

Runtime Analysis for Vector:

Code	Line Cost	# Times Executes	Total Cost
<code>courses = empty vector of Course</code>	1	1	1
<code>Open the file with filename</code>	1	1	1
<code>If the file cannot be opened, print an error message and return the empty vector</code>	1	1	1
<code>For each line in the file:</code>	1	n	n
<code>Split the line with commas</code>	1	n	n
<code>Parse the line into courseId, courseName (first two parts of the line)</code>	1	n	n
<code>Put rest of the split parts as prerequisites</code>	1	n	n
<code>If courseId or courseName is empty, print an error message and skip to the next line</code>	1	n	n
<code>Create a Course object with the parsed values and add it to the courses vector</code>	1	n	n
<code>Close the file</code>	1	1	1
<code>Return the courses vector</code>	1	1	1
Total Cost			$6n + 5$
Runtime			$O(n)$

Runtime Analysis for Hash:

Code	Line Cost	# Times Executes	Total Cost
<code>courses = empty hash table of Course</code>	1	1	1
<code>Open the file with filename</code>	1	1	1
<code>If the file cannot be opened, print an error message and return the empty hash table</code>	1	1	1
<code>For each line in the file:</code>	1	n	n
<code>Split the line with commas</code>	1	n	n
<code>Parse the line into courseId, courseName (first two parts of the line)</code>	1	n	n
<code>Put rest of the split parts as prerequisites</code>	1	n	n
<code>If courseId or courseName is empty, print an error message and skip to the next line</code>	1	n	n
<code>Create a Course object with the parsed values and add it to the courses hash table using courseId as the key</code>	1	n	n

Code	Line Cost	# Times Executes	Total Cost
Close the file	1	1	1
Return the courses hash table	1	1	1
Total Cost			$6n + 5$
Runtime			$O(n)$

Runtime Analysis for Tree:

Code	Line Cost	# Times Executes	Total Cost
<code>course_tree = empty CourseTree</code>	1	1	1
Open the file with filename	1	1	1
If the file cannot be opened, print an error message and return the empty tree	1	1	1
For each line in the file:	1	n	n
Split the line with commas	1	n	n
Parse the line into courseId, courseName (first two parts of the line)	1	n	n
Put rest of the split parts as prerequisites	1	n	n
If courseId or courseName is empty, print an error message and skip to the next line	1	n	n
Create a Course object with the parsed values	1	n	n
<code>course_tree = Call addCourse(course_tree, course)</code>	n	n	n^2
Close the file	1	1	1
Return the course_tree	1	1	1
Total Cost			$n^2 + 6n + 5$
Runtime			$O(n^2)$

Advantages and Disadvantages

Vector:

Vectors perform well when reading data from a file and creating a vector with that data. However, when it comes to basic lookups, vectors have a time complexity of $O(n)$, which can lead to poor performance, especially when searching for prerequisites. Vectors are a good choice for small datasets due to their simplicity and ease of use.

Hash Table:

Hash tables also excel in reading data from a file and creating a hash table. They offer fast and easy access to data with an average lookup time complexity of $O(1)$. However, sorting data in a hash table can be challenging since it lacks a natural order. Hash tables are well-suited for scenarios where quick data retrieval is essential, but sorting is not a primary concern.

Tree:

On the other hand, trees performed the least efficiently when reading data from a file. While a balanced tree can achieve an average lookup time complexity of $O(\log n)$, our data may not be suitable for a tree structure, resulting in a worse-case $O(n)$ time complexity. This is because we traverse each line in the file, resulting in an overall time complexity of $O(n^2)$. However, trees shine when it comes to sorting data, as they can achieve sorting in $O(n \log n)$, which is faster than vectors and hash tables ($O(n^2)$). Trees are a good choice when sorting is a primary requirement.