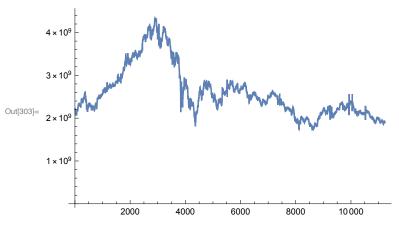
```
In[280]:= (* Fits to log stable below. Starting
           with 120d worth of data from WETH/USDC .... *)
  In[2]:= (* Import from csv *)
  In[3]:= Directory[]
 Out[3]= /Users/personal
In[281]:= Module[{directory = SystemDialogInput["Directory"]}},
        If[directory =!= $Canceled, SetDirectory[directory]]]
Out[281]= /Users/personal/Desktop/note7/points
  _{	ext{In}[5]:=} (* Go back and download WETH/USDC data from cron. Look at that *)
in[294]:= tblWethUsdc120d = Import["120/data-1626472963_weth-usdc-twap.csv"]
          \{\{, \text{ timestamp, twap}\}, \{0, 1.61878 \times 10^9, 2.23957 \times 10^9\},
           \{1, 1.61878 \times 10^9, 2.24054 \times 10^9\}, \{2, 1.61878 \times 10^9, 2.23817 \times 10^9\},
           \{3, 1.61878 \times 10^9, 2.25083 \times 10^9\}, \{4, 1.61878 \times 10^9, 2.25656 \times 10^9\}, \dots 11259 \dots \}
           \{11266, 1.62647 \times 10^9, 1.91147 \times 10^9\}, \{11267, 1.62647 \times 10^9, 1.90971 \times 10^9\},
Out[294]=
           \{11268, 1.62647 \times 10^9, 1.90596 \times 10^9\}, \{11269, 1.62647 \times 10^9, 1.90286 \times 10^9\},
           \{11270, 1.62647 \times 10^9, 1.90034 \times 10^9\}, \{11271, 1.62647 \times 10^9, 1.89838 \times 10^9\}\}
         large output
                       show less
                                   show more
                                                 show all
                                                            set size limit...
In[295]:= Length [tblWethUsdc120d]
Out[295]= 11271
In[296]:= FromUnixTime[tblWethUsdc120d[[2]][[2]]]
        Sun 18 Apr 2021 16:50:52 GMT-4.
Out[296]=
In[299]:= FromUnixTime[tblWethUsdc120d[[Length[tblWethUsdc120d]]][[2]]]
        Fri 16 Jul 2021 18:01:02 GMT-4.
Out[299]=
In[300]:= twapsWethUsdc120d =
        Table[tblWethUsdc120d[[i]][[3]], {i, 2, Length[tblWethUsdc120d]}]
```

In[302]:= (\* Same issues here for early data as UNI/WETH. Cut off first 40 elements \*)
twapsWethUsdc120dFiltered =

Table[twapsWethUsdc120d[[i]], {i, 40, Length[twapsWethUsdc120d]}]

In[303]:= ListLinePlot[twapsWethUsdc120dFiltered, PlotRange → All]



In[304]:= FromUnixTime[tblWethUsdc120d[[40]][[2]]]

Out[304]= Mon 19 Apr 2021 17:14:44 GMT-4.

In[305]:= FromUnixTime[tblWethUsdc120d[[Length[twapsWethUsdc120dFiltered]]][[2]]]

Out[305]= Fri 16 Jul 2021 10:27:07 GMT-4.

In[16]:= (\* Calculate the rs ... \*)

```
0.000559858, -0.00092094, -0.00154871, -0.000905547, -0.000584311,
         (\cdots 11210\cdots), -0.000975245, -0.000888855, -0.00068242, -0.000128976,
Out[306]=
         -0.00026784, -0.000921873, -0.00196508, -0.00162411, -0.00132945, -0.00102799
                                                  set size limit...
                                        show all
       large output
                   show less
                             show more
In[307]:= rsWethUsdc120dFiltered[[100]]
Out[307]= -0.00443888
In[308]:= ListLinePlot[rsWethUsdc120dFiltered, PlotRange → All]
      0.10
      0.05
Out[308]=
                                        8000
      -0.05
      -0.10
In[309]:= Length[rsWethUsdc120dFiltered]
Out[309]= 11 230
In[311]:= edistWethUsdc120dFiltered = EstimatedDistribution[rsWethUsdc120dFiltered,
        StableDistribution[1, aWU120d, bWU120d, locWU120d, scaleWU120d]]
Out[311] = StableDistribution [1, 1.41834, -0.0286247, -6.93658 \times 10^{-6}, 0.00140585]
In[312]:= FromUnixTime[tblWethUsdc120d[[5000]][[2]]]
Out[312]=
       Fri 28 May 2021 06:16:07 GMT-4.
In[313]:= FromUnixTime[tblWethUsdc120d[[Length[tblWethUsdc120d]]][[2]]]
       Fri 16 Jul 2021 18:01:02 GMT-4.
Out[313]=
 In[25]:= (* Seems a good place to estimate k
       values would be 1h candles (from note-7.nb) *)
 In[26]:=
 In[27]:= (* Some concrete numbers below in terms of funding rate ... *)
```

In[306]:= rsWethUsdc120dFiltered = Differences[Log[twapsWethUsdc120dFiltered]]

```
\ln[28] = (* What does e^{mu} * T + sig * (T/a)^{(1/a)} * F^{-1}(1-alpha)
       translate to for ETH/USDC fit? *)
 ln[29]:= (* And if d = f * e^{mu * T + sig * (T/a)^{(1/a)} * F^{-1}(1-alpha)},
      what f value should we use across the board
        to get k max interest rates on order of 1-10% daily? *)
 In[314]:= edistWethUsdc120dFiltered
out_{314} StableDistribution 1, 1.41834, -0.0286247, -6.93658 \times 10<sup>-6</sup>, 0.00140585
In[318]:= InverseCDF[edistWethUsdc120dFiltered, 0.99]
Out[318]= 0.0127859
In[320]:= InverseCDF[edistWethUsdc120dFiltered, 0.95]
Out[320]= 0.00460265
In[321]:= InverseCDF[edistWethUsdc120dFiltered, 0.90]
Out[321]= 0.00300704
In[322]:= Exp[InverseCDF[edistWethUsdc120dFiltered, 0.95]]
Out[322]= 1.00461
In[323]:= Exp[InverseCDF[edistWethUsdc120dFiltered, 0.99]]
Out[323]= 1.01287
 IN[37]:= (* Produce 1 hour candles from 10min cron data to use in k analysis ... *)
In[324]:= twapsWethUsdc120dFiltered1HourCandle = Table[
        twapsWethUsdc120dFiltered[[i]], {i, 1, Length[twapsWethUsdc120dFiltered], 6}]
In[325]:= ListLinePlot[twapsWethUsdc120dFiltered1HourCandle]
      4 \times 10^{9}
      3 \times 10^{9}
Out[325]=
      2 \times 10^{9}
      1 \times 10^{9}
                     500
                                 1000
                                             1500
In[326]:= rsWethUsdc120dFiltered1HourCandle =
```

Differences[Log[twapsWethUsdc120dFiltered1HourCandle]]

edistWethUsdc120dFiltered1HourCandle

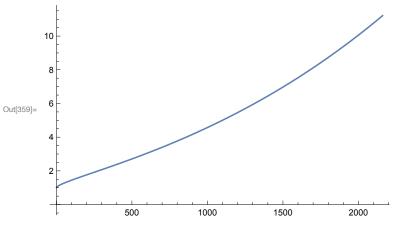
Out[338]= StableDistribution[1, 1.59768, -0.0971292, -0.000157254, 0.00790013]

(\* Not bad, especially on sigma and alpha ... \*)

 $_{\text{In[43]:=}}$  (\* Interesting ... compound less on the funding payments, have more leeway. How does that make sense wrt inverse cdf exponentiation? \*)

```
In[334]:= Plot[{InverseCDF[edistWethUsdc120dFiltered, x],
         InverseCDF[edistWethUsdc120dFiltered1HourCandle, x],
         InverseCDF[edistWethUsdc120dFiltered4HourCandle, x]},
       \{x, 0, 1.0\}, PlotRange \rightarrow \{-0.04, 0.04\}]
       0.04
       0.02
Out[334]=
                                       0.6
                                                8.0
                                                          1.0
      -0.02
In[335]:= Plot[{, InverseCDF[edistWethUsdc120dFiltered1HourCandle, x]},
       \{x, 0, 1.0\}, PlotRange \rightarrow \{-0.04, 0.04\}]
       0.04
       0.02
Out[335]=
                   0.2
                                       0.6
                                                8.0
                                                          1.0
      -0.02
In[336]:= InverseCDF[edistWethUsdc120dFiltered1HourCandle, 0.99]
Out[336]= 0.0459063
In[337]:= InverseCDF[edistWethUsdc120dFiltered, 0.99]
Out[337]= 0.0127859
In[339]:= Exp[0.012785934108095686`]
Out[339]= 1.01287
 ln[50] = (* Hmmm, so maybe plot e^(mu * T + sig * (T/a)^(1/a) * F^{-1}(1-alpha)) as a
       function of update times T. What does this tell us vs d we're looking for? *)
In[340]:= edistWethUsdc120dFiltered1HourCandle
Out[340]= StableDistribution[1, 1.5843, -0.0493885, -0.000101694, 0.0072772]
```

```
In[52]:= (* Define mu, sig functions for exponential term in d *)
 In[53]:= mu[a_, loc_] := loc
 ln[54]:= sig[a_, scale_] := scale / (1/a)^(1/a)
 In[55]:= (* Apply to our case *)
In[342]:= muWethUsdc120dFiltered1HourCandle =
       mu[1.5843003587383822`, -0.00010169418797317535`]
Out[342]= -0.000101694
In[343]:= sigWethUsdc120dFiltered1HourCandle =
       sig[1.5843003587383822`, 0.00727719566405363`]
Out[343]= 0.00972972
In[341]:= aWethUsdc120dFiltered1HourCandle = 1.5843003587383822`
Out[341]= 1.5843
In[345]:= edistWethUsdc120dFiltered1HourCandleNormalized =
       StableDistribution[1, aWethUsdc120dFiltered1HourCandle, 0, 0, 1]
Out[345]= StableDistribution[1, 1.5843, 0, 0, 1]
In[346]:= InverseCDF[edistWethUsdc120dFiltered1HourCandleNormalized, 0.90]
Out[346]= 1.99592
In[347]:= InverseCDF[edistWethUsdc120dFiltered1HourCandleNormalized, 0.95]
Out[347]= 2.84713
In[348]:= InverseCDF[edistWethUsdc120dFiltered1HourCandleNormalized, 0.99]
Out[348]= 6.48811
In[349]:= factorWethUsdc120dFiltered1HourCandle[t_, alpha_] :=
       Exp[muWethUsdc120dFiltered1HourCandle * t + sigWethUsdc120dFiltered1HourCandle *
           (t/aWethUsdc120dFiltered1HourCandle) ^ (1/aWethUsdc120dFiltered1HourCandle) *
           InverseCDF[edistWethUsdc120dFiltered1HourCandleNormalized, 1 - alpha]
In[350]:= factorWethUsdc120dFiltered1HourCandle[1, 0.01]
Out[350]= 1.04824
 <code>In[65]:= (* TODO: Redo this analysis! ... Below is in line with 4 hour candle above :) *)</code>
In[351]:= factorWethUsdc120dFiltered1HourCandle[4, 0.01]
Out[351]= 1.11947
In[352]:= factorWethUsdc120dFiltered1HourCandle[8, 0.01]
Out[352]= 1.19079
```



(\* So takes on order of 2 months to
 reach a 5x price cap on price bracket amount \*)

```
ln[360]:= Plot[Exp[(t)^{(1/1.5)}], \{t, 0, 3\}]
      8
Out[360]=
 In[77]:= (* This is where caps become very good :) *)
In[361]:= Plot[factorWethUsdc120dFiltered1HourCandle[t, 0.05], {t, 1, 24 * 30 * 12}]
      200
      150
Out[361]=
      100
      50
                  2000
                             4000
                                        6000
                                                   8000
 ln[79]:= (* Plot k AND (1-k)^m where m is diff depending on number of times we compound *)
 ln[80]:= (* Assume k min is determined by factor value
       at 95% confidence for different number of periods T *)
In[357]:= dmin95WethUsdc120dFiltered1HourCandle[t_] :=
       factorWethUsdc120dFiltered1HourCandle[t, 0.05]
In[358]:= kmin95WethUsdc120dFiltered1HourCandle[t_] :=
       (1-1/dmin95WethUsdc120dFiltered1HourCandle[t])/2
 In[83]:= (* Look at different time periods ... 1 (1h),
      4 (4h), 6 (6h), 8 (8h), 12 (12h), 24 (1d), 168 (7d) *)
In[362]:= kmin95T1hWethUsdc120dFiltered1HourCandle =
       kmin95WethUsdc120dFiltered1HourCandle[1]
Out[362]= 0.0102032
```

```
In[363]:= kmin95T4hWethUsdc120dFiltered1HourCandle =
       kmin95WethUsdc120dFiltered1HourCandle[4]
Out[363]= 0.0240508
In[364]:= kmin95T6hWethUsdc120dFiltered1HourCandle =
       kmin95WethUsdc120dFiltered1HourCandle[6]
Out[364] = 0.0308052
In[365]:= kmin95T8hWethUsdc120dFiltered1HourCandle =
       kmin95WethUsdc120dFiltered1HourCandle[8]
Out[365]= 0.0366706
In[366]:= kmin95T12hWethUsdc120dFiltered1HourCandle =
       kmin95WethUsdc120dFiltered1HourCandle[12]
Out[366]= 0.0467734
In[367]:= kmin95T1dWethUsdc120dFiltered1HourCandle =
       kmin95WethUsdc120dFiltered1HourCandle[24]
Out[367]= 0.0703214
In[368]:= kmin95T7dWethUsdc120dFiltered1HourCandle =
       kmin95WethUsdc120dFiltered1HourCandle[168]
Out[368]= 0.199422
In[369]:= (* Interesting ... around minimum of 3.26% every 6 hr
       compounding. Can work with that to have some buffer in event bad fit *)
In[370]:= drawDownMin95WethUsdc120dFiltered1HourCandle[t_, m_] :=
       1 - (1 - kmin95WethUsdc120dFiltered1HourCandle[m]) ^ (Floor[t/m])
```

```
In[371]:= Plot[{drawDownMin95WethUsdc120dFiltered1HourCandle[t, 1],
        drawDownMin95WethUsdc120dFiltered1HourCandle[t, 4],
        drawDownMin95WethUsdc120dFiltered1HourCandle[t, 6],
        drawDownMin95WethUsdc120dFiltered1HourCandle[t, 8],
        drawDownMin95WethUsdc120dFiltered1HourCandle[t, 12],
        drawDownMin95WethUsdc120dFiltered1HourCandle[t, 24],
        drawDownMin95WethUsdc120dFiltered1HourCandle[t, 168]}, {t, 1, 24 * 30}]
     1.0
     8.0
     0.6
Out[371]=
     0.4
                   100
                                200
                                            300
                                                         400
 _{ln[94]:=} (* Should like compare ratio of price bracket to d^(t/m). When set m for d,
      setting point at which d^m =
       price bracket[m].. But d is NOT an interest rate... k = (1-1/d)/2 makes this
```

interesting in terms of traders view on draw down to their OI ... \*) |n|95|= (\* Plot the actual interest rates seen per day for different values of m ★)

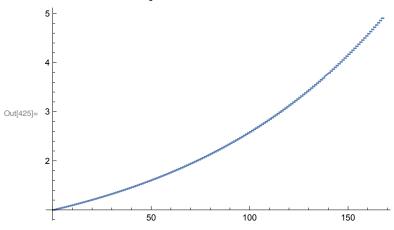
```
In[374]:= Plot[drawDownMin95WethUsdc120dFiltered1HourCandle[24, m], {m, 1, 24}]
      0.20
Out[374]=
      0.10
                                      15
                                                20
In[375]:= drawDownMin95WethUsdc120dFiltered1HourCandle[24, 1]
Out[375]= 0.218183
In[376]:= drawDownMin95WethUsdc120dFiltered1HourCandle[24, 4]
Out[376]= 0.135901
In[377]:= drawDownMin95WethUsdc120dFiltered1HourCandle[24, 8]
Out[377] = 0.106027
In[378]:= drawDownMin95WethUsdc120dFiltered1HourCandle[24, 12]
Out[378]= 0.091359
In[101]:= (* Floor is making this visual
        difficult. Make continuous for plot purposes ... *)
In[379]:= drawDownMin95WethUsdc120dFiltered1HourCandleContinuous[t_, m_] :=
       1 - (1 - kmin95WethUsdc120dFiltered1HourCandle[m]) ^ <math>(t/m)
In[103]= (* Below is min funding rate required extended to per day rate,
      if apply funding payment every m hours *)
```

```
In[380]= Plot[drawDownMin95WethUsdc120dFiltered1HourCandleContinuous[24, m],
       \{m, 1, 24\}, PlotRange \rightarrow \{0.05, 0.25\}]
     0.25
     0.20
Out[380] = 0.15
     0.10
      (* TODO: generalize this plot to 3d with alpha confidence on the other axis *)
IN[105]:= (* Less we compound, smaller max DAILY funding rate needed to overcome
       price bracket changes. But more short term (<1d) we likely take *)
In[381]:= (* Generalize this for any confidence level (not just 95%) *)
in[382]:= dminWethUsdc120dFiltered1HourCandle[t_, alpha_] :=
       factorWethUsdc120dFiltered1HourCandle[t, alpha]
In[383]:= kminWethUsdc120dFiltered1HourCandle[t_, alpha_] :=
       (1-1/dminWethUsdc120dFiltered1HourCandle[t, alpha])/2
In[384]:= drawDownMinWethUsdc120dFiltered1HourCandle[t_, alpha_, m_] :=
       1 - (1 - kminWethUsdc120dFiltered1HourCandle[m, alpha]) ^ (Floor[t/m])
In[385]:= drawDownMinWethUsdc120dFiltered1HourCandleContinuous[t_, alpha_, m_] :=
       1 - (1 - kminWethUsdc120dFiltered1HourCandle[m, alpha]) ^ (t/m)
In[386]:= (* If fit to 8h compounded rate but still pay every 10min,
      how much is k? (k paid every 10 min but use 8h compounding amount) \star)
IN[387]:= (* Function to rescale k min calibrated using factor's value at
        time m in the future. But then applied over shorter time span < m *)
In[388]:= (* d_shorter^(#periods of short in long) = d_longer; m > t here *)
In[389]:= rescaledKminWethUsdc120dFiltered1HourCandle[t_, alpha_, m_] :=
       (1-1/(dminWethUsdc120dFiltered1HourCandle[m, alpha])^(t/m))/2
In[390] = rescaledKminWethUsdc120dFiltered1HourCandle[1/6, 0.05, 8]
Out[390]= 0.000792806
In[116]= (* Calculate effective funding rate after 8 hours applied every 10 min *)
```

```
ln[397] = 1 - (1 - rescaledKminWethUsdc120dFiltered1HourCandle[1/6, 0.05, 8]) ^ (6 * 8)
Out[397]= 0.0373542
| In[398]:= (* Compare with draw down applied only once every 8 hours *)
      drawDownMinWethUsdc120dFiltered1HourCandle[8, 0.05, 8]
Out[398]= 0.0366706
In[119]:= (* Looks good *)
ln[120] = (* Plot price bracket * d^(t/m) over time t *)
In[121]:= (* Look at funding rates needed over different confidence levels, to compare *)
In[402]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.01, 8]
Out[402]= 0.221594
In[403]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.05, 8]
Out[403] = 0.106027
In[404]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.10, 8]
Out[404]= 0.0756562
ln[405]:= (* Last 95 \rightarrow 99% is what ramps it up significantly *)
In[406]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.01, 1]
Out[406]= 0.42805
In[407]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.05, 1]
Out[407] = 0.218183
In[408]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.10, 1]
Out[408]= 0.158401
In[409]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.05, 24]
Out[409]= 0.0703214
In[410]:= (* Similar with rescale. See if applied every 10 min
       for 8 hour value but after 1 d, 7d, 14d what drawdown is *)
In[411]= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.05, 8]
Out[411]= 0.106027
ln[412] = 1 - (1 - rescaledKminWethUsdc120dFiltered1HourCandle[1/6, 0.05, 8]) ^ (6 * 24)
Out[412] = 0.107929
log_{log} = rescaledKminWethUsdc120dFiltered1HourCandle[1/6, 0.05, 8]
Out[413]= 0.000792806
```

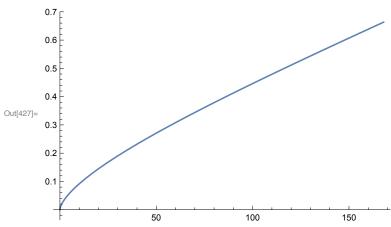
```
| In[414]:= drawDownMinWethUsdc120dFiltered1HourCandle[24 * 7, 0.05, 8]
Out[414]= 0.543678
ln[415] = 1 - (1 - rescaledKminWethUsdc120dFiltered1HourCandle[1/6, 0.05, 8]) ^ (6 * 24 * 7)
Out[415]= 0.550431
In[135]:= (* Beautiful. Anchoring at factor value at m sets funding rate to
       be min. Does compound surpass price bracket at the 8 hour mark? *)
      (* Look at rescaled draw down first to make sure consistent *)
In[416]:= rescaledDrawDownMinWethUsdc120dFiltered1HourCandle[t_, alpha_, m_, anchor_] := 1-
        (1 - rescaledKminWethUsdc120dFiltered1HourCandle[m, alpha, anchor])^(Floor[t/m])
In[417]:= rescaledDrawDownMinWethUsdc120dFiltered1HourCandle[24, 0.05, 1, 8]
Out[417]= 0.107727
In[418]:= rescaledDrawDownMinWethUsdc120dFiltered1HourCandle[24 * 7, 0.05, 1, 8]
Out[418]= 0.549717
      (* Great. 1h funding payments on 8h anchor look great *)
In[136]:= (* Look at (1 - 2k)^m over time .... Compound
       factor for different compound intervals. Assume funding
       payments applied every 1 h for simplicity with fits. *)
In[419]:= compoundFactorMinWethUsdc120dFiltered1HourCandle[t_, alpha_, m_, anchor_] :=
       (1-2*rescaledKminWethUsdc120dFiltered1HourCandle[m, alpha, anchor])^
        (Floor[t/m])
In[138]:= (* 8h payment at 95% confidence of VaR led to
        drawdown of 11% worst case due to funding. Use alpha=0.05,
     m=8. Rescaled funding st paid every 1 h *)
```

```
In[420]:= Plot[
        \{1/compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]\}, \{t, 0, 24\}
      1.20
      1.15
Out[420]=
      1.10
      1.05
                              10
                                        15
                                                  20
In[421]:= Plot[
        {compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]}, {t, 0, 24}]
      1.00
      0.95
Out[421]= 0.90
      0.85
In[422]:= drawDownMinWethUsdc120dFiltered1HourCandle[24, 0.05, 8]
Out[422]= 0.106027
\verb||n[423]| = 1 - compoundFactorMinWethUsdc120dFiltered1HourCandle[24, 0.05, 1, 8]| \\
Out[423] = 0.204281
In[424]:= (* Perfect. Draw down to OI imbalance
        should be about 2 times draw down to OI on a side *)
```



In[426]:= (\* Plot price bracket ... \*)

ln[427]:= Plot[factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1, {t, 0, 24 \* 7}]

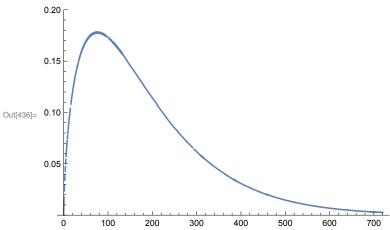


In[428]:= (\* Plot 1/compoundFactor vs price bracket \*)

```
_{\text{In}[429]:=} Plot[{factorWethUsdc120dFiltered1HourCandle[t, 0.05],
         1/compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]}, {t,
         0, 24 * 7}]
Out[429]= 3
                      50
                                     100
                                                     150
In[430]:= (* Look at the earlier times ... *)
In[431] = Plot[{factorWethUsdc120dFiltered1HourCandle[t, 0.05]},
         1/compoundFactorMinWethUsdc120dFiltered1HourCandle[t,~0.05,~1,~8]\big\},~\{t,~0,~24\}\big]
      1.25
      1.20
      1.15
Out[431]=
      1.10
      1.05
In[432]:= (* Look at later times ... *)
```

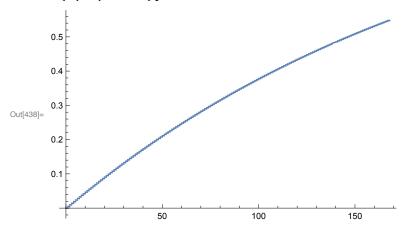
```
_{\text{In}[433]:=} Plot[{factorWethUsdc120dFiltered1HourCandle[t, 0.05],
         1/compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]}, {t,
         0, 24 * 30
      200
      150
Out[433]= 100
       50
               100
                      200
                                                          700
_{\text{In}[434]:=} (* and the product of the two to make sure decreasing over time ... *)
log_{[435]} = Plot[(factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8],
        \{t, 0, 24*7\}, PlotRange \rightarrow \{0, 0.2\}
      0.20
      0.15
Out[435]= 0.10
      0.05
```

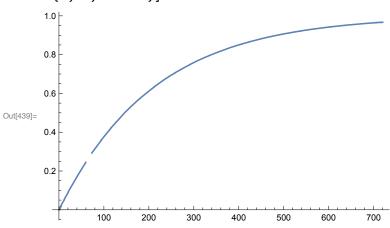
In[436]:= Plot[ (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) \* compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8],  $\{t, 0, 24*30\}, PlotRange \rightarrow \{0, 0.2\}$ 



In[437]:= (\* Compare with draw down over time \*)

In[438]:= Plot[{rescaledDrawDownMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]},  $\{t, 0, 24*7\}$ 

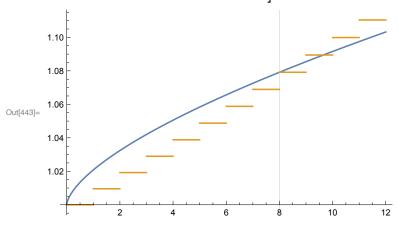




In[440]:=

In[441]:= (\* Anchor used in k is everything. What is the
 interpretation? Time when d^m is exactly equal to first term in
 price bracket[m]. Then d^m surpasses greatly in size as m → infty \*)

In[442]:= (\* So look at 1/compoundFactor vs price factor BEFORE hit the anchor to
 make sure 1/compoundFactor is less but we cross at anchor time ... \*)



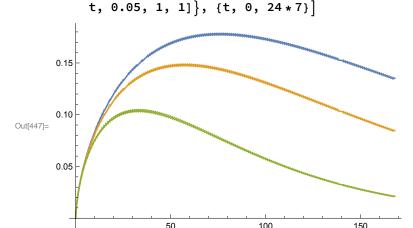
(\* Perfect. Interpretation is correct. \*)

(\* Then product of price bracket and compound factor is playing catch up for the first 8 hours in order to get to point where decreasing over time? \*)

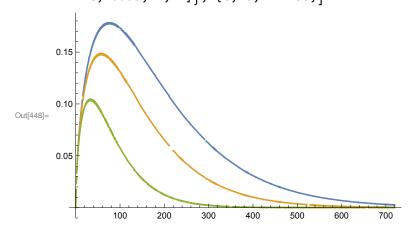
(\* Look at different price bracket
VaR growth over time without compound factor \*)

```
In[446]:= Plot[{ (factorWethUsdc120dFiltered1HourCandle[t, 0.10] - 1),
        (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1),
        factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1), {t, 0, 24 * 7}
      2.0
      1.5
Out[446]=
      1.0
      0.5
                     50
                                   100
                                                 150
log_{[445]:=} Plot[{(factorWethUsdc120dFiltered1HourCandle[t, 0.10] - 1),
        (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1),
        factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1, {t, 0, 24 * 30}
      12
      10
Out[445]=
                          300
                                 400
                                        500
      (* Try product of price bracket and compound
        factor for different anchor times in k calibration \dots *)
```

```
In[447]:= Plot[{ (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) *
        compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8],
       (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) *
        compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 4],
       (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) *
        compoundFactorMinWethUsdc120dFiltered1HourCandle[
```



In[448]= Plot[{ (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) \* compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8], (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) \* compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 4], (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) \* compoundFactorMinWethUsdc120dFiltered1HourCandle[ t, 0.05, 1, 1] $\}$ , {t, 0, 24 \* 30}]



In[449]:= (\* So most VaR to passive holders happens over shorter term when imbalance first created. Longer users hold positions and imbalance gets drawn down through funding, the more VaR gets curbed and eventually brought to zero \*)

100

200

```
In[451]:=
_{
m In[452]:=} (* What if we underestimate funding rate needed? As in should have used alpha=
       0.01 instead of alpha=0.05? what does this do to VaR over time? *)
In[453]:= Plot[{ (factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8],
        (factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 4],
        (factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[
          t, 0.05, 1, 1]\}, {t, 0, 24 * 7}]
     0.5
     0.4
     0.3
Out[453]=
     0.2
      0.1
In[454]:= Plot[{ (factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8],
        (factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 4],
        (factorWethUsdc120dFiltered1HourCandle[t, 0.01] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[
          t, 0.05, 1, 1]\}, {t, 0, 24 * 30}]
     0.5
     0.4
     0.3
Out[454]=
     0.2
     0.1
```

700

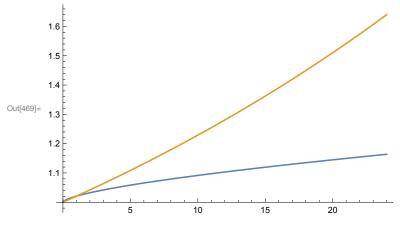
In[455]:= (\* Look at 1/compoundFactor (larger alpha than required) vs price factor BEFORE hit the anchor to see what new anchor time is  $\dots$  \*) In[456]:= Plot[{factorWethUsdc120dFiltered1HourCandle[t, 0.01], 1/compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]}, {t, 0, 12}] 1.25 1.20 1.15 Out[456]= 1.10 1.05 10 In[457]:= (\* Interesting, anchor time comes much later. Not great, but still exists ... However, VaR still seems to decrease tho, just more drawn out AND significantly higher max value/peak (about 2x for alpha=0.05). \*) In[458]:= Plot[{factorWethUsdc120dFiltered1HourCandle[t, 0.01], 1/compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]}, {t, [0, 24 \* 7]5 Out[458]= 3

150

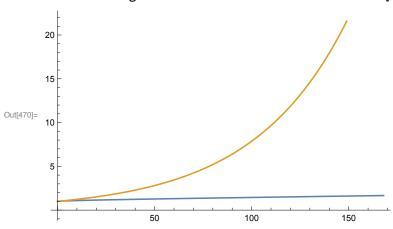
100

50

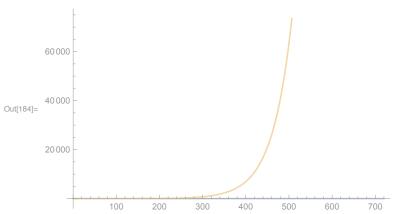
```
In[459]:= Plot[{factorWethUsdc120dFiltered1HourCandle[t, 0.01],
        1/compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8]}, {t,
        0, 24 * 30
      200
      150
Out[459]= 100
      50
              100
                     200
                           300
                                  400
                                         500
                                               600
                                                      700
ln[460]:= (* Instead of anticipated anchor of 8h, get anchor around 72h (3d). *)
In[461]:=
ln[462]:= (* What about set funding factor to not exp^{(m*t)^{1/a}}
       but \exp^{m*(t)^{(1/a)}}? What's difference in interest rate? *)
In[463]:= factorLargerWethUsdc120dFiltered1HourCandle[t_, alpha_] := Exp[
        muWethUsdc120dFiltered1HourCandle * t + sigWethUsdc120dFiltered1HourCandle * t *
           (1 / aWethUsdc120dFiltered1HourCandle) ^ (1 / aWethUsdc120dFiltered1HourCandle) *
           InverseCDF[edistWethUsdc120dFiltered1HourCandleNormalized, 1 - alpha]
In[464]:= factorLargerWethUsdc120dFiltered1HourCandle[8, 0.05]
Out[464]= 1.17932
In[465]:= factorWethUsdc120dFiltered1HourCandle[8, 0.05]
Out[465]= 1.07915
In[466]:= factorLargerWethUsdc120dFiltered1HourCandle[24, 0.05]
Out[466] = 1.6402
In[467]:= factorWethUsdc120dFiltered1HourCandle[24, 0.05]
Out[467]= 1.16366
In[468]:= (* Yea this gets out of control fast ... *)
```



 $\label{eq:local_local_local_local} $$ \inf_{factorWethUsdc120dFiltered1HourCandle[t, 0.05], $$ factorLargerWethUsdc120dFiltered1HourCandle[t, 0.05]}, $$ \{t, 0, 24 * 7\}$ ]$ 



Plot[{factorWethUsdc120dFiltered1HourCandle[t, 0.05],
 factorLargerWethUsdc120dFiltered1HourCandle[t, 0.05]}, {t, 0, 24 \* 30}]

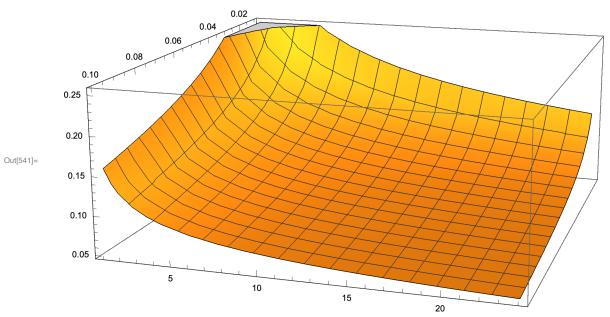


(\* We can't use the larger factor ... Actually a good preview for fits that are closer to Cauchy :/ \*)

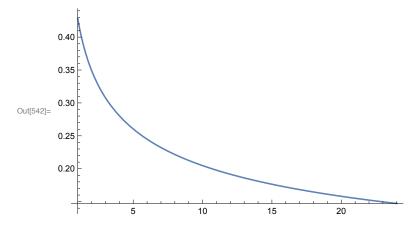
(\* Plot continuous draw down as 3d with alpha varying as well \*)

In[541]:= Plot3D[drawDownMinWethUsdc120dFiltered1HourCandleContinuous[24, a, m],

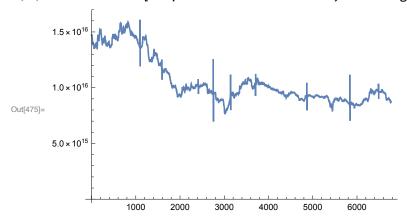
 $\{a, 0.01, 0.1\}, \{m, 1, 24\}]$ 



In[542]:= Plot[ drawDownMinWethUsdc120dFiltered1HourCandleContinuous[24, 0.01, m], {m, 1, 24}]



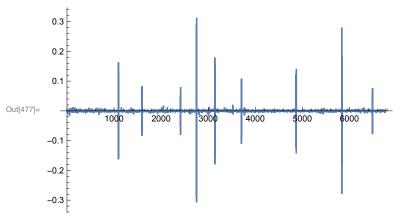
## In[475]:= ListLinePlot[twapsUniWeth120dFiltered , PlotRange → All]



## In[476]:= rsUniWeth120dFiltered = Differences[Log[twapsUniWeth120dFiltered]]

```
\{0.00192969, -0.000607667, -0.00173262, -0.000132253, -0.00086947, -0.000234575,
         0.00029493, 0.000681779, -0.000561976, -0.0000244193, -0.000716273, \dots 6749\dots
         -0.000151326, -0.000615037, 0.0018207, 0.00197972, 0.000885439, 0.000325081,
Out[476]=
         0.000715271, 0.0000924127, 0.000294919, -0.0000864918, -0.000395188
                   show less
                              show more
                                                    set size limit...
        large output
                                          show all
```

## In[477]:= ListLinePlot[rsUniWeth120dFiltered, PlotRange → All]



In[478]:= edistUniWeth120dFiltered = EstimatedDistribution[rsUniWeth120dFiltered, StableDistribution[1, aUW120d, bUW120d, locUW120d, scaleUW120d]]

Out[478]= StableDistribution[1, 1.28413, 0.00661751, -0.0000924243, 0.000844373]

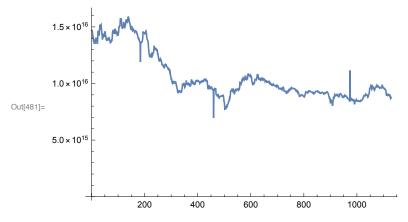
In[479]:= twapsUniWeth120dFiltered1HourCandle =

Table[twapsUniWeth120dFiltered[[i]], {i, 1, Length[twapsUniWeth120dFiltered], 6}]

In[480]:= Length[twapsUniWeth120dFiltered1HourCandle]

Out[480]= 1129

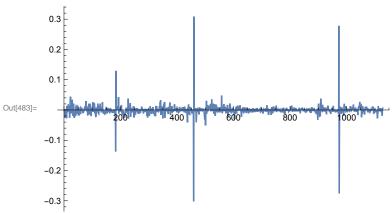
In[481]:= ListLinePlot[twapsUniWeth120dFiltered1HourCandle, PlotRange → All]



In[482]:= rsUniWeth120dFiltered1HourCandle =

Differences[Log[twapsUniWeth120dFiltered1HourCandle]]

In[483]:= ListLinePlot[rsUniWeth120dFiltered1HourCandle, PlotRange → All]



In[484]:= edistUniWeth120dFiltered1HourCandle =

EstimatedDistribution[rsUniWeth120dFiltered1HourCandle,

StableDistribution[1, aUW120dC1h, bUW120dC1h, locUW120dC1h, scaleUW120dC1h]]

Out[484]= StableDistribution[1, 1.44302, 0.0429383, -0.000419763, 0.00474788]

In[485]:= (\* Compare w WETH/USDC \*)

In[486]:= edistWethUsdc120dFiltered1HourCandle

Out[486]= StableDistribution[1, 1.5843, -0.0493885, -0.000101694, 0.0072772]

In[487]:= (\* Interesting ... larger scale on WETH/USDC but smaller alpha. Translates to in terms of InverseCDF ? \*)

InverseCDF[edistWethUsdc120dFiltered1HourCandle, 0.99]

Out[488]= 0.0459063

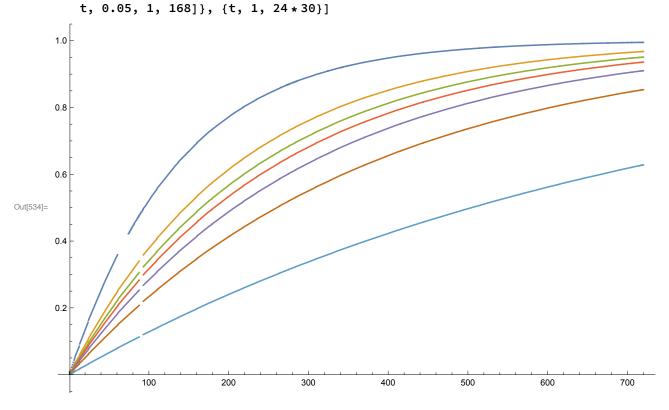
```
In[489]:= InverseCDF[edistWethUsdc120dFiltered1HourCandle, 0.999]
Out[489]= 0.183327
In[490]:= InverseCDF[edistUniWeth120dFiltered1HourCandle, 0.99]
In[491]:= InverseCDF[edistUniWeth120dFiltered1HourCandle, 0.999]
Out[491]= 0.203319
In[492]:= (* Slight difference in alpha starts to
       become apparent at super extreme ends of cdf *)
In[493]= Plot[{InverseCDF[edistWethUsdc120dFiltered1HourCandle, q],
         InverseCDF[edistUniWeth120dFiltered1HourCandle, q]}, {q, 0.95, 1}]
      0.08
      0.06
Out[493]=
      0.04
      0.02
                  0.96
                           0.97
                                     0.98
                                               0.99
                                                         1.00
In[494]:= Plot[{InverseCDF[edistWethUsdc120dFiltered1HourCandle, q],
         InverseCDF[edistUniWeth120dFiltered1HourCandle, q]}, {q, 0.995, 1}]
      0.40
      0.35
      0.30
      0.25
Out[494]=
      0.15
      0.10
                 0.996
                           0.997
                                     0.998
                                               0.999
                                                         1.000
      0.05
In[495]:= (* What about a=1.3? *)
In[496]:= edistUniWeth120dFiltered1HourCandle
Out[496]= StableDistribution[1, 1.44302, 0.0429383, -0.000419763, 0.00474788]
```

```
In[497]:= Plot[{InverseCDF[edistWethUsdc120dFiltered1HourCandle, q],
        InverseCDF[edistUniWeth120dFiltered1HourCandle, q],
        InverseCDF [Stable Distribution [1, 1.3, 0.05160448032592783`,
           -0.0005180625308600968`,0.004823033038389856`],q]}, {q, 0.95, 1}]
      0.10
      0.08
Out[497]= 0.06
      0.04
      0.02
                          0.97
                                                      1.00
In[498]:= Plot[{InverseCDF[edistWethUsdc120dFiltered1HourCandle, q],
        InverseCDF[edistUniWeth120dFiltered1HourCandle, q],
        InverseCDF[StableDistribution[1, 1.3, 0.05160448032592783`,
           -0.0005180625308600968`, 0.004823033038389856`], q]}, {q, 0.75, 1}]
      0.04
      0.03
Out[498]=
      0.02
      0.01
                 0.80
                                   0.90
                                             0.95
                                                      1.00
      (* Yea so miscalc on a greatly changes things up, as expected. Lower a,
      means higher inverse CDF earlier in upper range we care about \star)
      (* Set up factor calcs *)
      edistUniWeth120dFiltered1HourCandle
Out[504]= StableDistribution[1, 1.43975, 0.0516045, -0.000518063, 0.00482303]
In[503]:= edistUniWeth120dFiltered1HourCandle
Out[503]= StableDistribution[1, 1.44302, 0.0429383, -0.000419763, 0.00474788]
      (* Looking goood ... *)
```

```
In[505]:= muUniWeth120dFiltered1HourCandle =
       mu[1.4430192097069168`, -0.0004197632840157609`]
Out[505]= -0.000419763
In[506]:= sigUniWeth120dFiltered1HourCandle =
       sig[1.4430192097069168`, 0.004747879945834797`]
Out[506]= 0.00612173
In[507]:= aUniWeth120dFiltered1HourCandle = 1.4430192097069168
Out[507]= 1.44302
In[508]:= edistUniWeth120dFiltered1HourCandleNormalized =
       StableDistribution[1, aUniWeth120dFiltered1HourCandle, 0, 0, 1]
Out[508]= StableDistribution[1, 1.44302, 0, 0, 1]
in[509]:= factorUniWeth120dFiltered1HourCandle[t_, alpha_] :=
       Exp[muUniWeth120dFiltered1HourCandle * t + sigUniWeth120dFiltered1HourCandle *
           (t/aUniWeth120dFiltered1HourCandle) ^ (1/aUniWeth120dFiltered1HourCandle) *
          InverseCDF[edistUniWeth120dFiltered1HourCandleNormalized, 1 - alpha]
in[510]:= factorUniWeth120dFiltered1HourCandle[8, 0.05]
Out[510]= 1.06319
in[511]:= factorWethUsdc120dFiltered1HourCandle[8, 0.05]
Out[511]= 1.07915
In[512]:= dminUniWeth120dFiltered1HourCandle[t_, alpha_] :=
       factorUniWeth120dFiltered1HourCandle[t, alpha]
In[513]:= rescaledKminUniWeth120dFiltered1HourCandle[t_, alpha_, m_] :=
       (1-1/(dminUniWeth120dFiltered1HourCandle[m, alpha])^(t/m))/2
In[514]:= rescaledDrawDownMinUniWeth120dFiltered1HourCandle[t_, alpha_, m_, anchor_] := 1 -
        (1 - rescaledKminUniWeth120dFiltered1HourCandle[m, alpha, anchor]) ^ (Floor[t/m])
In[515]:= rescaledDrawDownMinUniWeth120dFiltered1HourCandle[24, 0.05, 1, 8]
Out[515]= 0.0876495
In[516]:= (* Make sure anchor is consistent again ... *)
In[517]:= compoundFactorMinUniWeth120dFiltered1HourCandle[t_, alpha_, m_, anchor_] :=
       (1-2*rescaledKminUniWeth120dFiltered1HourCandle[m, alpha, anchor])^
        (Floor[t/m])
In[518]:= 1 - compoundFactorMinUniWeth120dFiltered1HourCandle[24, 0.05, 1, 8]
Out[518]= 0.167909
```

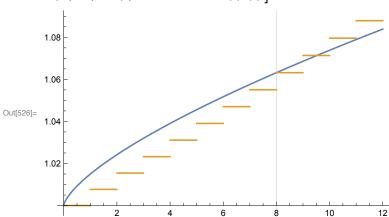
In[523]:= (\* Plot rescaled draw down over time \*)

```
In[534]= Plot[{rescaledDrawDownMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 1],
       rescaledDrawDownMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 4],
       rescaledDrawDownMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 6],
       rescaledDrawDownMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 8],
       rescaledDrawDownMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 12],
       rescaledDrawDownMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 24],
       rescaledDrawDownMinUniWeth120dFiltered1HourCandle[
```



In[525]:= (\* And anchor ... \*)

In[526]:= Plot[{factorUniWeth120dFiltered1HourCandle[t, 0.05], 1/compoundFactorMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 8]},  $\{t, 0, 12\}, GridLines \rightarrow \{\{8\}\}\]$ 

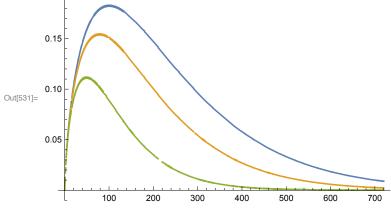


```
In[527]:= Plot[{ (factorUniWeth120dFiltered1HourCandle[t, 0.05] - 1) *
         compoundFactorMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 8],
        (factorUniWeth120dFiltered1HourCandle[t, 0.05] - 1) *
         compoundFactorMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 4],
        (factorUniWeth120dFiltered1HourCandle[t, 0.05] - 1) *
         compoundFactorMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 1], {t, 0, 24 * 7}]
     0.15
     0.10
Out[527]=
     0.05
                     50
                                   100
                                                150
In[528]:= (* This is kind of bad. Lower funding rate is translating to
       slower draw down in VaR over time, even with same framework. *)
In[529]:= (* TODO:
       Should have a framework that has similar curves regardless of inverse CDF *)
In[530]:= Plot[{ (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8],
        (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 4],
        (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) *
         compoundFactorMinWethUsdc120dFiltered1HourCandle[
          t, 0.05, 1, 1]\}, {t, 0, 24 * 7}]
     0.15
     0.10
Out[530]=
     0.05
```

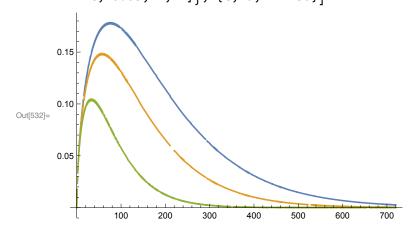
100

150

```
In[531]:= Plot[{ (factorUniWeth120dFiltered1HourCandle[t, 0.05] - 1) *
        compoundFactorMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 8],
       (factorUniWeth120dFiltered1HourCandle[t, 0.05] - 1) *
        compoundFactorMinUniWeth120dFiltered1HourCandle[t, 0.05, 1, 4],
       (factorUniWeth120dFiltered1HourCandle[t, 0.05] - 1) *
        compoundFactorMinUniWeth120dFiltered1HourCandle[
         t, 0.05, 1, 1]\}, {t, 0, 24 * 30}]
     0.15
```



In[532]:= Plot[{ (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) \* compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 8], (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) \* compoundFactorMinWethUsdc120dFiltered1HourCandle[t, 0.05, 1, 4], (factorWethUsdc120dFiltered1HourCandle[t, 0.05] - 1) \* compoundFactorMinWethUsdc120dFiltered1HourCandle[ t, 0.05, 1, 1], {t, 0, 24 \* 30}]



(\* Let's amp things up with something like ALCX/WETH which has 10m a < 1 ... Likely closer to what OVL/ETH and OVL/DAI will be. \*)