Sunday, November 21, 2021 9:23 PM (x, f(x)) but the nature of f is unknown. What to try? Halfspaces? Kerrels? Which one (1)? deep Feed Forward network benein answer: with nonlinear activations Prain to minimize error of output Gradient Descent 1811  $f(x) = \sum_{i} w_{i} U_{i}$ 

 $f(x) = \sum_{i} w_{i} u_{i}$   $\frac{\partial f}{\partial w_{i}} = u_{i}$   $f(x) = \sum_{i} w_{i} u_{i} \left(\sum_{i} w_{i,i} u_{i,i}\right)$  i

Qi, Qi,

$$\frac{\partial f}{\partial w_{i}} = \frac{\partial f}{\partial w_{i}} \cdot \frac{\partial w_{i}}{\partial w_{i}} = \frac{\partial w_{i}}{\partial w_{i}} \cdot \frac{\partial u_{i}}{\partial w_{i}}$$

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Letra: Induction + chain Rule base:  $\frac{\partial f}{\partial f} = 1$ . 24 - Ju from U Ui, receives induction hypothesis Hence computes  $\sum_{u} \frac{\partial f}{\partial u} \cdot \frac{\partial u}{\partial u_{i_1}} = \frac{\partial f}{\partial u_{i_1}}.$ The: O(M). Fast, general, but is it any good? - If no hidden layer then 6D -> OPT. It hidden layers, havily overparametrized more parameters than data then GD -> OPT. (But does it generalize?) almoximate any

New Section 2 Page 3

Meural Networks can approximate any continuous function. [Cybenko 89, Horrik-struckombe-While 89] Balon 93] suffices! sufficiently vide In fact, depth 2 (= 1 hidden layer) But depth can help - I furtheries that need a large representation with small depth and a small representation with moderate depth. In 1 neds activation units to be X→ - ∞ "oignoidal"  $T(X) \rightarrow 0$ ×-> 00  $\sigma(x) \longrightarrow 1$ What about ReLU? Init to together:

put two together: