 n_i 是个多重集，所以我们乘以多重集的全排列数：

$$\begin{aligned} C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k} \cdot \frac{k!}{3! 2!} &= \frac{C_n^{n_1} C_{n-n_1}^{n_2} \cdots C_{n_k}^{n_k}}{3! 2!} \cdot k! \\ &= \frac{n!}{3! 2! \cdot n_1! n_2! \cdots n_k!} \cdot k! \end{aligned}$$

公式的推导过程也说明了不同的解题思路。

计算过程总结：

1. 球一旦取出，组合计数完毕，就不再考虑球的不同。
2. 取出的球堆区别于堆内球的个数。
3. 可能某些堆球数相等，这些球堆看作是相同的堆。其实是一个多重集。

4.8.4 Distribution of Multiset

上面的问题里，单重集每个球不同，如果所有球全相同呢？若像单重集分组分配样规定 n_i ，则堆数确定，分组问题固定，只有 1 种方法。定向分配问题： n 个相同的球分成 k 组 n_i 定向派给不同盒子 b_i ，也只有 1 种方法。不定向分配数是多重集的全排列如 $\frac{k!}{3! 2!}$ 。

所以一般不规定堆内球数，如把 n 个同色球放入 k 个不同的盒子里，盒子不为空。其实这个问题可化成求 k 元线性不定方程的正整数解。方法数是：

$$C_{n-1}^{k-1}$$

此时小球可看作是只有 1 种元素的多重集 $M = \{ n \cdot a_1 \}$. 此模型可称为含 1 种元素的**多重集定向分配**问题。

如果盒子可以为空，则化成求方程的非负整数解。

含一种元素的**多重集分组和不定向分配**问题没有统一解法，因为分组和不定向要考虑去重问题，但是去重的前担是要知道 n_i 数值。所以只能一一列举出方程解，再考虑每种解的去重，无法直接写出计数公式。

4.9 Summary

分组分配总结：

1. 单重集分组：固序取堆、去 n_i 重。
2. 单重集定向分配：固序取堆。
3. 单重集不定向分配：固序取堆、去 n_i 重、排列。
4. 多重集定向分配：插板法、解方程。
5. 多重集分组和不定向分配：没有公式，只可一一列举。

Chapter 5

卡特兰数

5.1 卡特兰公式

卡特兰数 Catalan Number 在许多算法计数问题中都有应用，如出栈计数，二叉树形态计数等。卡特兰数也叫明安图数。因为最提出这数的是中国明代数学家明安图。但因为近代以来，科学技术主要由西方科学家发起，所以很多发现用西方人物命名。

明安图数其实是一个组合数：

$$C_n = \frac{C_{2n}^n}{n+1} = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{n!(n+1)!}$$

卡特兰数 C_n 表示对 n 个元素的某种顺序计数。注意这里符号 C_n 不是前面的 n 个元素的组合数里的 C_n^r .

卡特兰数可以写成另外一种形式：

$$\begin{aligned} C_n &= \frac{C_{2n}^n}{n+1} \\ &= \frac{1}{n+1} \frac{(2n)!}{n! n!} \\ &= \frac{1}{n(n+1)} \frac{(2n)!}{(n-1)! n!} = \left(\frac{1}{n} - \frac{1}{n+1}\right) \frac{(2n)!}{(n-1)! n!} \\ &= \frac{1}{n} \frac{(2n)!}{(n-1)! n!} - \frac{1}{n+1} \frac{(2n)!}{(n-1)! n!} = \frac{(2n)!}{n! n!} - \frac{(2n)!}{(n-1)! (n+1)!} \\ &= C_{2n}^n - C_{2n}^{n+1} \end{aligned}$$

请注意此化简过程用到

$$\frac{1}{n(n+1)} = \frac{1}{n} - \frac{1}{n+1}$$

在处理组合数问题时， $\frac{1}{n-1}, \frac{1}{n}, \frac{1}{n+1}$ 经常被用到来化简。这种倒数可以和阶成结合，组成新的组合数。

上面说的是卡特兰数结果，卡特兰数的递推关系式是：

$$\begin{aligned} C_n &= \frac{C_{2n}^n}{n+1} \\ &= \sum_{k=1}^n C_{k-1} C_{n-k} \\ &= C_0 C_{n-1} + C_1 C_{n-2} + \cdots + C_{n-1} C_0 \\ &= \sum_{k=0}^{n-1} C_k C_{n-1-k} \end{aligned}$$

如何由这个递推关系得到结果式，要用到产生式或叫母函数 Generating Function：

$$g(x) = C_0x^0 + C_1x^1 + \cdots + C_{n-1}x^{n-1} + C_nx^n + \cdots$$

关于如何用母函数求系数，细节请参考组合学课件，这里给出计算过程。上面公式里，我们发现每项是子规模的乘积，所以对母函数平方：

$$\begin{aligned} g^2(x) &= (C_0x^0 + C_1x^1 + \cdots + C_nx^n + \cdots)(C_0x^0 + C_1x^1 + \cdots + C_nx^n + \cdots) \\ &= C_0^2x^0 + (C_0C_1 + C_1C_0)x^1 + \cdots + (C_0C_n + C_1C_{n-1} + \cdots + C_nC_0)x^n + \cdots \\ &= C_1x^0 + C_2x^1 + \cdots + C_{n+1}x^n + \cdots \end{aligned}$$

对上式乘以 x 得：

$$x \cdot g^2(x) = C_1x^1 + C_2x^2 + \cdots + C_nx^n + C_{n+1}x^{n+1} + \cdots$$

对上式加 $C_0x^0 = 1$ 得：

$$\begin{aligned} 1 + x \cdot g^2(x) &= C_0 x^0 + C_1 x^1 + C_2 x^2 + \cdots + C_n x^n + \cdots \\ &= g(x) \\ x \cdot g^2(x) - g(x) + 1 &= 0 \end{aligned}$$

解上式得：

$$g(x) = \frac{1 \pm \sqrt[2]{1 - 4x}}{2x}$$

通过变换，得出母函数通项关系，去除系数 C_k ，进而解出母函数关于 x 的表达式。 $g(x)$ 是最开始的系数是由 C_k 定义的，通过转换后计算出系数，就得到 C_k .

根据二项式的推广：

$$\begin{aligned} (x+y)^\alpha &= \sum_{k=0}^{\infty} \binom{\alpha}{k} x^k y^{\alpha-k}, \quad a \in \mathbb{R} \\ \binom{\alpha}{k} &= \frac{\alpha(\alpha-1)\cdots(\alpha-k+1)}{k!} \end{aligned}$$

由此得：

$$\begin{aligned}
\sqrt[2]{1 - 4x} &= [1 + (-4x)]^{\frac{1}{2}} \\
&= \sum_{k=0}^{\infty} \binom{1/2}{k} (-4x)^k \\
&= 1 + \sum_{k=1}^{\infty} \binom{1/2}{k} (-4x)^k \\
&= 1 + \sum_{k=1}^{\infty} \frac{\frac{1}{2} \frac{-1}{2} \frac{-3}{2} \cdots \frac{3-2k}{2}}{k!} (-1)^k 2^{2k} x^k \\
&= 1 - \sum_{k=1}^{\infty} \frac{1 \ 3 \ \cdots \ (2k-3)}{k!} 2^k x^k \\
&= 1 - \sum_{k=1}^{\infty} \frac{1(2 \cdot 1) 3(2 \cdot 2) \cdots (2k-3)[2 \cdot (k-1)]}{k!(k-1)!} 2x^k \\
&= 1 - \sum_{k=1}^{\infty} \frac{1 \ 2 \ 3 \ 4 \ \cdots \ (2k-3)(2k-2)}{k!(k-1)!} 2x^k \\
&= 1 - \sum_{k=1}^{\infty} \frac{[2(k-1)]!}{k!(k-1)!} 2x^k
\end{aligned}$$

结合上式得：

$$\begin{aligned}
g(x) &= \frac{1 \pm \sqrt[2]{1 - 4x}}{2x} \\
&= \frac{1 \pm [1 - \sum_{k=1}^{\infty} \frac{[2(k-1)]!}{k!(k-1)!} 2x^k]}{2x}
\end{aligned}$$

考慮到定义时，系数 C_k 是正数，所以正负号里选负号：

$$\begin{aligned}
g(x) &= \frac{1 \pm \sqrt[3]{1 - 4x}}{2x} \\
&= \frac{1 \pm [1 - \sum_{k=1}^{\infty} \frac{[2(k-1)]!}{k!(k-1)!} 2x^k]}{2x} \\
&= \frac{1 - [1 - \sum_{k=1}^{\infty} \frac{[2(k-1)]!}{k!(k-1)!} 2x^k]}{2x} \\
&= \sum_{k=1}^{\infty} \frac{[2(k-1)]!}{k!(k-1)!} x^{k-1} \\
&= \sum_{k=0}^{\infty} \frac{(2k)!}{k!(k+1)!} x^k
\end{aligned}$$

通过系数对比，得出 $C_k = \frac{(2k)!}{k!(k+1)!} = \frac{1}{k+1} C_{2k}$.

5.2 卡特兰数应用

卡特兰数的来自于应用问题，13 通过元素进出栈顺序数问题，来说明公式推导过程。

长度为 $2n$ 的 Dyck Word (n 个 x 和 n 个 y 组成字符串) 数； n 对括号匹配组成合法运算式数； n 个节点组成二叉树方案数； $2n + 1$ 个节点的满二叉树数都是 C_n . 特别此 n 个节点的二叉树，添加 $n + 1$ 个叶子节点，形成满二叉树，个数都是 C_n .

二叉树前序序列和中序序列的关系。给定某二叉树前序序列或后序序列，求中序序列的可能数，结果也是卡特兰数。相当于以前序序列或后序序列入栈，中序序列出栈。

有 $n \times n$ 的小方格组成的正方形，要求从一个对角走到别一对角，只能横向或纵向行走，不能回头且不能穿过对角线，问有多少种单调路径？如从左下角往右上角行走，单调路径表示每一步只能向右或向上，即向最终方向走。如果不考虑对角线问题，则竖向应走 n 步，横向应走 n 步，共 $2n$ 步，方法数是 C_{2n}^n . 若考虑对角线限制，假若沿在对角线下方走，则说明任何时刻，右向步数不少于向上步数。具体参考上面提到的进出栈分析。

这些不同问题可以互相转化。如进栈、出栈，Dyck Word 里的 x 和 y , 左、右括号都互相对应。全部用数学描述是 $2n$ 个 ± 1 串。

注意卡特兰数 C_n 里有 n 表示规模，但是实际问题里， n 可能表示的是 n 对元素，而不是 n 个元素。如括号匹配里， n 对括号有 n 个左括号和 n 个右括号。

Chapter 6

数列

6.1 等差数列

我们知道等差数列的前 n 项和是首项加尾项乘以项数除以 2.

$$\begin{aligned} a_1 &= a_1 \\ &= a_0 + d \\ a_2 &= a_1 + d = a_1 + d \\ a_3 &= a_2 + d = a_1 + 2 \cdot d \\ &\dots \\ a_n &= a_{n-1} + d \\ &= a_1 + (n - 1) \cdot d \\ &= a_0 + n \cdot d \end{aligned}$$

这里特别提到 a_0 . 严格来说, 数列下标从 1 开始 (表示第一个项), 0 不属于数列下标, 但有时为了计算方便, 要借用 $a_0 = a_1 - d$.

等差数列, 任意连续三项中, 前后两项之和是中间项的 2 倍, 因中间项减等差 d 是前一项, 加等差 d 是后一项。

等差数列的前 n 项和:

$$S_n = \frac{(a_1 + a_n) \cdot n}{2}$$

6.2 等差数列幂和

等差数列的幂和是指等差数列前 n 项的 t ($t = 1, 2, \dots$) 次幂之和：

$$S_t(n) = \sum_{k=1}^n a_k^t = a_1^t + a_2^t + \dots + a_n^t$$

基本思路是升维：借用 $t+1$ 次二项展开式，得到数列相临两项的 $t+1$ 次幂差。一般来说，我们关注的是平方、立方，即 $t=1, 2$. 后面不加说明，假设 t 为 2，则 $t+1=3$ ：

$$\begin{aligned} (a+b)^3 &= a^3 + 3a^2b + 3ab^2 + b^3 \\ a_{n+1}^3 - a_n^3 &= (a_n + d)^3 - a_n^3 \\ &= 3d \cdot a_n^2 + 3d^2 \cdot a_n + d^3 \end{aligned}$$

对 n 遍历：

$$\begin{aligned} a_2^3 - a_1^3 &= 3d \cdot a_1^2 + 3d^2 \cdot a_1 + d^3 \\ a_3^3 - a_2^3 &= 3d \cdot a_2^2 + 3d^2 \cdot a_2 + d^3 \\ &\dots \\ a_{n+1}^3 - a_n^3 &= 3d \cdot a_n^2 + 3d^2 \cdot a_n + d^3 \end{aligned}$$

对 n 个式子求和，得出公式：

$$a_{n+1}^3 - a_1^3 = 3d \cdot \sum_{k=1}^n a_k^2 + 3d^2 \cdot \sum_{k=1}^n a_k + n \cdot d^3$$

此式很明显可以直接算出平方和。但此式受限于 a_0, d 没法直接化简，所以我们关键是往思路。其实等差数列前 n 项和可以看成 $t=1$ ，其前 n 项和除了首尾相加外，还可以借助 $t+1=2$ 次展开式。

下面以前 n 个自然数的平方和为例介绍求解思路 ($a_1 = 1, d = 1$)。首先，我们有：

$$\begin{aligned} a_{n+1}^3 - a_n^3 &= (n+1)^3 - n^3 \\ &= 3n^2 + 3n + 1 \end{aligned}$$

对 n 遍历：

$$\begin{aligned}
 2^3 - 1^3 &= 3 \times 1^2 + 3 \times 1 + 1 \\
 3^3 - 2^3 &= 3 \times 2^2 + 3 \times 2 + 1 \\
 &\dots \\
 n^3 - (n-1)^3 &= 3(n-1)^2 + 3(n-1) + 1 \\
 (n+1)^3 - n^3 &= 3n^2 + 3n + 1
 \end{aligned}$$

把这 n 个式子加起来：

$$\begin{aligned}
 (n+1)^3 - 1 &= 3 \cdot \sum_{k=1}^n k^2 + 3 \cdot \sum_{k=1}^n k + n \\
 3 \cdot \sum_{k=1}^n k^2 &= (n+1)^3 - 3 \cdot \frac{(1+n) \cdot n}{2} - (n+1) \\
 \sum_{k=1}^n k^2 &= \frac{n(n+1)(2n+1)}{6}
 \end{aligned}$$

通过公式，我们发现平方和 ($t = 2$) 与线性和 ($t = 1$) 的关系：

$$\frac{\sum_{k=1}^n k}{\sum_{k=1}^n k^2} = \frac{2n+1}{3}$$

对于其它等差数列，我们用同样方法。如计算 $1^2, 4^2, 7^2, \dots, (3n-2)^2$.

6.3 等差数列的积和

上面讲的是等差数列每项的 t 次幂和，如果求和时，每项不是 t 次幂，而改成相临 t 项积呢？为简便起见，这里假设 $t = 2$ ，更高次幂依此类推即可。

$$S(n) = \sum_{k=1}^n a_k \cdot a_{k+1} = a_1 \cdot a_2 + a_2 \cdot a_3 + \dots + a_n \cdot a_{n+1}$$

类似上面方法，思路是对乘积变换，前后间可能消除子项。具体是这样的，
升维：把二项积变换三项积：

$$a_n \cdot a_{n+1} = x \cdot a_{n-1} a_n a_{n+1} + y \cdot a_n a_{n+1} a_{n+2}$$

其中 x 和 y 是特定系数，实际上 $-x = y = \frac{1}{3d}$ ：

$$\begin{aligned}
x \cdot a_{n-1} a_n a_{n+1} + y \cdot a_n a_{n+1} a_{n+2} &= x \cdot (a_n - d) a_n a_{n+1} + y \cdot a_n a_{n+1} (a_n + 2d) \\
&= x a_n \cdot a_n a_{n+1} - x d \cdot a_n a_{n+1} + y a_n \cdot a_n a_{n+1} + 2y d \cdot a_n a_{n+1} \\
&= [(x+y)a_n + (2y-x)d] \cdot a_n a_{n+1}
\end{aligned}$$

x 和 y 的值应独立于 a_0, d 成立，则：

$$\begin{aligned}
(x+y)a_n + 2yd - xd &= 1 \\
x+y &= 0 \\
2y-x &= 1
\end{aligned}$$

可以算出 $-x = y = \frac{1}{3d}$ ：

$$a_n a_{n+1} = \frac{1}{3d} (-a_{n-1} a_n a_{n+1} + a_n a_{n+1} a_{n+2})$$

对 n 遍历得：

$$\begin{aligned}
a_1 a_2 &= \frac{1}{3d} (-a_0 a_1 a_2 + a_1 a_2 a_3) \\
a_2 a_3 &= \frac{1}{3d} (-a_1 a_2 a_3 + a_2 a_3 a_4) \\
&\dots \\
a_n \cdot a_{n+1} &= \frac{1}{3d} (-a_{n-1} a_n a_{n+1} + a_n a_{n+1} a_{n+2})
\end{aligned}$$

得出前等差数列的前 n 项积和：

$$S(n) = \sum_{k=1}^n a_k \cdot a_{k+1} = \frac{1}{3d} (a_n a_{n+1} a_{n+2} - a_0 a_1 a_2)$$

不难发现，此式关键是首尾两个三项积之差。注意这里借用了 a_0 . 下面以

$$S(n) = 1 \times 4 + 4 \times 7 + 7 \times 10 + \dots + (3n-2)(3n-2+3)$$

为例。可推出：

$$\begin{aligned}
(3n-2)(3n-2+3) &= \frac{1}{9} [-(3n-2-3)(3n-2)(3n-2+3) + (3n-2)(3n-2+3)(3n-2+6)] \\
&= \frac{1}{9} [-(3n-5)(3n-2)(3n+1) + (3n-2)(3n+1)(3n+4)]
\end{aligned}$$

每项被变换为加减法，可以通部分抵消，达到求和目的：

$$\begin{aligned}
 1 \times 4 &= \frac{1}{9}[-(-2) \times 1 \times 4 + 1 \times 4 \times 7] \\
 4 \times 7 &= \frac{1}{9}[-1 \times 4 \times 7 + 4 \times 7 \times 10] \\
 7 \times 10 &= \frac{1}{9}[-4 \times 7 \times 10 + 7 \times 10 \times 13] \\
 &\dots \\
 (3n-2)(3n+1) &= \frac{1}{9}[-(3n-5)(3n-2)(3n+1) + (3n-2)(3n+1)(3n+4)]
 \end{aligned}$$

这里 $a_0 = 1 - 3 = -2$. 所有等式相加，得：

$$S(n) = \frac{1}{9}[(3n-2)(3n+1)(3n+4) + 8]$$

6.4 幂和与积和的联系

至此等差数列的幂和与积和都可得出。我们发现求幂和与积和的通用思路是
升维。幂和借用 $t+1$ 次二展开式，而积和借用 $t+1$ 项积。

其实幂和可以用积和的方式计算：

$$\begin{aligned}
 a_n^2 &= a_n \cdot [(a_n + d) - d] \\
 &= a_n \cdot [a_{n+1} - d] \\
 &= a_n a_{n+1} - d \cdot a_n
 \end{aligned}$$

Part III

ICT

Chapter 7

Terminologies

7.1 Internet and internet

Capitalized Internet (Interconnected Network) is a *global* network of networks, using the TCP/IP *protocol suite* and consisting of private, public, academic, business, and government networks of local to global scope. There is only one Internet in the world!

On the other hand, the lower case internet refers to any instance of Interconnected Networks using the same type of protocols. An internet is may or may not connect to the Internet; may or may not use the TCP/IP protocol suite.

Chapter 8

Operating System

8.1 CRLF

This sections talks about keys (and their names) and keyboard.

We have *physical* keyboard with labels like 1, 2, Enter, Delete etc. The physically pressed keys are captured by OS and then translated *integer keycodes*. Programs read the keycodes and interpret them as appropriate *logical* keys.

We can change keycodes passed from OS to a program like switching left Ctrl and Caps. When Caps key is pressed, the Ctrl keycode is sent to the program.

Several logical keys have their own names. Specifically, DEL, ESC, LFD, SPC, RET, TAB, and *newline* all stand for themselves when seen in online posts. Name C-m (pressing the Return key) is translated to logical RET. C-k for pressing Control and k simultaneously. C-j is translated to LFD. Don't be fooled. Logical name DEL corresponds to Backspace on keyboard, not Delete.

Then let's have a look at ancient typewriter, comprising *Carriage Return* that helps feed a new line. When a new line is required, the carriage return pulls back the typing head and then a new paper line is fed up. So in the old times, a new line consists of a Carriage Return and a Line Feed.

In the PC age, the corresponding keyboard key is Enter. When it is pressed, the logical name is ENTER, also called (*electronical*) *newline*. So it is not uncommon that the Enter key has an arrow line as depicted in 8.1. The vertical line means line feed while the horizontal arrow means carriage return.

The two operations can be named as CR and LF respectively. Programming languages, Bash included, use \r and \n to denote the two names. In Linux, it is \n, while in Windows it is \r\n. Mac OS, to the contrary, is \r. We call this *line ending scheme*. It is critical to be aware of line ending difference, especially when web

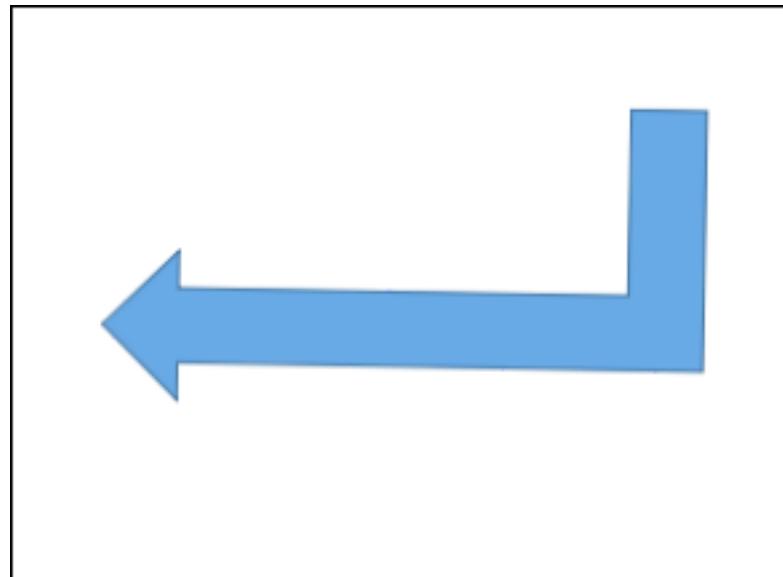


Figure 8.1: Enter/Return Key

techniques are involved like 15.1.

- C-m, ^M, \r, Carriage Return, RET are all the same thing.
- C-j, ^J, \n, Line Feed, LFD as well.

8.2 Memory

8.2.1 Cost of Reclaiming

The cost of memory *initialization* and *destruction* of kernel data objects can actually outweigh the cost of allocating them, which can result in significant performance drop.

Kernel is reluctant to free up memory unless required.

8.2.2 Slab Allocation

A slab is a set of one or more *continuous* memory pages *pre-allocated* for the slab allocator as an individual *cache*. This cache is further divided into *equal segments* (also called *chunk* or *slot*) in size of the object type that the cache is managing. It is a memory allocation mechanism intended for *small objects* of the *same type* like *inode* and *dentry*:

In this parlance, the word cache or caching refers to a memory storage for a specific type of object, such as *semaphores*, *process descriptors*, *file objects*, etc. It is **not** the *cache memory* between the main memory and CPU.

A small object may be 8 bytes, 16 bytes, or 256 bytes large, but usually far smaller than the size of a 4K memory page. If every small object is allocated a separate memory page, it would be a vast memory waste and lead to *internal* and/or *external* memory *fragmentation*.

The notion of *object caching* was primarily introduced in order to *avoid* the overhead such overheads.

As a slab is pre-allocated, memory allocation request can be instantly satisfied in one of the preserved slot. Destruction of the object does not reclaim the slot but only puts the slot into the list of free slots by the slab allocator. This process eliminates the need to search for suitable memory space and greatly alleviates memory fragmentation.

From file `/proc/meminfo`, Slab is the total amount of available slots. SReclaimable can be freed up by kernel for other usage while SUnreclaim cannot.

For slab details, execute `man 5 slabinfo` and `slabtop`. Here is an excerpt 8.1:

#	name	<active_objs>	<num_objs>	<objsize>	<objperslab>	<pagesperslab>	: tunables	<limit>	<batchcount>	<sharedfactor>	: slabdata	<active_slabs>	<num_slabs>	<sharedavail>
2	ext4_groupinfo_4k	364	364	144	28	1 : tunables	0	0	0 : slabdata	13	13	0	0	0
	squashfs_inode_cache	0	0	640	25	4 : tunables	0	0	0 : slabdata	0	0	0	0	0
4	fuse_inode	3864	3864	768	21	4 : tunables	0	0	0 : slabdata	184	184	0	0	0
	PINGv6	0	0	1152	28	8 : tunables	0	0	0 : slabdata	0	0	0	0	0
6	RAWv6	56	56	1152	28	8 : tunables	0	0	0 : slabdata	2	2	0	0	0
	tw_sock_TCPv6	0	0	240	17	1 : tunables	0	0	0 : slabdata	0	0	0	0	0
8	request_sock_TCPv6	0	0	304	26	2 : tunables	0	0	0 : slabdata	0	0	0	0	0
	dma-kmalloc-16	0	0	16	256	1 : tunables	0	0	0 : slabdata	0	0	0	0	0
10	dma-kmalloc-8	0	0	8	512	1 : tunables	0	0	0 : slabdata	0	0	0	0	0
	dma-kmalloc-192	0	0	192	21	1 : tunables	0	0	0 : slabdata	0	0	0	0	0
12	kmalloc-8192	72	72	8192	4	8 : tunables	0	0	0 : slabdata	18	18	0	0	0
	kmalloc-4096	249	272	4096	8	8 : tunables	0	0	0 : slabdata	34	34	0	0	0
14	kmalloc-512	864	912	512	16	2 : tunables	0	0	0 : slabdata	57	57	0	0	0

Listing 8.1: Slab Info

The first column is the *names* of different types of slabs. *kmalloc-512* means this slab is designated for 512-byte objects. So is *dma-kmalloc-192* for 192-byte objects. To filter slabs larger than or equal to 10M, run:

```
awk '{ if ( $3*$4/1024/1024 > 10 ) { print $1, $3*$4/1024/1024 } }' /proc/slabinfo
```

Chapter 9

Domain Name System

9.1 Contact

HU Zhan
zhan.hu@chinacache.com

Table 9.1: Contact

9.2 Outline

The system resolves a *fully qualified domain name* (FQDN) of a host to IP and mainly comprises:

- A distributed and decentralized *database* implemented in a hierarchy of *name servers*.
- An application layer protocol over UDP port 53, which is utilized by other application layer protocols like HTTP. TCP 53 is widely supported nowadays.
- The name servers are often UNIX machines running the Berkeley Internet Name Domain (BIND) or Dnsmasq software.
- Work in Client-Server mode.

Roles:

- Domain: administration space.
- Domain Name: name of administration space.

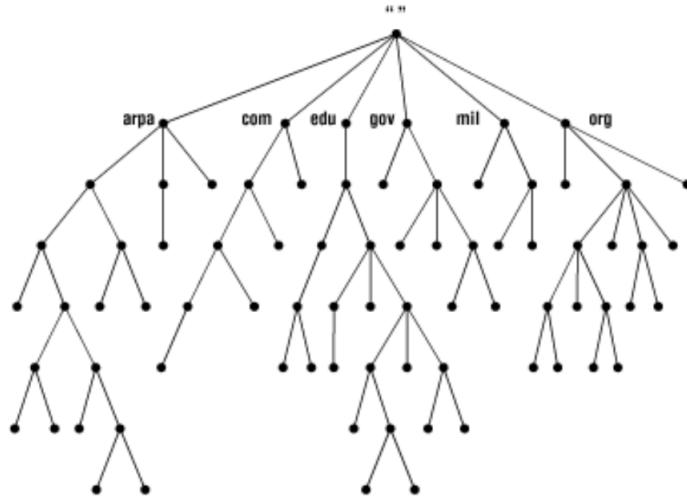


Figure 9.1: Domain Tree

- Domain Name Servers: implement DNS database and resolve subdomain names.

9.3 Domain Tree

Domains define *administration space* of different levels and sizes, and can be demonstrated in a *tree* structure as depicted in figure 9.1. External nodes represents physical *hosts*. Nodes in the tree is assigned labels, like *com*, *cn*, etc. A *null* "" label is reserved for the *root*. But in text it is written as a *dot*. Host nodes are labelled by *hostnames* 9.5. We will find, later in the post, each *administration entity* is responsible for managing *name resolution* in its own space.

A node and the corresponding subtree represents a domain. The root represents the whole space in DNS, namely *root domain*. Each domain can be further divided into additional partitions, called *subdomains*. For example, node *edu* defines a subdomain of the root domain. Domains at the second and third layers are called *Top-level Domain (TLD)* and *Authoritative Domain* respectively.

We assign a *name* to each domain, namely *domain name*. Domain name is the sequence of labels from the domain node (root node of the subtree) to the root, with *.* separating the labels. In this post, *root node* refers to that of a subtree, while *root* refers to that of the whole tree.

For instance, *root domain name* is written as a dot *<.>* while *<com.>* is an instance of *TLD name*. *bing.com.* is an *Authoritative Domain Name*. Attention please; there

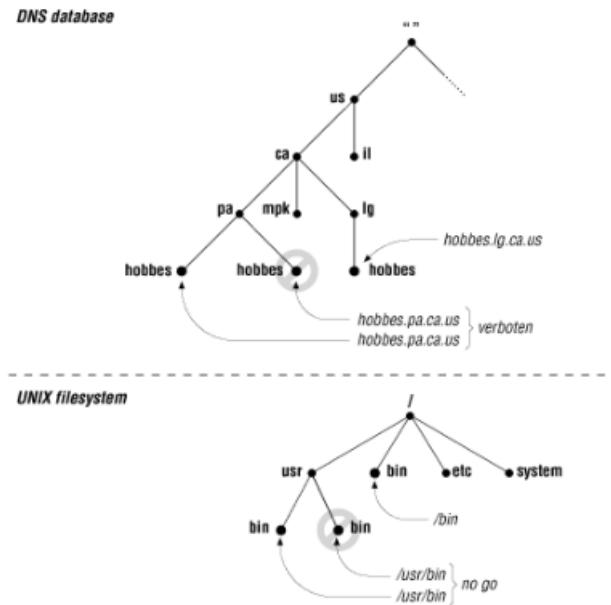


Figure 9.2: Domain Name Uniqueness

is one and only one root domain name! The concepts can be illustrated as below:

node => subtree => domain/subdomains => domain name

DNS requires that sibling nodes have different labels to guarantee *uniqueness* of domain names. Figure 9.2, has two sibling nodes with *hobbes* label. That is not acceptable.

The relation between domain and domain name is interesting. We can say a domain has a domain name. We can also say a domain contains a bunch of subdomain names. For example, a TLD named as *edu*. contains all subdomain names ending with *edu*. like *berkeley.edu*. and *ustc.edu*.

Each host has domain name as well. Domain name of a host is associated with information like IP address, name aliases, mail routings etc. in the database. It is the original intention of DNS to record and resolve the information associations.

Domain tree resembles the organization of an UNIX filesystem - a database of directories and files, namely pathnames. Pathname is analogous to domain: internal domain and directory pair, external domain (host) and file pair are analogous. A slight difference is the name order. In UNIX filesystem, a pathname is written in a top-down manner while a domain name in *reverse order* - upward to the root.

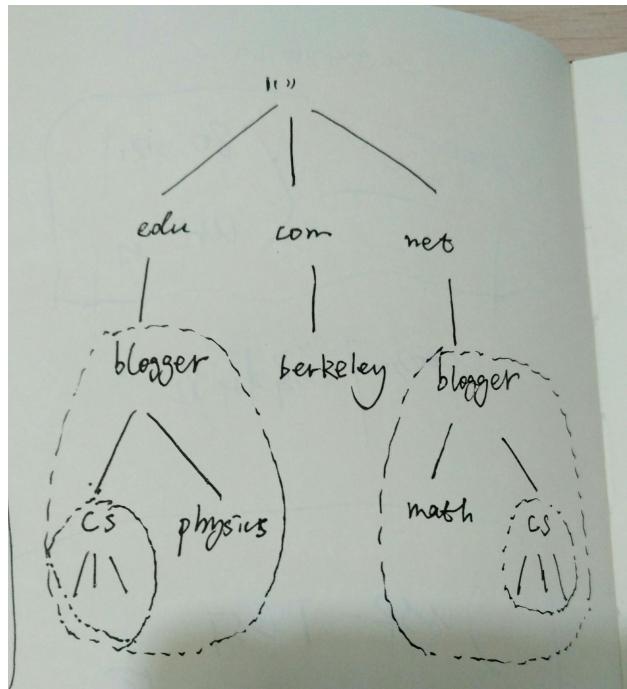


Figure 9.3: Relative Domain Name

9.4 FQDN

Domain name can be either *absolute* or *relative*. When a domain name ends with the root label (dot), it is an absolute domain name and also called Fully Qualified Domain Name (FQDN). The root label is different from the dot separator, though they look the same. All domains discussed in the prior section are absolute. Relative domain names provided to server side will be transformed to absolute versions by appending current ORIGIN. The partial transformation may be done in the client side by *resolver* (check section 9.15).

An absolute domain name resembles an absolute pathname in UNIX filesystem - relative to the root. A relative domain name resembles a relative pathname - relative to the root node of a subtree.

A relative domain name like `cs.blogger` without trailing dot, can be anywhere in the tree and may correspond to one or more subdomains and subtrees as in figure 9.3. Analogously, multiple relative pathnames with the same name are allowed.

With respect to DNS, we'd better use FQDN as much as possible to rid confusion.

Without explicit note, all domain names are *absolute* in this post.

www	google	com	.
FQDN			
Authoritative Domain Name			
TLD			
Dot Root Domain			
www	google	com	.

Table 9.2: Host FQDN

9.5 Host

As analyzed above, each *host* has a domain name that is also a FQDN (easy to remember by humans). Alternatively, a host can also be identified by its IP address (used by routers). FQDN of a host can be divided into two parts, namely hostname - the first segment, and authoritative domain name - the rest part, demonstrated in table 9.2:

hostname in the context of DNS is different from that of command `hostname`. Instead, it is an identifier meaningful to DNS. In the target host, both values are not necessarily identical.

Take `www.example.com.` for example, `www` is the hostname, while `example.com.` is the authoritative domain name. Both names together constitute the host's FQDN.

FQDNs we use daily are actually aliases of their *canonical* versions and are far more mnemonic. A canonical FQDN may have multiple aliases. For example, `cn-0001.cn-msedge.net.` has two aliases, one of which is `www.bing.com..`

```
1 ; dig +nocookie www.bing.com cname
2
3 ;; ANSWER SECTION:
4 www.bing.com.      60    IN   CNAME  cn.cn-0001.cn-msedge.net.
cn.cn-0001.cn-msedge.net. 36    IN   CNAME  cn-0001.cn-msedge.net.
```

About the `dig` command, refer to section 15.22.14.

9.6 Name Server

How the DNS database is implemented? How domain names are resolved? Such questions lead to the topic in this section - *domain · name server*¹.

¹域 · 名字服务器

As mentioned in section 9.3, an administration entity manages domains and sub-domains of its own space. An entity can further delegates administration of sub-domains to other organizations. A domain is administrated by one and only one entity. To the contrary, an entity can administrate one or more domains. The core functionality of domain administration is to implement domain · name servers and database therein, like domain names, IPs, aliases. The entity should resolve names of all subdomain under its coverage directly or delegate the resolution to a sub-entity.

At the very top, we have *root domain · name servers*², then *TLD · name servers*³ at next layer, and *authoritative domain · name servers*⁴. Root domain name servers are responsible to resolve TLD names while TLD name servers are for authoritative domain names. Authoritative domain name servers resolve host FQDNs instead.

9.7 Resource Record

Now let's have a closer insight into what DNS database looks like. We call a DNS entry in the database Resource Record (RR). The relationship line can be put like below:

```
doname name => administration space => administration entity =>
domain name · servers => database => subdomain RRs => subdomains
resolution
```

RRs are indexed by domain names in DNS database. The snippet 9.1 are excerpts from one of the root domain name servers. Each entry is queried by TLD name <com.>.

2	com.	172800	IN	NS	a.gtld-servers.net.
4	com.	172800	IN	NS	b.gtld-servers.net.
	com.	172800	IN	NS	c.gtld-servers.net.
	com.	172800	IN	NS	l.gtld-servers.net.
	com.	172800	IN	NS	m.gtld-servers.net.

Listing 9.1: DNS Database Index

There exist multiple types of RRs like SOA, PTR etc. But they are not the core of the post. Here are four common types of RRs as follows:

- A: (domain name, ip)
- NS: (domain name, domain name server)

²根域 · 名字服务器

³顶级域 · 名字服务器

⁴权威域 · 名字服务器

- CNAME: (alias, canonical domain name)
- MX: (mail domain name, alias)

If a domain name server contains an A record for a particular subdomain name, it is *authoritative* for that name. Needless to say, it is an authoritative domain name server. If a domain name server contains an SOA record, it is also authoritative (check section 9.13). In this post, authoritative domain name server only refers to those resolving host FQDNs.

Most of the RRs in a name server are NS records that specify alternative domain name servers (at a lower level⁵) from which the subdomain name can be resolved. It is sensible that internal FQDNs require only NS records as they just do auxiliary jobs for resolving external FQDNs (that of hosts).

Those alternative domain name servers, in return, are all physical hosts in the system and should have their own external FQDNs. Accordingly, there *must* exist A records somewhere in the system. In other words, the selected external FQDN should be resolved first before the original query. This process may repeat several times during the resolution course.

9.8 Root Domain Name Server

There are overall 13 root domain name servers over the world, namely {a..m}.root-servers.net.. The relevant 13 IP addresses are fixed and kept by all name servers in the system, such that there is no need to resolve root domain name. This makes sure the resolving system starts with an initial entrance.

Those 13 name servers are authoritative for TLD names (i.e. com. and net.) and contain NS records, pointing where TLD names can be resolved. From excerpt 9.2, the root domain name server *b.root-servers.net.* contain 13⁶ NS records the TLD name *com..*

⁵A NS RR reflects the delegation of administration.

⁶The number of TLD name server is also 13.

```

1 ; <>> DiG 9.11.2-P1 <>> +trace www.bing.com
2 ;; global options: +cmd
3 .          82248 IN NS d.root-servers.net.
4 .          82248 IN NS k.root-servers.net.
5 .          82248 IN NS c.root-servers.net.
6 .          82248 IN NS e.root-servers.net.
7 .          82248 IN NS b.root-servers.net.
8 .          82248 IN NS j.root-servers.net.
9 .          82248 IN NS h.root-servers.net.
10 .         82248 IN NS i.root-servers.net.
11 .         82248 IN NS f.root-servers.net.
12 .         82248 IN NS m.root-servers.net.
13 .         82248 IN NS g.root-servers.net.
14 .         82248 IN NS l.root-servers.net.
15 .         82248 IN NS a.root-servers.net.
16 ;; Received 736 bytes from 127.0.0.1#53(127.0.0.1) in 2 ms

17 com.        172800 IN NS d.gtld-servers.net.
18 com.        172800 IN NS c.gtld-servers.net.
19 com.        172800 IN NS i.gtld-servers.net.
20 com.        172800 IN NS j.gtld-servers.net.
21 com.        172800 IN NS l.gtld-servers.net.
22 com.        172800 IN NS f.gtld-servers.net.
23 com.        172800 IN NS a.gtld-servers.net.
24 com.        172800 IN NS g.gtld-servers.net.
25 com.        172800 IN NS h.gtld-servers.net.
26 com.        172800 IN NS e.gtld-servers.net.
27 com.        172800 IN NS m.gtld-servers.net.
28 com.        172800 IN NS b.gtld-servers.net.
29 com.        172800 IN NS k.gtld-servers.net.
30 ;; Received 1172 bytes from 199.9.14.201#53(b.root-servers.net) in 198 ms

```

Listing 9.2: RRs in Root Name Server

Specially, root name servers are authoritative for each other and should contain A records as in excerpt 9.3. The root name server *j.root-servers.net.* are authoritative for *a.root-servers.net.* .

```

1 a.root-servers.net. 3600000 IN A 198.41.0.4
2 root-servers.net. 3600000 IN NS a.root-servers.net.
3 root-servers.net. 3600000 IN NS b.root-servers.net.
4 root-servers.net. 3600000 IN NS c.root-servers.net.
5 root-servers.net. 3600000 IN NS d.root-servers.net.
6 root-servers.net. 3600000 IN NS e.root-servers.net.
7 root-servers.net. 3600000 IN NS f.root-servers.net.
8 root-servers.net. 3600000 IN NS g.root-servers.net.
9 root-servers.net. 3600000 IN NS h.root-servers.net.
10 root-servers.net. 3600000 IN NS i.root-servers.net.
11 root-servers.net. 3600000 IN NS j.root-servers.net.
12 root-servers.net. 3600000 IN NS k.root-servers.net.
13 root-servers.net. 3600000 IN NS l.root-servers.net.
14 root-servers.net. 3600000 IN NS m.root-servers.net.
15 ;; Received 825 bytes from 192.58.128.30#53(j.root-servers.net) in 3 ms

```

Listing 9.3: A RR in Root Name Server

9.9 DNS Query

The resolution process goes in the reverse direction than FQDN. A FQDN is scanned from right to left along the tree in a top-down approach. Query is sent to a *local default name server* first and then routed hierarchically.

A local name server commonly is given by ISP and acts as a DNS proxy for all its customers. Though it does not belong to the DNS hierarchy, a local name server is critical to DNS resolution.

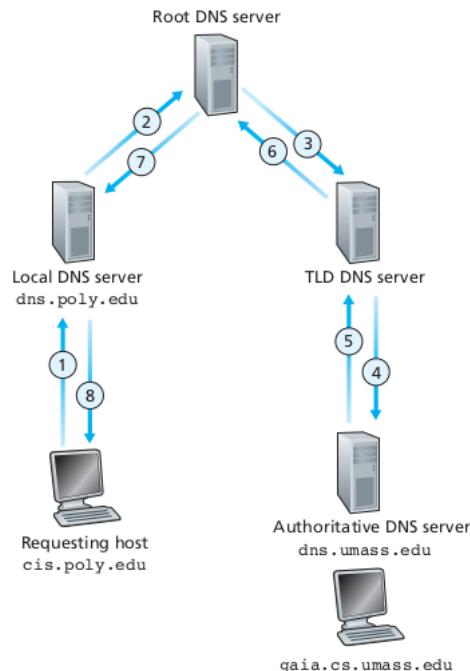


Figure 9.4: Recursive queries in DNS

Local name servers send customers' queries to the a root domain name server first, and then repeat *iteratively* or *recursively* through the system.

Iterative method means each DNS reply is sent back directly to the original query client and new queries are sent out accordingly. Resursive queries 9.4 mean each name server along the path acts as a DNS proxy and forwards the query on behalf of the preceding client and returns A records to it.

In reality, the resolution process may combine both methods. In figure 9.5, request from *cis.poly.edu.* to *dns.poly.edu.* belongs to recursive query while those from *dns.poly.edu* to all other upstream name servers belong to interative queries.

9.10 DNS Cache

Upon receving authoritative results from upper level, a name server chooses to **cache** the mapping results for a fixed period (the 2nd column of *dig* output), within which, new matched queries are served immediately. DNS caching can manifestly reduce DNS resolution time and improve user experience.

Although a domain name can be resolved by different domain name servers with DNS cache, those servers must have an authoritative source (check SOA in section

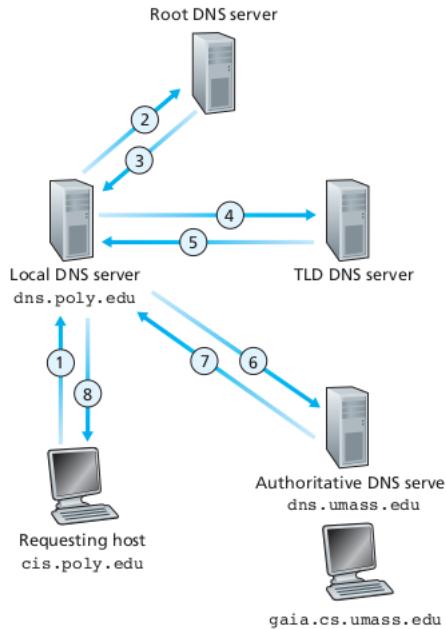


Figure 9.5: Iterative and recursive queries in DNS

9.13).

9.11 Round Robin

Round Robin is a technique of load distribution/balancing, provisioning multiple and redundant service hosts by managing DNS responses to address queries.

Most network application have a list of backend hosts and IPs thereof. The order of IPs returned are permuted in a round robin way.

Generally, a client application just pick the very first IP from the reply, so that different clients would receive service from different backends, thus distributing the overall load among servers.

9.12 Anycast

Apart from Round Robin, the system also adopts Anycast to eliminate the bottleneck of 13 root name servers. Name server IP has a bunch of backend hosts.

With the help of BGP routing and Automation System (AS), DNS queries are distributed to a geographically nearby host.

9.13 Zone Data File

RRs are actually defined in *zone data files* of name servers. As mentioned, a domain name server cannot have all the records of the whole database. A zone data file contains only part of the complete database. The term zone is analogous to domain, but not identical. For example, a zone data file may contain only part of RRs for a domain.

Basically, there are two types of zone data file. One is in the form of db.DOMAIN that maps domain names to IPs, which is called *forward mapping*. Take domain name *bing.com* for example, forward mapping records are stored in file *db.bing.com*.

The other type is for reverse mapping that maps IPs to domain names in the form of db.ADDR, where ADDR is the network address without trailing zeros. Take block 192.249.249.0/24 for example, its zone data file is *db.192.249.249*. Records in this type are called PTR.

Zone data files are also called *db* files. Any DNS implementation (i.e. BIND and Dnsmasq) must have these zone data files to support lookups. Also, they must comply with the same data format - master file format 9.14.

How these files are organized and located depends on configuration file. For BIND 8 or 9, the configuration file is */etc/named.conf*. The format of configuration file is flexible and depends on implementations.

9.14 Master File Format

Text after semicolon to the end of a line is treated as comments. Code \$TTL set the cache time of a record.

Start of Authority (SOA) record is a must for every domain name server, indicating this server is the *best* source of information for the data within this zone. There can be one and only one SOA record in each a data zone file.

Here is an excerpt of a SOA query for *www.bing.com..*. Obviously, db files on servers *ns1.cn-msedge.net.* and *msnhst.microsoft.com.* should contain such SOA record.

```
; dig www.bing.com soa
2 cn-msedge.net.      59  IN  SOA ns1.cn-msedge.net. msnhst.microsoft.com
. 2017032701 1800 900 2419200 240
```

SOA record is also used to do zone data file synchronization periodically among distributed domain name servers in the system. Ideally, each server should cache

as many RRs as possible. However, it is infeasible as the size is too much to hold and the increased synchronization traffic is beyond negligibleness.

Pointer (PTR) record accomplishes reverse mapping. The firstly field is a concatenation of a reverse network address and suffix domain *in-addr.arpa*. PTR records must point to *canonical* domain names instead of aliases:

```
; dig -x 204.79.197.200
2 200.197.79.204.in-addr.arpa. 2806 IN PTR a-0001.a-msedge.net.
```

In a *db.domain* file, symbol @ can be used to replace current ORIGIN. For example, a MX record 9.4 usually starts with @:

```
# db.movie.edu
@ IN SOA terminator.movie.edu. al.robocop.movie.edu. (
    1h ; serial number
    3h ; refresh after 3 hours
    1h ; retry after 1 hour
    1w ; expire after 1 week
    1h ) ; negative expiration
```

Listing 9.4: MX RR

9.15 Resolver

Once DNS is implemented, how to make use of it? We need *resolver*. Resolvers are the clients that access name servers when any programs running need name resolution.

Resolvers require configuration (*/etc/resolv.conf*) beforehand and allow customization of the following items:

- default *domain* directive;
- *search* list directive;
- *nameservers* directive;
- *sortlist* directive;
- *optoins* directive.

The *domain* and *search* directives are mainly used to make users' lives easier by saving them some typing. Both directives generate a list of relative domain names. When domain names sent to the resolver are relative (not FQDN), it would prepend the input to the each relative domain name in the list. The resulted domain names sent to namer servers is still relative, and will be appended by current ORIGIN.

Chapter 10

HTTP

Request for Comments - RFC2616 is now replaced by the 723x series, of which RFC7230 is the starting point, defining HTTP message and message routing.

10.1 Glossary

HTTP was created for the World Wide Web (WWW) architecture, and much of the architecture is reflected in the terminology and syntax defined in RFC723x series.

HTTP is a *stateless* protocol that operates by exchanging messages over transport-layer or session-layer connection in a *client-server* mode.

client and *server* refer to only the *role* that HTTP *programs* perform for a *particular* connection. The same program might act as a client on some connections or a server on others. A client *establishes* a connection for the purpose of sending one or more *requests*, a server instead *accepts* connections in order to serve requests by sending *responses*.

connection means a transport-layer connection of TCP/IP protocol stack between two endpoints. *endpoint* is either the client or server side of the connection. *peer* is a *remote* endpoint. *request* from client and *response* from server emphasize data transmission.

user agent refers to any of the various *client programs* on behalf of end users, including but not limited to browsers (i.e. Firefox), spiders (web-based robots like Googlebot), command-line tools (i.e. Curl), custom applications, and mobile apps.

The term *origin server* refers to the *server program* that can *originate* authoritative responses for a target resource.

An *entity* is comprised of *entity headers* and *entity body*. *entity body* and *payload* both refer to the body part of a HTTP message like equation (10.1). But entity emphasizes the data representation of target resource while payload emphasizes syntax of HTTP message.

$$\begin{aligned} \text{message-body} &= \text{Transfer-Encoding(entity-body)} \\ &= \text{Transfer-Encoding(Content-Encoding(Content-Type(target-resource)))} \end{aligned} \tag{10.1}$$

target resource, on the contrary, means the contents stored on origin server. For each content, the server might have multiple *representations* reflecting different versions of the content, like modification date, compression etc. In other words, a content may have multiple target resources that in turn may have multiple entities.

HTTP supports the use of *intermediaries* to satisfy requests through a *chain of connections*. There are three common intermediaries: *proxy*, *gateway*, and *tunnel*. In some cases, a single intermediary might change its type among proxy, gateway and tunnel based on the nature of each request.

Terms *upstream* and *downstream* are used to describe directional requirements in relation to *message flow* regardless of requests or responses: all messages flow from upstream to downstream. *inbound* and *outbound* are used to describe directional requirements in relation to the response: inbound means downstream response from the origin server and outbound means downstream response to the user agent.

Proxy refers to *forwarding proxy* and Gateway refers to *reverse proxy*. A proxy is a message-forwarding agent selected by clients. A gateway acts as an origin server for outbound connections but translates received requests to another server, which is transparent to clients. Gateways are often used to do CDN for performance improvement, load balancing across multiple machines. Check the 502 (Bad Gateway) status code in section 10.4.5.

A proxy or gateway is defined in the context of HTTP communication. There are also proxies that can act on *lower* layers of the network protocol stack, filtering or redirecting HTTP traffic without the knowledge or permission of HTTP participants. For example, *interception proxy* (also commonly known as *transparent proxy*) is selected by neither client nor server sides.

A tunnel is just a *blind relay* between two connections without changing the messages. Once active, a tunnel is not considered a party to the HTTP communication. The tunnel is not aware of any HTTP syntax or semantics.

Before ending this section, let's recall the term stateless. This term means each request can be understood or parsed standalone, without any prior knowledge. A server MUST NOT assume that two requests on the same connection are from the

same user agent. Specially, the “stateless” feature enables reuse of *cache*, and load balancing across multiple servers.

10.2 Cache

A cache is a local store of previous response messages and a relevant subsystem that controls its storage, retrieval, and deletion.

The purpose of a cache is to store *cacheable* responses in order to reduce the *response time* and network *bandwidth consumption* on future, equivalent requests. Please pay attention, not all responses are cacheable such as that of POST and PUT (read more in section 10.3.1).

The effect of a cache is that the request/response chain is shortened if one of the intermediaries along the chain has a cached response applicable to that request like figure 10.1.

10.2.1 URL URI

URI is the superset of URL in general. However, within an URL, the part after the domain name (including the leading forwardslash) is also a type of URI which, in RFC, is called *resource identifier*.

Regarding Nginx, variable `request_uri` is the equivalent of URI while variable `uri` is the normalized `request_uri` without query string.

10.3 HTTP Method

10.3.1 PUT POST

POST and PUT both can be used for *creating* and *updating* resources on servers.

PUT sends an entity with a specified URI location to the server. If there already exists an entity on that URI, it will be updated (replaced by the new one). Otherwise, the new entity is created (put) on the server. So we know that the PUT method requires an given URI identifier in the request.

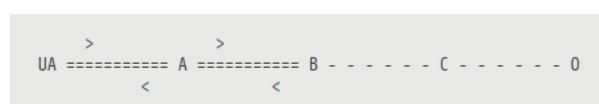


Figure 10.1: Shortened HTTP Chain

PUT is *idempotent* (幂等) similar to variable assignment like `x = 5`. If an entity are put multiple times, it makes no difference and the result is guaranteed.

POST is almost the same as PUT but cannot be used to create a new entity on a given URI. That is to say, the identifier part of an URI when creating is determined by the server side semantics. For example, this request would probably receive a 4xx status code (probably 404) when creating a new question to `stackoverflow.com`:

```
1 POST /questions/http-put-vs-post HTTP/1.1
Host: stackoverflow.com
```

Instead, please remove the resource identifier:

```
2 POST /questions/ HTTP/1.1
Host: stackoverflow.com
```

The server will create the resource identifier on demand. Therefore, POST creates a *subsidiary* resource. Here is an excerpt from the Internet:

From the other side of the fence: PUT if the client determines the resulting resource's address, POST if the server does it.

Apparently, POST is *not idempotent* when *creating* the same entity multiple times as the identity part is not controlled by the client side, resulting in duplicate entities located under different URIs.

As both PUT and POST create or update entities, responses are *not cacheable* as those operations are expected to execute *only once* by nature. If a PUT or POST request was cached, then cache servers (including user agents) would repeat the request unintentionally and the relevant entity would be created or updated repeatedly too. To the contrary, a GET method only reads entity from servers and can be cached.

10.3.2 GET POST

The advantage of GET over POST is that everything about a GET request is stored in the URI. So it is quite easy to be manipulated on the fly; recorded by search engine; bookmarked by browser; cached by proxy etc.

In terms of method security, POST is advantageous over GET. When GET something from the server, the request URI can be tracked through browser history, server log and search engine (i.e. Google). On the other hand, desired action

RFC 7231	HTTP/1.1 Semantics and Content	June 2014
Code Reason-Phrase Defined in...		
100 Continue Section 6.2.1		
101 Switching Protocols Section 6.2.2		
200 OK Section 6.3.1		
201 Created Section 6.3.2		
202 Accepted Section 6.3.3		
203 Non-Authoritative Information Section 6.3.4		
204 No Content Section 6.3.5		
205 Reset Content Section 6.3.6		
206 Partial Content Section 4.1 of [RFC7233]		
300 Multiple Choices Section 6.4.1		
301 Moved Permanently Section 6.4.2		
302 Found Section 6.4.3		
303 See Other Section 6.4.4		
304 Not Modified Section 4.1 of [RFC7232]		
305 Use Proxy Section 6.4.5		
307 Temporary Redirect Section 6.4.7		
400 Bad Request Section 6.5.1		
401 Unauthorized Section 3.1 of [RFC7235]		
402 Payment Required Section 6.5.2		
403 Forbidden Section 6.5.3		
404 Not Found Section 6.5.4		
405 Method Not Allowed Section 6.5.5		
406 Not Acceptable Section 6.5.6		
407 Proxy Authentication Required Section 3.2 of [RFC7235]		
408 Request Timeout Section 6.5.7		
409 Conflict Section 6.5.8		
410 Gone Section 6.5.9		
411 Length Required Section 6.5.10		
412 Precondition Failed Section 4.2 of [RFC7232]		
413 Payload Too Large Section 6.5.11		
414 URI Too Long Section 6.5.12		
415 Unsupported Media Type Section 6.5.13		
416 Range Not Satisfiable Section 4.4 of [RFC7233]		
417 Expectation Failed Section 6.5.14		
426 Upgrade Required Section 6.5.15		
500 Internal Server Error Section 6.6.1		
501 Not Implemented Section 6.6.2		
502 Bad Gateway Section 6.6.3		
503 Service Unavailable Section 6.6.4		
504 Gateway Timeout Section 6.6.5		
505 HTTP Version Not Supported Section 6.6.6		

Figure 10.2: HTTP Status Code

of POST method is embedded in the message body and cannot be cached. However, both methods use plain text transfer and can sniffed easily unless HTTPS is adopted.

10.4 HTTP Response Status Code

In this section, *response code*, *status code*, and *response status code* are referred to interchangeably, and mean almost the same thing: an three-digit integer from web server indicating the request and reponse status. The name *response* represents the HTTP reply message.

For authorative reference, check RFC7231. Figure 10.2 defines the list of available official codes. They are grouped into five categories, with the first digit defining the code class:

- 1xx *informational response*: the request was received, continuing process.
- 2xx *successful response*: the request was successfully received, understood, and accepted.
- 3xx *redirect*: futher action needs to be taken in order to complete the request.

- 4xx *client error*: the request contains bad syntax or cannot be fulfilled.
- 5xx *server error*: the server failed to fulfill an apparently valid request.

HTTP clients are not required to understand all registered status codes, though such understanding is obviously desirable. However, a client MUST understand the class (namely, the first digit) of any received code, and treat an unrecognized status code as being equivalent to the x00 status code of the x class where x belongs to 1, 2, 3, 4, 5, with the exception that a *recipient* (i.e. proxy server) MUST NOT cache a response with an unrecognized status code.

Responses with status codes (by default, 200, 203, 204, 206, 300, 301, 400, 404, 410, 414, and 501) can be cached for heuristic expiration unless otherwise indicated the method definition or explicit cache controls. RFC7234 defines HTTP caches and the associated header fields that control cache behavior or indicate cacheable response messages.

10.4.1 Informational 1xx

The 1xx class of status code indicates an *interim* response for communicating connection status or request progress *prior* to completing the requested action and sending a final response.

The 100 (Continue) status code indicates that the initial part of a request has been received and has not yet been rejected by the server. The server intends to send a final response after the request has been fully received and acted upon.

The 101 (Switching Protocols) status code indicates that server is willing to change application protocol like upgrading to a newer HTTP version.

10.4.2 Successful 2xx

The 2xx class of status code is mostly desired, indicating the request was successfully received, understood, and accepted.

Of the 2xx class, the 200 (OK) status code is what a client expects largely and always (except the CONNECT method) has a payload, though an origin server MAY generate a payload body of zero length.

The 201 (Created) status code indicates that the request has been fulfilled and one or more new resources have been created (PUT, POST etc. methods).

The 202 (Accepted) status code indicates that the request has been accepted for processing, but the processing has not been completed.

Method	Permanent	Temporary
POST to GET	301	302
POST	308	307
GET		303

Table 10.1: Redirect and Method Rewrite

The 203 (Non-Authoritative Information) status code indicates that the request was successful but the enclosed payload has been modified by a transforming proxy. For example, image format is changed in an intermediate web proxy.

The 204 (No Content) status code indicates that the server has successfully fulfilled the request and that there is no additional content to send in the response payload body (PUT, POST etc. methods). Action is successfully applied to the server and the user agent will inform its user the success (i.e. a dialog pop up).

The 206 (Partial Content) code means the server is successfully fulfilling a range request for the target resource by transferring one or more parts of the selected representation that corresponds to the satisfiable ranges found in the request's Range header field.

10.4.3 Redirection 3xx

The 3xx (Redirection) class of status code indicates that further action needs to be taken by the user agent in order to fulfill the request. Most of the time, the user agent will send another request to the new URI specified in Location header field in the response.

User agents diverge on the method applied to the second request. In HTTP 1.0, 301 (Moved Permanently) and 302 (Found) are defined to use the same method as the original request, while 303 (See Other) rewrites method as GET regardless of the original method. However, most user agent implementations always rewrite the method as GET despite 301, 302 or 303.

Considering the implementation prevalence, HTTP/1.1 *has to* acknowledge the de facto practice, and added 307 (Temporary Redirect) and 308 (Permanent Redirect) to *explicitly* disallow method rewrite. In other words, original POST method cannot be rewritten to GET. Table 10.1 is a summary of method rewrite from RFC7231 and RFC7238.

Permanent redirect means future requests of the target resource should be sent to the new URI while temporary redirect sticks to the old URI. When upgrading HTTP to HTTPS or switching *php* to *html*, 301 permanent redirect can be adopted. The 302 status code can be classified into *on-domain* redirect (same domain name) and

off-domain redirect (different domain name). For example, users are usually redirected to a login URI temporary. Regardless of 301 or 302, domain name redirect is discouraged, which requires proper design at the very beginning of service deployment.

The 303 (See other) redirect explicitly rewrites request method as GET/HEAD to *retrieve* the target resource, and does not imply permanent or temporary redirect. Name “retrieve” is chosen as the new URI in the response is intended to provide only *descriptive* information on the final target. Consequently, 302 redirect is also called *indirect redirection* as further redirections may be required.

The redirect difference between 301 and 302 make a difference when Search Engine Optimization (SEO) is concerned. If domain name change is done with 301 redirect, then the Page Ranking (PR) of the old domain name is probably lost. When a 302 redirect is encountered, search engine by default attributes the page ranking to the original URI. Search engines may downgrade the PR as a target resource is preferred to be located by an unique URI.

Specially, 302 redirect is utilized to do URL Hijacking, basically, stealing PR of another domain for the favor of hijackers’ page contents. At the very beginning, a hijacker should find a way to achieve 302 redirect. For example, hack the target web server and embed a 302 directive directly in the HTML file or through Nginx *rewrite* directive. Other methods are like DNS Hijacking, Bypass Interception etc. When a user searches keywords covered in the hijacker’s page, search engine would probably return the original URL that would be then redirected to the hijacker’s URL. Once succeeded, the PR of the original page is contributed to the hijacker’s page.

Another interesting code is 304 (Not Modified). This code is returned when a conditional GET or HEAD request is received but the condition is evaluated to false. In other words, the target is not modified and the user agent has a up-to-date representation of the target resource. There is no need to transfer another representation of the target resource. Therefore, the 304 response *must not* contain a message-body.

More details, please check section 10.5.1.

10.4.4 Client Error 4xx

The 4xx class indicates the client seems to have erred. The 400 (Bad Request) status code means the server cannot fulfill the request due to malformed request syntax, invalid URI, deceptive request routing etc.

401 (Unauthorized) indicates that the request has not been applied because it lacks valid authentication credentials for the target resource. 403 (Forbidden) indicates

that the server understands the request but refuses to authorize it like invalid credentials.

404 (Not Found) indicates the server cannot find a current representation for the target resource or is not willing to disclose existence.

410 (Gone) indicates access to the target resource is no longer available (i.e. removed) at the origin server. It is common for limited-time, promotional services and for resources belonging to individuals no longer associated with the origin server's site.

405 (Method Not Allowed) indicates that the method received in the request-line is known by the origin server but not supported by the target resource.

416 (Range Not Satisfiable) indicates none of the ranges in the request's Range header field *overlap* the current extent of the selected resource.

10.4.5 Server Error 5xx

The 5xx (Server Error) class indicates that the server is aware that it has erred or is incapable of performing the requested method. The 500 (Internal Server Error) code indicates the server encountered an unexpected condition that prevented it from fulfilling the request. The 501 (Not Implemented) code means the server does not support the functionality required to fulfill the request.

The 502 (Bad Gateway) status code means the server, while acting as a proxy or gateway, received an invalid response from an inbound (upstream direction) server it accessed while attempting to fulfill the request. The 504 (Gateway Timeout) code indicates that the server, while acting as a gateway or proxy, did not receive a timely response from an upstream server it needed to access in order to complete the request.

The 503 (Server Unavailable) indicates the server is currently unable to handle the request due to temporary overload or scheduled maintenance. The situation might be alleviated after some delay.

10.5 Headers

10.5.1 Last-Modified

Last-Modified is a response header field providing a timestamp indicating the date and time at which the origin server believes the selected representation was last modified.

If-Modified-Since is a request header field, making the entity transfer conditional on the modification date of remote version being more recent than the field value.

When a cache party is involved, it will typically use the value of the cached message's Last-Modified field to generate If-Modified-Since. However, occasionally, other source data might be used such as the Date header field of the cached message.

The combination of Last-Modified and If-Modified-Since limits the scope of a web traversal to resources that have recently changed and reduce bandwidth.

10.5.2 ETag

ETag is another response header field providing the current *entity tag* for the selected representation, as determined at the conclusion of handling the request. It is an opaque string (i.e. a MD5 hash) differentiating between multiple representations of the same entity.

Similar to the Last-Modified and If-Modified-Since pair, a client can also use ETag values using If-Match or If-None-Match (analyzed below) to do conditional requests and may save bandwidth and response time. However, ETag is more reliable than date value when it is inconvenient to store modification dates or when date values is not accurate due to clock synchronization

The preferred behavior for an origin server is to send both a strong entity-tag and a Last-Modified value in successful responses to a retrieval request.

10.5.3 If-None-Match

The If-None-Match header field makes the request method conditional on a recipient cache or origin server either not having any current representation of the target resource when the field value is '*', or having a selected representation with an entity-tag that does not match any of those listed in the field value.

Most of the time, the field value is set to be a list of cached entity-tags. The server only responds a representation of which the entity-tag does not appear in the list.

The special asterisk can prevent unsafe methods (i.e. PUT and POST) from creating or updating a target representation multiple times, resulting in "lost update" issue as any entity-tag on the server will match the wildcard '*'.

On the other hand, there is the If-Match header field in a request. Upon receiving such requests, the server only performs the method when the representation entity-tag match any of the field value. If the value is wildcard '*', it requires at least one representation exist.

Request Header	Reponse Header
If-Match	Etag
If-None-Match	Etag
If-Modified-Since	Last-Modified

Table 10.2: Conditional Header and Cache Validator

Table 10.2 shows the combination of conditional headers.

10.5.4 Forwarded

Forwarded is an *extended* and *optional* HTTP *header field* that, when used, contains a list of parameter:identifier pairs that disclose information for the *client*, about the host header field and/or the proto, or by *proxies* when one or more proxies are involved in the chain of *request* connections

This header field is only used for HTTP requests and is not to be used in HTTP responses. Due to the sensitive nature of disclosed information, this header field should be turned off by default. Further, it applies to reverse proxies, as well as forwarding proxies. The following are samples added by a proxy:

Forwarded: `for=_gazonk`
² Forwarded: `For=[2001:db8:cafe::17]:4711`
 Forwarded: `for=192.0.2.60;proto=http;by=203.0.113.43`

The identifier is a Obfuscated Identifier that keep the IP address secret, while still allowing the “Forwarded” header field to be used for tracing and debugging.

From RFC7230, a *header field* consists of a *case-insensitive* field name followed by a colon (:), optional leading whitespace, the field value and optional trailing whitespace. The field name “Forwarded” can be written as lower case “forwarded”. Pay attention please, *parameters* in the field value are also case-insensitive. So “for” and “For” are equivalent.

Pairs should be semicolon-separated within the field value part. Each parameter must not occur more than once per field value. In other words, an individual proxy can add only one instance of a particular parameter.

A subsequent proxy that wants to add a new field value can either append it to the last field value after a *comma separator*, or add another “Forwarded” header field. Here is an example:

¹ Forwarded: `for=192.0.2.43, for=198.51.100.17`

The two for pairs are separated by a comma, representing two field values added different proxies in the request chain.

For the list of field values, the very first field value is added by the very first proxy, and each subsequent field value is appended by each subsequent proxy. The for parameter for the last proxy in the chain is not required, as the upstream server get its IP from the TCP connection directly.

A proxy can add a set of parameter:identifier pairs; it can also remove existing pairs added by previous proxies. Because this header field is optional, any proxy in the chain may choose not to update this header field. Please read more details from RFC7239.

However, in reality, the “Forwarded” header field name is implemented as *X-Forwarded-For*. Nginx has two relevant built-in variables to record the field value, namely `$proxy_add_x_forwarded_for` and `$http_x_forwarded_for`. The syntax is a bit different from what is specified in the RFC. Here is a common setting on a reverse proxy:

<code>proxy_set_header</code>	<code>X-Forwarded-For \$proxy_add_x_forwarded_for;</code>
-------------------------------	---

Both variables may or may not be related to another built-in variable `$remote_addr` which is the IP address of the preceding origin in the chain, derived from the underlying TCP connection. Basically, `$proxy_add_x_forwarded_for` will *append* `$remote_addr` to `$http_x_forwarded_for` that is the received field value of “X-Forwarded-For” from the preceding origin in the chain. If the Nginx is the very first proxy, then `$http_x_forwarded_for` would be empty.

By the way, the field value of “X-Forwarded-For” can be forged easily by manipulating the request header:

<code>curl http://www.example.com -H 'X-Forwarded-For: a.b.c.d' -H 'X-Real-IP : e.f.g.h'</code>

Often, the “X-Forwarded-For” is accompanied by another optional field X-Real-IP that records the `$remote_addr` like:

<code>proxy_set_header</code>	<code>X-REAL-IP \$remote_addr;</code>
-------------------------------	---------------------------------------

Unlike the *add* or *append* nature of `$proxy_add_x_forwarded_for`, X-REAL-IP is always overwritten by the current proxy. So it cannot be forged by manipulating the request header.

10.6 CORS

The *name origin* refers to a *tuple* consisting of *protocol*, *domain* and *port*:

```
(protocol, domain, port)
```

It is a property derived from web URL. Any variation of the three values denotes a different origin. Two URLs have the *same origin* if the protocol, domain, and port (if specified) are the same for both. The two URLs below have different origin as the ports are different.

```
1 http://www.example.com/data/cat.jpg  
https://www.example.com/data/cat.jpg
```

Script (i.e. JS) URLs in the form of *about:blank* or *javascript:* do not define a origin as protocol, domain, and port are *all absent*. Such script *inherits* the origin of the document containing the URL.

Before telling about what Cross-Origin Resource Sharing (CORS) is, let's have a look at same-origin policy. It is a critical mechanism that restricts how a document or script loaded from one origin can interact with a resource from another origin.

We call interactions between different origins *cross-origin* access, such as when we use XMLHttpRequest. It is a rule enforced by web browsers, not that of web servers. By default, a web browser does not allow cross-origin HTTP requests, where CORS comes into being. Figure 10.3 gives a clear illustration.

Loading the script file itself does **not** belong to cross-origin access and is not restricted by the same-origin policy. It is what the script executes after loading that do cross-origin access.

CORS refers to Cross-Origin Resource Sharing, letting a web server specify whether other web servers are permitted to load content from it. It uses additional HTTP headers to tell a *browser* that a web application for one *origin* has permission to access selected resources from another web application for a *different origin*.

A web application should execute *cross-origin HTTP request* when it requests a resource served by a different origin than its own. Such requests contain a HTTP header named as *Origin*. For example, the frontend Javascript code for a web application served under the origin of <http://domain-a.com> uses XMLHttpRequest to make a request for data <http://api.domain-b.com/data.json>. The request headers include *Origin: http://domain-a.com* which manifests how the term “origin” comes into being.

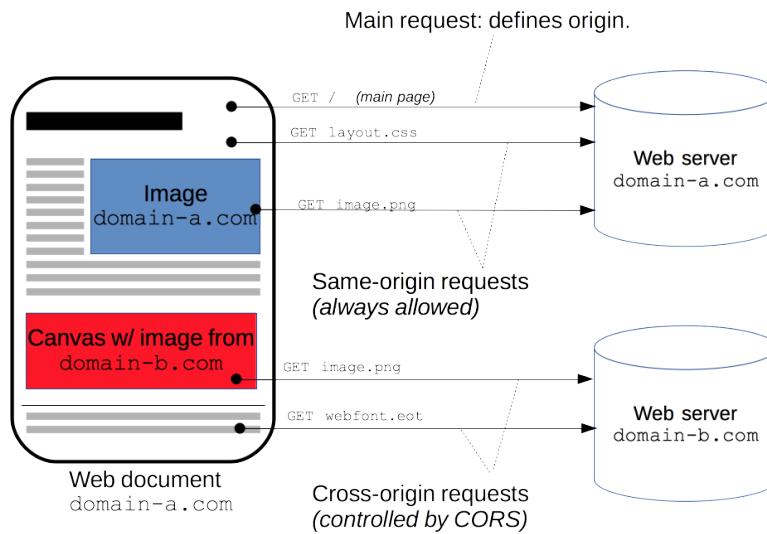


Figure 10.3: Cross-Origin Resource Sharing

Whether the response is blocked or not by the browser depends on response header Access-Control-Allow-Origin, indicating whether the response can be shared with requesting code from the given origin like:

```
Access-Control-Allow-Origin: *
2 Access-Control-Allow-Origin: http://api.domain-b.com
Access-Control-Allow-Origin: null
```

The special wildcard * means to allow CORS from any origin. Apart from the simple XMLHttpRequest, CORS also supports other methods like Preflighted Request. CORS is only one of the mechanisms to achieve cross-origin access. There exists JSONP to execute the same will. However JSONP is almost outdated and you only require it for older browsers.

简单用中文说：

- The Same-Origin Policy 叫同源策略。在没有同源策略之前，浏览器里不同源的代码和内容可以随意交互，不受限制。这会带来安全隐患，如 Origin A 的恶意代码可以访问 Origin B 上的安全信息。
- 完全遵守同源策略也使 HTTP 应用灵活性降低。如同一 Origin 里的域名可以有很多别名 CNAME，因此诞生了跨域（跨源）访问机制。其中一种就是本文讲的 CORS。简单来讲，就是服务器端告诉浏览器，哪些 Origin 可以对本 Origin 进行跨域访问。
- Origin A 服务器上的 js 脚本以 CORS 方式抓取 origin B 服务器上的内容，浏览器会检查 B 的响应头 Access-Control-Allow-Origin，如果响应

头中包含 origin A 则显示返回的内容，否则禁止。

- Origin A 从 Origin C 加载 JS 脚本这个行为本身不属于自己，不受同源策略限制。脚本在加载完毕后，对 Origin B 执行的请求才是跨域访问。
- 跨域只存在于浏览器端，不存在于 android/ios/Node.js/python/java 等其它环境。跨域请求能发出去，服务端能收到请求并正常返回数据，只是结果可能被浏览器拦截了。如果需要禁止对服务器的访问，则需要上“防盗链”或“鉴权”。

10.7 Websocket

The websocket protocol is a different protocol from HTTP for its own purpose, though they are related. Basically they are at the same layer over protocol stack and both sit on top of TCP connection.

Websocket is created not to replace HTTP but to meet new web requirements like *high throughput* and *low latency*. In order to be compatible with existing web infrastructure, Websocket makes use of HTTP handshake by the header fields Upgrade: websocket and Connection: Upgrade at port 80 or 443. Upon receiving the HTTP handshake request, the websocket server responds with status code 101 (Switching Protocols). From then on, the protocol is switched from HTTP to websocket. All following transmission is carried over the TCP connection just established. Like HTTP, it is a *message* protocol with each message 6 bytes headers. However, 6 bytes is negligible compared to HTTP headers.

At the very beginning, Websocket is one of the features (i.e. Local Storage and Geolocation) defined by the HTML5 specification and is now moved to a standalone protocol to keep the subject focused. Hence, it is not unusual to call it HTML5 Websocket.

Next I will talk about the purpose of Websocket and why it is invented alongside with HTTP. HTTP requires *synchronization* with strict *request* and *response* pair order. Only the *client* side can initiate the communication while the *server* side cannot. We call it a request/response protocol.

A HTTP/1.0 TCP connection allows only one request sent out at any given moment on a given TCP connection. After getting the response, the TCP connection would be closed and the client can send out a new request. However, a new TCP connection needs to be created. Such a synchronized request and response method brings in extra bandwidth and increases latency.

That is changed in HTTP/1.1 where the keep-alive feature keeps the underlying TCP connection open for further request and response pairs. Therefore, it is also called HTTP Persistent Connection. Another feature of HTTP/1.1 is HTTP pipeline.

Based on persistent connection, The client do not have to wait for responses before sending out new requests. So requests can sent out in line in series. However, the responses must arrive in the exact order as requests. Therefore, it is not a true multiplexing method. Most existing infrastructure (including Chrome/Firefox) disables HTTP pipeline by default.

HTTP/1.1 introduces Transfer-Encoding mechanism, an interface towards the TCP socket. It us not unusual we call it HTTP Streaming as Transfer Encoding allows sending of a resource representation in a set of chunks sequentially. Chunks are sent and received from the persistent TCP socket. It is HTTP application's role to re-assemble the chunks. Upon receiving all the chunks, the client reassembles them as a whole - the response! Transfer-Encoding fits dynamically generated content.

However, the request/response model still cannot satisfy modern real-time transmission requirements. The request and response headers are still present but most of them are almost identical - *redundant* data. Also, the pipeline by nature demands strict order! That is to say, the synchronization feature is still present, which suffers from Head-of-Line (HOL blocking). If the very first request of the pipeline is somehow not delivered as fast as expected, the requests behind are all blocked! Accordingly, clients (also applies to HTTP/1.0) need to make many requests use multiple connections to a server in order to achieve concurrency and thereby reduce latency.

On the other hand, Websocket is a *asynchronous full-duplex* protocol designated for *high throughput* and *low latency*. Firstly, it is a full-duplex protocol. Once the TCP connection is established, it is ready for data transmission from and to either side, regardless of client or server, namely *server push*. HTTP may utilize polling or long polling (somehow a stupid workaround) or *plugins* like Java Applet, Flash, and Silverlight. However, a plugin may not be accepted by intermediaries (CDN, proxies or firewalls), require custom ports, and is subject to security vulnerabilities. Websocket reuses well-known port 80 or 443 to be compatible with existing web deployment. When a firewall or proxy intermediate party is detected, Websocket automatically sets up a tunnel to pass through by issuing a HTTP CONNECT method.

As you see, data is sent out on demand, which is also called *server push*. Once data is ready, it is pushed to the client immediately. The asynchronous nature increases throughput greatly as the request/response synchronization hazard is relieved. Both sides can send data simultaneously. Figure 10.4 illustrates the transmission schemes between Websocket and HTTP.

With high throughput and low latency, Websocket fits application like video games, stock trending, customer support, live streaming etc. Whereas, HTTP has its own vantage points. It is much simpler and has a well-supported ecosystem. Unless required, please resort to HTTP first. Also, they can be combined together in live streaming like HTTP+Websocket+FLV. Figure 10.5 shows the data flow of existing

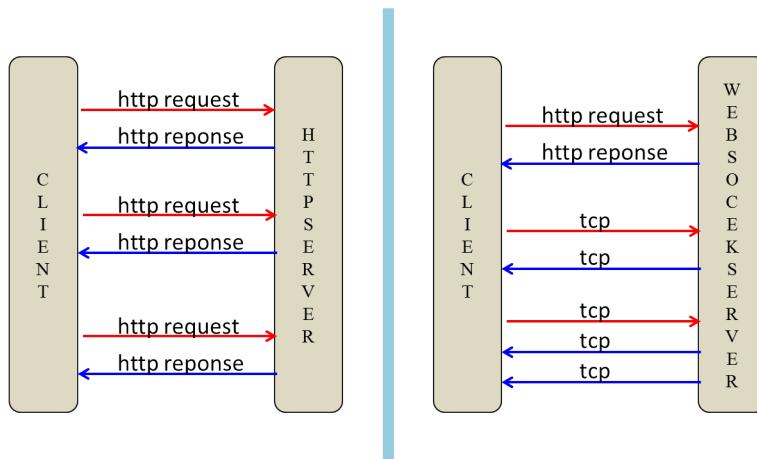


Figure 10.4: Websocket vs HTTP

live streaming applications.

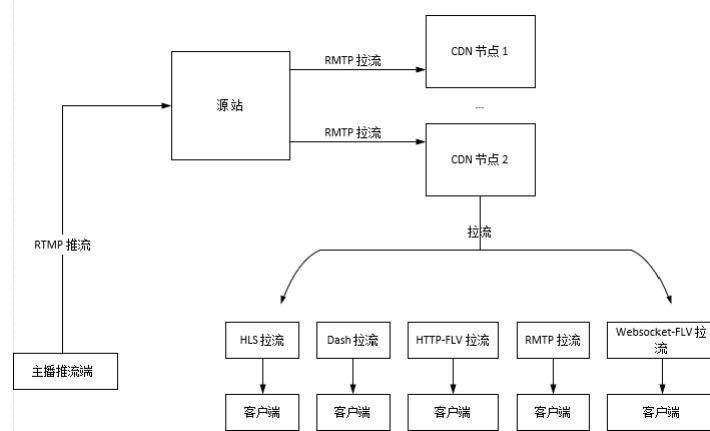


Figure 10.5: Live Streaming

To understand Websocket better, read [再谈 Websocket 架构设计 and About Websocket](#).

10.8 HTTP/2

In section 10.7, we discussed the difference between HTTP/1.0, HTTP/1.1 and Websocket. Websocket is an ideal alternative to HTTP when serving applications of high throughput and low latency like live streaming. However, it is *less supported* by real world infrastructure compared with HTTP. That is how HTTP/2 (not 2.0)

comes into being. The name h2 identifies the protocol where HTTP/2 over TLS while h2c identifies HTTP/2 over cleartext TCP.

HTTP/2 intends to be compatible with antecedent HTTP versions. So all request/response semantics are preserved but the syntax of conveying those semantics has changed. HTTP/2 is an *optimized* version of HTTP protocol. It improves throughput and reduces latency by introducing multiplexed request/response streams without HOL problems, Header Compression, HPACK, and unsolicited push of object representations from servers to clients. All the benefits are attributed to the *binary frame* layer introduced between HTTP and TCP. Different from the original text format, frame is binary.

In the context of HTTP/2, a HTTP message (either a request or a response) is splitted to smaller parts as *frames*. A frame refers to the *smallest* unit of communication within an HTTP/2 connection and consists of a header¹ with 5 fields and a variable-length (可变长) frame payload structured according to the frame type field.

Frame type indicates the purpose of a frame. For instance, the HEADERS frame and DATA frame form the basis of a HTTP message. The HEADERS frame corresponds to HTTP header while the DATA frame corresponds to message payload. Other frame types like SETTINGS, WINDOW_UPDATE, and PUSH_PROMISE are used in support of other HTTP/2 features. WINDOW_UPDATE implements *flow control*.

Header fields must be converted to lowercase within a HEADERS frame before sending out. Due to the existence of DATA frames, *connection-specific* header fields like transfer-encoding, keep-alive, Proxy-Connection, Upgrade etc. must **NOT** be used in HTTP/2.

Another concept is *stream* that is a *bidirectional* flow of frames within the HTTP/2 connection. Each stream consists of a set of frames, to realize a request/response pair. A single HTTP/2 connection can contain multiple concurrent streams, with either endpoint interleaving frames along the connection. In other words, in the frame layer, a stream represents a request/response exchange.

With so many frames over a HTTP/2 connection mangled, how to identify the affiliations between frames and streams? Streaming Identifier! Frames of a particular stream is identified by an integer assigned to by the endpoint initiating the stream. The independency of streams solves the HOL blocking issue. Frames of a stream can arrive in an intermingled way.

HTTP/2 *interleaves* requests and responses over a single persistent TCP connection with the requirement of pipeline order dismissed. Exchange of request/response pairs is *independent* of one another and organized into streams (discussed below). That is to say the exchange of an individual request/response pair creates a new stream and close it (a frame with the END_STREAM flag set) once done. So the

¹the frame header, not the HTTP header

blocking of a request/response pair of one stream does not prevent the progress of pairs of other streams.

HTTP/1.1 only support compression of message body, but HTTP/2 extends this feature to header fields as well. Header compression comprises of two index tables and the static Huffman Encoding, resulting a compression rate ranging from 0.5 to 0.95. The first index table is static table, storing 61 predefined common headers like 2 :method GET, 3 :method POST etc. The second is dynamic table, storing variable or customized headers for host, uri etc. starting from the index of 62. Huffman Encoding is a general variable-length coding scheme that the higher the probability of a event, the shorter its code is. From Static Huffman Encoding,

This Huffman code was generated from statistics obtained on a large sample of HTTP headers.

So the code for each character of headers is fixed, namely static, in accord with historical data.

Like Websocket 10.7, HTTP/2 supports *server push* allowing a server speculatively sending data to a client when the server anticipates that data is needed, namely response before request. This mechanism is a trade-off between bandwidth and latency. If the unsolicited response is unwanted, the bandwidth would be wasted. On the contrary, server push reduces latency significantly.

HTTP/1.x uses the concept of *start line*, namely the request line and response line. However, HTTP/2 requires that all header fields a key-value pair. To be compatible, HTTP/2 introduces *pseudo-header fields* beginning with colon : giving each start line value a name. Possible request pseudo-header names are :method, :scheme, :authority (namely the host), path, etc. URIs that do not contain a path component MUST include a value of '/'. Remember that pseudo-header fields are not standard HTTP header fields. :method, :scheme and :path are a must for HTTP/2 request. Every response must have the :status pseudo-header field.

10.9 HTTP References

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Chapter 11

ICT Operation

11.1 Cheat Sheet

Table 11.1 for release information; 11.2 for account information; table 11.3 for handy tips.

Command	Usage
<code>fgrep -qa docker /proc/1/cgroup; echo \$? cat /etc/{os,redhat}-release; rpm -q centos-release</code>	Docker container Distribution name

Table 11.1: Verify Linux Release

Command	Usage
<code>groupadd -g 2000 name</code>	Create a group
<code>useradd -ms /bin/bash -u 1000 -g name name</code>	Create an account and specify the login group
<code>groupmod -g 1000 -n newname name</code>	Change group ID and name
<code>usermod -u 1000 -g newname -aG wheel name</code>	Change account ID, login group ID, and append to the 'wheel' group
<code>gpasswd [-a -d] name name</code>	Add or delete account 'name' to group 'name'
<code>getent [passwd group hosts]</code>	Administrative database
<code>groups username</code>	Groups username joins
<code>users</code>	Users logged in to the system
<code>id</code>	Print uid, gid and groups

Table 11.2: Linux Account Management

Command	Usage
<code>cat >> file.md << EOF</code>	Append contents to a file from STDIN with a <i>here document</i>

Table 11.3: Rock Tips

11.2 Linux Tools

11.2.1 free

`free -hwt` commands display the amount of memory allocations, by analyzing the contents of file `/proc/meminfo`:

	total	used	free	shared	buffers	cache	available
2 Mem:	3.7G	781M	1.5G	160M	558M	985M	2.8G
Swap:	1.0G	0B	1.0G				
4 Total:	4.7G	781M	2.5				

Listing 11.1: Free Memory

Always keep euqation:

$$\text{total} = \text{used} + \text{free} + \text{buffers} + \text{cache}$$

in mind.

- *used* memory is allocated to user space processes.
- *free* memory is not allocated or freed up.
- textit{shared} memory (mostly by `tmpfs`) is part of *used*, shared among processes.
- Kernel *buffers* and *cache* is allocated to kernel itself. *cache* refers to memory used by the *page cache* and *reclaimable slabs*. For details about *cache* and *slab*, please read 8.2.
- *available* is the estimated amount of memory for starting new applications, *without* swapping.

Ideally, *available* should be the sum of *free*, *buffers* and *cache*. However, **not all reclaimable slabs** can be freed in time as some may be in use. So the actual *available* size is slightly smaller.

Part IV

Algorithm

Chapter 12

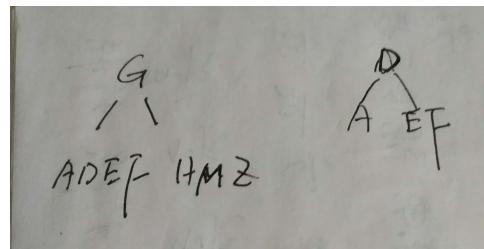
Tree

12.1 前序中序求后序

给出一个二叉树的前序遍历 GDAFEMHZ 和中序遍历 ADEFGHMZ, 求后序遍历。首先, 二叉树的前序遍历, 中序遍历, 后序遍历的区别是根节点是先、中、后访问。问题的关键是:

1. 前序遍历的第一个节点是根节点;
2. 在中序遍历里找到根结点, 其左边是左子树节点, 右边是右子树节点;
3. 对左子树重复上面两步;
4. 对右子树重复上面两步。
5. 二叉树被求出, 从而得到对应的后序遍历。

上面的例子里, 从前序遍历知 G 是根节点, 从后序遍历知, 左子树是 ADEF, 右子树是 HMZ, 此顺序就是左子树的中序遍历顺序。



但还要找到对应的前序顺序。对左子树 ADEF 来说, 在前序遍中的顺序是 DAFE, 说明左子树的根节点是 D, 从其中序顺序可知, 左子树是 A, 右子树是 EF. 重复此过程即可得出二叉树, 再得出后序遍历 AEFDHZMG.

同理, 已知后序遍历和中序遍历, 也可求出前序遍历。唯一的区别是后序遍

历的最后一个节点是根节点，每次找根节点时从最后找。不管是哪种题，中序遍历一定要有！

Chapter 13

栈

13.1 进栈出栈

栈是一种连续数据结构，数据在栈内连续存储。栈有栈顶和栈底类似链表的首部和尾部，区别是栈在垂直上下方向生长，链表在水平左右向生长。如果需要，我们也可以用水平示意图表示栈，左边是栈底，往右生长，如数组模拟栈就是这种思路。C/C++ 内存中的栈区即是一种栈结构。

给定一有 n 个元素的有序序列 a_1, a_2, \dots, a_n , 对栈有两种基本操作：进栈 push 和出栈 out. 无论是进栈还是出栈，都是对栈顶进行操作。进栈也称压栈，表示保持元素间相对顺序把元素存到栈顶，而出栈则表示取出栈顶的元素。

进栈、出栈组成一个动态操作序列，在 n 个元素依次进栈的过程中，伴随着元素随机出栈。动态操作序列有 $2n$ 个步骤，其中 n 个是进栈操作，另 n 个是出栈操作。进出栈操作结束，栈为空，进栈的 n 个元素亦全部出栈。

进栈顺序事先给定，用下标 i 表示，表示为 $a_i, i \in \{1, 2, \dots, n\}$. 出栈序列是进栈序列的某种排列，可记为 $a_{j_l}, j_l \in \{1, 2, \dots, n\}, l \in \{1, 2, \dots, n\}$. a_i 进栈操作和 a_{j_l} 出栈操作相间出现。 $2n$ 个动态操作序列可记成：

$$c_k, k \in \{1, 2, \dots, 2n\}, c_k \text{ 是 } a_i \text{ 进栈或 } a_{j_l} \text{ 出栈}$$

可以肯定 c_1 肯定代表 a_1 进栈， c_{2n} 表示某元素出栈。

实际上给定一个完整的出栈序列 a_{j_l} 我们可以还原进出栈操作序列 c_k , 所以通常只需出栈序列 a_{j_l} 即可。给出进栈序列 a_i 在 c_k 中的位置，我们可以推出剩下 n 个位置的出栈序列 a_{j_l} .

13.2 先进后出

进栈出栈遵循**先进后出，后进先出**的原则。对于当前栈内元素，后进栈的压在先进栈的上边，栈顶永远是当前最后一个进栈元素，所以先进栈的肯定比后进栈的后出栈，或说后进栈的肯定比先进栈的先出栈。换句话说，任一时刻，栈的状态决定了当前栈内元素的相对出栈顺序。

总结起来，进出栈序列 c_k 满足：

- a_i 间的相对位置固定，因为进栈顺序事先给定。
- a_i 和 a_{j_l} 符合先进后出。

可以看出，上面说的进栈出栈，不是指所有 n 个元素全部一次性入栈，再一次性出栈。实际过程是进栈、出栈两种操作是交替进行，只要栈不为空，就有可能进行出栈操作。如 a_1, a_2 依次入栈（栈顶到底依次是 a_2, a_1 ，所以 a_2 肯定比 a_1 先出栈），接着 a_2 立即出栈， a_3 入栈（栈内依次是 a_3, a_1 ，所以 a_3 肯定比 a_1 先出栈）。

前对对进出栈过程分析的比较清楚，任一时刻的栈内元素符合先进后出原则。那么此原则是如何体现在完整操作序列 c_k 里的呢？

出栈序列里任一元素 a_{j_l} ，比其后出且先进的元素倒序。这些元素排在 a_{j_l} 后面（后出栈），而且下标比 j_l 小（先进栈）。它们（包括 a_{j_l} 在内）一定是按下标降序排列！

我们可以据此判断一个出栈序列是否正确。如 $3, 4, 5, 1, 2, 9, 8, 7, 6$ 是出栈序列的下标 j_l ，显然这个出栈序列不正确，因为出现了 $3, 1, 2$ 。存在某个栈状态，3 压在 1 和 2 上面，栈内元素由上到下依次是 $3, 2, 1$ 。

为了便于运算，我们一般用下标直接代替元素本身！在验证时，我们遍历 j_l ，从其开始，后面比其小的是否全部降序。由上例， $4, 1, 2$ 和 $5, 1, 2$ 都不合法。

13.3 栈深度最小值

给出出栈序列 a_{j_l} ，问栈深度最小值是多少。

在进出栈动态操作过程中，元素或进栈或出栈，栈内元素个数不定。栈需容纳未出栈元素。如果每进栈一次，再出栈一次，则栈深度只需 1 即可。如果所有元素全部入栈再出栈，则栈深度最少为 n 。

对于一般情况，该如何算呢？其实很简单，只需利用上面的降序原则。遍历出栈序列，对 a_{j_l} ，数出从其开始往后，降序元素个数（包含 a_{j_l} ），最大值即为栈的最小深度。

13.4 出栈序列数

出栈序列数是指，给出进栈序列 a_i , 有多少种出栈序列 a_{j_i} ?

操作序列 c_k 有 $2n$ 个位置，一旦确定了进栈序列 a_i 的 n 个位置，则立马得到出栈序列。也可以选出 n 个位置作为出栈序列，但是出栈序列内部还有先后问题，所以用前一种思路更好。

从 $2n$ 个位置中选取 n 个的方法数是组合数 C_{2n}^n ，但进栈序列的选位方法数比这小。如 a_1 进栈肯定在第 1 位，而且 a_i 肯定不能排在最后 n 个位置。所以最终的方法数肯定是 C_{2n}^n 除以或减去某个数。

如果对进出栈计数，用 $+1$ 表示一次进栈， -1 表示一次出栈，则任何时候栈内元素个数就是这些 ± 1 的和。显然，任一时刻，栈内元素不能是负数个，入栈次数肯定不少于出栈次数， $+1$ 个不小于 -1 个数， ± 1 的和 ≥ 0 。

对应到 c_k , $k \in \{1, 2, \dots, 2n\}$ 序列，从头至尾扫描（水平示意图），对 k 编历，对任意 k ，前 k 个位置里， $+1$ 个数不少于 -1 个数。进出栈操作完毕， n 个 $+1$ 和 n 个 -1 总和为 0 。有时为了方便，直接用 \pm 表示即可。有的地方用 $+1$ 和 0 分别表示进栈、出栈，最后的 C_k 是一个二进制数。

总结起来是，**进出栈序列 C_k 的所有前缀子串皆满足 $+1$ 个数不小于（大于等于） -1 个数。**

特别地，当 $k = 1$ 时，前 1 位只能是 a_1 进栈，和加 1 为 1。当 $k = 2n$ 时，最后 1 位是某元素出栈，和减 1 为 0。

所以我们要在 C_{2n}^n 的基础上排除和为负的情况，也即在栈为空时或为负时，进行出栈操作，也即在遍历 k 的过程中遇到和为负数情况。

假设在遍历 k 的过程中，第 1 次遇到和为 -1 时，有 m 个 -1 ，则 $+1$ 为 $m - 1$ 次，此时 $k = 2m - 1$, $m \in \{1, 2, \dots, n\}$. 显然 k 是奇数， m 最大值是 n . 特别地，第 k 位是 -1 ，前面 $2m - 2$ 位中，分别有 $m - 1$ 位 $+1$ 和 -1 . 后面 $2n - k$ 位里面有 $n - m + 1$ 个 $+1$ ，剩下 $n - m$ 位是 -1 .

对于奇数 k ，非法方法数是不是

$$C_{2m-2}^{m-1} C_{2n-(2m-1)}^{n-(m-1)} = C_{2m-2}^{m-1} C_{2n-(2m-1)}^{n-m}$$

呢？此式表示前 $2m - 2$ 个位置里选 $m - 1$ 个出来放 $+1$ 表示进栈，剩下的 $2n - (2m - 1)$ 个位置里选 $n - (m - 1)$ 个放剩下的 $+1$. 从 -1 的角度分析，结果是 $C_{2m-2}^{m-1} C_{2n-(2m-1)}^{n-m}$. 答案是否定得！因为这种选取方法不能保证前面 $k - 1$ 位里不出现和为负的情况。

我们可以换个思路。第 1 次遇到和为 -1 时，后面 $2n - k$ 位的和是 $+1$ ，即进栈次数比出栈多 1. 如果交换后面的 ± 1 ，则可以得到一个满射，组合计数不变。交换后面的 ± 1 后， $2n$ 位里面有 $n + 1$ 个 -1 和 $n - 1$ 个 $+1$ ，总和为 -2 ,

出栈比进栈多 2 次。反过来，总和为 -2 时总能找到第 1 次和为 -1 的情况。所以总的非法进出栈方法数是 $C_{2n}^{n+1} = C_{2n}^{n-1}$ ，那么合法进出栈总数为：

$$C_{2n}^n - C_{2n}^{n+1} = \frac{C_{2n}^n}{n+1}$$

这其实是一个卡特兰数 5。

至此，我们从组合数的角度直接得出进栈数序列数为卡特兰数。进出栈序操作序列，对应对组合数学问题，是在 $2n$ 个位置上，选取 n 个放 +1 或 -1，要求是对位置 k 遍历，和为非负整数。

13.5 进出栈递推方法

下面我们从递推方法分析进出栈问题。分析算法问题时，我们可以找出问题不同规模之间的联系，具体点就是递推关系。在算法领域，初始条件非常重要。同一公递推公式因为不同的初始条件而产生不同的数列。

用 $f(n)$ 表示出栈序列数。先看进出栈的小规模问题。明显 $f(1) = 1$ ，只有 1 个元素 a_1 时，其进栈再出栈，只有一种可能。对于 $f(2) = 2$ 时：

1. 第一种是 a_1 进， a_1 出， a_2 进， a_2 出： $+ - + -$
2. 第二种是 a_1 进， a_2 进， a_2 出， a_1 出： $+ + - -$

当 $n > 2$ 时，我们就要抽象分析了。分析有两个思路。第一种是考虑 n 个元素里，哪个最先出栈，也即出栈序列里，谁是第 1 个元素。第二种是考虑第 1 个元素 a_1 出栈时所在位置，也即 a_1 在出栈序列排第几位。我们先看第一种思路。

13.5.1 最先出栈元素

如果是 a_1 最先出栈，则出栈序列是 $a_1, a_{j_1}, j_1 \in \{2, 3, \dots, n\}$ 。很明显， c_k 前两位是 $+ -$ ，表示 a_1 进栈后立马出栈。 a_1 进栈、出栈后不影响其后元素的进出栈，因为后面 $n - 1$ 个元素根本还没入栈，这是一个 $n - 1$ 规模的子问题，有 $f(n - 1)$ 种可能。

如果是 a_2 最先出栈。此时其前元素 a_1 已入栈并且没出栈。同理 a_2 最先出栈不影响后面元素 $a_i, i \in \{3, 4, \dots, n\}$ 的出栈序列，因为后面元素根本还没入栈。其后元素有 $f(n - 2)$ 种可能出栈序列。其前面的 a_1 穿插于其后元素出栈序列之间。

对于一般情况， $a_k, k \in \{1, 2, \dots, n\}$ 最先出栈。此时 $a_i, i \in \{1, 2, \dots, k - 1\}$ 已入栈并且没出栈。由前面分析可知，这 $k - 1$ 个元素元素下标比 k 小（先

进栈), 但比 a_k 后出栈, 在出栈序列里必须是 (相对) 降序排列 (包括 a_k 在内), 即 a_k, a_{k-1}, \dots, a_1 . 因为在 a_k 先出栈的条件下, 从栈顶到栈底依次是 $a_{k-1}, a_{k-2}, \dots, a_1$. 特殊的, 如果 $k = n$, 则 a_n 最先出栈, 说是所有 n 个元素依次全部进栈, 然后依次倒序出栈。

对于下标比 k 大的元素而言, a_k 最先出栈不影响 $a_i, i \in \{k+1, k+2, \dots, n\}$ 出栈。后面元素的出栈是规模为 $n - k$ 的子问题, 有 $f(n - k)$ 种可能。

这个一般情况有多少种可能呢? 考虑出栈序列 $a_k, a_{j_l}, j_l \neq k, j_l \in \{1, 2, \dots, n\}$. 除了第 1 位 a_k , 余下 $n - 1$ 位里先选 $k - 1$ 个出来按序放 $a_{k-1}, a_{k-2}, \dots, a_1$. 余下的 $n - k$ 位是 $a_i, i \in \{k+1, k+2, \dots, n\}$ 的出栈序列, 对应序列数是 $f(n - k)$. 所以最终是是:

$$C_{n-1}^{k-1} f(n - k) = C_{n-1}^{n-k} f(n - k), k \in \{1, 2, \dots, n\}$$

为保证定义完备性, 当 $k = n$ 时, 我们定义 $f(n - n) = f(0) = 1$. 所以 $a_i, i \in \{1, 2, \dots, n\}$ 的出栈序列数是:

$$\begin{aligned} f(n) &= \sum_{k=1}^n C_{n-1}^{n-k} f(n - k) = \sum_{k=1}^n C_{n-1}^{k-1} f(n - k) \\ f(1) &= f(0) = 1 \end{aligned}$$

很可惜这个结果是错的! 乘法原理要求相乘的两个部分没有交集。上面的分析里, 保证了后面 $n - k$ 个元素的出栈相对序列, 也保证了前面 $k - 1$ 个元素倒序出栈, 但当两个部分合在一起时, 用乘法原理时, 有部分不符合要求。如 $a_k, a_{n-1}, a_2, a_1, a_{n-3}, \dots$ 这个出栈序列里, a_k 前面的 a_2, a_1 保持了降序, a_k 后面的 a_{n-1}, a_{n-3} 是子问题, 但是合在一起时, $a_{n-1}, a_2, a_1, a_{n-3}$ 这 4 个元素不是严格降序。

虽然这个分析错误, 但能加强我们对进出栈问题的理解。

13.5.2 a_1 出栈位置

下面从最先入栈的元素 a_1 , 也即第 1 个元素出栈序号入手分析问题。设 a_1 第 $k, k \in \{1, 2, \dots, n\}$ 位出栈, 则在 a_1 前有 $k - 1$ 个元素出栈, a_1 后有 $n - k$ 个元素出栈。

可以肯定, a_1 第 k 位出栈时, 栈刚好为空, 表明有 k 个元素入栈并完全出栈。那么这 $k - 1$ 个元素是哪些呢? a_1 第 1 位入栈后, 有 $k - 1$ 个元素先入进出栈, a_1 等这些元素出栈后才最后出栈。明显这 $k - 1$ 个元素就是 $a_i, i \in \{2, 3, \dots, k - 1\}$.

假设 $a_l, k \leq l \leq n$ 在前 k 个出栈元素中。若 a_l 在第 1 位出栈，据上一小节思路，这 k 个位置显然放不下 a_l, a_{l-1}, \dots, a_1 这 l 个元素。若 a_l 在第 2 位，则 a_l 和 a_1 间的距离更短了，而且此时第 1 位是比 a_l 更靠后的元素了，同样容不下那么多元素。

以 $k = 2$ 为例， a_1 出栈前要等 1 个元素先出栈。这个元素只能是 a_2 。假若是 a_3 ，则出栈序列是 a_3, a_1, \dots ，显然中间的 a_2 没有正确出栈。从另一个角度看， a_3 第 1 个出栈，这个序列没有保证 a_3, a_2, a_1 间相对降序出栈。因此 a_1 等的不可能是 a_2 后的任何元素。

这 k 个元素的进出栈是一个完整的子问题，最先入栈的最后出栈。由于第 k 位确定为 a_1 ，则规模为 $k - 1$ 。方法数是 $f(k - 1)$ 。

在 a_1 后面进出栈的元素是 $a_i, i \in \{k + 1, k + 2, \dots, n\}$ 这 $n - k$ 个元素。通过上面分析得， a_1 在第 k 位出栈时，其前 $k - 1$ 个元素和后 $n - k$ 个元素的进出栈序列完全独立，互不影响。后面 $n - k$ 个元素的进出栈也是一个完整的子问题，规模为 $n - k$ ，方法数是 $f(n - k)$ 。

根据乘法原理， a_1 第 k 位出栈时，方法数为 $f(k - 1)f(n - k)$ 。由此 n 个元素的进出栈方法数是：

$$\begin{aligned} f(n) &= \sum_{k=1}^n f(k - 1)f(n - k) \\ f(0) &= 1 \end{aligned}$$

此公式就是卡特兰数 5 的递推公式。不像上节，这节分析没有错误。两个子问题的进出栈序列集合交集为空，符合合乘法原理。

不难发现，进出栈动态操作过程中，一旦栈为空，就得到一个规模更小的完整子问题。进出栈问题，可以分成很多小的子问题，这些子问题间互不影响。特别地，当出栈序列为 a_1, a_2, \dots, a_n 时，每一步出栈操作都定义了一个子问题，规模为 1，一共有 n 个子问题。任意 k, a_k 进栈再出栈时栈为空，构成一个进出栈子问题。

前面分析中，在给出 a_1 出栈得到两个子问题，刚好互逆，并集是进出栈序列的全集。对这两个子问题，我们还可以分成规模更小的子问题。这是从已知结果前提下，一个递归分解过程。

另外，在出栈序列里，若 a_1 所在位置为 k ，可以肯定 a_1 前的元素必须是 $a_i, i \in \{2, 3, \dots, k - 1\}$ 。同理， a_1 后的元素肯定是 $a_i, i \in \{k + 1, k + 2, \dots, n\}$ 。如果出现超出此范围的元素，则出栈序列非法。由此也可以快速排除一个非法的出栈序列。不过，这只是进出栈序列的一个必要非充分条件，不能用来找出正确出栈序列。

13.5.3 递归编程

进出栈问题里，栈的状态可以由两个参数表示，特入栈元素（栈外）个数 n 和栈内元素个数 k , n 和 k 组成一个有序队 (n, k) , 我们用符号 $f(n, k)$ 表示进出栈操作序列。下一步可以进栈 $f(n - 1, k + 1)$, 也可以是出栈 $f(n, k - 1)$. 显然 $k = 0$ 时不能出栈。

$f(n, 0)$ 表示初始状态, $f(0, 0)$ 表示操作结束。用此思路, 我们可以用递归函数 $f(n, k)$ 列出所有进出栈序列。

13.6 进出栈总结

1. 进出栈序列串, 任意前缀子串满足 $+1$ 个数不小于 -1 个数。
2. 出栈序列串, 任意 k , 下标比 k 小的并排 a_k 后的元素, 其下标降序。
3. 出栈序列串, a_1 出栈时, 左边是 a_i , $i \in \{1, 2, \dots, k - 1\}$ 子问题, 右边是 a_i , $i \in \{k + 1, k + 2, \dots, n\}$ 子问题。
4. 进出栈动态过程中, 每次栈为空时, 得到一个子问题, 所有子问题合并不是总问题。

Chapter 14

Regular Expression

To learn regular expression, read [Quickstart](<https://www.regular-expressions.info/quickstart.html>) first. Check the bit-by-bit authoritative tutorial for details. To test and check regular expressions, go to regex101.com.

Pay attention to the terms character class [] and capture group (). A character class match *one and only one* character. So a[1-9] does not match a single character a.

In regular expression, a dot matches any character except visual newline. A negated character class matches a newline instead like [^a-z]. To avoid that, use [^a-z\r\n].

Regex is not intended for or good at *inverse* search. But we can mimic this behavior by *lookaround* at Lookahead and Lookbehind Zero-Length Assertions. It is quite useful when we want to exclude something when matching.

For example, if the command is grep, use option -P to enable PCRE engine. The code below excludes entries of which the URI part does not contain *itunes-assets*.

```
cclog hpc access 201902141200 201902151200 | \
2 grep -P -m2 'http://aod\.itunes\.apple\.com/(?!itunes-assets).*headers
='
```

However, we can resort to -v to do the same work.

```
cclog hpc access 201902141200 201902151200 | \
2 grep -m2 'http://aod\.itunes\.apple\.com/.*headers=' \
grep -v 'itunes-assets'
```

So when to use *lookahead* and when to use *lookbehind*? From my experience, if you don't want to match something *immediately* following a *literal string*, then use *lookahead*. Similarly, if you don't want to match something immediately preceding a literal *literal string*, use *lookbehind*.

Like ^ and \$ (for start and end of *string*), \b is also an anchor for start and end of *word* like \bhello\b. It can be called as *boundary*. The counterpart \B matches at every position where \b cannot match.

To match a valid IPv4 address, use:

```
^(25[0-5]|2[0-4][0-9]|01)?[0-9]?)(.)  
{3}(25[0-5]|2[0-4][0-9]|01)?[0-9]?)$
```

When using regular expression, many commands (i.e. [sed](#)) use forward slash / as delimiters. In such cases, forward slash should be escaped. You can use another delimiter (i.e. #) to avoid escaping.

Most of the time, forward slash is not special and escaping is not required.

Recall in C language, a variable matches [A-Za-z_][A-Za-z_0-9]*.

Part V

Programming

Chapter 15

Bash

15.1 Contact

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Table 15.1: Contact

15.2 Stop List

- The NUL byte is an ASCII *control character* 0x00 (binary 00000000) resembling \t \b. It is a valid character occupying one byte in memory but not visible `printf` can produce them with \0 in the format spec. GNU/BSD `find` can terminate filenames with them (-print0). Bash's `read` can stop (delimit) on them with -d ''.
- Bash Manual
- Definitions
- shellcheck
- Expansion \$: variable, parameter, command, pathname, arithmetic, history, brace
- Substitution: process, command
- Bash Parser
- Quoting: escape character \, single quotes, double quotes, ANSI-C Quoting

- declare -p name
- Term *newline* refers to a *visual* and *electronical* new line, which is what is shown (a real new line) when Enter key is pressed.
- Apart from builtins and functions, other (external) commands (i.e. find; `awk`) are executed in a sub-shell. *pipeline* and process substitution also runs in a sub-shell. You see that, the shell script and commands within it run at different levels.
- A sub-shell is an *enhanced* sub-process, almost an identical copy of the parent shell process. They share the same variables, functions, `export`, and even `$$` equals to that of parent process. In other words, sub-shell inherits almost everything! From Bash 4.0 onward, the `BASHPID` is set the child process instead. However, variable assignments within sub-shell would not bring side effects to the parent process like `var=1; (var=2; echo $var) ; echo $var`. Read more at FAQ disappear.
- Use builtin `PWD` variable instead of `pwd` command.
- Command-line Tools can be 235x Faster than your Hadoop Cluster
- Command *option* and *argument* are slightly different. Options are usually specified with a hyphen and a single character (i.e. `grep -E`) that is defined by the command author. Arguments are generated by users like `printf "hello , world".`
- *filename* and *pathname* are used interchangeably.
- Some synonyms for globbing/glob (depending on the context in which it appears) are pattern matching, pattern expansion, filename expansion, wildcard and so on. Unquoted glob does filename expansion. Bash uses glob while `awk`, `sed`, and `grep` use regular expression. Specially, for `find`, strings passed to the `-name` option are used as glob.
- Regular expression; Extended regular expression. `!re !ere !bre`
- Pattern matching; Extended pattern matching `shopt -s extglob !pe`
- `echo "\n" ; printf "\n" ; printf '%s' '$'\n'.` A literal backslash followed by a literal n (\n) within a double or single quoted string preserve their literal character meaning instead of *newline*. To print as a newline, use `printf`. Whether \n is treated as a newline depends on the context. To insert a lietal newline, use ANSI-C Quoting `'$'foo\nbar'`.
- set vs. shopt.
- In Bash man page, check Lists for how Bash commands

15.3 Bash Parser

Bash Parser gives details on how Bash processes script files or command lines, which helps us understand the basic logic behind. Figure 15.1 is a simplified image illustration.

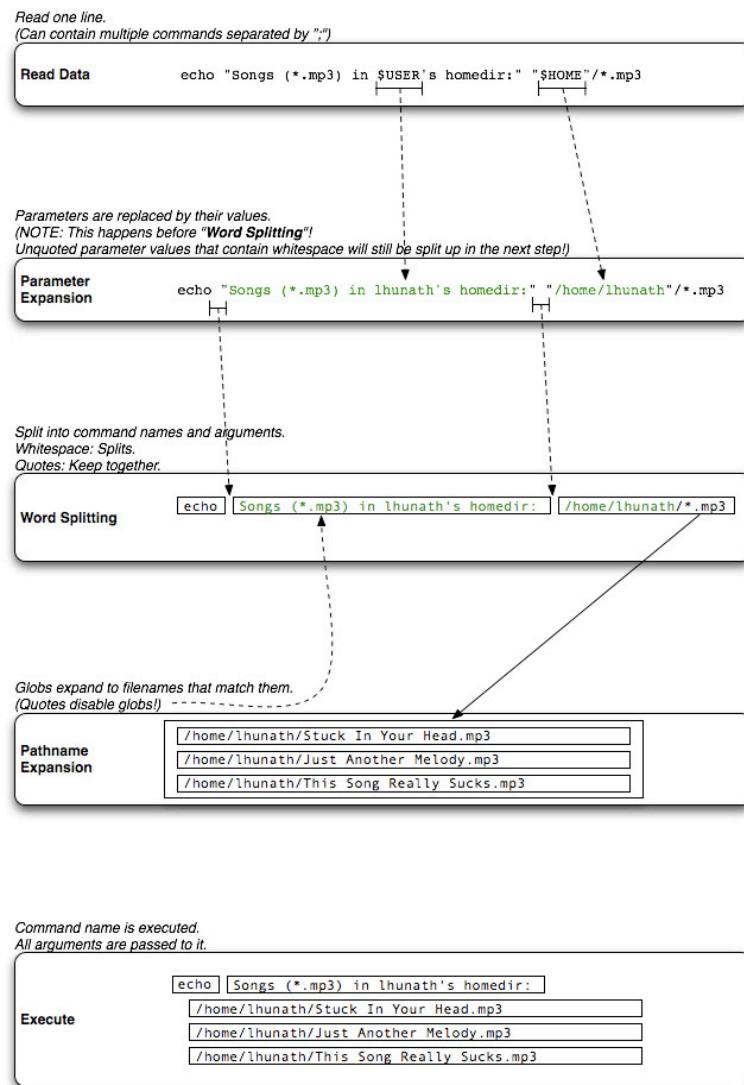


Figure 15.1: Bash Parser

Figure 15.2 is a better presentation. From which, we find *expansion* plays a critical role in the whole procedure.

Basically, the parser carries out the following procedures:

1. Read script source line by line. For each line,

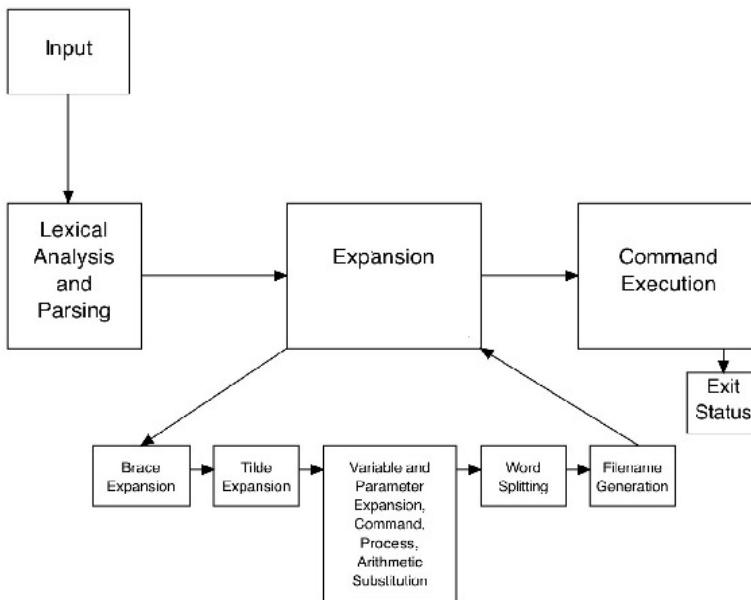


Figure 15.2: Bash Architecture

2. Process quotes.
3. Split a line into commands. For each command,
4. Process redirections and brace expansions.
5. Perform expansions, including parameter expansion, command/process/arithmetic substitution etc.
6. Word Splitting: split the command into command name and arguments list.
7. Execute the command.

15.4 Command History

Bash provides command-line tools for editing and manipulating command history. Check the [HISTORY EXPANSION](#) as per the man page. Advancing in the Bash shell is an excel tutorial.

One of the those is [history](#), listing previously executed Bash commands. [fc](#) is the counterpart for Sh shell.

There exist a list of internal variables related to history commands, like:

```
$HISTCMD $HISTFILESIZE !N !-N !! !$
```

Especially, !! is a synonym for !-1. !\$ expands to the last word of the preceding command. Usually, it will be the last argument.

Generally, we have Event Designator that select a command from history, Word Designator that select a *Bash word* from the selected command, and Modifiers are a sequence of modifiers to adjust the selected command. An event designator starts with the exclamation mark ! .

One of the most useful modifier is p that print but not execute the selected command.

15.5 Code Disassembling

I think it is a good practice to retrospect what have been learned recently, reviewing progress and summarize experience. Additionally, I'd like to make use of such chances to format the knowledge in my own wording. Such an *output* process testifies whether knowledge settles down and consolidates.

This section disassembles the missTime code line by line. Especially, I should explain *how* and *why*. The complete code is attached at A.4.

15.6 Quoting

Quoting is used to remove the special meaning of certain characters (i.e. whitespace for word splitting) or words to the shell. For example, it prevents reserved words from being recognized as such. It can also prevent parameter expansion.

There exist multiple quoting mechanism, namely:

- the escape character \
- single quote
- double quote
- ANSI-C quote

A non-quoted \ preserves the literal meaning of the next character, with the exception of newline. \newline is treated as a line continuation like

```

2 echo \
3   'hello, world'
4 echo 'hello,
world'
```

For quotes, there is no need to append the trailing backslash. The newline splits the string into two lines.

Single quotes preserve the literal meaning of each character within the quotes, except single quote (even preceding by a backslash which also preserves its literal meaning) like:

```
1 echo 'what\'s your name?'
```

The backslash does not serve as escape. This is an illegal Bash statement and it actually is parsed as three parts, namely <what\>, <s your name?> and the final apostrophe '. The second part is not quoted and the third single quote is unbalanced and Bash expects another single quote. The revised versions are legal but may not be our desired results.

```
2 echo 'what\'s your name?  
2 echo 'what\'s your name?'jim'
```

But if we `printf '\n'`, a newline is correctly printed. Why? That is because \n is literally passed to the command `printf`. It is the responsibility of `printf` to interpret \n as newline. For Bash, they are just a backslash \ and character n, not a newline.

Apparently, single quotes is kind of *strong* quoting method to preserve character meaning. But we can precede it by backslash \$ to preserve the escaping ability of \, where escaped characters are replaced by their ANSI-C Quoting. For example, `$'\t'` presents a horizontal tab and a single quote itself. Therefore, if we want to include a literal single quote within single quotes, we can precede the quotes with dollar \$.

Double quotes is somewhat relatively flexible. It preserves the literal meaning of all characters, except that of \$, ', \ etc. Within double quotes, \ can be used to escape \$, ", ', \ and newline. For example,

```
echo "  
    looooooooooooooooooooooo  
    \  
    ,line. \$"  
  
4 echo '  
    looooooooooooooooooooooo  
    \  
    ,line. \$'
```

A double-quoted string preceded by a dollar sign `$"string"` will cause the string to be translated according to the current *locale*. If the current locale is C or POSIX, the dollar sign is ignored. If the string is translated and replaced, the replacement is double-quoted. Attention, this is not parameter expansion, nor ANSI-C quoting.

15.7 printf and echo

```
printf 'Usage: ./missTime <number-of-test> <input-file>\n\n'
```

Use Bash's built-in or system's `printf` instead of `echo`. `printf` supports all C language format to allow flexible output. For instance, We can use it to assign variables by `-v` option:

```
printf -v var "hello, world\n"; declare -p var
```

To check Bash's `printf`, just run `help printf`. My Gentoo's system version is located at `/usr/bin/printf` that is part of GNU coreutils. In terminal emulator, `type -a printf` lists both versions. Unlike `echo`, `printf` does not append a *newline* by default.

For the full contention, check Why is `printf` better than `echo`? and echo protability considerations.

As the page writes, *never use options/arguments to echo* like `-e`. Also, do not use it to print *uncontrolled data* such as external input (filename, arguments etc. from user).

In summary, `printf` is far more reliable and safer. It litterally output as the format specifies.

A final note, to output sequential dashes like `---`, `printf` can do as follows:

```
2 printf -- '---\n'
2 printf '%s\n' "___"
2 printf '---\n' # error
```

For the principle behind, just read Bash manual, the OPTIONS section. Basically, everything after two consecutive dashes is treated as arguments (i.e. filenames). In other words, it signals the end of command options and disable further option processing.

Command `tee -a` writes to both standard output and files, which can be combined with `printf` like:

```
printf '%s\n' "hello, world" | tee -a file.txt
```

Single quotes are preferred in the format part unless you want parameter expansion there.

Let's have a look at another sample:

```
1 printf '%s\n' '1d' w | ed -s "$_full"
3 sed -i -e '1d' "$_full"
```

You will find there is only one format specification `%s` but two arguments '`1d`' and `w` (not quoted). In such case, the format specifiers are reused:

The format is re-used as necessary to consume all of the arguments.
If there are fewer arguments than the format requires, extra format specifications behave as if a zero value or null string, as appropriate, had been supplied.

15.8 Exit Codes and Boolean

```
1 [[ "$1" == @(-h|--help) ]] && exit 0
```

`exit` terminates the current shell *process* while `return` just terminates a *function* execution.

Both give numeric 0 for success execution and other specific codes for different error types. Here is a list of Bash Reserved Exit Codes.

The relation between Shell exit codes and boolean is as follows: *exit and return codes are just numeric integers*. They are not boolean values. To be logically consistent, we should correctly interpret the integer codes.

Bash treats 0 for true while others (1 included) for false. Numeric 1 is just one instance among the whole set of failure codes. It is not what we might think that false is bound to 1. Let's have a closer look at the procedure.

A sub-shell decides the status of execution. If a desired outcome is captured, it is logically true/successful. Otherwise, different failure outcomes are treated as false.

Upon successful execution, numeric 0 is returned back to the parent process. Actually, any number could be returned to represent successful execution, but as the link points out 0 is *platform and encoding independent*.

Now that numeric 0 is returned for success and other numerics for failure, the caller or the topmost Bash process should correctly interpret numeric codes to boolean true/false when `if`, `[[]]`, or `while` are involved.

Attention that, *true* and *false* are not reserved words in Bash. But we have commands `type -a true false`. Up to now, you may find, many commands has two versions: one from GNU coreutils and the other from Bash builtins.

To test if a command is successfully executed, just test the command:

```
if command ; then : ; fi
```

The next code also works, but it is *stupid*. It runs a new command `[[` to test another command's exit code.

```
# -or-
2 command; if [[ $? -eq 0 ]]; then : ; fi
```

Here, we find another command pair `type -a [.` `[[` is only available to Bash.

15.9 read

```
read -r _ _ _ _ip _ <(ip -4 -o addr show scope global dev bond0)
2 _ip="${_ip%/*}"
```

`read` is another Bash builtin that read a line from standard input and split it into fields based on IFS¹. Check details at Word Splitting. You are recommended to include the `-r` argument as it disables backslash escape.

`read` assigns the first splitted word to the first name, the second word to the second name and so on, with any leftover words assigned to the last name.

Why are there *underscores* before and after `_ip`? Mainly, they are just placeholders to skip unwanted splitted words, explained in the next section.

Thus, the first three underscres capture the three words ahead while the last underscore captures everything else, including the IFS characters and leaving the remaining part untouched.

¹The default Internal Field Separator is `<space>`, `<tabular>`, and `<newline>`, namely `$' \t\n'`.

Attention that, `read` uses IFS as *field* separator while use -d as *record* separator.

15.9.1 readonly

The builtin `readonly` command with the form

```
readonly [-aAf] [name[=value] ...]
```

2
`readonly -p`

marks each *name* as *readonly*. if a *value* is supplied, do assignment before marking as read-only.

15.10 Special Parameters

These parameters may *only be referenced*; assignment to them is not allowed. Let's see how they are expanded.

- `*: $*` expands to positional parameter. Without double quotes, each positional parameter expands to a separate word. Within double quotes, all positional parameters expand to a single word with the value of each positional parameter separated by the first character of variable IFS.
- `@: $@` is similar to `$*`, except that when in double quotes, each positional parameters also expand a separate word.
- `#: $#` expands to the number of positional parameters in decimal.
- `?: $?` expands to the exit status of the most recently executed *foreground* pipeline.
- `-: $-` expands to the current *option* flags as specified upon invocation, by the `set` builtin command, or those set by the shell itself (such as `bash -i`).
- `$: $$` expands the process ID of the *topmost* shell. In a sub-shell (i.e. (), it expands the process ID of the invoking shell (upper level) as it is *inherited*. In a sub-shell, use `BASHPID` instead, which expands to the process ID of *current* shell. `echo $$ $BASHPID; ls -l /proc/self; (echo $$ $BASHPID; ls -l /proc/self)`. Also check `/proc/self`.
- `!: $!` expands to the process ID the *job* most recently placed into the background.
- `0: $0` expands to the name of shell or shell script.

- `_`: `$_` expands to the last argument of previous simple command. Read the next section.

15.11 Underscore

Firstly, Bash regards *underscore* `_` as special parameter. Meanwhile, it is a standalone legal *name* (variable) and can be part of a variable as well. In short, it is the only parameter that is also a valid *variable name*.

```
echo 'hello, world'
2 declare -p _ ; declare -p _
```

As a special parameter, the value of underscore `_` is assigned *automatically* by Bash process as depicted in the next section, namely *expansion* 15.15. At the very beginning, it is set to the absolute *pathname* of the shell or script file. Subsequently, *expands* to the last argument of previous simple command.

Though it is a variable, we can **not** assign value to it explicitly. In other words, assignment to it is legal but in vain.

```
_="a"
2 declare -p _
```

That is the reason we use it as a placeholder for `read` command. Its value is *unstable* and got *overridden* immediately after each Bash command. Values assigned to it take no effects. We can verify this behavior by:

```
read -r _ var <<< 'hello, world'
2 declare -p _
# -or-
4 printf '%s\n' "$_"
```

The code outputs `declare -- _="var"` since the last argument of `read` is a name (`var` here).

Pay attention to the difference between `declare` (only the name is required) and `printf` (name should be expanded by `$`).

15.12 globstar

The special glob character * matches any string of any length, including the *null* string.

When the `shopt -s globstar` option is enabled, two adjacent two adjacent *'s used as a single pattern will match all files and zero or more directories and subdirectories. If followed by a /, two adjacent *'s will match only directories and subdirectories.

globstar is also called *recursive glob*.

15.13 extglob

Here are a few *extglob* samples. To turn on this Bash feature, just `shopt -s extglob` on a *newline*.

extglob changes the way certain characters are parsed. It is necessary to have a newline (**not** just a semicolon) between `shopt -s extglob` and any subsequent commands to use it. This is because the command line is parsed before `shopt` command is evaluated. Check the parser section before.

Likewise, you cannot put `shopt -s extglob` inside a statement block that uses extended globs, because the block as a whole must be parsed when it's defined; the `shopt` command won't take effect until the block is evaluated, at which point it's too late. In fact as Bash parses the entire statement block before evaluating any of it, you need to set *extglob* outside of the outermost block.

The first example below, does not turn on *extglob* correctly and report error.

```

1 shopt -u extglob
2 shopt -s extglob ; touch foo bar ; echo @($foo|$bar)
# -bash: syntax error near unexpected token `('
4
5 _ip=127.0.0.1 _std_array[6]="$https://www.baidu.com/a/b/c/d?v=k"
6 printf '%s\n' "${_std_array[6]}"
7 shopt -q extglob; _extglob_set=$?
8 (( _extglob_set )) && shopt -s extglob
9 _delete_url=${_reply_array[X-True-Cache-Key]##http?(s)://}
10 (( _extglob_set )) && shopt -u extglob
11
12 bash -c $'shopt -u extglob\nshopt -s extglob ;'
13 url="https://www.google.com/a/b/c" ;
14 _delete_url=${url##http?(s)://} ;
15 shopt -u extglob; printf "%s\n" "${_delete_url}"
16
17 shopt -u extglob
18 var='--help' ; [[ "$var" == @(-h|--help) ]] && echo 'yes'

```

The second case replaces the `::/host/` with `::/ip/`, which combines the features of *extglob* and *parameter expansion* in the form `$(parameter/pattern/string)`. In the pattern part, we should escape the backslash \while in the string part, leave as it is since this part is literally substituted.

The next two cases show both `$(parameter/pattern/string)` and `[[` use *extglob* internally even we turn it off.

But to be consistent and robust, we are still recommended to put it on separate lines. This rule applies to other shell options as well.

15.14 Process Substitution

Still the same code snippet at previous section, we have

```
< <(ip -4 -o addr show scope global dev bond0)
```

`>(list)` and `<(list)` are called Process Substitution *operators* that allow a process's input or output to be referred to using a filename, which the process get inputs from or output results to a file. Attention, a sub-shell is spawned when process substitution happens (there is a pair of parentheses there).

The keyword *list* here may be a normal command or a pipeline of commands. No space may appear between the `<`, `>` and the left parenthesis `(`, otherwise the form would be interpreted as a redirection.

The operators execute commands in *list* in a sub-shell and send the output to a file. The operator is then substituted with the pathname of that file. Process Substitution is supported on systems that support named pipes (FIFOs) or the /dev/fd/ method of naming opened files. We can just think of the two forms as just filenames, which is done by giving the list a name in the filesystem:

process substitution = filename

For the input form >(list), writing to the file will provide input for the enclosed *list* like:

```
# command ... >(list) ...
2
echo >(true)
4
cat file.txt > >(wc -l)
```

The first example displays filename of the command substitution. The second *redirects* the output of `cat` to the input filename.

If the output form <(list) is used, the file can be read to obtain the output of the *list* like:

```
# command ... <(list) ...
2
echo <(true) # print the output filename
4
cat <(list) # print the contents of the output filename
6
# compare the two output filenames
comm -3 <(sort a.txt | uniq) <(sort b.txt | uniq)
```

Back to the beginning code, the leftmost < is a normal I/O redirection, meaning read from the process substitution. Pay attention to the extra space between the two <, otherwise it would be a Here Document.

15.15 Parameter Expansion

```
1 _num_of_tests=${1:-10}
```

The purpose of this code is to assign value to `_num_of_tests` from either user input or the default 10.

The special \$ symbol of Bash introduces *parameter expansion*, *command substitution*, or *arithmetic expansion*. The terminology - *parameter* - is defined in the manul, please have a read. To put it simple, parameter is an entity that stores values, it can be a *name*, a *number*, or special parameters like * @ # _ etc., of the list, underscore is explained in a prior section.

name is what we usually call as *variable* or *function name*. Also referred to as an *identifier*.

The parameter symbol to be expanded may be enclosed in braces which are *optional* but *safer* as braces separate the variable from characters immediately following it.

The basic form is \${parameter}. Our case is \${parameter:-word} that means the expansion of *word* is substituted if *parameter* is null or unset, otherwise the value of *parameter* is substituted.

Here are three extra examples:

```

for f in full real; do declare "_$f"="${_log_time}-${_num_of_tests}-$f.
log"; done
2 for f in "${_full}" "${_real}"; do echo -n >| "$f"; done

```

This code uses `echo -n` to create an empty new file, which can also be accomplished by `touch` or `printf ''`

15.16 Brace Expansion

Brace expansion is used to generate arbitrary strings. It takes the following forms:

```

# {string1,string2,...,stringN}
2 {a,b,c,d}
# {<START>..<END>}
4 {1..10}
# {<START>..<END>..<INCR>} (Bash 4)
6 {1..10..2}
# <PREAMBLE>{....}
8 # {.....}<POSTSCRIPT>
# <PREAMBLE>{.....}<POSTSCRIPT>
10 a{b,c,d,.txt

```

Both the PREAMBLE and POSTSCRIPT parts are optional. The last example above can expand to `a.txt` for the trailing comma ,.

Within the braces, we can place either a series of comma-separated strings, or a *sequence expression*. There should be *no* space between the list elements. Results of expanded strings are not sorted; let to right order is preserved.

A sequence expression takes the form `{x..y[..incr]}`, where x and y (both inclusive) are either integers or single characters, and incr, an optional argument, is an integer. Both x and y must be of the same type.

Supplied integers may be prefixed with 0 to force each term to have the same width like `for i in {01..12}; do echo $i; done`.

It is different to globbing that matches filenames by default (unless used in parameter expansion).

This mechanism is similar to pathname expansion, but the filenames generated **need not exist**.

That means `{foo,bar}.txt` expands to `foo.txt` and `bar.txt`. Whether the two strings are used as filenames or not depends on how you use it.

```
for f in {foo,bar}.txt ; do echo "$f" ; ls "$f" ; done
```

But glob `*.txt` only expands to *existing* files. If no files are matched, it expands to the glob itself unless `nullglob` is enabled which makes it expand to *null string*.

```
2 bash -c $'shopt -u nullglob\nfor f in *.txt; do ls "$f"; done'  
bash -c $'shopt -s nullglob\nfor f in *.txt; do ls "$f"; done'
```

From section Bash Parser 15.3, we know brace expansion happens before all the rest expansions. Any characters special to other expansions are preserved in the result: *strictly textual*. So brace expansion makes

```
echo {a,b}$PATH
```

be

```
echo a$PATH b$PATH
```

before PATH is parameter-expanded.

Similarly, a brace expansion with range like `{1..200}` can not be expressed like:

```
2 a=1 b=200  
echo {$a..$b}
```

Actually such code does not satisfy a legal brace expansion requirement. Within the *unquoted braces pair*, there should be *at least* a comma or a sequence expression. The textual \$a and \$b (not parameter-expanded), the dots inbetween included, neither contains a comma nor are sequence expression. Hence, during the brace expansion phase, the code is ignored. When it comes to the parameter expansion, it becomes a single string {1..200}.

Brace construction is normally used when the common prefix or suffix of strings to be generated are much longer:

```

1 mkdir /usr/local/src/bash/{old,new,dist,bugs}
2 #
3 chown root /usr/{ucb/{ex,edit},lib/{ex?.?*,how_ex}}
4 #
5 echo {{A..Z},{a..z}}
6 #
7 echo {A..Z}{0..9}
```

You will find from the code, brace expansion can be nested. It also supports concatenation.

15.17 Parameter Transformation

```

1 printf 'curl -ksSI '
# 4.4
3 printf -- '-H %s ' "${_headers_array[@]@Q}"
printf -- '-H %s --resolve %s %s\n\n' "x-c3-debug:enabled" "${_
_resolve@Q}" "${_url@Q}"
5
# < 4.4
7 printf -- '-H %q ' "${_headers_array[@]}"
printf -- '-H %q --resolve %q %q\n\n' "x-c3-debug:enabled" "${_resolve}
" "${_url}"
```

Since Bash 4.4, parameter transformation is supported in the form \${parameter@operator}. Of the operators, Q expands the parameter as a string that is the value of parameter quoted in a format that can be reused as input like ar=(a 1 "b ; c") ; printf '%s\n' "\${ar[@]@Q}".

Before Bash 4.4, we can resort to printf '%q' which quotes the argument in a way that can be reused as shell input.

15.18 regex Test

```

1 _headers_regex=$'\^~\$headers=(.*)@\\|#\\(\'''
2 _headers_regex='^~$headers='''(.*)@\\|#\\('''
3 _https_regex='^https://'
[[ "${_int_log}" =~ $_regex ]] && printf '%s\n' "${BASH_REMATCH[1]}"

```

Bash support the extended regular expression by *conditional command* [[with binary operator =~.

If the pattern is properly matched, results is assigned to built-in variable BASH_REMATCH . It is an array variable with index 0 the portion of the string matching the entire regular expression (the complete match, **not** the whole string). The element with index *n* is the portion of the string matching the *n*th parenthesized sub-expression (capture group). If there are nested parenthesis level, the inner index is that of the outer level plus 1.

BASH_REMATCH is *read only*. We cannot change its value. Usually, just assign it to a temporary variable.

Pay attention the two methods to define the regular expression. The first one is preceded by a \$ within which \ ' is correctly interpreted. While the 2nd version, put the \ ' outside of single quotes 'foo-bar'.

15.19 Array

Bash provides one-dimentional *indexed* and *associative* array variables. The *declare* builtin can explicitly declare an array:

```

declare -a indexed_array # optional
2 declare -A associative_array=()

```

Indexed array can be any vairable, and hence a declaration is optional.

Any reference to a variable using a valid subscript is legal, and bash will create an array if necessary.

On the contrary, associative array *must* be declared before usage.

Indexed arrays are zero-based while associative array resembles Python *dictionary*, with key and value pairs stored. Pairs are not sorted.

When assigning elements to an array, please enfold the *subscript* with square brackets.

```

1 indexed_array[0]=12
2 indexed_array=( [1]='a' 'b' 'c' )
3 printf '%s\n' "${indexed_array[@]}"
4 #
5 declare -A associative_array=( ['addr']='usa' )
6 associative_array['name']='jim'
7 associative_array=( ['age']=30 )
8 for key in "${!associative_array[@]}"; do printf '%s: %s\n' "$key" \
9 "${associative_array[$key]}"; done

```

Array elements can be referenced by the form `${name[subscript]}`. The curly braces are required to avoid conflicts with filename expansion operators.

`${}`. Without curly braces parameter expansions refer to the *longest valid variable name* or *shortest positional parameter*. `${var}bar` expands the parameter named `var` while `${var}bar` expands `varbar`. `${123}` references `argv[1]` and `${123}` references `argv[123]`. Braces are required for positional parameters > 9, special PEs, and array expansions: `${10}`, `${var##pat}`, `${arr[5]}`. BRACES AREN'T A SUBSTITUTE FOR QUOTES!

If the *subscript* is omitted, `$name` implies a subscript of zero `0`, which suggests *name* is an indexed array or an associative array with a key of zero `0`.

```

1 unset ar; declare -A ar=( [0]=a ["hello"]=1 )
2 declare -p ar; printf '%s\n' "$ar"
[[ -v ar ]] && echo "yes"

```

To print array:

```

1 # indexed array
2 printf '%s\n' "${indexed_array[@]}"
3 # associative array
4 for key in "${!indexed_array[@]}"
5 do
6     printf '%s: %s\n' "$key" "${indexed_array[$key]}"
7 done

```

The code above uses special subscript `@` that expands to positional parameter. Another special subscript is `*`, when double quoted, expanding to a single word with each element separated by the first character of the IFS which by default is *space*. Hence:

1. For printing, use `@` instead of `*` unless explicitly required.

2. When setting custom IFS, pay attention to the character sequence.

Now, let's have a look at the following code:

```

1 declare -A _reply_array=()
2 while IFS=':' read -r key value
3 do
4     [[ -n "$key" && "$key" != [:space:] ] && "$key" != + ]] || continue
5     _reply_array[$key,$key]="$value%$'\r'"
6 done < "curl-reply.log"

```

Listing 15.1: curl CRLF

1. Associative array must be declared.
2. The first character of IFS is set to space.
3. -r argument of `read` is adopted.
4. `continue` starts the next loop instantly.
5. `key` is transferred to lower case by parameter expansion in the form \${parameter,,pattern}. `pattern` is omitted.
6. Remove trailing *carriage return* \r from `curl`.

The sixth item is really hostile to programmers. Basically, `curl` feeds back messages with CRLF instead of \n. We can check this by `sed -n l`. To reuse some returned headers, we should firstly remove the extra \r.

15.20 Command Substitution

Similar to Process Substitution 15.14 above, command substitution performs the expansion by executing the command within a sub-shell.

It allows the output of a command to substitute the command itself, with trailing newlines delete. We can just think of command substitution as a string and using the output of a command as an argument. No filenames are involved.

It takes the following two forms. The *backquote* form is deprecated and discouraged.

```

1 $(command)
2 `command` # deprecated

```

If the substitution appears within double quotes like "\$(command)", *word splitting* and *filename expansion* are not performed on the results, which is a *preferred* method.

Command substitution is useful when we want to assign a command output to a variable like `_date=$(date -Idate)"`.

The command substitution `$(cat file)` can be replaced by the equivalent but faster `$(< file)` (without sub-shell). The later one is a *special* case of command substitution. It does not invoke any command and Bash just substitutes it with the contents of file.

15.21 Assignment and Simple Command

```

2 IFS=$'\n' _log_array=( $( awk -F'[:space:]'@{in|out}#\\"[[[:space:]]*'\ \
3   '{ for (i = 1; i <= NF; ++i) print $i; }' << "${line}" ) )
# better
4 mapfile -t _log_array << awk -F'[:space:]'@{in|out}#\\"[[[:space:]]*'\ \
5   '{ for (i = 1; i <= NF; ++i) print $i; }' << "${line}" )
#
6 IFS=''; read -ra _headers_array << "${BASH_REMATCH[1]}"
7 _headers_array=( "${_headers_array[@]#//-H}" )
8

```

In the first assignment uses `awk` command substitution with output assigned to an indexed array directly. This substitution is not double-quoted, so word splitting and pathname expansion happens before assignment. The second assignment uses `awk` process substitution and mapfile 15.22.8 (explained in a standalone section), which is much *faster* and *safer* method.

Why, in this section, I want to talk about assignment and simple command? We can think of simple command as just a command name followed by its arguments. From Simple Command Expansion, we find:

If no command name results, the variable assignments affect the current shell environment. Otherwise, the variables are added to the environment of the executed command and do not affect the current shell environment. If any of the assignments attempts to assign a value to a readonly variable, an error occurs, and the command exits with a non-zero status.

The only command `awk` is executed in a sub-shell, The two assignments `IFS=$'\n'` `_log_array=` affect the current shell. That is to say, from here on, the new `IFS` value is changed for the whole Bash process. Instead, the `IFS` associated with the `read` statement only affects the `read` command itself.

Let's reformat the code like:

```

1 IFS=$'\n'
2 _log_array=( $( awk -F'[:space:]'@{in|out}#\\"[[[:space:]]*'\ \
3   '{ for (i = 1; i <= NF; ++i) print $i; }' << "${line}" ) )
4 IFS=$' \t\n'

```

It becomes more understandable and more clearer.

Extra notes :

Recall that indexed array can be declared by -a argument. `read` command supports reading into an indexed array by the same argument.

`"${_headers_array[@]#/‐H}"` is another example of parameter expansion in the form `${parameter/pattern/string}`. It inserts `-H` in front of each array element.

15.22 Commands

15.22.1 sed

`sed`, as described in the manual, is a stream editor for filtering and transforming text.

We can use it to delete empty lines:

```
2 sed -i.bak '/^[:space:]*$/d' file.txt
2 sed -i.bak '/[^[:space:]]/!d' file.txt
```

The `-i[SUFFIX]` or `--in-place[=SUFFIX]` option edits files in place (makes backup if SUFFIX supplied).

Form `/regexp/` matches lines against the regular expression. In the example above, `^[:space:]*$` matches empty lines. The trailing command `d` means to delete matched lines.

To support extended regular expressions, add option `sed -r` like: `sed -r 's/[[[:blank :]]+/\g' /proc/slabinf0`. Otherwise, the plus symbol should be escaped like: `sed 's/[[[:blank :]]\+\g' /proc/slabinf0`.

The variant version is somewhat not so obvious but usually faster if the file has less empty lines. Pay attention to the exclamation mark `!` before command `d`. This version means as long as a non-space character is matched, don't delete the line.

Another useful form is `s/regexp/replacement/` that matches file lines against the *regexp* and replaces the matched parts with *replacement*. We can use `=` in the *replacement* to represent the matched parts like `s/hello/=&/` means to enclose string *hello* with symbol `=`.

The snippet below replaces *google* with *bing* if the URL contains *foo*. Note that in the regular expression part, dot should be escaped while in the replacement part

not. A version with `awk` are also provided for reference. Please read more in `awk` section.

```

1 var=$'https://www.google.com/foo?v=xyz\nhttp://www.baidu.com/bar?v=uvw\
n'
2 printf '%s\n' "$var"
3 sed '/foo/s/www\.google\.com/www.bing.com/' <<< "$var"
4
5 var=$'https://www.google.com/foo?v=xyz\nhttp://www.duckduckgo.com/bar?v
=uvw\n'
6 printf '%s\n' "$var"
7 awk -F'/' 'BEGIN { ORS="/" } /foo/{ $3="www.bing.com" ; for ( i=1; i<
NF; i++ ) print $i }' <<< "$var"

```

In the meanwhile, special escapes \1 through \9 refers to the corresponding matched sub-expressions in the *regexp*. To enable this feature, we should add option `-E` or `-r`. For example, `-E s/(h.)l(.o)/\2/` will replace the word *hello* with *lo*.

To match a continuous lines block, we have:

```

1 sed -n '/addr1/,/addr2/p'
2 #
3 printf 'hello\nworld\nbash\nhello\nchina\n' | sed -n '/he/,/wo/p'

```

- the line which `addr1` matched will always be accepted, even if `addr2` selects an earlier line.
- If `addr2` is a *regexp*, it will not be tested against the line that `addr1` matched. In other words, if it is other forms (check man page, i.e. number), test is required.
- If `addr2` is not matched, all lines starting from `addr1` to the end of file are matched.

Similarly, `awk` has also such block address feature. Check the relevant section below.

Here is an sophisticated example:

```

~$ cat file
1 # Title: foobar
2 # Subject: Subject
3 # Body: Message body
4
5 # Title: foobaz
6 # Subject: Another Subject
7 # Body: Another message body
8
9
10 sed '/Title/,/Subject/s/fooo/test/' file

```

Finally, to differentiate the concepts of *pattern space* and *hold space* is important to master `sed -n '1!G;h;$p'`.

15.22.2 ed

`ed` is line-oriented text editor. `Sed` is a stream editor.

A stream editor is used to perform basic text transformations on an input stream (a file or input from a pipeline). While in some ways similar to an editor which permits *scripted edits* (such as `ed`), `sed` works by making **only one pass** over the input(s), and is consequently more efficient. It is `sed`'s ability to filter text in a pipeline which particularly distinguishes it from other types of editors.

Due to the *stream* and *one pass* features of `sed`, it cannot move back to earlier lines, where `ed` comes into usage.

```
ed -s "${_full}" <<< $"-3d\nw'
2 ed -s "${_full}" <<< $"-3d\n,n,p'
```

`$` refers to the last line and `$-3` means the last but 3rd line. Similar to `sed`, command `d` means to delete the matched line.

Command `w` means save the file. Usually `ed` allows only one command in a line except `p` etc. Consequently, we need `\n` to separate `d` and `w`. `sed` on the other hand, allows semicolon `;` to separate different commands.

15.22.3 awk

From the manual, `awk` is a pattern scanning and processing *language*. You see! It is a programming language, not just a command line tool.

There exist multiple `awk` implementations, of which `gawk` is, by default, deployed on all Linux distributions. This version is the standard implementation for Linux, while the original `awk` was written for Unix v7. The original `awk` authors then released a new version called `nawk` or `bawk` but rarely used. Another version is `mawk` that runs faster as it is based on a byte-code interpreter. On Linux systems, `awk` is a symbolic link to either `gawk` or `mawk`. To speed up `awk`, we can set `LC_ALL=C awk 'foobar'`.

The basic form is as:

```

1 gawk [ POSIX or GNU style options ] -f program-file [ -- ] file ...
2 gawk [ POSIX or GNU style options ] [ -- ] program-text file ...

```

`awk` reads source code either from a external file or from inline text.

We usually write *program-text* like *pattern { action statements }*. Action statements (enclosed in braces, { and }) will be performed on the matched lines. Either the *pattern* or *action statements* part may be missing, but *not both*. A missing action is equivalent to *{ print }*.

pattern can be but not limited to */regular expression/*. The surrounding forward-slash is required like `awk '/[a-z][1-9]/ {print $1}'`. If the forwardslash is omitted, `awk` will treat it as a variable which usually evaluates to null as it is probably undefined.

Another pattern is *Relational expression* with operators like + - * / % etc. It is usually used to test whether certain fields match certain regular expressions with ~ or !~ like `awk '$4 ~ /^https/ {print $4}'`. Also, surround the regular expression with forwardslash.

However, a literal string (i.e. `http://`) with quotes is acceptable like `awk '$4 ~ "^\https://\//\/" {print $4}'`. But we'd better use double backslash \ to escape special characters.

`awk` also has BEGIN and END patterns which are not tested against the input and can have their own action statements. Actions defined in the BEGIN are performed before any input read while those of END are performed when input is completely read.

We usually can change built-in variables in BEGIN part like FS RS OFS ORS, where F refers to *field* while R means *record*. Prefix O for *print output*.

```

1 awk 'BEGIN { print "Count \"hello\" " }
2 /hello/ { ++n }
3 END {print "\"hello\" appears in", n, "lines." }' file.txt
4
5 var=$'https://www.google.com/foo?v=xyz\nhttp://www.duckduckgo.com/bar?v
6 =uvwxyz'
7 awk 'BEGIN { FS=OFS="/" } $4~/^foo.*/ { $3="s3.bing.net" ; print }' <<<
8 "$var"

```

For more details, refer to the PATTERNS AND ACTIONS section of the manual.

Here is a real case:

```
awk 'BEGIN {IGNORECASE=1}; /[-_]cache:/ { print substr($0, 3) }'
```

`awk` accepts regular expression as FS like 15.26. Here is a real case:

```
1 gawk -F'\\^~\\$' '{ print $1 }' <<< '1^~$2'
2 mawk -F'\\^~\\$' '{ print $1 }' <<< '1^~$2'
4 awk 'BEGIN { FS="|" }; { print $2 }' <<< "abc|123"
```

Like `sed`, `awk` also accepts range pattern `pattern1, pattern2`. It matches all input records starting with a record that matches `pattern1`, and continuing until a record that matches `pattern2`, inclusive. It does not combine with any other sort of pattern expression.

```
1 awk '/pat1/,/pat2/'
2 #
3 printf 'hello world\nchina\n' | awk '/he/,/wo/'
4 printf 'hello world\nchina\n' | sed -n '/he/,/wo/p'
5 #
6 printf 'hello\nchina\n' | awk '/he/,/wo/'
```

If a record matches both patterns, then that single record is also regarded as a range, which is slightly different from `sed`.

Attention that, `awk` does not support *lookahead* or *lookahead* since it uses POSIX Extended Regular Expression (ERE).

Check What is NR==FNR in awk?. Generally, NR is the total number of records (lines) read so far. FNR is the line number (number of lines) in the current file. Hence, FNR == NR means `awk` is processing the first file as FNR is reset to 1 for each new file.

Here is an interesting code:

```
1 awk 'BEGIN { p = 0 }; tolower($0) ~ /keyword/ { p = !p ; next }; p'
      file.txt
2 awk 'tolower($0) ~ /keyword/ { p = !p ; next }; p' file.txt
```

It prints all lines after a line with 'keyword' (case-insensitive) until a second line with 'keyword'. If there is only one line with 'keyword', the it prints lines until the end of file.

By default, variables are initialized to "" or 0 if not initialized by the BEGIN pattern. Hence, the BEGIN { p = 0 } is optional. Variables defined by -v is better in that it accepts values from Shell like:

```
awk -v var="$SHELL" 'BEGIN { print var }'
```

Then I want to talk about how awk calls system commands:

- system(cmd-line)
- cmd-line | getline

system() may not be available on non-Posix systems. Remember to close the opened command line as it has a file descriptor associated.

```
1 awk 'BEGIN { cmd="ls /"; system(cmd); close(cmd) }'
      awk 'BEGIN { cmd="ls /"; while(cmd|getline) print; close(cmd) }'
```

grepawk

!grepawk writes:

```
Awk can do almost everything grep can do. Instead of doing grep 'foo' |
awk '{ statement }', try awk '/foo/{ statement }'
```

15.22.4 grep

grep print lines matching a regular expression pattern. It has has two extensions, namely egrep and fgrep. egrep is equivalent to grep -E, while fgrep is equivalent to grep -F.

egrep uses the *extended regular expression* engine. Check the [REGULAR EXPRESSIONS](#) section for details. Specially, grep -P uses PCRE engine (that of Perl) which supports *lookaround* as stated in a previous section.

egrep interprets pattern as an extended regular expression while fgrep interprets it as a list of fixed strings separated by newlines.

By default, it prints the matched lines. If we supply the -v option, not-matched lines are printed.

Another special option is -o that prints only the matched parts instead of the whole line.

Key Binding	Readline Function
C-h	DEL, Backspace
C-_ , C-x C-u , C-/	undo
C-l	clear the screen, clear
C-r	backward search
C-s	forward search

Table 15.2: Readline Key Bindings

15.22.5 readline

GNU Command Line Editing is provided by Readline Library allowing users to edit command lines as they are typed in. Both Emacs and Vi editing modes are available:

```
# enable
2 set -o emacs
set -o vi
# disable
4 set +o emacs
set +o vi
6
```

I am astonished that readline copies the key bindings from Emacs, though it supports that of Vi editor. Table 15.2 lists some common key bindings:

If the terminal happens to turn on Flow Control, then C-s will freeze your terminal. Use C-q to disable it.

15.22.6 xargs

Compare the following two commands, we find that the first line just prints `--help` while the second prints the help message of `cat` command.

```
echo '--help' | cat
2 # vs
echo '--help' | xargs cat
```

`xargs` builds and executes `command` from standard input. It mainly reads items from standard input, delimited by blanks and newlines, and pass the input to `command` as `arguments`.

Actually, the idea is to concatenate a few items together and build a new command to execute. It is sort of converting STDIN contents to the command's arguments,

not passing the contents to as input.

In the first example above, `cat` uses STDIN as the argument. And the contents of the argument is literal string `--help`. But in the second example, `cat` uses the contents of STDIN as its argument with the help from `xargs`. From this perspective, we find the necessity of `xargs` in spite of just *pipeline*.

`-d` option changes the default delimiters (blank and newline) like `echo '11@22@33' | xargs -d '@' echo`.

When building the new command, `xargs` may encounter filenames containing newlines or blanks which will break the results as the filename will be splitted.

This issue could be solved by passing `-0` option to `xargs`, replacing the default delimiters to *null character* `\000`.

Obviously, `-0` option is equivalent to `-d'\0'`. This option is usually combined with `find ... -print0 | xargs -0 ...`. Check the 235x *Faster* link in section 15.2 for example.

By default, `find` prints each found file followed by a new line. But `-print0` removes the newline:

```

1 find . -type f -name *.txt -print | sed -n l
2 # ./test.log$                                # ./sample.log$ 
3 find . -type f -name *.txt -print0 | sed -n l
4 # ./test.log\000./sample.log\000$
```

For safety, `xargs` supports interactive execution by `-p`, prompting the user about whether to run the built command.

Please further read `xargs` 命令详解, `xargs` 与管道的区别.

15.22.7 find

`find` is a powerful command, especially when followed `-exec` option. It usually takes the form:

```
find [-H] [-L] [-P] [-D debugopts] [-Olevel] [starting-point...] [
      expression]
```

`-H` `-L` `-P` control the treatment of symbolic links. The `-L` option follows symbolic links while `-H` does not follow symbolic links, except while processing the command line arguments.

The term *starting point* means a list of names of files or directories to be examined. By default it is the current directory, namely the single dot.

The *expression* part is complicated. It is a kind of query specification describing how we match files and what we do with the files that were matched. An expression is composed of a sequence of things:

<POSITIONAL OPTIONS> <GLOBAL OPTIONS> <TESTS> <ACTIONS> <OPERATORS>

Check the relevant sections in the manual, to find out what they are. Of the list, OPERATORS join together the other items within the expression. They include for example -o (meaning logical OR) and -a (meaning logical AND). Where an operator is missing, -a is assumed.

Here are a few examples of find:

```

1   find -L /path/to/search -type f \(
2     -iname "*filename*" -o -name '*.txt'
3     \)
4
5   find -L /path/to/search -type f -iname '*.apk' -printf "%f\n" -exec cp
6     -fv '{}' /path/to/copy \;
7
8   find APPs/ -maxdepth 1 -type f -iname '*.apk' -exec bash -c 'for file;
9     do file="${file##*/}"; mkdir -p ROM/system/preset_apps/"${file%.apk}"
10    }; cp APPs/"${file}" ROM/system/preset_apps/"${file%.apk}"; done'
11    bash '{}' +
12
13   find -P history/ -type f -name '*.HEIC' -exec bash -c 'for file; do mv
14     -v "$file" "${file%.*}.heic"; done' 'bash' {} +
15   find ROM/system/media/wallpaper/ -depth -type f ! -path '*/wallpaper_15
16     .png' -delete
17
18   find ROM/system/media/wallpaper/ -depth -type d -empty -delete
19
20
21   find -L . -type f -iname '*abc*' -exec bash -c 'mv "$0" "${0/abc/def}"'
22     '{}' \;
23   export _pkg_name
24
25   find -H -maxdepth 1 -type f \(
26     -name '*.jpg' -o -name '*.png' \) -exec
27     bash -c 'for img; do mv "$img" pics/"${_pkg_name}"; done' bash
28     '{}' +
29
30   find . -type f -name '*.jpg' -exec bash -c 'for f; do mv $f ${f//"$0"};
31     done' '$'\302\240' '{}'
32

```

1. -name and -iname uses glob after *word splitting*. It is recommended to quote the glob (explained below).
2. The surrounding parentheses force precedence of operators.
3. -type, -iname, and -name are all TESTS.
4. -printf and -exec are ACTIONS.

5. `-exec command ;` and `-exec command {} +` are different. The first form executes the *command* once for each file. The string special `{}` is replaced by the current file name being processed. Both `{}` and the semicolon `;` may be quoted (i.e. `'{}'`) or escaped (i.e. `\;`) depending on the SHELL. The symbol `{}` `+` appends each selected file name at the end and runs the *command* with all the files as arguments. The number of filenames is only limited by the system's maximum command line length. If the command exceeds this length, the command will be called multiple times. For example `-exec ls {} +`. After the `;` and `+`, other ACTIONS can be supplied.
6. `-maxdepth` and `-mindepth` are GLOBAL OPTIONS.
7. `-exec bash -c 'foo-bar' bash '{}'` `+`. The second literal string *bash* serves as the `$0` positional parameter to the Bash shell while `'{}'` `+` serves as others. Without the second *bash* string, the very first file name would be the zeroth positional parameter like `-exec bash -c 'mv \"$0\" \"${0/abc/def}\"' '{}'` `\;`. This code will replace the *abc* part of the zeroth positional parameter with *def*.

From Bash manual, command `for` takes the form:

```
for name [ [ in [ word ... ] ] ; ] do list ; done
```

If the *in word* part is omitted, *name* expands to the positional parameters.

The following two lines only differ whether a explicit `0` positional parameter is supplied. In the first case, `shift` makes `for` to skip the *bash* string. Otherwise, *bash* would be processed as file name.

```
1 -exec bash -c 'shift; for f; do foo-bar; done;' bash '{}' \;
2 -exec bash -c 'for f; do foo-bar; done;' '{}' \;
3 -exec bash -c 'shift; for f; do foo-bar; done;' '{}' \;
```

If `-type d TEST` is supplied, then probably the `0` positional parameter is the current directory, namely the single dot. Sometimes we don't want it to be processed within `for`. That is where the third case comes into usage. Alternatively, we can use the GLOBAL OPTION `-depth` which processes files within before the directory itself.

Hence, some of the examples above should be rectified!

Now let's have a look at code:

```
set -x
```

```

2 touch main.conf ; find . -type f -name main*
4 touch main.conf main1 ; find . -type f -name main*
6 touch main.conf main1 ; find . -type f -name 'main*'
8 set +x

```

Without quoting, `main*` expands to filenames before passed to `find`. The second `find` command becomes

```
find . -type f -name main.conf main1
```

That is an illegal command form. Hence the second example reports:

```
find: paths must precede expression: 'main1' find: possible un-
quoted pattern after predicate '-name'?
```

So, always quote the glob after `-name` option.

Another interesting point is how `find` calculate *access* and *modification* time. Take the option `$-mtime` for example, `find` firstly calculates *days* passed since modification:

$$(\text{current-time} - \text{modification-time})/86400$$

The decimal fraction is *rounded downwards* to the floor like C language division. In a more fine-grained unit like *minute*, so the real modification age is probably greater than that. When option `-mtime n` is used, files of which the *calculated modification age* is *equal to n* are matched. The real modification age of the matched files belongs to n to $n.\bar{9}$ days.

To strictly find out files whose calculated modification age is greater than but not equal to n days (*at least $n + 1$ days ago*), we use `-mtime +n`. On the contrary, `-mtime -n` requires the calculated age is less than but not equal to n (*at most $n - 1$ days*).

This rule also applies to other *timestamp* options like `-atime`, `-ctime` etc. These options are all measured in units of day, to get more accurate results, change to unit of *minute* like `-amin`, `-cmin`, `-mmin`.

`find` also supports comparing timestamp of two files with `-newer file`, `-newerXY` file where X and Y are one of a B c m t. For details, refer to the 'TESTS' section of the man page.

In addition to timestamp, we also have the `-size ± n[cwbkMG]`. Unlike the calculated timestamp, the decimal fraction part of file size is *rounded upwards* to the next unit. So, when the unit is `M`, a 1-byte file is rounded up to `1M`; if the unit is `k`, then a 1-byte file is rounded up to `1k`. Take `-size -1M` (less than `1M`) for example, the 1-byte file rounded to `1M` is not matched.

`-1k` and `-1M` only match files of size 0. To match a file size within $[0, 1M]$, use `-2M, -1025k; 1M` for $(0, 1M]$; `-1024k` for $[0, 1M)$. To avoid mistake introduced by different units, we can stick to the byte unit `c`.

Why file size is rounded up? By default, `-size` uses unit of *512-byte block*. If a file size is 513 bytes, then it would take 2 blocks.

In a nutshell, there exist two factors to consider when testing timestamp or size, namely:

- the real timestamp/size versus the calculated ones;
- option argument $[\pm]n$ denoting less than, equal to or greater than.

So to find a file modified at least 10 days ago and smaller than `1M`, use:

```
find . -type f -mtime +9 -size -1024k
```

15.22.8 mapfile

`mapfile` reads lines from the standard input into the indexed array variable `array`, or from file descriptor FD if the `-u` option is supplied. The built-in variable `MAPFILE` is the default array if no array argument is supplied. It has a built-in synonym `readarray`.

```
1 mapfile -t _log_array <<(
2   awk -F'[:space:]*'@($in|$out)#
3     '{ for (i = 1; i <= NF; ++i) print $i;
4       }' <<< "${line}" )
#
```

The `-t` option removes trailing newline from each line input. `-d` options can set a new delimiter than the default newline.

Please read section ?? to find out how `while` loop achieves the same goal.

15.22.9 time

Before opening this section. I want to talk about a bit on Command Grouping. Command grouping groups a list of commands to be executed as a unit. It takes two forms:

```
1 ( list )
2 { list; }
```

The parentheses executes commands of the *list* in a sub-shell environment. while curly braces executes them in current shell.

- Especially, the trailing semicolon is required.
- Curly braces are *reserved words* of Bash. So they must be separated from the *list* enclosed by by *blanks* or other shell metacharacters.
- Parentheses are *operators*, and are recognized as separate tokens even they are not separated from the *list*.

When commands are grouped, redirections may be applied to the entire command list. For example, the output of all the commands in the list may be redirected to a single stream. This is how we capture the *time* output.

```
1 { time curl -kLsSvo /dev/null "${_headers_array[@]}" \
    -H "x-c3-debug:enabled" --resolve "${_resolve}" "${_url}"
2>&1 | \
3     awk 'BEGIN {IGNORECASE=1}; /<[:space:]>.*[_-]cache:/ { print
        substr($0, 3) }' ; } 2>&1 | tee -a "${_full}"
5 set -x; { echo foo; } 2> file; set +x; echo "file: $(< file)"
```

This section describes how to capture the time used for a command (into a file).

Script `time cmd` prints the execution time of the *cmd* followed to *time's stderr*, not that of *cmd*. We should tell apart the *stdout* and *stderr* of *time* and *cmd*.

Basically, we group the script with either `{ }` (preferred) or `()` (sub-shell). Within the group, we capture output (*stdout* and *stderr*) of *cmd* while outside the group, we capture that of *time*.

The second case is `set -x`. Similar to `time`, I want to capture the command executed into file.

```
The progress meter exists to show a user that something actually is
happening. The different fields in the output have the following meaning:

% Total    % Received % Xferd  Average Speed          Time          Curr.
                                                Dload  Upload Total Current Left   Speed
0 151M     0 38608   0      0  9406      0 4:41:43 0:00:04 4:41:39 9287

From left-to-right:
%           - percentage completed of the whole transfer
Total       - total size of the whole expected transfer
%           - percentage completed of the download
Received    - currently downloaded amount of bytes
%           - percentage completed of the upload
Xferd      - currently uploaded amount of bytes
Average Speed
Dload      - the average transfer speed of the download
Average Speed
Upload     - the average transfer speed of the upload
Time Total - expected time to complete the operation
Time Current - time passed since the invoke
Time Left   - expected time left to completion
Curr.Speed - the average transfer speed the last 5 seconds (the first
              5 seconds of a transfer is based on less time of course.)

The -# option will display a totally different progress bar that doesn't
need much explanation!
```

Figure 15.3: Progress Meter of curl

15.22.10 curl

At the very first, I want to show the curl PROGRESS METER that shows down-loading status in figure 15.3.

To simplify the progress meter, curl supports `-#` or `--progress-bar` option.

Another useful option is `-D` that dump the respond headers to a file for later reference. Cookies from the respond headers could be read by a second curl invocation by option `-b`, `--cookie`. But pay attention to the [curl CRLF issue 15.1](#). If followed by a dash `-D-`, headers will be dumped to STDOUT.

curl POST PUT

To post data to a remote server, firstly, we specify the HTTP request method by `-X POST` or `--request POST`. The data to be posted should be specified by option `-d`, `--data`. curl will send the data to the HTTP server in the same way a browser does when a user has filled in an HTML form and press the submit button. For example:

```
curl -v -X POST --data 'name=jim' http://www.example.com/api/info
```

Data can be loaded from a file, which is done by `-d '@data.file'`. Attention that, the argument is single-quoted:

```

1 curl -v -X POST -d '@data.txt' http://223.202.75.26:32000/bm-app/apir
2   /9120/qryLocationInfoAndIp
3
4 # data.txt:
5 name=jim&age=23

```

If `-d '@-'` is used, then data is read from STDIN:

```

1 curl -v -X POST -d '@-' http://223.202.75.26:32000/bm-app/apir/9120/
2   qryLocationInfoAndIp
3 name=jim&age=23
4 ^D

```

There are two common data formats, namely “urlencoded” and “JSON”, taking the following two forms:

```

1 -H "Content-Type: application/x-www-form-urlencoded"
2
3 -H "Content-Type: application/json"

```

Other formats like XML are not unusual as well. By default, “urlencoded” is used as it is concise and neatly organized. So the “Content-Type” header can be omitted. Check this example:

```

1 curl -v -X POST -H "Content-Type: application/x-www-form-urlencoded" -d
2   'name=jim&age=23' http://223.202.75.26:32000/bm-app/apir/9120/
3   qryLocationInfoAndIp

```

For JSON data, it is recommended to load from external file:

```

1 curl -v -X POST -H "Content-Type: application/json" -d '@api.json' http
2   ://223.202.75.26:32000/bm-app/apir/9120/qryLocationInfoAndIp
3
4 curl -v -X POST -H "Content-Type: application/json" -d '{"name": "jim",
5   "age": 23}' http://223.202.75.26:32000/bm-app/apir/9120/
6   qryLocationInfoAndIp

```

If the `-d` option is supplied multiple times, `curl` will *url-encode* the data before sending out. `--data 'name=jim' --data 'age=23'` will be merged as `'name=jim&age=23'`. It is quite handy for form fields, though `curl` supports option `-F`, `--form`.

The `-d` option has multiple variants like `--data-raw`, `--data-urlencode`, `--data-binary` etc. `--data-urlencode` is useful when if the data contain spaces like:

```

curl -v -G "http://localhost:30001/data" --data-urlencode "msg=hello
world" --data-urlencode "msg2=hello world2"
2
# /data?msg=hello%20world&msg2=hello%20world2

```

Read more in man page and check curl.md.

15.22.11 wget

Use wget to download a remote directory with `-r`, `--recursive` option:

```

wget -r -l2 -np -R "index.html*,mp3" -nH --cut-dirs=1 http://example.
com/dir1/dir2/

```

- `-l`, `--level` specifies the maximum recursion depth. By default, it is 5. Value `inf` means *infinite* recursion.
- The `-np`, `-no-parent` option does not ever ascend to the parent directory when retrieving recursively.
- An *intex.html* is automatically generated, which can be disabled by option `-R`, `--reject` which rejects files by *suffix* or *filenames* if wildcard characters `*` `? []` are used. For example, `-R pdf` excludes PDF files while `temp*` excludes filenames with leading string `temp`.
- By default, invoking Wget with `-r http://fly.srk.fer.hr/` will create a local directory beginning with the host `fly.srk.fer.hr/`. Option `-nH`, `--no-host-directories` removes that.
-
- `--cut-dirs=number` ignores *number* directory prefixes.

In the example above, `-nH`, `--cut-dirs=1` creates a local directory `dir2/` without leading `fly.srk.fer.hr/dir1/` pathname. If we change *number* to 2, then all files are downloaded in current directory `< . >`

A similar option is `-m`, `--mirror` to mirror a site. It is equivalent to `-r -N -l inf --no-remove-listing`.

```

wget -m -np -nH --cut-dirs=0 -Epk -R "index.html*,mp3" -X "/video-dir/
sexy" [--restrict-file-names=nocontrol] http://192.168.0.105:8080/a
/

```

- `-E`, `--adjust-extension` appends suffix `.html` to `application/xhtml+xml` or `text/html` filenames if it does not end with `regex \.[Hh][Tt][Mm][Ll]?`.
- `-p`, `--page-requisites` downloads linked resources to display a given HTML.
- `-k`, `--convert-links` converts the links in the document to make them suitable for local offline viewing.
- `-X` is to reject unwanted directories, similar to `-R`, `--reject`. Please use the full pathname *relative* to the URL. `-X "/video-dir/sexy"` means to exclude `http://192.168.0.105:8080/a/video-dir/sexy`. The leading forwardslash is optional.
- `--restrict-file-names=nocontrol`. The term *restrict* means to allow only characters of filename valid and safe to your local operating system. Invalid filename characters (including those unprintable control characters) are *escaped*. Argument `unix` would escape forwardslash / and unprintable control characters. The argument `nocontrol` tells Wget *not* to escape control characters. It solves Chinese mojibak issue as parts of which fall into the range of control characters.

Re-downloading of the same pathname By default, downloading multiple copies of the same pathname would result in new copies ending with number suffixes like `pathname.1`, `pathname.2` etc., which is called clobbered. Option `-r` would overwrite the old copy with new one from server. Option `-nc`, `--no-clobber` just refuses to download any new copies and preserve the old copy. When option `-N`, `--timestamping` is used, whether or not to download a new copy depends on the local and remote timestamp and size of the file. Remember, do not specify `-no` and `-N` concurrently. Therefore, either `-r -nc` or `-r -N`.

To use proxy `wget` supports `-e` option like `wget -e https-proxy=127.0.0.1:8080`. Of course, the proxy setting could set put in `/etc/wgetrc` or `~/.wgetrc` like:

```
use_proxy=on
2
http-proxy=127.0.0.1:8080
4
https-proxy=127.0.0.1:8080
ftp-proxy=127.0.0.1:8080
```

To turn off all proxies, set `use_proxy` as *off*.

15.22.12 rsync

We can use `rsync` to synchronize files between a source and a destination. Specially, if one end is a remote host, `rsync` can transfer data over *remote shell* (default to `ssh`) or *rsync daemon* (directly over TCP).

If the host is followed by one single colon, `ssh` connection is used. The option `-e`, `--rsh=COMMAND` specifies the remote shell to use. If it is two colons (i.e. `foo::`) or `rsync://`, *rsync daemon* is used.

```

# -e "ssh" is optional
2 rsync -avzP -e "ssh" ~/workspace/src/ dev:~/dev/
# customize SSH port
4 rsync -avzP -e "ssh -p 2222" ~/workspace/src/ dev:~/dev/

6 # -n, --dry-run
rsync -n -avzP ~/workspace/src/ dev:~/dev/
8
# --delete to mirror the source and dest
10 rsync -avzP --delete ~/workspace/src/ dev:~/dev/

```

We cannot emphasize too much the paramount importance of trailing forwardslash `/`:

- If `/` is placed at the end of the source folder, `rsync` will copy the contents of the folder.
- If the source folder is not followed by `/`, `rsync` will copy both the folder and contents therein.
- If `/` is placed at the end of the target folder, `rsync` will paste the data directly inside that folder.
- If the target folder is not followed by `/`, `rsync` will create the target folder and then paste the data inside.

15.22.13 tr

Command `tr` translates, squeezes, and/or deletes characters from standard input, writing to standard output. It takes form as:

<code>tr [OPTION]... SET1 [SET2]</code>

SET1 and/or SET2 define ordered sets of characters like `[:alpha:]` and `c-g` (without brackets). The format of the SET1 and SET2 arguments resembles the format

of regular expressions 14; however, they are not regular expressions, only lists of characters.

The `-c -C --complement` option replaces SET1 with its complement (all of the characters that are not in SET1). Currently `tr` fully supports only single-byte characters. So characters like Unicode Chinese are not supported.

translate means to substitute each character of its input that is in SET1 to the *corresponding* character in SET2 (required). Therefore, we usually want the lengths of both sets are equal.

To replace comma with newline `tr ',' '\n' < file`. It is quite handy though we can do that with [sed](#) or [awk](#).

A common use of `tr` is to convert lowercase characters to uppercase.

```

1 tr abcdefghijklmnopqrstuvwxyz ABCDEFGHIJKLMNOPQRSTUVWXYZ
2 tr a-z A-Z # discouraged method
4 tr '[[:lower:]]' '[[:upper:]]'
```

The bare range `a-z` and `A-Z` are discouraged as it is not portable and depends on implementation.

Option `-d` deletes characters in SET1 and do **not** *translate*. For example `tr -d '\0'` removes all zero bytes.

`-s` can be treated as a special case of `-d`, which *squeezes* repeated occurrence. For example, `tr -s '\n'` merge multiple blank lines to a single one.

Let's have a look at:

```

1 tr -d -axM # fail
2 tr -d -- -axM
4 tr -d axM-
tr -d '[=-=]axM'
```

The code want to delete four characters in which hyphen is included. In the first case, `-a` will be treated as command-line option. The last method uses *equivalence class*. For details, check the `info tr` page.

15.22.14 dig

The `+trace` option traverses the resolution system in a *iterative* resolution method. At the very first, local name server (i.e. `/etc/resolv.conf`) is used to obtain a list of

root domain name server unless `@name-server` is specified. For example:

```
# dig +trace www.bing.com. @1.2.4.8
```

15.23 Math

Arithmetic in Bash is *integer* math only. To do floating point math, resort to *bc* command.

We call a *math form* as *math context*. The basic math form is `$()` with the complete syntax at arith expr, which is called Arithmetic Expansion. Basically, within a math context, we use the same syntax as C language like.

```
# POSIX sh
2 i=$((j + 3))
3 lvcreate -L "$((24 * 1024))" -n lv99 vg99
4 q=$((29 / 6)) r=$((29 % 6))
5 if test "$((a%4))" = 0; then ...
6 echo "$((2**3))"
```

Within a math context, pay attention to the concept of the *evaluation value* of each *arithmetic expression* and the value returned to the Bash environment by the context itself (name it context value?).

- All C arithmetic operators are supported, including `?:`. Bash brings in *exponentiation* operator `**`.
- Within a single math context, multiple expressions can be separated by *comma*. Value of the last expression becomes that of the math context.
- Variable *name* in a math context are substituted with their values (unset or empty variables are evaluated as 0). There is no need to use parameter expansion (i.e. `${i}`) within math context.
- Numbers without leading 0 are treated as base 10. Numbers with a leading 0x are treated as base 16. Numbers with a leading 0 (not followed by x) are treated as base 8.

15.23.1 Arithmetic Command

Besides, Bash offers two extra forms of math context by *commands* for which, the math context *also* gets an exit status, and side effects. Similar to arithmetic expres-

sion \$(), the context value of an arithmetic command is that of the command exit code.

Exit code of arithmetic command depends on but not equal to evaluation value of the last expression. If the expression evaluates to 0 and the command is considered a failure. To be logically consistent with Bash, the command returns 1 . Otherwise, the command is regarded successful and return 0.

Consequently,

- Evaluation and boolean logic (0 false, non-zero true) of math expressions are in accord with C syntax.
- Exit code and boolean logic (0 true, non-zero false) of math commands are in accord with Bash.
- Return either 0 or 1. Nothing else. This is different to the Arithmetic Expansion above. So we can the Arithmetic Command as a `test` with `for` or `while`.
- Please go back and read Exit Codes and Boolean 15.8.
- Whatever numeric values are involved, boolean logic must be guaranteed. This is the rule that we follow when scripting. Forget about the details then. Check Arithmetic expressions and return codes.

The first arithmetic command is `let`:

```

1 let a=17+23
2 echo "a = $a"          # Prints a = 40
#
4 let a=17 a+=23 a=0    # the last expression evaluates to 0
5 echo $?                # 1 (false)
#
6 let a[1]=1+1           # Wrong (if a1=1+1 exists or shopt -s failglob)
7 ( shopt -s failglob; let a[1]=1+1 )
8 touch a1=1+1; let a[1]=1+1; declare -p a
10 let 'a[1]=1+1'        # right

```

Note that each arithmetic expression has to be passed as a single argument to the `let` command, so you need quotes if there are spaces or globbing characters.

`let a[1]=1+1` is not right as [] are glob characters, which matches one and only one of the enclosed characters like regular expression.

Bash expands globs which appear *unquoted* in commands, by matching *filenames* relative to the current directory. The expansion of the glob results in 1 or more words (0 or more, if certain options are set), and those words (filenames) are used in the command.

So Bash tries to expand `a[1]=1+1` as filename `a1=1+1` before `let` is executed. If that file exists or `failglob` is turned on, Bash reports:

```
bash: no match: a[1]=1+1
```

Now let's move on to the next arithmetic command `(())`. It resembles Arithmetic Expansion but removes the leading dollar \$ sign. It is identical to `let` but does not require quotes since expressions inside are delimited by Bash metacharacters (and).

```

1 ((a=$a+7))      # Add 7 to a
2 ((a = a + 7))   # Add 7 to a. Identical to the previous command.
3 ((a += 7))       # Add 7 to a. Identical to the previous command.
4
5 ((a = RANDOM % 10 + 1))    # Choose a random number from 1 to 10.
6 echo $?           # % is modulus, as in C.
7
8 echo "$(( a = RANDOM % 10 + 1 ))" # becomes Arithmetic Expansion

```

Specially, we can compare integers with `(())`. `>` or `<` inside `(())` means greater/less than, not output/input redirection involved. Recall that I have talked about expression evaluation and context exit code above. Integer comparision expression also follows the same rules.

The only difference is that arithmetic expression within the command is logic operation: only evaluates to 1 or 0. If the comparison is true (command executes successfully), the expression evalutes to 1 and returns 0. If it is false, the expression evaluates to 0 and returns 1.

`(())` is used more widely than `let`, because it fits so well into an `if` or `while` command like

```
if (( $# > 2 )) ; then printf 'there are more than 2 arguments\n'; fi
```

15.23.2 bc calculator

To do floating point calculation, we use `bc`. However, by default, it truncates according to the `scale` argument instead of rounding.

We increase `scale` and pass the result to xargs `printf` like:

```

1 bc <<< 'scale=3; 7/242.906' # 0.028
2 bc <<< 'scale=2; 7/242.906' # 0.02
3
4 bc <<< 'scale=3; 7/242.906' | xargs printf "%2f\n" # 0.03

```

Another possible workaround is to use ± 0.5 trick with the final result like:

```

2   rounding()
3   {
4       if (( $(bc <<< "$1 < 0") )) ; then offset=-0.5 ; else offset=0.5;
5       fi
6       printf "%.$2f\n" "$( bc -l <<< 'scale=$2; (((10^$2)*$1)+$offset)
7           /(10^$2)' )"
8       printf '%.*f\n' "$2" "$( bc -l <<< 'scale=$2; (((10^$2)*$1)+$offset
9           /(10^$2)' )"
10  }

```

Within the rounding function, we should set the offset according to the sign of the number. If the number is negative, we choose to round it toward the left side of number line. Or we can say to round toward its absolute value. Of course, if we want to always round toward the right side, then just use 0.5 .

About `printf '%.*f\n' "$2"`, the asterisk means the width is given as argument before the string or number is printed.

15.24 Redirection

Redirection takes the form as `lhs op rhs`, which can *open*, *duplicate*, *move* or we want to *close* file descriptors.

- *lhs* is always a file descriptor, namely an integer like 0 , 1 , 2 , or 3 . If the *op* is $<$ then there is an *implicit 0* as $0<$. If it's $>$ or $>>$, there is an *implicit 1* as $1>$ or $1>>$.
- *op* is $<$, $>$, $>>$, $>|$, or $<>$. Two special redirections $<<$ (here document) and $<<<$ (here string) usually require string(s) for *rhs*. Details, read the official manual.
- *rhs* is the thing that the file descriptor will describe. It can be a filename, or the place where another descriptor goes (prefixed with $\&$ like $\&1$), or $\&-$ that will close the *lhs* file descriptor.

When redirection is used, the *lhs* is pointed to what *rhs* is **currently** pointed to. If, later on, *rhs* is pointed to another place, *lhs* remains and won't follow *rhs*'s update. We can think of a file descriptor as C language pointer.

To check which place file descriptors are currently pointed, we can:

```

1 ll /proc/$$/fd/
2
3 # total 0
4 # dr-x----- 2 outsinre outsinre 0 Feb 14 15:49 .
5 # dr-xr-xr-x 9 outsinre outsinre 0 Feb 14 15:49 ..
6 # lrwx----- 1 outsinre outsinre 64 Feb 14 15:49 0 -> /dev/pts/2
7 # lrwx----- 1 outsinre outsinre 64 Feb 14 15:49 1 -> /dev/pts/2
8 # lrwx----- 1 outsinre outsinre 64 Feb 14 15:49 2 -> /dev/pts/2
9 # lrwx----- 1 outsinre outsinre 64 Feb 14 21:10 255 -> /dev/pts/2
10
11 for fd in 0 1 2 255; do cat /proc/$$/fdinfo/$fd; echo; done

```

In the following code, *cmd* reads input from filename *myFile*. File described 3 is associated with 1 (standard output, */dev/pts/2*). But the script does not make use of the new descriptor. 2 (standard error, */dev/pts/2*) is redirected to */dev/null*. Standard output (implicit 1, */dev/pts/2*) is redirected to 2, which is now pointed to */dev/null*.

```

# Good! This is clearly a simple command with two arguments and 4
# redirections
2 cmd arg1 arg2 <myFile 3<&1 2>/dev/null >&2

```

There are two special redirection forms *fd1>&fd2* and *fd1<&fd2*. As mentioned earlier, if *fd1* is omitted, the default value are 1 and 0 respectively.

They are called *descriptor copy* or *descriptor duplication*. Technically speaking, the two forms **make no difference**. Yeah, they are equal in Bash grammar except the different implcity *lhs*.

fd1 is opened (created) if it does not exist, and pointed to where *fd2* is currently pointed. Whether *fd1* is opened for reading or writing, depends on *fd2*. If the file *fd2* linked with is on read mode, then we can use *fd1* for reading. Similarly, we can write to *fd1* when *fd2* points to a file on write mode. Obviously, if the file is on read/write mode, *fd1* can be used to read from and write to that file.

In a script, we can do like this:

```

exec m>&n
2 exec m<&n
# -or-
4 cmd arg1 arg2 m>&n
cmd arg1 arg2 m<&n

```

It is necessary to tell apart *>*, *<* and *>&*, *<&* as the *&* requires an integer descriptor followed while the former needs a filename. More importantly, *>*, *<* cares about the

read and write mode. `>` opens a file descriptor for writing (redirecting output). The other one for reading (redirecting input). Apparently, `>>` is for appending redirected output.

To open a file descriptor for both reading and writing, we can:

```
1 [n]<>word
3 exec 3</>/path/to/filename
```

If *n* is omitted, it defaults to 0. If the filename of *word* expansion does not exist, it is created.

Sometimes, we need to store the integer value in a variable. Then enclose it with braces:

Each redirection that may be preceded by a file descriptor number may instead be preceded by a word of the form `{varname}`. In this case, for each redirection operator except `>&-` and `<&-`, the shell will allocate a file descriptor greater than or equal to 10 and assign it to *varname*. If `>&-` or `<&-` is preceded by `{varname}`, the value of *varname* defines the file descriptor to close.

```
1 fd=0; echo "hello, world" >> /tmp/foo; exec {fd}</tmp/foo;
2 printf '%d\n' $fd
3 read -r -u "$fd" line; printf '%s\n' "$line"
```

We can also *move* a file descriptor, which first duplicate the *rhs* and then close it.

```
1 [n]<&digit-
2 [n]<&digit-
3 m<&n-; m>&n-
4 <&4-; 0<&4-
5 >&4-; 1>&4-
```

Read more at [Switch stdout and stderr, What does 3>&1 1>&2 2>&3 do in a script](#) and [Closing a file descriptor, >& vs. <&-](#).

15.25 Set or Not

It happens when we want to test whether a *name* is set or not. Just use:

```
1 [[ "${array[key]}+abc" ]] && echo "exists"
```

This code applies to both indexed and associative array. "\${array[key]}+abc" is actually a special form of parameter expansion with the colon omitted. The original form is \${parameter:+word}. From the manual, we find:

if the colon is omitted, the operator tests only for existence [of parameter]

- if array[key] is set, return abc.
- if array[key] is not set, return nothing

However, we still can add the colon but the substitution procedure is carried out, though that does not affect the logic.

```
1 # degrade performance
2 [[ "${array[key]}:+abc" ]] && echo "exists"
```

Another method is to use built-in *test* option -v VAR:

-v VAR True if the shell variable VAR is set.

When to check for existence in this method, do **not** use parameter expansion. The name itself is enough.

```
1 [[ -v ar["hello"] ]] && echo "exists"
2 declare a=1; [[ -v a ]] && echo "exists" || echo "no"
3
4 declare -A ar=( [0]=1 ['b c']=2 ); [[ -v ar ]] && echo "yes"
5 declare -A ar=( [a]=1 ['b c']=2 ); [[ -v ar[@] ]] && echo "yes"
```

The first two lines test whether a name set.

The third tests the key of 0. In the 4th case, the bare a[@] (without \$ prefixed) is **not** a parameter expansion and hence it does **not** expand to postional index. This code tests for any array element. If there exists at least one element set, then exits true.

A different version is:

```
1 # test var
2 _regex="^declare -[aA] ${var}[=|$]"
3 [[ "$(declare -p $ar)" =~ "${_regex}" ]] && echo "yes"
```

Here is a function to test whether a specific value is stored in array. It is mainly for index arrays. If it is an associative array, just use the corresponding key to test.

```
1 #!inarray
# Usage: inarray "$value" "${array[@]}"
3 inarray() { local n=$1 h; shift; for h; do [[ $n = "$h" ]] && return;
done; return 1; }
```

15.26 String as Delimiter

To split string with just a single delimiter, we just need `read` command and IFS variable.

In the section 15.22.3, `mapfile`, `awk`, and *process substitution* are used to split a string with another string. I will introduce Split strings with group delimiters in this section.

```
2 _headers_sep='@|#(|'
2 _headers_regex=$'\\^\\~\\$headers=(.*))@\\|#\\(\\'' #''
4 tmp_headers="${BASH_REMATCH[1]}${_headers_sep}" _headers_array=()
while [[ -n $tmp_headers ]]
do
    _headers_array+=(" ${tmp_headers%%${_headers_sep}*}" )
    tmp_headers="${tmp_headers##${_headers_sep}}"
done; unset tmp_headers
```

We define the string delimiter as `_headers_sep`. When doing the parameter expansion, there is no need to escape those characters as `_headers_regex` does.

15.27 signal(7)

POSIX signals are classified into *reliable signals* and *real-time signals*. Reliable signal, hereinafter, is called *standard signal*.

Each signal has a default *disposition* that determines the `action` to perform when the process is delivered the signal. For instance, Action `Term` terminates a process and action `IGN` ignores the process etc. However, a process can change the default by `sigaction(2)` or `signal(2)`. The signal disposition is a *per-process* attribute: in a multithreaded application, the disposition of a particular signal is *the same* for all threads.

Some system calls or library functions allow the caller to *send* a signal like `kill(2)` and `raise(3)`; other system calls and library functions suspend execution of the calling process or thread until a signal is caught (*receive* a signal) like `pause(2)` and `sigsuspend(2)`.

A signal takes the form of an upper case string (i.e. `SIGTERM`) or an integer (i.e. `15`). The fixed prefix `SIG` can be removed (i.e. `TERM`). Standard signals like `SIGHUP` 1, `SIGINT` 2, `SIGKILL` 9, `SIGTERM` 15 and `SIGSTOP` 19 are often used when doing system operation.

`SIGHUP` tells a process to reload configuration files. `SIGINT` sends a terminal interrupt signal by `Ctrl-C` to terminate a process. Similarly, `Ctrl-Z` suspends execution. `SIGTERM` also terminates a process but it can be caught (and interpreted) or ignored, allowing a graceful termination by releasing resources and saving states. `SIGTERM` is almost identical to `SIGINT`, `Ctrl-C`. `SIGKILL` terminates a process immediately (`kill`) in a brute force way. It cannot be caught or ignored, and the receiving process cannot perform any clean-up upon receiving the signal: the *last resort* to terminate a process. The `SIGSTOP` tells the operating system to *stop* a process for later resumption by `SIGCONT`.

Linux provides the `kill(1)` command line (the user interface of `kill(2)` system call) to send a signal to a process. `kill [-l | -L]` lists available signals. Without specifying the signal, `SIGTERM` is sent. The following three lines are equivalent:

```

2  kill [-s | --signal] <signal> <pid1> <pid2> [...]
3  kill -15 12345
4  kill -SIGTERM 12345
5  kill -TERM 12345

```

Recall that, the 3rd column of `ps -ef` command prints the parent process ID (PPID or GPID). To send a signal to the process group, prefix the GPID with a *minus* symbol. A GPID of `-1` is special as it indicates all processes except the kill process itself and `init`.

Chapter 16

C Language

16.1 申明和定义

1. `extern` 申明 `declare` 一个变量，只说明存在某个数据类型的变量符号存在（插入到符号表里），而不分配空间。一般来说，在一个文件定义，在另一个要访问该变量的文件里申明（如头文件）。
2. 没有 `extern` 关键字时，一般就是变量定义。变量定义隐含了申明。定义时要分配内存空间。
3. 函数的声明不需要给出 `extern` 关键字。

16.2 作用域和生存周期

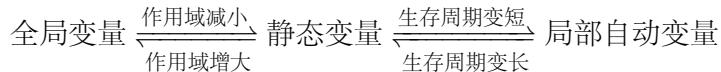
变量的属性有作用域和生存周期（storage duration）之分。从作用域来说有全局变量和局部变量。从生存周期来说有自动变量（automatic variable）和静态变量（static）。

全局变量在花括号外定义的，默认从定义处开始，到文件结束可见。要想真正实现“全局”的作用域，得在引用前申明变量（函数同理）。局部变量在花括号内部定义，只在花括号内可以被访问，也即局部作用域。花括号可以包裹函数体，也可以是包裹一小段块代码。同名局部变量覆盖 `override` 全局变量，此时要访问全局变量应用花括号和 `extern` 关键字。

生存周期和作用域紧密相联。自动变量是指进入作用域时分配内存，而离开时释放内存，变量被销毁。静态变量在进程运行期间一直存在，不受作用域影响。注意静态变量可以在花括号内（代码块或函数）定义！

自动变量和局部变量是同一个概念，只是强调的属性不同罢了，可以称为“局部自动变量”。

静态变量其实是全局变量的缩小版，作用域缩小，不能被 `extern` 申明引用，所以静态变量在花括号外或文件之外是不可见的。静态变量只在所定义花括号内（局部作用域）或花括号外所定义处至当前文件结尾（文件作用域）范围内有效。同时，静态变量又可以看成是局部自动变量的升级版，主要是生存周期变长，作用域（文件作用域）可能增大。静态变量是非常特殊的可以按作用域分成局部静态变量和文件静态变量。



下面总结几个要点：

1. 鉴于作用域的重要性，我们一般先定义变量、函数，再引用。否则要先申明，才能引用。
2. 全局、静态变量没有显式初始化时，程序会默认初使化为 0. 初始话（显式或隐式）只会进行一次，即使定义语句多次被进程触及。
3. 局部自动变量没有显式初始化时，初始值不确定，依赖编译器，因为 C 语言对此没有规定。局部自动变量定义时应初使化。
4. 提倡定义全局常量，尽量避免定义全局变量。如果实在需要，用 `static` 静态变量减小作用域。
5. `extern` 申明、引用其它文件的全局变量。最好放在头文件里。
6. C++ 对所有变量、对象全部要初始化！

16.3 编译内存布局

C 语言编译后虚拟内存分很多区域。我们这里说的是虚拟内存，假设机器上只有一个程序在运行，占有全部内存。实际中程序执行时所用的内存由操作系统分配在物理内存上：虚拟内存到物理内存的映射！

图 16.1 给出了虚拟内存的安排，简洁地说，就两部分，代码区和数据区。数据区按作用域、生命周期可分堆、栈、常量、全局、静态。对于全局和静态变量，按是否初始化，分为初始化和未初始化。常量肯定算作初始化的。其中的 `uninitialized data`, 也即 `BSS` 表示 “block started by symbol”. 总结来看是：堆，栈，常，代，全、静（初始化或未初使化）。

特别的，图中的最高地址处的命令行参数和环境变量也算作是栈，只不过是程序在加载时分配，相当于最早入栈的。其中命令行参数部分是传给 `main` 函数的 `argc` 和 `argv`. 程序运行时还可以指定环境变量，而不是用系统默认的，如语言编码等。如 `LC=zh_CN.GB18030 ./a.out arg1`.

High address	Command-line arguments		Initial value	
	Environment variables.			
	Stack (downward)			
	...			
	Heap (upward)			
	Uninitialized global and static data (bss)			Initialized to zero by exec
	Initialized global and static data			Read from .exe/.out by exec
	(Initialized) Constant data			
Text/code				
Low address				

栈	堆	全、静	常	代
数据				代码
未初始化时初值不确定	未初始化	初始化		
依赖编译器	缺省为 0			

Figure 16.1: C Memory Layout

那么编译后的可执行文件如 a.out (Linux 的 ELF 格式) 或.exe 是什么样的结构呢？可执行文件里没有 BSS 段，因为还没有值，只有真正执行时才会有对应的内存。同理栈、堆也不存在，这三部分只对进程有意义。只有常量，初始化过的全局和静态变量。不过可执行文件还包含符号表，段表，库链接表，调试等内容。

堆需手动分配、释放，常用 new/delete 和 malloc/free 操作，由低地址往高地址增长。堆的特点是可根据需求动态分配大小 dynamic allocation on demand. new/malloc 在堆上分配的内存空间是全局有效的。如果不手动 delete/free，则这些分配到的内存程序执行过程中一直被其占据，直到程序结束，造成常说的“内存泄露”，导致程序被卡死。所以通常在相同作用域内申请和释放（如函数内）。

栈是机器自动分配、释放。主要放函数参数，局部变量（自动变量）等。栈上内存只在函数局部才有效，函数结束会立即被释放。相反，栈的增长方向是由高往低，这样是合理的，如果往同一个方向增长，不便于两个区间的

管理。

常量区是指存放常量的地方，如：

```
char * p = "hello, world";
2 printf("%d", 3);
```

里 p 是自动变量，分配在栈上。但是字符串 “hello, world” 和数字 3 这样的属于量放在常量区。常量区也算作初始化区的一部分。

代码区不用说就是存放放程序代码的地方。

全局变量区是指存放全局变量的地方。静态区是放静态变量的地方。通常这两个区是合并在一起的。而且这个“全静区”是可以分成未初始化区和已初始化区两部分。

程序执行时，先把可执行文件（代码，常量，已初始化全、静变量）加载进内存低地址，再分配未初始化的全、静变量空间。进一步环境变量和程序参数入栈。后面就是在运行时栈和堆的操作了。

说了这么多，我们来看看 Linux ELF 可执行文件的结构：

```
zack@tux ~/workspace/c $ size a.out
2 text      data      bss      dec      hex filename
2391      616       16      3023     bcf a.out
```

Listing 16.1: EFL Layout

这里 text 指代码段大小，data 是已初使化全、静变量和常量段大小，bss 段内数据全零。后面的 dec 和 hex 是前面列的和。

16.4 数组和链表

数组和链表都是线性存储结构，但实现方法不同，通常前者在栈上由机器自动分配，后者在堆上由程序动态分配。实现方法的不同表现出对应的优缺点。

优缺点	结构	数组	链表
访问		通过下标随机访问	要遍历链表顺序查找
增删		慢：要先扩容再移动元素	快：只需修改指针指向

Table 16.1: 数组和链表

如果是在中间插入删除（如有序结构），则数组更麻烦，移动的元素更多。

Chapter 17

CPP

Chapter 18

Python Programming

18.1 ABCs

1. Dynamic typing. Contrary to static language, dynamic programming don't have declaration or data type associated.
2. Interpret and execute: source code -> bytecode -> machine code. It is different from C/CPP compilation.
3. Object-oriented Programming (OOP). Everything is object, variables included.
4. Easy but powerful language for scripting and rapid application development.

Dynamic versus Static Static typed programming language do *type checking* (i.e. the process of verifying and enforcing the constraints of types) at *compile-time* as opposed to run-time. Type is associated with compile-time identifiers.

Dynamic typed programming language do *type checking* at *run-time* as opposed to compile-time. Type is associated with run-time values.

```
1 def silly(a):
2     if a > 0:
3         print('greater than zero')
4     else:
5         print(5 + '3')
6
7 silly(1)
8 silly(-1)
```

Listing 18.1: Python Type Checking

Statement `silly(1)` executes perfectly fine and prints 'greater than zero'. Immediately, the next statement `silly(-1)` raises type error:

¹ `TypeError: unsupported operand type(s) for +: 'int' and 'str'`

18.2 Terminology

1. the prompt of shell.
2. Procedure-oriented programming (imperative); functional programming (declarative).
 - (a) imperative statement vs functional expression/declaration.
 - (b) a statement may include an expression (including assignment) or may be just a definition or declaration.
 - (c) the key diff is *side effect*.
3. literal constants: number & string

18.3 Execution

To execute Python code, we have basically two forms, namely the *interactive shell* and *source code interpretation*.

To get out of an interactive environment, we press `Ctrl-d` or input `exit()`. Please be noted to add the parentheses pair.

18.4 Syntax

Preliminary summaries:

- Comments are any text to the right of a `#` symbol.
- Literal constants include *numbers* (integers and floats) and *strings*, like `52.3E-4`.
 - Compared to literal constants, Python has *variable* which store values that vary during execution.
 - There is no separate integer type such as *long* or *short*.
 - There is no separate *char* type either.

- Strings are enclosed with single, double and even triple quotes. Triple quotes can span over multiple lines. Choose one appropriately. For instance, for a string containing both double and single quotes, we use triple quotes on the outer side.
- Apart from numbers and strings, we can define our own variable types as *class*.
- Python starts counting from 0.
- Surround top-level function and class definitions with two blank lines.

18.5 Identifier

Variables are just an example of identifiers. Identifiers are names given to identify something such as variables, function names, class etc.

Identifiers follow the following rules:

- The first character must be a letter of alphabeta (ASCII) or an underscore _.
- The rest of an identifier can consist of letters, underscores, and digits.
- Identifiers are case-sensitive.

Examples of invalid identifiers are:

```
1 2things, this contains spaces, my-name, <abc
```

_my_name is a valid identifier.

18.6 Strings

As mentioned in the above section, strings belong to literal constants that are immutable like that in C/CPP. However, we can construct a new string by different techniques such as the *format* method.

```
1 # comment to the right of symbol '#'
2 print('hello, world')
3
4 # number and string
5 age = 20
6 name = 'jimgray'
7
8 # 0 and 1 represents the argument indices
9 print('{0} is {1} years old when he went to HKUST'.format(name, age))
```

```

11 print('He was at his {1} years old'.format(name, age))
12 # give parameter a name
13 print('we can name the parameters: {name} is {age}')
14     'years old when he went to HKUST'.format(name=name, age=age))
15 print('{0:.3f}'.format(1.0/3))
16 print('{0:_^11}'.format('hello'))
17 # formated string (f-string) is an expression evaluated at runtime
18 print(f'his name is {name} and he is {age} years old.')
19 print('''this a multi-line string.
The second sentence.'''')

```

Listing 18.2: Python Strings

`print` append newline \n to each statement. We can specify the `end` parameter to terminate this behaviour like:

```

1 print('a', end='')
2 print('b', end='')

```

18.6.1 Escape Sequence

Although we can enclose a string containing a quotation mark with double quotes, backslash can escape special symbols. For example, "what's your name" are equal to 'what\'s your name'.

To escape the backslash itself, we use double backslash like \\.

If we want to specify a two line string, just insert a \n symbol. Similarly, we have \t for tabular symbol.

You may already know that a bare backslash at the end of line continues the previous element like:

```

1 "this is the 1st string. \
2 this is the 2nd string."

```

18.6.2 Raw String

Raw string means ignoring escape sequences within the string. Just prepend the string with r or R.

```
r"Newlines are indicated by \n"
```

Listing 18.3: Raw String

When dealing with *regular expression*, we'd better use raw string, which otherwise would require a log of backslash escaping.

Part VI

Networking

Chapter 19

TCP/IP

19.1 Segment Datagram and Frame

Before everything else, let's have a look at terminologies *segment*, *datagram* and *frame*.

Generally speaking, they refer to a *unit* of data transmitted through the protocol stack without differentiating protocols.

However, when talking about *segment*, we mean a TCP packet, including both the TCP headers and TCP payload. On the other hand, *datagram* means payload and headers of an IP packet. The two terms are also called *packet* in general. Interestingly, a UDP packet is also called datagram. Maybe this is due to UDP's *at best* strategy.

Lastly, a *frame* is a *Link layer* (mostly the Ethernet) unit. But it is weird to call it a packet.

You may also hear of *fragment*. When an IP datagram is too large to fit a MTU ??, the payload part is split into smaller parts, forming multiple new units. This is also called *fragmentation*.

By the way, in the Physical layer, we usually use *transmit* or *transmission*. More details about those terms, read Definition of Network Units.

19.2 MTU and MSS

Let's talk about *Maximum Transmission Unit (MTU)* first. It is the largest IP packet that can be transmitted over **all** links from source to destination. So MTU refers to the maximum payload of Ethernet frames, **not** including frame headers (20 bytes).

It is a physical parameter (i.e. set in router) that specifies the size of the largest protocol data unit (i.e. IP datagram) that can be sent in a single link layer transmission. MTU usually appear in association with network Interfaces (i.e. routers, PC NICs, serial ports etc.).

Maximum Segment Size (MSS) is confined to MTU. It refers to the maximum amount of application-layer data that can be placed in a TCP segment, **not** including segment headers or Option fields. So we can say it is a parameter of the *Options fields*. Although it is named after *segment*, MSS does not count TCP headers and Options field.

So both terms refer to payload only! Their relations can be expressed by equation (19.1).

$$\text{MTU} = \text{IP Headers (20 bytes)} + \text{TCP Headers (20 bytes)} [+ \text{TCP Options}] + \text{MSS} \quad (19.1)$$

For general Ethernet links, MSS is $1500 - 20 - 20 = 1460$. For Point-to-Point Protocol over Ethernet (PPPoE), it requires extra 8 bytes (6 bytes PPPoE plus 2 bytes PPP) overhead. Therefore the MTU is $1500 - 8 = 1492$ bytes and corresponding MSS is 1452 bytes.

Chapter 20

Data Bills

20.1 Contact

HU Zhan
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Table 20.1: Contact

20.2 95th Percentile

95th percentile is a commonly used commercial scheme to calculate and evaluate the regular and sustained used of a network connection. It is a kind of Burstable Billing that measures bandwidth based on *peak use*.

Generally, it allows the usage to exceed a specified threshold for a short period of time without the financial penalty of purchasing a higher Committed Information Rate (CIR is another billing method) from an ISP.

There are two critical factors involved in this scheme, namely the *percentile* and the *sampling interval*. Usually, they are 95% and 5m respectively and therefore it is also called *95/5 percentile* (or *95 percentile*).

Given a monthly billing cycle, 95/5 percentile allows a customer to have a short (i.e. threshold is $30 \times 24 \times 5\% = 36$ hours) burst in traffic without overage charges. More specifically, bandwidth could be used at a higher rate for up to $24 \times 60 \times 5\% = 72m$ a day with no financial penalty. That is to say, 95% of the time, the usage is below this amount. Conversely, 5% of the samplings may be bursting above this rate.

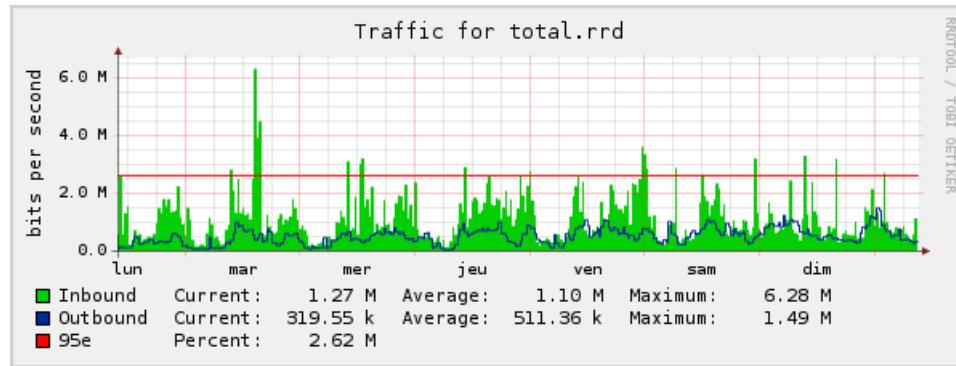


Figure 20.1: 95/5 Percentile

How is *this amount* or *this rate* is calculated? Usually a time-bandwidth chart is drawn to visualize bandwidth usage through a bill cycle like figure 20.1 whose *integral area* reflects the total data transmitted.

Bandwidth is sampled at an interval of 5 minutes from the switch or router. During an interval, the average bandwidth is calculated as the number of bits transferred throughout the interval divided by the duration ($5\text{m} = 300\text{s}$).

At the end of the month, all the bandwidth samples ($30 \times 24 \times 60 \div 5 = 8640$) are sorted from highest to lowest. The top 5% ($8640 \times 5\% = 432$) samples are thrown away and the next highest sample $432 + 1 = 433$ becomes the billable use for the entire month. Obviously, $432 \times 5 \div 60 = 36\text{h}$.

In the figure 20.2, the billable value falls around 6Mbps, or 60% of the highest burst. From this figure, we find the sorted slope is quite steep. The sharp burst contributes a lot to the final bill though not much bandwidth is used (small area).

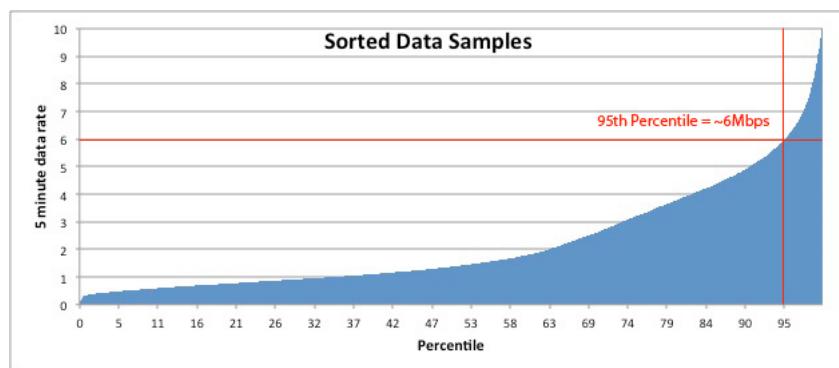


Figure 20.2: Sorted Percentile

Conversely, at any moment during the billing cycle, even if peak traffic only appears for a short *instant* and no additional traffic is generated, the billing amount can be

sbusstantially higher than average usage billing. This is not the end of the story. Although we get the billable value, it may not take affect when paying bills. For example, what if all customers' 95th percentile value are pretty small? In that case, the ISP's infrastructure would be wasted and lose money.

In reality, 95th percentile assumes a *base commit rate* (and fees associated) that must be guranteed by customers. The 95th percentile value only takes effect when it is higher than the base commit rate, otherwise the base value would be used irrespective of the 95th percentile. The higher the base commit rate is, the cheaper the bandwidth fee becomes.

Base commit rate is *not CIR* (where hard bandwidth must be reserved for a customer) but just a billing gurantee even the real bandwidth usage is 0. It is fairly to both the carrier and the customer in terms of the service delivered to the customer and the ability of the carrier to scale its infrastructure to meed different customers' needs.

20.3 Other Billing Methods

The 95th percentile is utilized mostly between ISP and business customers in a datacenter while CIR is adopted between ISP and individuals for home cable, fiber, DSL etc. Hard bandwidth is guranteed and no burst is allowed. Customers pay for the fixed bandwidth value.

Apart from 95th percentile and CIR, *actual throughput billing* is used in limited and shared bandwidth networks like mobile data networks (i.e. 4G) where resources overprovisioning is not possible due to limited spectrum availability. Customers just pay for what they get on demand. ISP will simply record how much data you moved over the circuit for that interval. It is also used by some web-based VPS platforms to bill customers.

You can read more about billing methods on billing methods explained and analyzed and check figure 20.3.

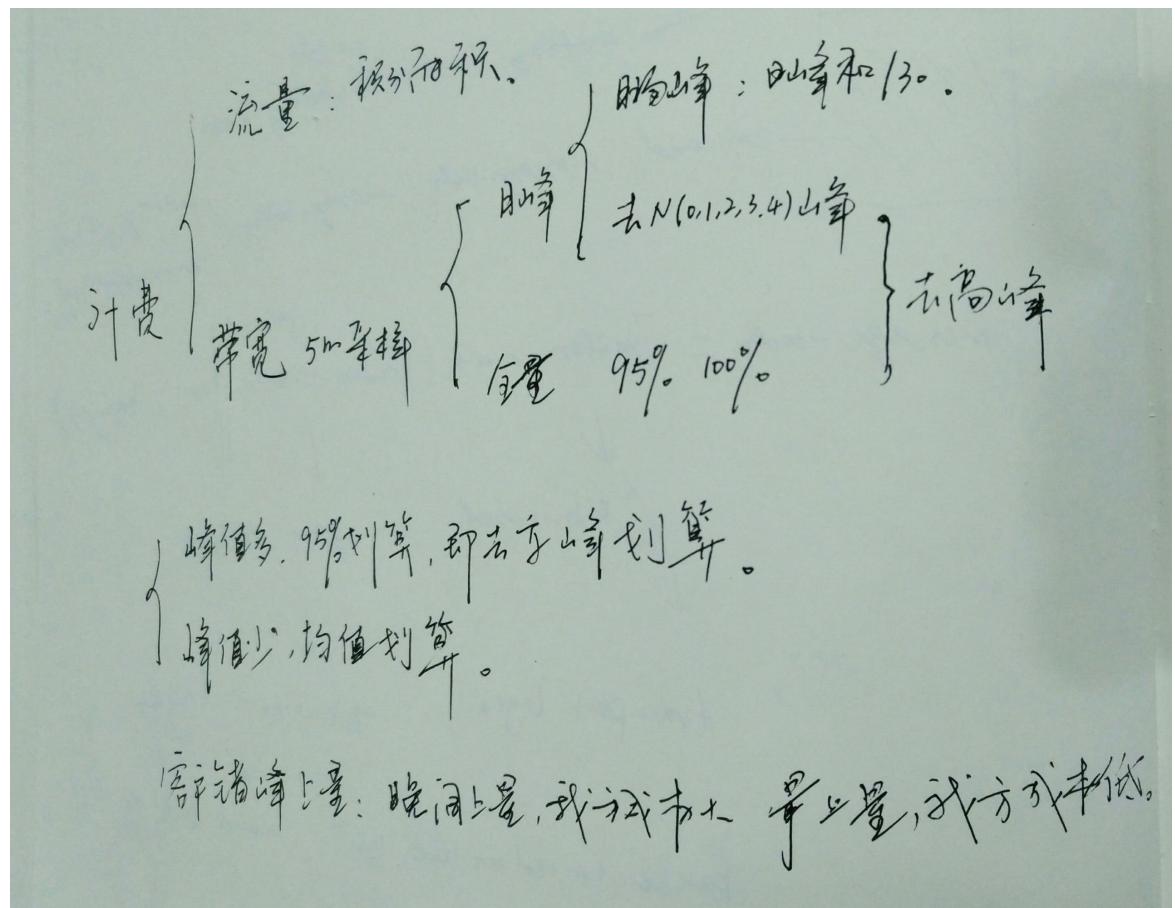


Figure 20.3: Billing Methods

Chapter 21

Networking Tools

todos

Part VII

Brainteaser

Chapter 22

Brain Teasers

补全数列空缺

例 3 5 10 25 75 () 875. 观察此数列发现，相邻两项的数间没有什么特别关系，相乘相加都不是。这时应考虑相邻三、四项项的关系，会发现 $3 \times 5 + 10 = 25$ ，类似地有 $5 \times 10 + 25 = 75$. 因此空处的值应是 $10 \times 25 + 75 = 325$. 再来一个例子，5 6 16 28 60 (). 分析得出 $5 \times 2 + 6 = 16$, 还有 $6 \times 2 + 16 = 28$. 所以空处的值应是 $28 \times 2 + 60 = 116$. 此两例考虑连续多个数之间的递推关系，类似于 Fibonacci Sequence.

牛吃草

一块匀均生长的草地，可供 27 头牛吃 6 周，或 23 牛吃 9 周，问多少牛可吃 18 周？

我们先设一头牛吃草的速度是 a , 单位可以是 kg/w, 则 6 周吃 $27 \times 6 \cdot a$ kg 的草。设草的生长速度是 b , 单位可以是 kg/w, 那么 6 周长了 $6 \cdot b$ kg 的草。那么是不是 $27 \times 6 \cdot a = 6b$ 呢？

不是！因为牛吃草前，草地上本来就有部分草，设为 c kg, 则 $27 \times 6 \cdot a = 6b + c$, 同理我们得出：

$$\begin{aligned} 27 \times 6 \cdot a &= 6 \cdot b + c \\ 23 \times 9 \cdot a &= 9 \cdot b + c \\ x \times 18 \cdot a &= 18 \cdot b + c \end{aligned}$$

通过前两个方程，可得出 $b = 15 \cdot a$ 和 $c = 72 \cdot a$, 进而求出 $x = 19$.

相向而行

甲乙两地相距 90 米，A, B 二人分别从甲乙同时出发，在两地来回跑动。甲的速度是 3 m/s, 乙的是 2 m/s. 问 10 分钟内甲乙相遇几次？

第一次相遇时二人行使 90 米，时间是 $90 \div (3 + 2) = 18\text{s}$. 相遇后二人背向而行，直至达到对端。此时二人又行使了 90 米，用时 18s.

二人再次相向而行，准备下一次相遇。此后一直重复此过程。可以发现相遇一次二人行使了 180 米，花时 36s, 所以 10 分钟相遇次数是 $10 \times 60 \div 36 = 16\frac{2}{3}$, 结果是分数，那么是 16 次还是 17 次呢？

应是 17 次，因为第次相遇时，在 36s 的前半程，所以分数部分应四舍五入！

上面这种方法不够明了。第一次相遇需 18s, 下一次相遇需 36s, 再下一次相遇需 36s, 此后每一次相遇都需 36s. 我们找相遇的时间点更合理，得到一个等差数列：

$$\begin{aligned} t_1 &= 18 \\ t_2 &= 18 + 36 \\ &\dots \\ t_n &= 18 + (n - 1) \cdot 36 \end{aligned}$$

根据 $t_n = 10 \times 60$ 可以算出 $n = 17\frac{1}{6}$. 由此可知，相遇 17 次，因为剩下的 $1/6$ 还没到第 17 次相遇时间点。

背向而行

有一 300 米圆跑道，甲乙在同一地点背向而行，速度分别是 3.5m/s 和 4m/s. 问第 10 次相遇时，甲离出发地还有多远？

每相遇一次，两人共行走了 300 米，其中甲行走了 $\frac{3.5}{(3.5+4)} \times 300 = 140$ 米，而乙行走了 160 米。

那么相遇 10 次时，甲累计走了 $10 \times 140 = 1400$ 米，而 $1400 \div 300 = 4 \dots 200$ ，也就是说走了 4 圈后，第 5 圈走了 200 米，所以离出发点还剩 100 米。

交换变量

有两个整数 $a = 5, b = 7$, 不通过临时变量，如何交换二者的值？

方法一：异或 XOR. 异或的意思是，让两个数的二进制位互相比对，同为 0 或 1 时结果为 0, 有一个 1 一个 0 (相异) 时结果为 1. 所以任何数异或自己的结果是 0. 对应的 C 语言结果是：

```
1 a = a^b;  
2 b = a^b;  
3 a = a^b;
```

Listing 22.1: Swap by XOR

方法二：加減法。

```
1 a = a + b;  
2 b = a - b;  
3 a = a - b;  
4 // Or  
5 a = (a + b) - (b = a)
```

Listing 22.2: Swap by Arithmetic Operations

Chapter 23

行测图行推理

23.1 规律总结

首先分析图形外观，考察图形画法，得出图形里的分部要素，也可称为元素。

1. 边。三角形、四边形、五边形……
2. 曲线。
3. 圆。
4. 区。图形被分割成不同的封闭区域。
5. 交点。边上的交点。

找出各图形元素后，再分析其规律。

1. 行列。从行和列两个维度来分析规律。
2. 数量。每种元素的数量可能呈某种关系，如相等，差数列。还可以是行、列上数量关系。如边数，交点数，区域数等。
3. 笔画。是否是一笔画完。
4. 对称。如轴对称（竖轴、横轴），旋转对称（中心对称，180度），不对称。如英文字母的对称性。还可能数对称轴（相同的、不同的）的数量。
5. 旋转。图形整体依次顺时针、逆时针旋转一个角度。
6. 翻转。图形整体以某轴翻转180度。如水平翻转。
7. 平移。某元素在图内平移一定距离。如小方格每次移顺时针移3个位置。

8. 相对。不同元素在图内相对位置发生变化。相对位置可以是内部、外部，相交、相接、分离，也可以是直角处、圆弧处，还可以是在最长边、最短边处。
9. 加减。相邻图形或元素之间加减组合出新图。如第1个图形和第2个图形组合起来是第3个图形。常见的是九宫格里，行、列间图形是加减关系。有时甚至是先旋转再加减。
10. 类别。图形可以按其属性分类。如同为生活类用品，同属用腿、用手、手脚并用的运动项目。

Part VIII

Chemistry

Chapter 24

走进化学世界

化学就是研究物质及其变化，它不仅研究已经存在的物质，还要研究和创造自然界原本不存在的新物质。例如，半导体材料，电阻几乎为零的超导体，有记忆能力的新材料，等等。

化学在保证人类生存和提高生活质量上有很大帮助。例如：

- 化肥和农药，增加粮食产量。
- 化学合成药物，指抑制细菌和病毒。
- 化学新能源、新材料。

近代化学突破源于两点：

1. 物质是由分子原子构成的，分子中原子的重新组合是化学变化的基础。
2. 元素周期表。

这两个突破使得化学研究有迹可寻。化学的科学定义：**化学是在分子、原子层上研究物质性质、组成、结构与变化规律的科学**。研究物质是指研究其性质、组成和结构等静态特征，而变化是化学反应，也即原子的重新组合，这是一个动态过程。

24.1 性质及变化

物质变化分两种：

- 物理变化：没有生成新物质的变化，如物质形态发生变化。气态、液态、固态三态之间的相互转换的过程就是物理变化。
- 化学变化或叫化学反应：生成新物质的变化（原子重新组合），常表现为颜色变化，放出气体，生成沉淀等。化学变化还伴随物质能量变化，

如吸热、放热、发光等。

虽然物理变化也通常伴随能量转换，但主要借用外部能量。而化学变化和能量可以只来自物质本身，不需要外部能量辅助。

依据物质变化过程中表现出的性质，可有：

- 化学性质：物质在化学变化中表现出的性质。例如，铜在潮湿的空气中生成铜绿。
- 物理性质：物质不需要化学反应就表现出来的性质。物质颜色、状态、气味、硬度、熔点、沸点、密度等都是物理性质。例如，常态下，氧气是种无色、无味的气体。注意，物理性质可能是物理变化过程表现出的性质，如物质的三态。

外界条件改变时，物质性质也会随着变化，因此，描述物质性质时往往要注明条件。如，当温度升高时，固态冰变成液态水，再加温，水会沸腾。液体的沸点是物理性质，但受大气压强的影响。大气稀薄的地方，大气压强变小，这时水的沸点会降低，容易烧开。

24.1.1 大气压

由于大气压强是变化的，人们把 $1atm = 101kPa = 76cm$ 水银柱重量当作标准大气压强。大气压强是指大气对浸在它里面的物体产生的压强，也叫大气压或气压，可以用空气的重力或分子热运动来解释其产生机理，而且这两种解释是等价的。

那么如何用重力和分子热运动解释呢？在密封空间内，气压的产生应从微观上来解释。气体分子热运动时，撞击空间内壁，产生作用力（内壁也同时产生反作用力），这个作用力就是气体压力。没有内壁就不会产生气体压力！压强是单位面积上的压力，表示强度，不用考虑内壁的存在。

由于分子作用力各向同性，所以任一点的压强在不同方向上相同。

对于空气呢？空气分子同样作热运动，但是没有内壁，怎么产生压力呢？有地球引力！地球引力相当于上述密闭空间内壁的反作用力。所以空气中任意一点也有空气压力，进而也有压强。同理，空气压力也是各向同性的。

至于压强的数值计算，两种情况有所不同，关键是算出分子热运动的作用力。对于密闭空间，它是 $P = nTR/volume$. 对于空气，因为重力和空气分子热运动产生的撞击力平衡，大气压强是大气施加于单位面积上的重力，即该地单位面积垂直向上延伸到大气层顶的空气柱的总重力。简单的数学公式是 $P = m \cdot g / area$. 实际中要考虑不同高度处重力加速度 g 的不同。

24.2 化学实验

24.2.1 注意事项

- 手不接触药品，不尝药品，鼻孔不可太靠近瓶口（特别是气体）。
- 实验剩余药品不能放回原瓶，不能随意丢弃，不能带出实验室。要放入指定容器。
- 节约药品。未说明剂量时，液体一般取 $1 - 2 \text{ mL}$ ，固体只需盖满试管底部即可。
- 保护眼睛，如果进了药液，应立即用清水清洗，要眨眼睛。

24.2.2 药品取用

- 固体：广口瓶。药匙（粉状、颗粒）、摄子（块状），取完应擦净。玻璃容器横放，块状放容器口，缓缓竖立，滑入底。药匙送粉状入试管底，再直立。
- 液体：细口瓶。倾倒法。瓶塞倒立桌面，瓶口紧挨试管口，瓶身标签面朝手心。定量取液，用量筒。量液时，视线与凹液面最低处保持水平。仰视偏多，俯视偏少。取少量液体用滴管，应保持橡胶帽朝上，不可平放、倒放，否则腐蚀橡胶帽或污染试剂。滴管应悬空滴液，不可接触容器口，否则因为试剂太少，沾在内壁。用完即洗。

24.2.3 物质加热

一般用酒精灯。不可以向燃着的酒精灯添加酒精，也不可以用一个点燃另一个。用灯帽熄灭，不可用嘴吹。熄灭后，取下灯帽再盖上。

加热试管液体：

1. 试管外壁应干燥，液体不超过容积的 $1/3$ 。
2. 试管夹由试管底部套上、取下。
3. 先使试管底部均匀受热，再用外焰固定加热。
4. 试管口不要对着自己或他人。
5. 加热后的试管不能立即接触冷水或用冷水冲洗。

三层火焰

本节顺便说下蜡烛然烧问题。蜡烛然烧时，蜡固体先熔化、气化，再与空气中氧气发生化学反应。

外焰是红白色，温度高；而内焰为红色且边缘是蓝色，温度低。焰心没有发生燃烧，所以不烧手。温度的高低主要由与氧气接触面积决定。外焰处氧气最多，燃烧最充分，温度最高。焰心处氧气已消耗殆尽，所以没有燃烧。

色温和温度是两个不同的概念。色温反应的是单个分子的能量，能量越高，颜色越偏蓝。温度是分子热运动的宏观测量，不仅要考虑单个分子能量，还应考虑分子总个数。在相同分子个数情况下，蓝焰温度肯定比黄色或红色高。

但在蜡烛然烧时，外焰温高除了氧气多外，和热气体上升也有关系。另外，既然外焰燃烧更充分，为何不见蓝色。实际是有蓝色的，只是被遮住了。外焰处蜡蒸气非常多，被外焰加热后，变成白炽色，把燃烧的蓝色吸收了。所外焰的高温不是因为黄色，而是蓝色（充分燃烧）和上升热气。

24.2.4 仪器连接

玻璃管，胶皮管，橡胶塞：

1. 玻璃管和橡胶塞：玻璃管口用水湿润，对准橡胶塞上的孔稍用力转动、插入。
2. 玻璃管和胶皮管：玻璃管口用水湿润，稍用力即可插入。
3. 容器口和橡胶塞：慢慢转动橡胶塞，塞入容器口（如试管）。
4. 气密性检查：用手握紧试管，观察水中导管口是否有气泡冒出，有则好。

24.2.5 洗涤玻璃容器

必需洗涤玻璃容器，否则影响实验效果。以洗试管为例：

1. 倒掉废液。
2. 注入半试管水，振荡后再倒掉。
3. 重复上一步骤。
4. 如试管内壁还有不易洗掉残留物质，用试管刷刷洗。洗刷时，须转动或上下移动试管刷。

洗过的玻璃容器内壁附着的水既不聚成水滴，也不股下流，表明仪器已洗干净。

Chapter 25

空气

25.1 简介

空气的主要成分是氮 78%, 氧 21%, 稀有气体 0.94%, 二氧化碳 0.03%, 其它气体和杂质占 0.03%. 其中氮和氧几乎各占 1/5 和 4/5. 稀有气体主要是氦 hàn, 氖、氩、氪、氙 xiān, 氪等。

- 混合物：由两种或两种以上的物质混合而成的物质。组成混合物的各种成分保持着它们各自的性质。
- 纯净物：只有一种物质组成。纯净物可以用化学式表示，如氮气是 N₂, 磷是 P, 五氧化二磷是 P₂O₅ 等。

25.2 成分

各主要成分。

Chapter 26

物质列表

化学式 \ 参数	名称、别名	颜色和状态
CuSO_4	硫酸铜、胆矾、蓝矾	(无水) 灰白色粉末、(有水) 蓝色结晶固体
H_2O	水	无色液体
$\text{KAl}(\text{SO}_4)_2 \cdot 2\text{H}_2\text{O}$	十二水合硫酸铝钾、明矾	无色或白色的八面体晶体
Fe	铁	银白色固体
Al	铝	银白色固体
O_2	氧气	无色无味气体

Table 26.1: 常见物质列表

Periodic Table of the Elements

1	$\frac{2}{2}$ H	1_s	Hydrogen	1.00784-1.00811	Z	$\frac{\text{eng}}{\text{ss}}$	$\frac{\text{ss}}{\text{saw}}$
3	$\frac{0.98}{2}$ Li	2_s	4	$\frac{1.57}{2}$ Be	2_s		
	Lithium		Beryllium	9.0121831(5)			
11	$\frac{0.93}{3}$ Na	3_s	12	$\frac{1.31}{3}$ Mg	3_s		
	Sodium		Magnesium	24.304-24.307			
19	$\frac{0.82}{4}$ K	4_s	20	$\frac{1.00}{4}$ Calcium	21	$\frac{1.36}{3}$ Scandium	22
	Potassium			40.078(4)	Titanium	Titanium	Titanium
37	$\frac{0.82}{5}$ Rb	5_s	38	$\frac{0.95}{5}$ Rubidium	39	$\frac{1.22}{4}$ Strontium	40
				85.4678(3)	Yttrium	Zirconium	Zirconium
55	$\frac{0.79}{6}$ Cs	6_s	56	$\frac{0.89}{6}$ Cesium	6_s	$\frac{57}{71}$ Barium	$\frac{72}{*}$ Lanthanides
				132.90545196(6)		Hafnium	Tantalum
87	$\frac{0.7}{7}$ Fr	7_s	88	$\frac{0.9}{7}$ Francium	7_s	$\frac{89-103}{Rf}$ Actinides	$\frac{104}{Rutherfordium}$ (261)
				(223)		Thorium	Dubnium
*	$\frac{57}{La}$ Lanthanum	$\frac{1.1}{1}$ $5d^*$	58	$\frac{1.12}{1}$ $4f^*$	59	$\frac{1.13}{1}$ $4f$	60
89	$\frac{1.1}{Ac}$ Actinium	$\frac{6d^*}{2}$	90	$\frac{1.3}{1}$ $5f^*$	91	$\frac{1.5}{1}$ $5f^*$	92
**	$\frac{**}{Th}$ Thorium						

2	1_s	He	Helium	4.002602(2)
5	$\frac{2.01}{B}$ Boron	2_p	6	$\frac{2.55}{C}$ Carbon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	14	$\frac{1.90}{Si}$ Silicon
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	7	$\frac{3.01}{N}$ Nitrogen
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	15	$\frac{2.19}{P}$ Phosphorus
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	8	$\frac{3.44}{O}$ Oxygen
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	16	$\frac{2.58}{S}$ Sulfur
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	9	$\frac{3.98}{F}$ Fluorine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	17	$\frac{3.16}{Cl}$ Chlorine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	18	$\frac{3.00}{Ar}$ Argon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	19	$\frac{3.00}{Kr}$ Krypton
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	20	$\frac{3.00}{Ne}$ Neon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	21	$\frac{3.00}{Xe}$ Xenon
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	22	$\frac{3.00}{Rn}$ Radon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	23	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	24	$\frac{3.00}{Rn}$ Radon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	25	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	26	$\frac{3.00}{Rn}$ Radon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	27	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	28	$\frac{3.00}{Rn}$ Radon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	29	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	30	$\frac{3.00}{Rn}$ Radon
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	31	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	32	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	33	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	34	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	35	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	36	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	37	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	38	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	39	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	40	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	41	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	42	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	43	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	44	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	45	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	46	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	47	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	48	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	49	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	50	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	51	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	52	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	53	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	54	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	55	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	56	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	57	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	58	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	59	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	60	$\frac{3.00}{At}$ Astatine
	10.806-10.821	12.0096-	12.0116	14.00728
13	$\frac{1.61}{Al}$ Aluminum	$3p$	61	$\frac{3.00}{At}$ Astatine
	26.9815385(7)	28.084-28.086	30.973761998(5)	32.059-32.076
5	$\frac{2.01}{B}$ Boron	2_p	62	$\frac{3.00}{At}$ Astatine
	10.806-10			

English-Chinese Periodic Table of Elements 英漢元素周期表

1 / Ia												18 / VIIa																																																																							
1 H hydrogen 1.0079 $1s^1$	1 氫	alkalai metals					alkaline earths		lanthanoid		actinoid		transition metals		13 / IIIa 14 / IVA 15 / Va 16 / Vla 17 / VIIa																																																																				
2 / IIa		atomic num 元素 symbol oxidation states					other metals		semi-metals		non-metals		halogens		noble gases																																																																				
3 Li lithium 6.941 $[He]2s^1$	4 Be beryllium 9.0122 $[He]2s^2$	element name atomic weight electron configuration					Solid Liquid Gas Synthetic Unknown																																																																												
11 Na sodium 22.990 $[Ne]3s^1$	12 Mg magnesium 24.305 $[Ne]3s^2$																																																																																		
19 K potassium 39.09 $[Ar]4s^1$	20 Ca calcium 40.078 $[Ar]4s^2$	21 Sc scandium 44.956 $[Ar]4s^3d^1$	22 Ti titanium 47.867 $[Ar]4s^3d^1$	23 V vanadium 50.942 $[Ar]4s^3d^1$	24 Cr chromium 54.938 $[Ar]4s^3d^5$	25 Mn manganese 55.845 $[Ar]4s^3d^5$	26 Fe iron 56.933 $[Ar]4s^3d^6$	27 Co cobalt 58.933 $[Ar]4s^3d^7$	28 Ni nickel 58.693 $[Ar]4s^3d^8$	29 Cu copper 63.546 $[Ar]4s^3d^{10}$	30 Zn zinc 65.409 $[Ar]4s^3d^{10}$	31 Ga gallium 69.723 $[Ar]4s^3d^{10}4p^1$	32 Ge germanium 72.64 $[Ar]4s^3d^{10}4p^2$	33 As arsenic 74.922 $[Ar]4s^3d^{10}4p^3$	34 Se selenium 78.96 $[Ar]4s^3d^{10}4p^4$	35 Br bromine 79.904 $[Ar]4s^3d^{10}4p^5$	36 Kr krypton 83.798 $[Ar]4s^3d^{10}4p^6$	37 Rb rubidium 85.468 $[Kr]5s^1$	38 Sr strontium 87.62 $[Kr]5s^2$	39 Y yttrium 88.906 $[Kr]5s^24d^1$	40 Zr zirconium 91.224 $[Kr]5s^24d^2$	41 Nb niobium 92.906 $[Kr]5s^24d^3$	42 Mo molybdenum 95.94 $[Kr]5s^24d^4$	43 Tc technetium 98.00 $[Kr]5s^24d^5$	44 Ru ruthenium 101.07 $[Kr]5s^24d^6$	45 Rh rhodium 102.91 $[Kr]5s^24d^7$	46 Pd palladium 106.42 $[Kr]5s^24d^8$	47 Ag silver 107.87 $[Kr]5s^24d^9$	48 Cd cadmium 114.82 $[Kr]5s^24d^{10}$	49 In indium 118.71 $[Kr]5s^24d^{10}5p^1$	50 Sn tin 121.76 $[Kr]5s^24d^{10}5p^2$	51 Sb antimony 127.60 $[Kr]5s^24d^{10}5p^3$	52 Te tellurium 126.90 $[Kr]5s^24d^{10}5p^4$	53 I iodine 131.29 $[Kr]5s^24d^{10}5p^5$	54 Xe xenon 131.29 $[Kr]5s^24d^{10}5p^6$	55 Cs cesium 132.905 $[Xe]6s^1$	56 Ba barium 137.327 $[Xe]6s^2$	57 Lu lutetium 178.49 $[Xe]6s^24f^15d^1$	58 Hf hafnium 180.95 $[Xe]6s^24f^15d^2$	59 Ta tantalum 183.84 $[Xe]6s^24f^15d^3$	60 W tungsten 186.21 $[Xe]6s^24f^15d^4$	61 Re rhenium 190.23 $[Xe]6s^24f^15d^5$	62 Os osmium 195.08 $[Xe]6s^24f^15d^6$	63 Ir iridium 196.97 $[Xe]6s^24f^15d^7$	64 Pt platinum 200.59 $[Xe]6s^24f^15d^8$	65 Au gold 204.88 $[Xe]6s^24f^15d^9$	66 Hg mercury 207.2 $[Xe]6s^24f^15d^{10}$	67 Tl thallium 210.76 $[Xe]6s^24f^15d^{10}5p^1$	68 Pb lead 208.98 $[Xe]6s^24f^15d^{10}5p^2$	69 Bi bismuth 212.60 $[Xe]6s^24f^15d^{10}5p^3$	70 Po polonium 213.22 $[Xe]6s^24f^15d^{10}5p^4$	71 At astatine 222.0 $[Xe]6s^24f^15d^{10}6p^1$	72 Rn francium [223] $[Rn]7s^1$	73 Fr radium [226] $[Rn]7s^2$	74 Ra lawrencium [262] $[Rn]7s^25f^16d^1$	75 Db rutherfordium [267] $[Rn]7s^25f^16d^2$	76 Sg dubnium [268] $[Rn]7s^25f^16d^3$	77 Bh seaborgium [271] $[Rn]7s^25f^16d^4$	78 Hs bohrium [270] $[Rn]7s^25f^16d^5$	79 Mt hassium [277] $[Rn]7s^25f^16d^6$	80 Ds meitnerium [281] $[Rn]7s^25f^16d^7$	81 Rg darmstadtium [282] $[Rn]7s^25f^16d^8$	82 Nh roentgenium [285] $[Rn]7s^25f^16d^9$	83 Fl copernicium [289] $[Rn]7s^25f^16d^{10}$	84 Mc nihonium [293] $[Rn]7s^25f^16d^{10}7p^1$	85 Lv flerovium [299] $[Rn]7s^25f^16d^{10}7p^2$	86 Ts moscovium [293] $[Rn]7s^25f^16d^{10}7p^3$	87 Og itennessine [294] $[Rn]7s^25f^16d^{10}7p^4$	88 Yb Livermorium [293] $[Rn]7s^25f^16d^{10}7p^5$	89 Hg tennessine [294] $[Rn]7s^25f^16d^{10}7p^6$	90 Tm oganesson [294] $[Rn]7s^25f^16d^{10}7p^7$	91 Bk yterbium [294] $[Rn]7s^25f^16d^{10}7p^8$	92 Cf meitnerium [258] $[Rn]7s^25f^16d^{10}7p^9$	93 Pu berkelium [251] $[Rn]7s^25f^16d^{10}7p^{10}$	94 Am einsteinium [252] $[Rn]7s^25f^16d^{10}7p^{11}$	95 Cm fermium [257] $[Rn]7s^25f^16d^{10}7p^{12}$	96 Er mendelevium [258] $[Rn]7s^25f^16d^{10}7p^{13}$	97 Tb nobelium [259] $[Rn]7s^25f^16d^{10}7p^{14}$	98 Dy radon [222] $[Rn]7s^25f^16d^{10}7p^{15}$	99 Ho radon [222] $[Rn]7s^25f^16d^{10}7p^{16}$	100 Tm radon [222] $[Rn]7s^25f^16d^{10}7p^{17}$	101 Gd radon [222] $[Rn]7s^25f^16d^{10}7p^{18}$	102 Pr radon [222] $[Rn]7s^25f^16d^{10}7p^{19}$
57-70 lanthanoids 镧系元素	57 La lanthanum 138.91 $[Xe]6s^25d^1$	58 Ce cerium 140.12 $[Xe]6s^24f^15d^1$	59 Pr praseodymium 140.91 $[Xe]6s^24f^15d^2$	60 Nd neodymium 144.24 $[Xe]6s^24f^15d^3$	61 Pm promethium [145] $[Xe]6s^24f^15d^4$	62 Sm samarium 150.36 $[Xe]6s^24f^15d^5$	63 Eu europium 151.96 $[Xe]6s^24f^15d^6$	64 Gd gadolinium 157.25 $[Xe]6s^24f^15d^7$	65 Tb terbium 158.93 $[Xe]6s^24f^15d^8$	66 Dy disprosium 162.50 $[Xe]6s^24f^15d^9$	67 Ho holmium 164.93 $[Xe]6s^24f^15d^{10}$	68 Er erbium 167.26 $[Xe]6s^24f^15d^{11}$	69 Tm thulium 168.93 $[Xe]6s^24f^15d^{12}$	70 Yb ytterbium 173.04 $[Xe]6s^24f^15d^{13}$	117 Ts itennessine [294] $[Rn]7s^25f^16d^{10}7p^7$	118 Og oganesson [294] $[Rn]7s^25f^16d^{10}7p^8$	57-70 actinoids 锕系元素																																																																		

English-Chinese Periodic Table of Elements 英漢元素周期表

1 / Ia												18 / VIIa															
1 氢 H hydrogen 1.0079 1s ¹	2 / IIa						alkalai metals	alkaline earths	lanthanoid	actinoid	transition metals	5 硼 B boron 10.811 [He]2s ² p ¹	6 碳 C carbon 12.011 [He]2s ² p ²	7 氮 N nitrogen 14.007 [He]2s ² p ³	8 氧 O oxygen 15.999 [He]2s ² p ⁴	9 氟 F fluorine 18.999 [He]2s ² p ⁵	10 氖 Ne helium 4.0026 1s ²										
3 鋰 Li lithium 6.941 [He]2s ¹	4 錫 Be beryllium 9.0122 [He]2s ¹						other metals	semi-metals	non-metals	halogens	noble gases	13 鋁 Al aluminum 26.982 [Ne]3s ² 3p ¹	14 硅 Si silicon 28.086 [Ne]3s ² 3p ²	15 磷 P phosphorus 30.974 [Ne]3s ² 3p ⁴	16 硫 S sulfur 32.065 [Ne]3s ² 3p ⁴	17 氯 Cl chlorine 35.453 [Ne]3s ² 3p ⁵	18 氩 Ar argon 39.948 [Ne]3s ² 3p ⁶										
11 鉀 Na sodium 22.990 [Ne]3s ¹	12 錦 Mg magnesium 24.305 [Ne]3s ²						Solid	Liquid	Gas	Synthetic	Unknown	13 / IIIa	14 / IVa	15 / Va	16 / VIa	17 / VIIa											
19 鈀 K potassium 39.098 [Ar]4s ¹	20 鈥 Ca calcium 40.078 [Ar]4s ²						atomic num 元素 symbol oxidation states element name atomic weight electron configuration	alkalai metals	alkaline earths	lanthanoid	actinoid	transition metals	5 硼 B boron 10.811 [He]2s ² p ¹	6 碳 C carbon 12.011 [He]2s ² p ²	7 氮 N nitrogen 14.007 [He]2s ² p ³	8 氧 O oxygen 15.999 [He]2s ² p ⁴	9 氟 F fluorine 18.999 [He]2s ² p ⁵	10 氖 Ne helium 4.0026 1s ²									
37 鈦 Rb rubidium 85.468 [Kr]5s ²	38 鈷 Sr strontium 87.62 [Kr]5s ²						3 / IIIb	4 / IVb	5 / Vb	6 / VIb	7 / VIIb	8 / VIIIb	9 / VIIlb	10 / VIIIlb	11 / Ib	12 / IIb											
55 銀 Cs cesium 132.905 [Xe]6s ¹	56 鈽 Ba barium 137.327 [Xe]6s ²						21 鈮 Sc scandium 44.956 [Ar]4s ³ d ¹	22 鈦 Ti titanium 47.867 [Ar]4s ³ d ²	23 鈦 V vanadium 50.942 [Ar]4s ³ d ³	24 鈦 Cr chromium 54.936 [Ar]4s ³ d ⁵	25 鈮 Mn manganese 55.845 [Ar]4s ³ d ⁷	26 鐵 Fe iron 56.845 [Ar]4s ³ d ⁸	27 鈮 Co cobalt 58.933 [Ar]4s ³ d ⁹	28 鎳 Ni nickel 58.693 [Ar]4s ³ d ¹⁰	29 銅 Cu copper 63.546 [Ar]4s ³ d ¹⁰	30 銅 Zn zinc 65.409 [Ar]4s ³ d ¹⁰	31 銅 Ga gallium 69.723 [Ar]4s ³ d ¹⁰ 4p ¹	32 銅 Ge germanium 72.64 [Ar]4s ³ d ¹⁰ 4p ²	33 銅 As arsenic 74.922 [Ar]4s ³ d ¹⁰ 4p ³	34 銅 Se selenium 78.96 [Ar]4s ³ d ¹⁰ 4p ⁴	35 銅 Br bromine 79.904 [Ar]4s ³ d ¹⁰ 4p ⁵	36 銅 Kr krypton 83.798 [Kr]5s ² 4d ¹⁰ 5p ⁵					
87 鈔 Fr francium [223] [Rn]7s ¹	88 鈑 Ra radium [226] [Rn]7s ²						39 鈮 Y yttrium 88.906 [Kr]5s ² 4d ¹	40 鈮 Zr zirconium 91.224 [Kr]5s ² 4d ²	41 鈮 Nb niobium 92.906 [Kr]5s ² 4d ³	42 鈮 Tc molybdenum 95.94 [Kr]5s ² 4d ⁵	43 鈮 Ru technetium 98 [Kr]5s ² 4d ⁷	44 鈮 Rh ruthenium 101.07 [Kr]5s ² 4d ⁹	45 鈮 Pd rhodium 102.91 [Kr]5s ² 4d ¹⁰	46 鈮 Ag silver 106.42 [Kr]5s ² 4d ¹⁰	47 銀 Cd cadmium 112.41 [Kr]5s ² 4d ¹⁰	48 銀 In indium 114.82 [Kr]5s ² 4d ¹⁰ 5p ¹	49 銀 Sb antimony 118.71 [Kr]5s ² 4d ¹⁰ 5p ²	50 銀 Te tellurium 121.76 [Kr]5s ² 4d ¹⁰ 5p ³	52 銀 I iodine 126.90 [Kr]5s ² 4d ¹⁰ 5p ⁵	53 銀 Xe xenon 131.29 [Kr]5s ² 4d ¹⁰ 5p ⁶	54 銀 Kr krypton 83.798 [Kr]5s ² 4d ¹⁰ 5p ⁵						
71 鑄 Lu lutetium 174.97 [Xe]6s ² 4f ¹ 5d ¹	72 鑄 Hf hafnium 178.49 [Xe]6s ² 4f ¹ 5d ²						73 鑄 Ta tantalum 180.95 [Xe]6s ² 4f ¹ 5d ³	74 鑄 W tungsten 183.84 [Xe]6s ² 4f ¹ 5d ⁵	75 鑄 Re rhenium 186.21 [Xe]6s ² 4f ¹ 5d ⁷	76 鑄 Os osmium 190.23 [Xe]6s ² 4f ¹ 5d ⁸	77 鑄 Ir iridium 192.22 [Xe]6s ² 4f ¹ 5d ⁹	78 鑄 Pt platinum 195.08 [Xe]6s ² 4f ¹ 5d ¹⁰	79 金 Au gold 196.97 [Xe]6s ² 4f ¹ 5d ¹⁰	80 汞 Hg mercury 200.59 [Xe]6s ² 4f ¹ 5d ¹⁰	81 鑄 Tl thallium 204.38 [Xe]6s ² 4f ¹ 5d ¹⁰	82 鑄 Pb lead 207.2 [Xe]6s ² 4f ¹ 5d ¹⁰	83 鑄 Bi bismuth 208.98 [Xe]6s ² 4f ¹ 5d ¹⁰ 6p ¹	84 鑄 Po polonium [209] [Xe]6s ² 4f ¹ 5d ¹⁰ 6p ²	85 鑄 At astatine [210] [Xe]6s ² 4f ¹ 5d ¹⁰ 6p ⁵	86 氪 Rn radon [222] [Xe]6s ² 4f ¹ 5d ¹⁰ 6p ⁶	55 鑄 Ts tennessine [294] [Rn]7s ² 5f ¹ 6d ¹⁰ 7p ¹	117 鑄 Og oganesson [294] [Rn]7s ² 5f ¹ 6d ¹⁰ 7p ¹					
57-70 lanthanoids 鑭系元素	58 鑑 La lanthanum 138.91 [Xe]6s ² 4f ¹ 5d ¹	59 鑑 Ce cerium 140.12 [Xe]6s ² 4f ¹ 5d ¹	60 鑑 Pr praseodymium 140.91 [Xe]6s ² 4f ¹ 5d ¹	61 鑑 Nd neodymium 144.24 [Xe]6s ² 4f ¹	62 鑑 Pm promethium [145] [Xe]6s ² 4f ¹	63 鑑 Eu europium 150.36 [Xe]6s ² 4f ⁷	64 鑑 Gd gadolinium 151.96 [Xe]6s ² 4f ⁷	65 鑑 Tb terbium 157.25 [Xe]6s ² 4f ⁹	66 鑑 Dy dysprosium 162.50 [Xe]6s ² 4f ¹⁰	67 鑑 Ho holmium 164.93 [Xe]6s ² 4f ¹¹	68 鑑 Er erbium 167.26 [Xe]6s ² 4f ¹²	69 鑑 Tm thulium 168.93 [Xe]6s ² 4f ¹³	70 鑑 Yb ytterbium 173.04 [Xe]6s ² 4f ¹⁴	57 鑄 Ac actinium [227] [Rn]7s ² 6d ¹	90 钷 Th thorium 232.04 [Rn]7s ² 6d ¹	91 钷 Pa protactinium 231.04 [Rn]7s ² 5f ⁶ d ¹	92 钷 U uranium 238.03 [Rn]7s ² 5f ⁶ d ¹	93 钷 Pu neptunium [237] [Rn]7s ² 5f ⁶ d ¹	94 钷 Am americium [243] [Rn]7s ² 5f ⁶ d ¹	95 钷 Cm curium [247] [Rn]7s ² 5f ⁶ d ¹	96 钷 Bk berkelium [247] [Rn]7s ² 5f ⁶ d ¹	97 钷 Cf californium [251] [Rn]7s ² 5f ⁶ d ¹	98 钷 Einsteinium einsteiniun [285] [Rn]7s ² 5f ⁶ d ¹	99 钷 Fm fermium [289] [Rn]7s ² 5f ⁶ d ¹	100 钷 Md mendelevium [258] [Rn]7s ² 5f ⁶ d ¹	101 钷 No nobelium [259] [Rn]7s ² 5f ⁶ d ¹	102 钷 Es tennessine [294] [Rn]7s ² 5f ⁶ d ¹
actinoids 鋼系元素	89 鑄 Ac actinium [227] [Rn]7s ² 6d ¹	90 钷 Th thorium 232.04 [Rn]7s ² 6d ¹	91 钷 Pa protactinium 231.04 [Rn]7s ² 5f ⁶ d ¹	92 钷 U uranium 238.03 [Rn]7s ² 5f ⁶ d ¹	93 钷 Pu neptunium [237] [Rn]7s ² 5f ⁶ d ¹	94 钷 Am americium [243] [Rn]7s ² 5f ⁶ d ¹	95 钷 Cm curium [247] [Rn]7s ² 5f ⁶ d ¹	96 钷 Bk berkelium [247] [Rn]7s ² 5f ⁶ d ¹	97 钷 Cf californium [251] [Rn]7s ² 5f ⁶ d ¹	98 钷 Einsteinium einsteiniun [285] [Rn]7s ² 5f ⁶ d ¹	99 钷 Fm fermium [289] [Rn]7s ² 5f ⁶ d ¹	100 钷 Md mendelevium [258] [Rn]7s ² 5f ⁶ d ¹	101 钷 No nobelium [259] [Rn]7s ² 5f ⁶ d ¹	102 钷 Es tennessine [294] [Rn]7s ² 5f ⁶ d ¹													

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Appendices

Appendix A

Too Big to Fit

A.1 Appendix Tips

The *appendix* package provides *appendices* environment that renames each chapter to Appendix A, Appendix B, etc. Similarly, sections are renamed to A.1, A.2, etc. respectively.

A.2 Embedded fonts in PDF

Here is an example of PDF file generated by L^AT_EX. We use command tool *pdffonts* to examine embedded fonts:

1	name	type	encoding	emb	sub	uni	object	ID
3	TVICFK+Tinos	CID TrueType	Identity-H	yes	yes	yes	5	0
	XYTJRZ+AdobeSongStd-Light-Identity-H	CID Type 0C	Identity-H	yes	yes	no	7	0
5	NJETOY+Tinos-Italic	CID TrueType	Identity-H	yes	yes	yes	9	0
	VMQFJA+Tinos-Bold	CID TrueType	Identity-H	yes	yes	yes	15	0
7	ILVYSG+NotoSansHans-Bold-Identity-H	CID Type 0C	Identity-H	yes	yes	yes	20	0
	HEDEEX+migu-1m-regular	CID TrueType	Identity-H	yes	yes	yes	50	0
9	KQTNVZ+CMSSY10	Type 1C	Builtin	yes	yes	no	55	0

Listing A.1: L^AT_EX 内嵌字体

A.3 pgfplotstable template

```

1 \begin{table}[tbp]
2   \centering
3   \pgfplotstabletypeset[ multicolumn names, % allows
4     to have column header name col sep=comma, % the separator in our
5     .csv file
6     display columns/0/.style={ % numbering starts at 0
7       column name=$Ampere$, % header name of first column
8       column type={S},string type % use siunitx for formatting
9     }, display columns/1/.style={ column name=$Voltage$, column
10      type={S},string type }, display columns/2/.style={ column
11      name=$Energy$, column type={S},string type }, every head
12      row/.style={ before row=\toprule}, % have a rule at top
13      after row={\si{\ampere} & \si{\volt} & \si{joule} \\ % the
14      siunitx units seperated by & \midrule % rule under units
15      }, every last row/.style={ after row=\bottomrule % rule at
16      bottom }, ]{pgfplotstable.csv} % filename/path to file
17   \caption{Table automation from .csv file.}
18   \label{table-automation-from-csv}
19 \end{table}

```

Listing A.2: pgfplotstable template

```

1 \begin{figure}[!h]
2   \centering
3   \begin{tikzpicture}
4     \begin{axis}
5       width = \linewidth, % Scale the plot to \linewidth
6       grid = major, grid style = dashed,
7       xlabel = Voltage \$U\$, ylabel = Currency \$I\$, % Set the labels
8       x unit = \si{\volt}, y unit = \si{\ampere}, % Set the respective units
9       axis lines = left % only display the left and bottom axes
10      legend style = { at = {(0.5,-0.2)}, anchor = north }, % Put
11      the legend below the plot x tick label style = { rotate =
12      90, anchor = east } %
13      Display labels sideways ]
14      % add a plot from table; you select the columns by using the
15      % actual column header name in the .csv file
16      \addplot table[x=value 1,y=value 2,col
17      sep=comma]{pgfplots.csv}; \legend{\$U\$ - \$I\$}
18      % add another plot
19      \addplot {x^2 - 2*x + 1}; % add a tailing semicolon
20      \addlegendentry{\$x^2 - 2x + 1\$} % use addlegendentry instead
21      of legend
22      \end{axis}
23   \end{tikzpicture}
24   \caption{pgfplots by table csv file}
25   \label{fig:pgfplots-by-table-csv-file}
26 \end{figure}

```

Listing A.3: pgfplots template

A.4 missTime

```

#!/bin/bash
2  if [[ "$1" = @(-h|--help) ]]
4  then
5    printf 'Usage: bash missTime [<refr-Y/N> [<number-of-test> [<input-file>]]]\n
6 refr-Y/N: \t\trefresh or not (default: Y).
7 number-of-test: \t\tnumber of tests (default: 5).
8 input-file: \t\tfile contains the log.\n
9 bash missTime y 2 input.raw
10 cclog hpc access 5m | grep -E "TCP_HIT.*iosapps.apple.com.*headers=" | tail -2
   | bash missTime\n'

12  exit 0
13 fi
14
15 _refr_opt=${1:-Y}
16 if [[ ! "$_refr_opt" =~ ^[YyNn]$ ]]
17 then
18   printf '%s: Y/y/N/n expected!\n' "$1"
19   exit 1
20 fi
21
22 _num_of_tests=${2:-5}
23 if [[ ! "$_num_of_tests" =~ ^[0-9]*$ ]]
24 then
25   printf '%s: integer expected!\n' "$_num_of_tests"
26 fi
27
28 _infd=0; [[ -f "$3" ]] && exec {_infd}< "$3"
29
30 read -r _ip _ <<(ip -4 -o addr show scope global dev bond0) ; _ip="${_ip%/*}"
31
32 _headers_regex=$'^\^~\$headers=\'.*\')@|\#(\^\' #'
33 _https_regex='^https://'
34 _refr_port="770"
35
36 _log_dir="${HOME}/logs-missTime"
37 mkdir -p "${_log_dir}"
38 for f in *.log; do mv "$f" "${_log_dir}"/" 2>/dev/null; done
39
40 while IFS=$' \t\n' read -p "Log expected:" -u "${_infd}" -r line
41 do
42   mapfile -t _log_array <<( awk -F'[:space:]'@|{in|out}#\|\([[:space:]]*\' { for
43     (i=1; i<=NF; ++i) print $i; } << "$line" )
44   _std_log="${_log_array[0]}"; _inr_log="${_log_array[1]}"
45   [[ "${_log_array[2]}" ]] && _ext_log="${_log_array[2]}"
46
47   read -ra _std_array << "$_std_log"; _log_time="${_std_array[0]}"; _url="${_
48   _std_array[6]}"
49
50   if [[ ! "$_inr_log" =~ $_headers_regex ]]
51   then
52     printf '%s: log format error.\n' "$_log_time"
53     continue
54   fi
55   tmp_headers="${BASH_REMATCH[1]}@#(" _headers_array=()
56   while [[ $tmp_headers ]]
57   do
58     _headers_array+=(" ${tmp_headers%%\n}@|\#\(\*)")
59     tmp_headers="${tmp_headers#\n}@|\#\(\*)"
60   done; unset tmp_headers
61
62   IFS=':' read -r _scheme _ _host _uri << "$_url"
63   if [[ "$_scheme" == "https" ]]
64   then
65     _protocol_port=443
66   else
67     _protocol_port=80
68   fi
69   _resolve="${_host}:$_protocol_port:$_ip"
70
71   for f in full real; do declare "_f="${_log_time}-$_num_of_tests-$f.log"; done
72   for f in "${!full[@]}"; do echo -n> "$f"; done
73   {
74     printf -- ##### missTime #####
75     printf 'HN:\n$IP:\nLOG:\nRefr:\nTest:\nt%$n\n' "$(hostname)" "$_ip"
76     printf '%s\n' "$_log_time" "$_refr_opt" "$_num_of_tests"
77     printf 'cclog:\n$%n\n' "${line}"
78     printf 'standard part:\n$%n\ninternal part:\n$%n\n' "$_std_log" "$_inr_log"
79     [[ "$_ext_log" ]] && printf 'external part:\n$%n\n' "$_ext_log"
80     printf 'curl -kS\ \\n'; printf -- '-H \'%s\' \\n' "${_headers_array[@]}"
81     printf '-- $'-H \'x-c3-debug:enabled\' \\n--resolve \'%s\' \\n\'%s\\n\' "$_
82     _resolve" "$_url"\ '#'
83     printf 'curl -kS\ \' ; printf -- '-H %q \' "${_headers_array[@]}\' ; printf -- '-H %
84     q --resolve %q\'\n' "x-c3-debug:enabled" "$_resolve" "$_url"
85   } | tee -a "${!full[@]}"
86
87   _headers_array=( "${_headers_array[@]#/H}" )
88   printf ''> "$curl-reply.log"
89   ( set -x; curl -kS\ "${_headers_array[@]}" -H "x-c3-debug:enabled" --resolve "$_
90   _resolve" "$_url" ; ) 2>&1 ) | tee -a "${!full[@]}" "curl-reply.log"

```

Listing A.4: missTime Line by Line

```

1  [[ "$_refr_opt" == [Nn] ]] && continue
2
3  declare -A _reply_array=()
4  while IFS=':' read -r key value
5  do
6    [[ "$key" && "$key" != [:space:] ]] && "$key" != + ]] || continue
7    _reply_array[$key]=${value%$'\r'}
8  done < "curl-reply.log"
9
10 {
11   # for key in "${!_reply_array[@]}"; do printf '%s: %s\n' "$key" "${_reply_array[
12     $key]}"; done ; printf '\n'
13   printf 'X-Cache: %s\n' "${_reply_array[X-Cache]}" ; printf 'X-Cache-Remote: %s\n'
14   "${_reply_array[X-Cache-Remote]}" ; printf 'CC_CACHE: %s\n' "${_reply_array[
15     CC_CACHE]}"
16 } | tee -a "${_full}"
17
18 shopt -q extglob; _extglob_set=? ; (( _extglob_set )) && shopt -s extglob
19 _delete_url=${_reply_array[X-True-Cache-Key]##http?($s):://}
20 (( _extglob_set )) && shopt -u extglob
21
22 [[ "${_scheme}" == "https" ]] && _delete_url=${_delete_url//:/443}
23 _refr_url=http://127.0.0.1:${_refr_port}/delete/${_delete_url}
24 printf 'refr url: %s\n' "${_refr_url}" | tee -a "${_full}"
25
26 for i in $(seq 1 ${_num_of_tests})
27 do
28   printf -- '---%sth---\n' "${i}" | tee -a "${_full}" "${_real}"
29
30   printf 'refr code: ' | tee -a "${_full}"
31   curl -ksSo /dev/null "%{response_code}" -H "User-Agent: DataDelete" "${_
32     _refr_url}" | tee -a "${_full}"
33   printf '\n' | tee -a "${_full}"
34
35   sleep 0.05s
36   { time curl -kLSvO /dev/null "${_headers_array[@]}" -H "x-c3-debug:enabled" --
37     resolve "${_resolve}" "${_url}" 2>&1 | awk 'BEGIN {IGNORECASE=1}; /[:space
38     :].*[-_]cache:/ {print substr($0, 3)} ; } 2>&1 | tee -a "${_full}"
39
40   ed -s "${_full}" <<< '$'-3d\nw'
41   ed -s "${_full}" <<< '$'-3,-2p' >> "${_real}"
42   done
43   printf '%s\n' '1d' w | ed -s "${_full}" # sed -i -e '1d' "${_full}"
44
45 done
46 rm -f "curl-reply.log"

```

Listing A.5: missTime Line by Line

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Postscript

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