

PROBLEMS 1

1-1 How much charge is represented by 6400 electrons?

1-2 An energy source forces a constant current of 2A for 10s to flow through a lightbulb. If 4.6 Kj is given off in the form of light and heat energy, calculate the voltage drop across the bulb.

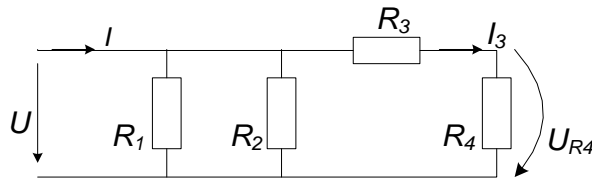
1-3 How much energy does an 80 W electric bulb consume in three hours?

1-4 A device draws 10 A when connected to a 230 V line. How long does it take to consume 80 Kj?

1-5 The charge entering the positive terminal of an element is $q(t) = 10 \sin 4\pi t$ mC while the voltage across the element is $u(t) = 2 \cos 4\pi t$ V. a) Find the power to the element at $t=0.3s$; b) Calculate the energy delivered to the element between 0 and 0.8s.

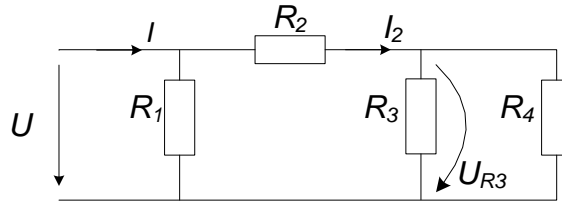
1-6 A 12V car battery supported a current of 150 mA to a bulb. Calculate: a) the power absorbed by the bulb; the energy absorbed by the bulb over one interval of 30 minutes.

1-7 For the circuit below we know: $R_1=15\Omega$, $R_2=10\Omega$, $R_3=7\Omega$, $R_4=5\Omega$ and supplying voltage $U=24V$. Calculate: a) the equivalent resistance regarding the supplying terminals, R_e ; b) the total current absorbed by the resistances, I ; c) the current through the resistance R_3 , I_3 ; d) the voltage on the resistance R_4 , U_{R4} ; the power dissipated in the resistance R_2 , P_{R2} .



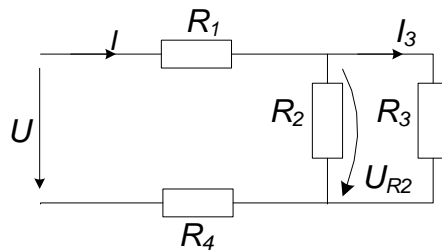
Problem 1-7

1-8 For the circuit below we know: $R_1=10\Omega$, $R_2=9\Omega$, $R_3=15\Omega$, $R_4=10\Omega$ and supplying voltage $U=60V$. Calculate: a) the equivalent resistance regarding the supplying terminals, R_e ; b) the total current absorbed by the resistances, I ; c) the current through the resistance R_2 , I_2 ; d) the voltage on the resistance R_3 , U_{R3} ; the power dissipated in the resistance R_4 , P_{R4} .



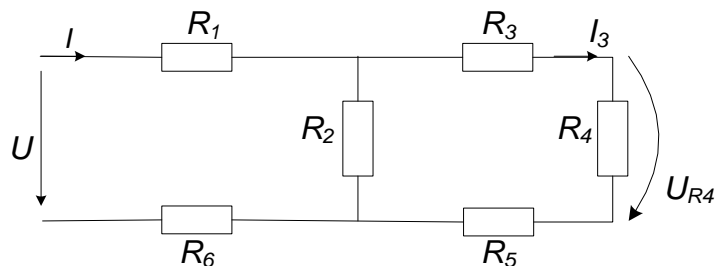
Problem 1-8

1-9 For the circuit below we know: $R_1=4\Omega$, $R_2=10\Omega$, $R_3=15\Omega$, $R_4=5\Omega$ and supplying voltage $U=75V$. Calculate: a) the equivalent resistance regarding the supplying terminals, R_e ; b) the total current absorbed by the resistances, I ; c) the current through the resistance R_3 , I_3 ; d) the voltage on the resistance R_2 , U_{R2} ; the power dissipated in the resistance R_4 , P_{R4} .



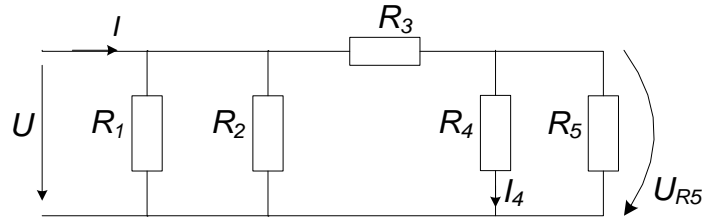
Problem 1-9

1-10 For the circuit below we know: $R_1=5\Omega$, $R_2=3\Omega$, $R_3=2\Omega$, $R_4=1\Omega$, $R_5=3\Omega$, $R_6=3\Omega$ and supplying voltage $U=30V$. Calculate: a) the equivalent resistance regarding the supplying terminals, R_e ; b) the total current absorbed by the resistances, I ; c) the current through the resistance R_3 , I_3 ; d) the voltage on the resistance R_4 , U_{R4} ; the power dissipated in the resistance R_5 , P_{R5} .



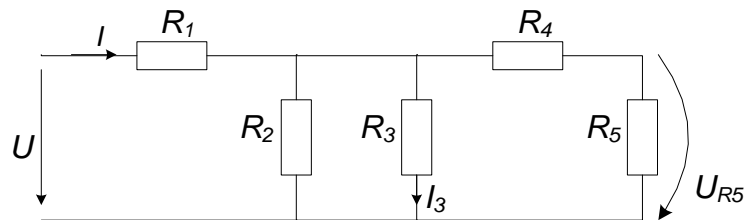
Problem 1-10

1-11 For the circuit below we know: $R_1=60\Omega$, $R_2=20\Omega$, $R_3=8\Omega$, $R_4=3\Omega$, $R_5=6\Omega$ and supplying voltage $U=120V$. Calculate: a) the equivalent resistance regarding the supplying terminals, R_e ; b) the total current absorbed by the resistances, I ; c) the current through resistance R_4 , I_4 ; d) the voltage on resistance R_5 , U_{R5} ; the power dissipated in resistance R_2 , P_{R2} .



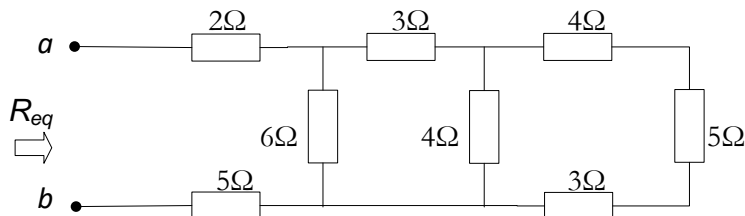
Problem 1-11

1-12 For the circuit below we know: $R_1=9\Omega$, $R_2=60\Omega$, $R_3=20\Omega$, $R_4=6\Omega$, $R_5=4\Omega$ and supplying voltage $U=150V$. Calculate: a) the equivalent resistance regarding the supplying terminals, R_e ; b) the total current absorbed by the resistances, I ; c) the current through the resistance R_3 , I_3 ; d) the voltage on resistance R_5 , U_{R5} ; the power dissipated in resistance R_4 , P_{R4} .



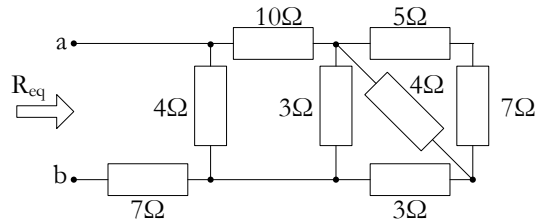
Problem 1-12

1-13 Find the value of the equivalent resistance, R_{eq} , between terminals a and b, for the sub-circuit shown below.



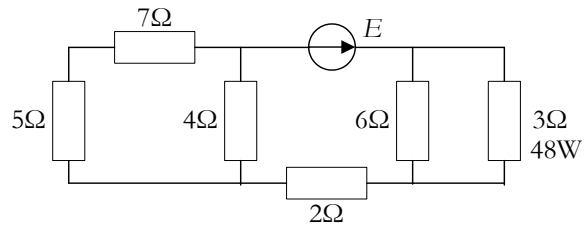
Problem 1-13

1-14 Find the value of the equivalent resistance, R_{eq} , between terminals a and b , for the sub-circuit shown below.



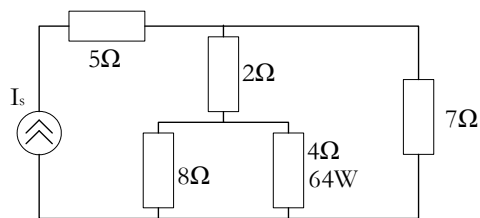
Problem 1-14

1-15 Determine the voltage of source E , for the circuit below if the power dissipated in the 3Ω resistance is $48W$.



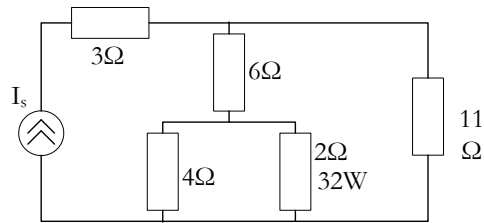
Problem 1-15

1-16 Determine the current I_s generated by the current source in the circuit below if the power dissipated in the 4Ω resistance is $64W$.



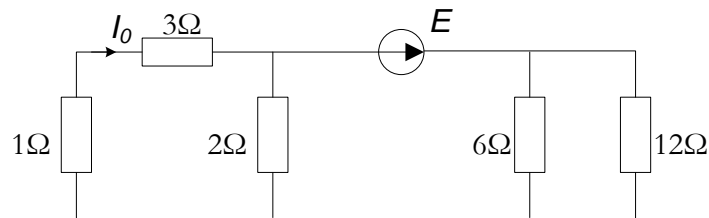
Problem 1-16

1-17 Determine the current I_s generated by the current source in the circuit below if the power dissipated in the 2Ω s resistance is $32W$.



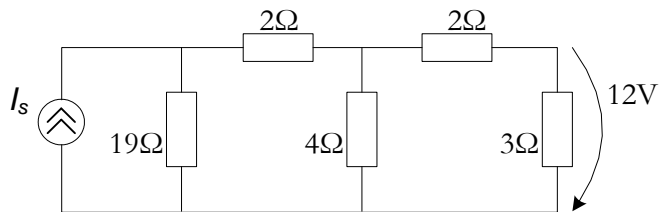
Problem 1-17

1-18 Determine the voltage E generated by the voltage source in the circuit below if the current flow to the 3Ω s resistance is $I_0=4A$.



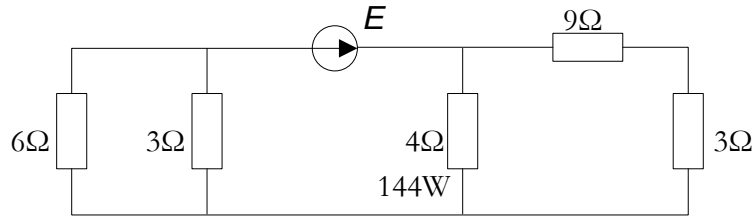
Problem 1-18

1-19 Determine the current I_s generated by the current source in the circuit below if the voltage drop on the 3Ω s resistance is $12V$.



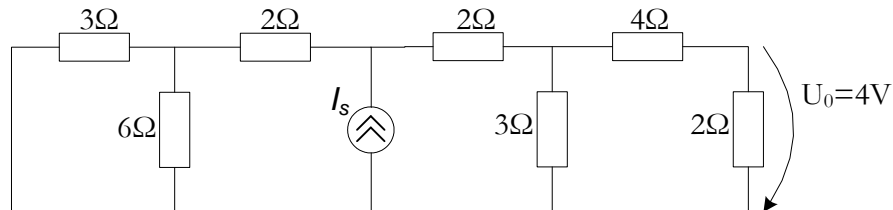
Problem 1-19

1-20 Determine the voltage E generated by the voltage source in the circuit below if the power dissipated in the 4Ω s resistance is $144W$.



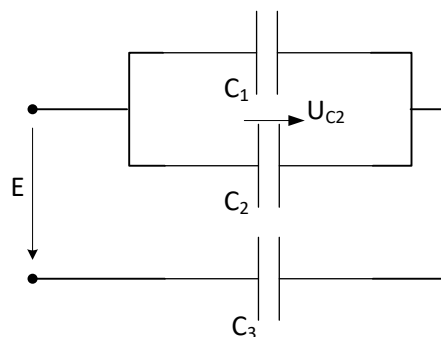
Problem 1-20

1-21 Determine the current I_s generated by the current source in the circuit below if the voltage drop on the 2Ω s resistance is $4V$.



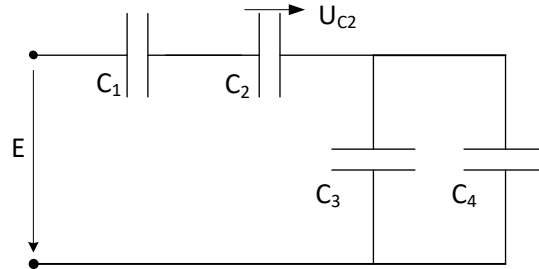
Problem 1-21

1-22 For the circuit below we know: $C_1=3\mu F$, $C_2=9\mu F$, $C_3=6\mu F$ and the supplying voltage $U=60V$. Find: a) equivalent capacitance regarding the supplying voltage terminals, C_e ; b) total charge absorbed by the capacitors, Q_e ; c) voltage on the capacitor C_2 , U_{C2} ; d) charge on the capacitor C_1 ; e) energy of the capacitor C_3 , W_{C3} .



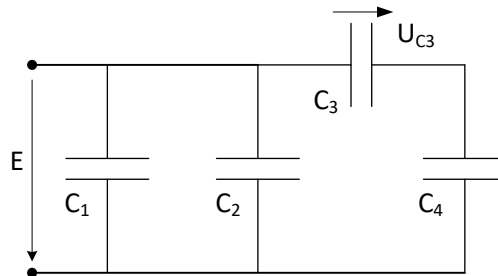
Problem 1-22

1-23 For the circuit below we know: $C_1=12\mu F$, $C_2=4\mu F$, $C_3=1\mu F$, $C_4=5\mu F$ and the supplying voltage $U=24V$. Find: a) equivalent capacitance regarding the supplying voltage terminals, C_e ; b) total charge absorbed by the capacitors, Q_e ; c) voltage on capacitor C_2 , U_{C2} ; d) charge on capacitor C_4 ; e) energy of capacitor C_3 , W_{C3} .



Problem 1-23

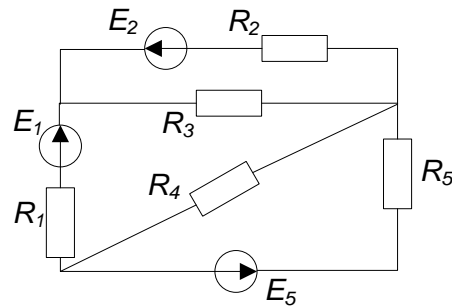
1-24 For the circuit below we know: $C_1=5\mu F$, $C_2=7\mu F$, $C_3=12\mu F$, $C_4=4\mu F$ and the supplying voltage $U=20V$. Find: a) equivalent capacitance regarding the supplying voltage terminals, C_e ; b) total charge absorbed by the capacitors, Q_e ; c) voltage on capacitor C_3 , U_{C3} ; d) charge on capacitor C_1 ; e) energy of capacitor C_4 , W_{C4} .



Problem 1-24

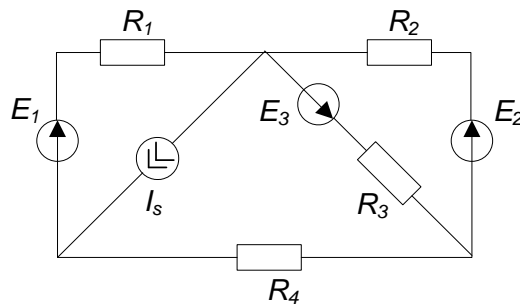
PROBLEMS 2

2-1 For the circuit below we know: $R_1=5\Omega$, $R_2=10\Omega$, $R_3=6\Omega$, $R_4=3\Omega$, $R_5=2\Omega$, $E_1=10V$, $E_2=5V$, $E_5=5V$. Identify the number of nodes and circuit branches and calculate the branch currents using: a) the Kirchhoff Laws; b) the nodal analysis; c) the mesh analysis. Calculate the generated and removed power in the circuit and verify the power conservation theorem.



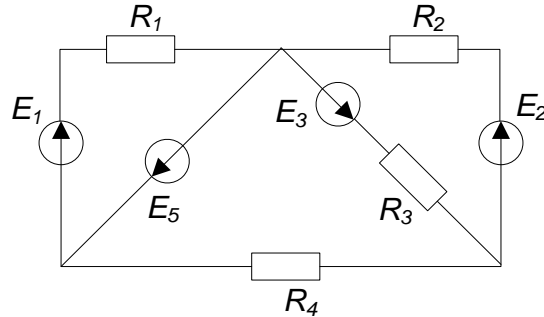
Problem 2-1

2-2 For the circuit below we know: $R_1=2\Omega$, $R_2=2\Omega$, $R_3=6\Omega$, $R_4=2\Omega$, $E_1=12V$, $E_3=6V$, $I_S=4A$. Identify the number of nodes and circuit branches and calculate the branch currents using: a) the Kirchhoff Laws; b) the nodal analysis; c) the mesh analysis. Calculate the generated and removed power in the circuit and verify the power conservation theorem.



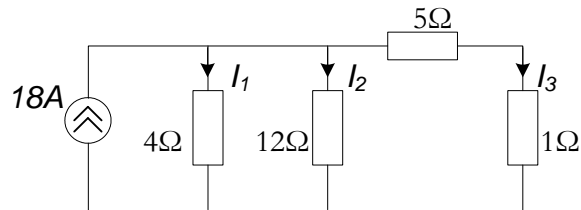
Problem 2-2

2-3 For the circuit below we know: $R_1=2\Omega$, $R_2=2\Omega$, $R_3=6\Omega$, $R_4=2\Omega$, $E_1=12V$, $E_3=6V$, $E_5=10V$. Identify the number of nodes and circuit branches and calculate the branch currents using: a) the Kirchhoff Laws; b) the nodal analysis; c) the mesh analysis. Calculate the generated and removed power in the circuit and verify the power conservation theorem.



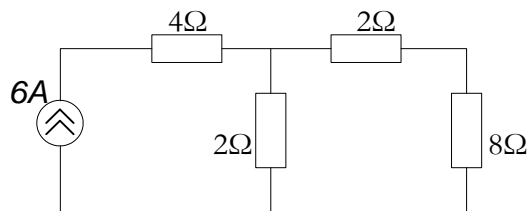
Problem 2-3

2-4 Find the currents I_1 , I_2 , I_3 for the circuit below and verify the power conservation theorem.



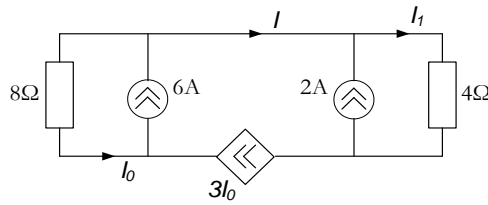
Problem 2-4

2-5 For the circuit below calculate the dissipated power in the 8Ω 's resistance.



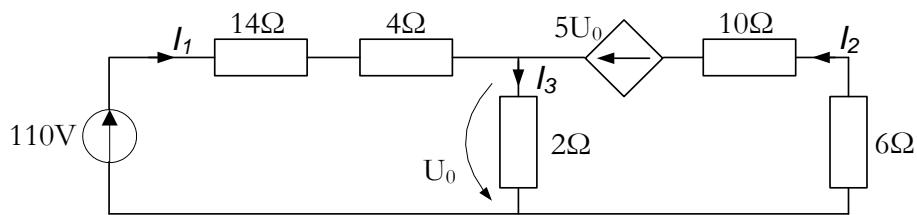
Problem 2-5

2-6 Find the currents I , I_0 , I_1 for the circuit below and verify the power conservation theorem.



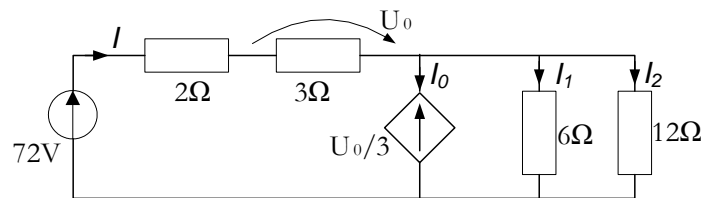
Problem 2-6

2-7 Find the currents I_1 , I_2 , I_3 for the circuit below and verify the power conservation theorem.



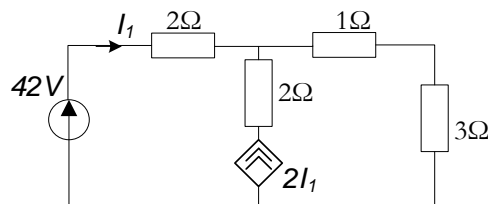
Problem 2-7

2-8 Find the currents I , I_1 , I_2 , I_0 for the circuit below and verify the power conservation theorem.



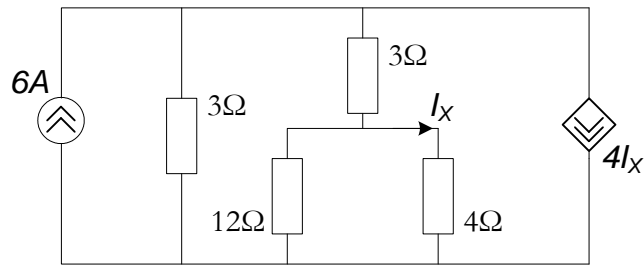
Problem 2-8

2-9 Find the currents I_1 for the circuit below and verify the power conservation theorem.



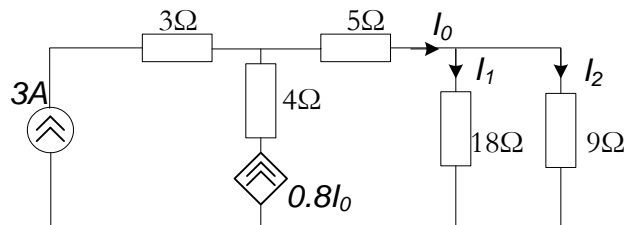
Problem 2-9

2-10 Find the currents I_x for the circuit below and verify the power conservation theorem.



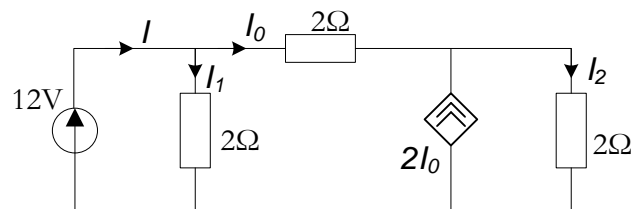
Problem 2-10

2-11 Find the currents I_0 , I_1 , I_2 for the circuit below and verify the power conservation theorem.



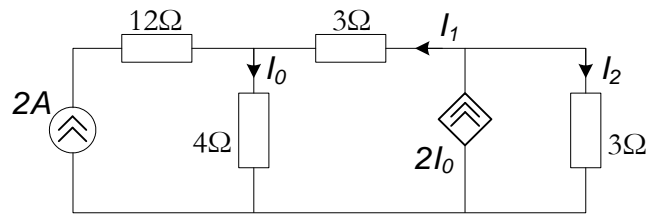
Problem 2-11

2-12 Find the currents I_0 , I_1 , I_2 , I for the circuit below and verify the power conservation theorem.



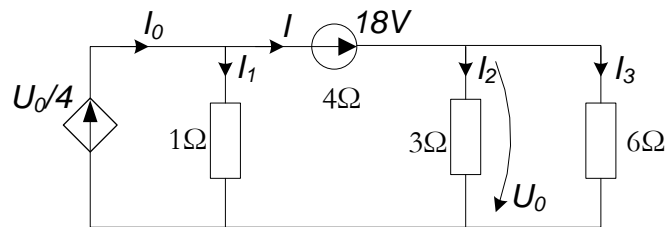
Problem 2-12

2-13 Find the currents I_0 , I_1 , I_2 for the circuit below and verify the power conservation theorem.



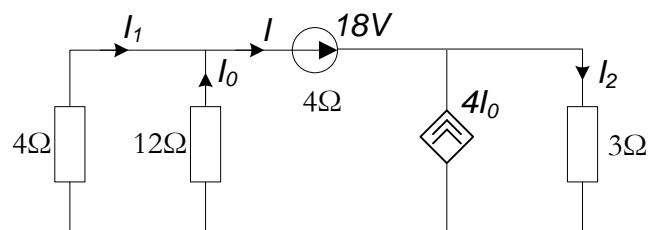
Problem 2-13

2-14 Find the currents I_0 , I_1 , I_2 , I_3 , I for the circuit below and verify the power conservation theorem.



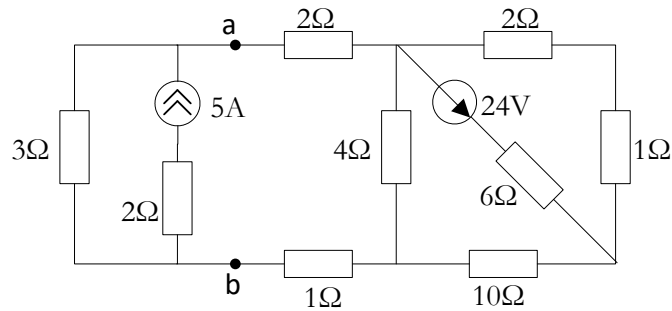
Problem 2-14

2-15 Find the currents I_0 , I_1 , I_2 , I for the circuit below and verify the power conservation theorem.



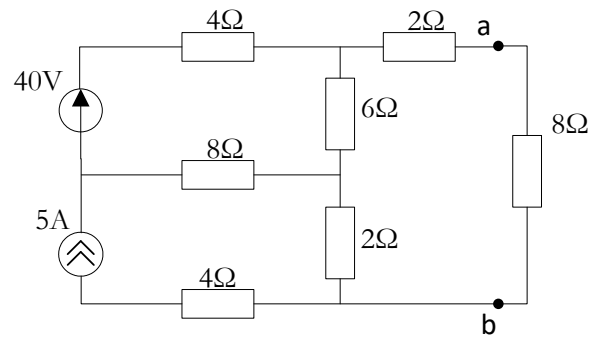
Problem 2-15

2-16 Suppress all the sources in the circuit below and calculate the equivalent resistance, R_{eq} , regarding to the terminals a and b .



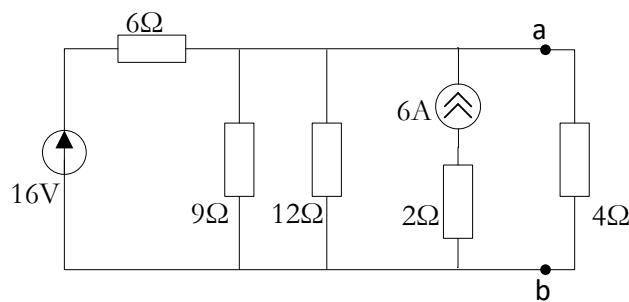
Problem 2-16

2-17 Suppress all the sources in the circuit below and calculate the equivalent resistance, R_{eq} , regarding to the terminals a and b .



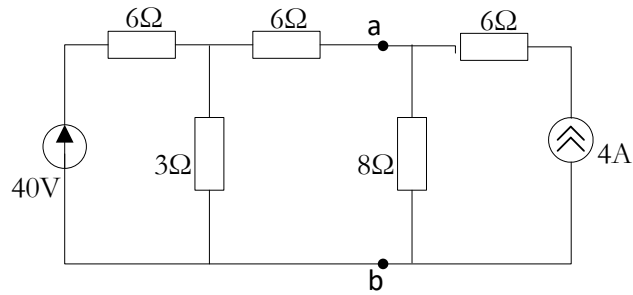
Problem 2-17

2-18 Suppress all the sources in the circuit below and calculate the equivalent resistance, R_{eq} , regarding to the terminals a and b .



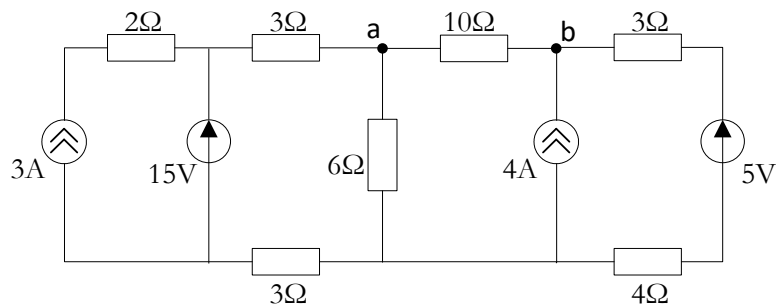
Problem 2-18

2-19 Suppress all the sources in the circuit below and calculate the equivalent resistance, R_{eq} , regarding to the terminals a and b.



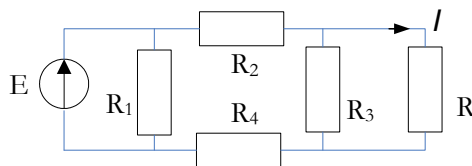
Problem 2-19

2-20 Suppress all the sources in the circuit below and calculate the equivalent resistance, R_{eq} , regarding to the terminals a and b.



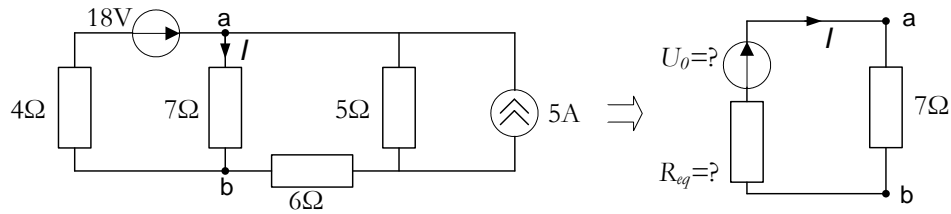
Problem 2-20

2-21 Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the resistance R for the circuit below. Find the current I through the resistance R . Circuit parameters: $E=15V$, $R_1=220\Omega$, $R_2=150\Omega$, $R_3=R_4=R=100\Omega$.



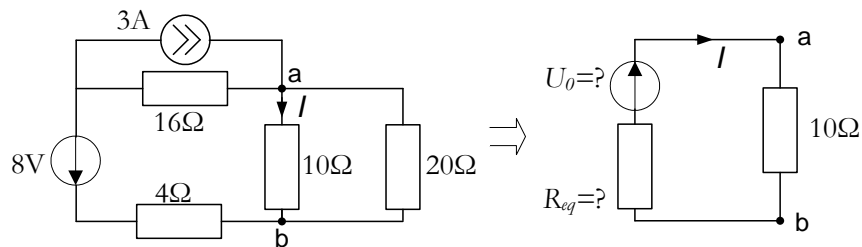
Problem 2-21

2-22 Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 7Ω s resistance (terminals a and b) for the circuit below. Find the current I through the 7Ω s resistance.



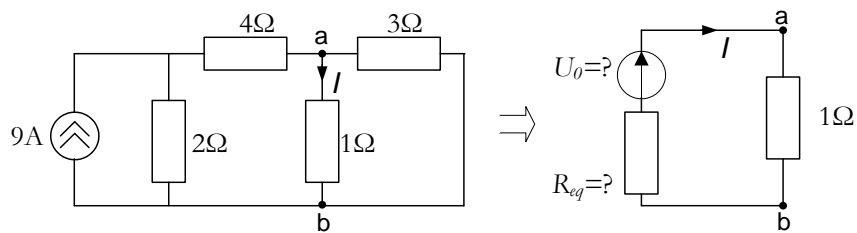
Problem 2-22

2-23 Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 10Ω s resistance (terminals a and b) for the circuit below. Find the current I through the 10Ω s resistance.



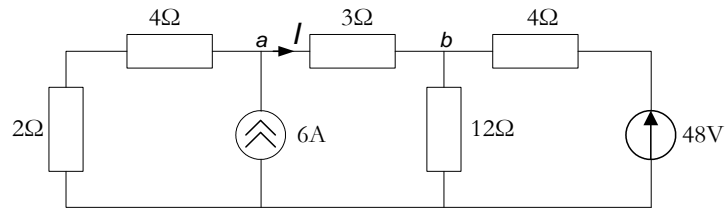
Problem 2-23

2-24 Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 1Ω s resistance (terminals a and b) for the circuit below. Find the current I through the 1Ω s resistance.



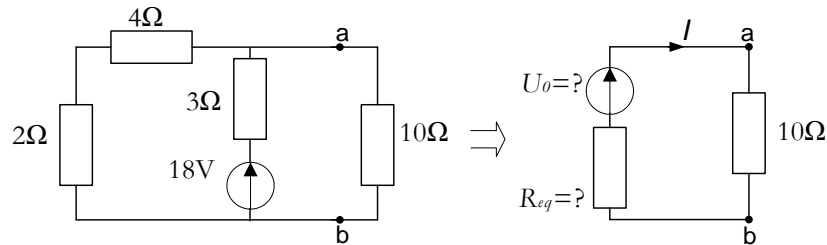
Problem 2-24

2-25 Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 3Ω s resistance (terminals a and b) for the circuit below. Find the current I through the 3Ω s resistance.



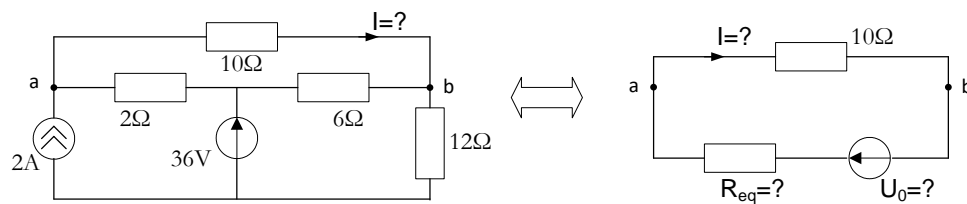
Problem 2-25

2-26 Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 10Ω 's resistance (terminals a and b) for the circuit below. Find the current I through the 10Ω 's resistance.



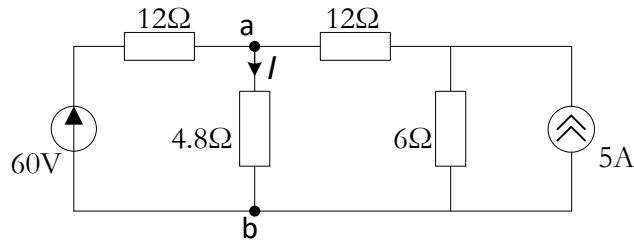
Problem 2-26

2-27 Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 10Ω 's resistance (terminals a and b) for the circuit below. Find the current I through the 10Ω 's resistance.



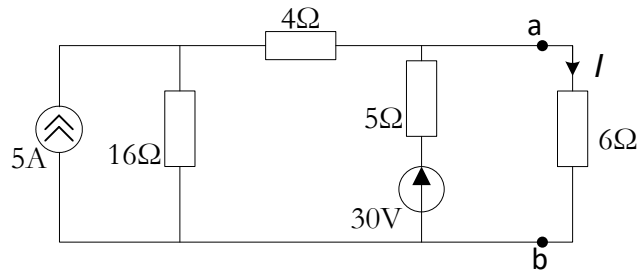
Problem 2-27

- 2-28** Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 4.8Ω 's resistance (terminals a and b) for the circuit below. Find the current I through the 4.8Ω 's resistance.



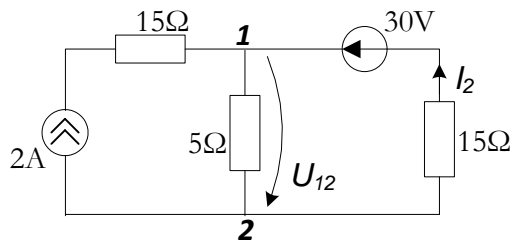
Problem 2-28

- 2-29** Determine the Thevenin equivalent circuit (R_{eq} , U_0), viewed by the 6Ω 's resistance (terminals a and b) for the circuit below. Find the current I through the 6Ω 's resistance.



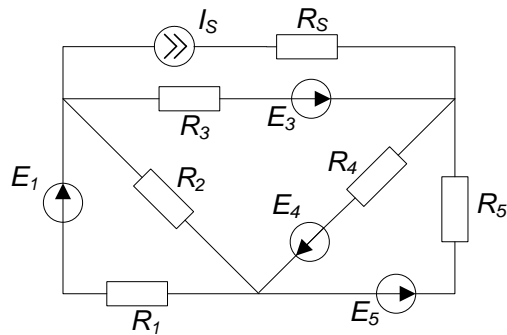
Problem 2-29

- 2-30** For the circuit below, determine: a) the currents in the circuit; b) the current I_2 using the Thevenin's theorem; the voltage on the 5Ω 's resistance, U_{12} . Verify the power conservation theorem.



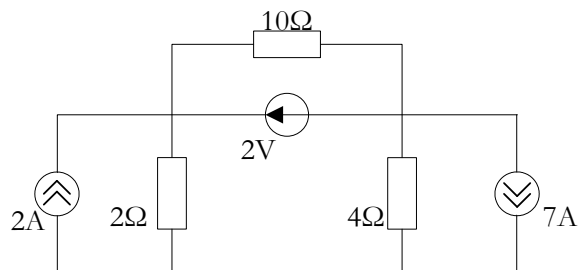
Problem 2-30

- 2-31** For the circuit below, use the nodal analysis to calculate the potential of the nodes. Find the currents in the circuit. The circuit parameters are: $R_1 = R_4 = 4\Omega$, $R_2 = 2\Omega$, $R_3 = 6\Omega$, $R_5 = 3\Omega$, $R_s = 10\Omega$, $E_1 = E_3 = 6V$, $E_4 = 3V$, $E_5 = 4V$, $I_s = 2A$.



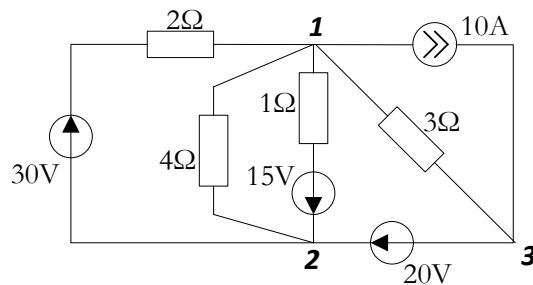
Problem 2-31

- 2-32** For the circuit below, use the nodal analysis to calculate the potential of the nodes. Find the currents in the circuit.



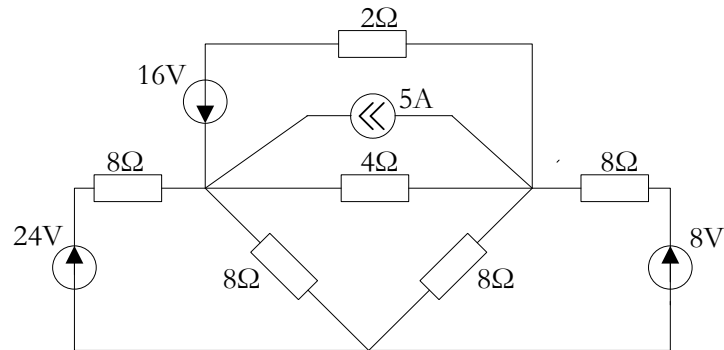
Problem 2-32

- 2-33** For the circuit below, use the nodal analysis to calculate the potential of the nodes. Find the currents in the circuit.



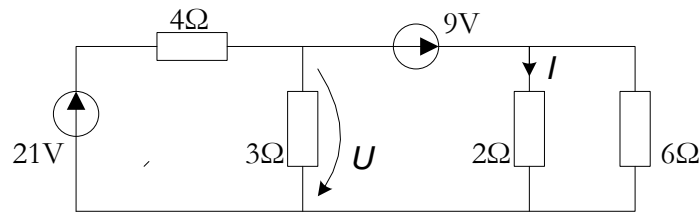
Problem 2-33

2-34 For the circuit below, use the nodal analysis to calculate the potential of the nodes. Find the currents in the circuit.



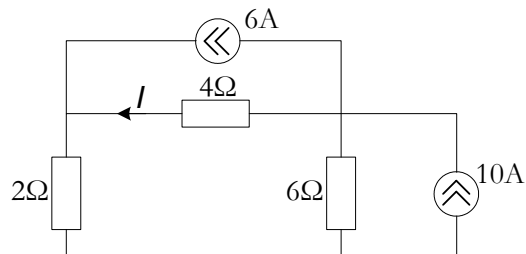
Problem 2-34

2-35 For the circuit below, calculate the voltage U using: a) Norton's theorem; b) the nodal analysis. Calculate the current I using Thevenin's theorem.



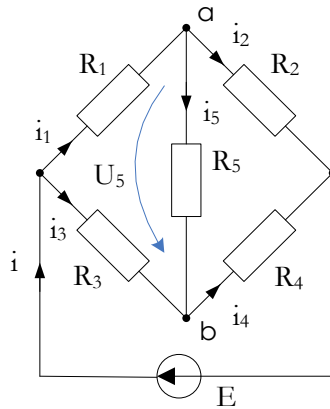
Problem 2-35

2-36 For the circuit below, calculate the currents through the circuit using: a) the Kirchhoff laws; b) the nodal analysis; c) the mesh analysis. Verify the current I by using Thevenin's theorem. Verify the power conservation theorem.



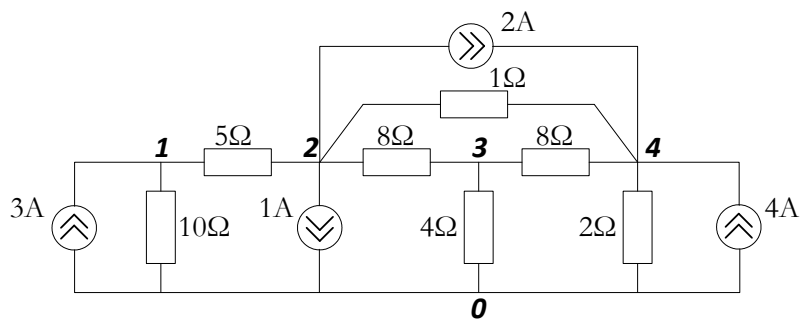
Problem 2-36

2-37 For the circuit below, calculate: a) the current i_5 using the Thevenin's theorem; the voltage U_5 using Norton's theorem.



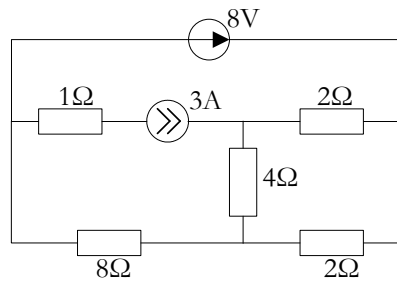
Problem 2-37

2-38 For the circuit below, use the nodal analysis to calculate the potential of the nodes. Find the currents in the circuit.



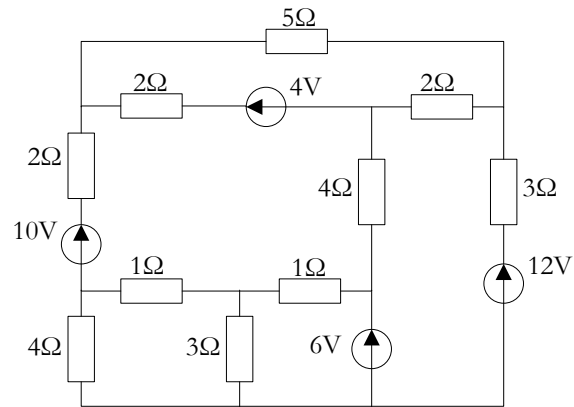
Problem 2-38

2-39 For the circuit below, use the mesh analysis to find the currents in the circuit.



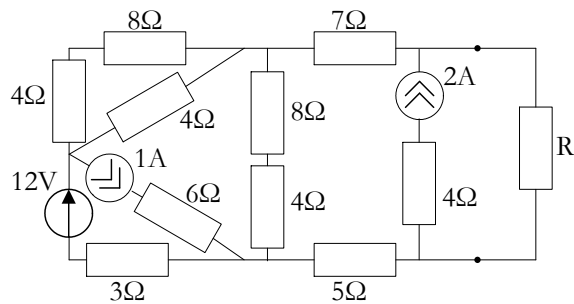
Problem 2-39

2-40 For the circuit below, use the mesh analysis to find the currents in the circuit.



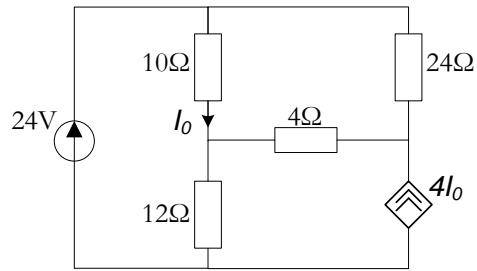
Problem 2-40

2-41 For the circuit below, determine the value of the resistance R which will absorb the greatest power from the circuit.



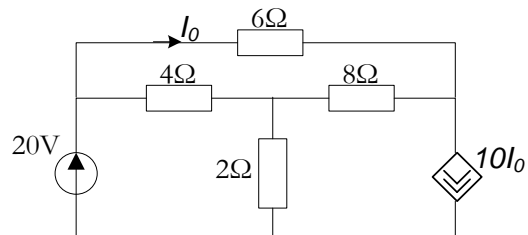
Problem 2-41

2-42 For the circuit below, use the mesh analysis to find the currents in the circuit



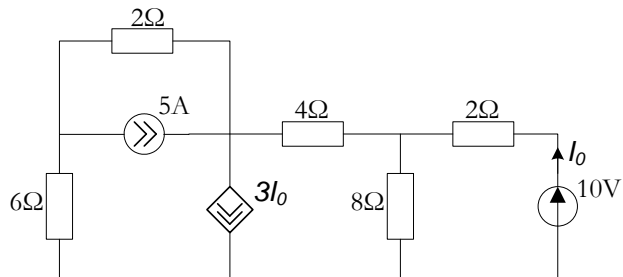
Problem 2-42

2-43 For the circuit below, use the mesh analysis to find the currents in the circuit



Problem 2-43

2-44 For the circuit below, use the mesh analysis to find the currents in the circuit.



Problem 2-44

PROBLEMS 3

3-1 Given the sinusoid $10 \sin(10\pi t - 45^\circ)$, calculate its amplitude, rms value, angular frequency, period, frequency and phase angle.

3-2 Find the phase angle between $u_1(t) = 200\sqrt{2} \sin(5t + 30^\circ)$ and $u_2(t) = 50 \cos(5t)$. Does u_1 leads or lags u_2 ?

3-3 Find the phase angle between $i_1(t) = -4 \sin(417t + 30^\circ)$ and $i_2(t) = -7 \cos(417t - 35^\circ)$. Does i_1 leads or lags i_2 ?

3-4 Given $i_1(t) = 2\sqrt{2} \sin(\omega t + 45^\circ) \text{ A}$ and $i_2(t) = 2\sqrt{2} \cos(\omega t - 45^\circ) \text{ A}$, find their sum $i(t) = i_1(t) + i_2(t)$.

3-5 Given $u_1(t) = 20\sqrt{2} \sin(\omega t + 45^\circ) \text{ V}$ and $u_2(t) = -10\sqrt{2} \cos(\omega t - 30^\circ) \text{ V}$, find their sum $u(t) = u_1(t) + u_2(t)$.

3-6 Find the sinusoids corresponding to these phasors: a) $\underline{U} = -10 e^{j30^\circ} \text{ V}$; b) $\underline{I} = 2\sqrt{2}(\cos 45^\circ - j \sin 45^\circ) \text{ A}$; c) $\underline{I} = j(5 - j12) \text{ A}$.

3-7 Using the phasor approach, determine the current $i(t)$ in a circuit described by the integrodifferential equation

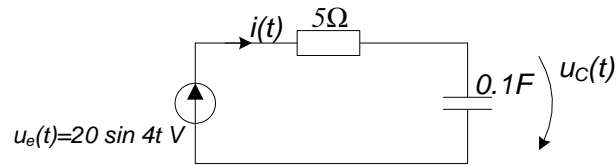
$$4i(t) + 8 \int i(t) dt - 3 \frac{di(t)}{dt} = 50\sqrt{2} \sin(2t + 75^\circ).$$

3-8 Find the voltage $u(t)$ in a circuit described by the integrodifferential equation

$$2\sqrt{2} \frac{du(t)}{dt} + 5\sqrt{2} u(t) + 10\sqrt{2} \int u(t) dt = 50\sqrt{2} \sin(5t - 30^\circ)$$

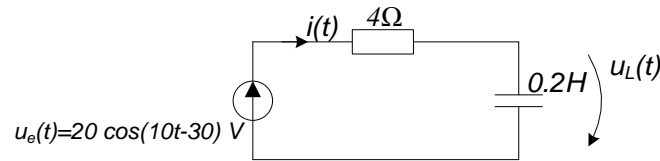
using the phasor approach.

3-9 Find the circuit current, $i(t)$, and capacitor-voltage, $u_C(t)$, for the circuit below.



Problem 3-9

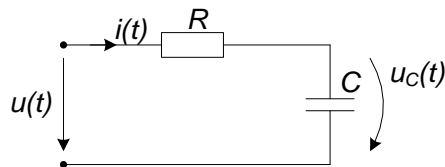
3-10 Find the circuit current, $i(t)$, and the inductance-voltage, $u_L(t)$, for the circuit below.



Problem 3-10

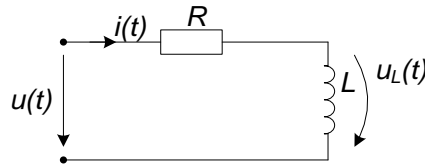
3-11 Through a circuit branch, a sinusoidal current at $t=0$, has $i(0) = 5\text{A}$, and at $t_1 = 2.5 \text{ ms}$ reaches the peak value. If the sinusoidal period is $T = 20 \text{ ms}$, find: a) the phase angle of the current; b) the instantaneous form of the sinusoidal current.

3-12 The sinusoidal current in the circuit below, has 50Hz frequency and the peak value $i_m = 2.82\text{A}$. Calculate the instantaneous value of the supplying voltage and the instantaneous value of the capacitance-voltage, when $R = 200\Omega$ and $C = 15.9 \mu\text{F}$. The current phase angle will be considered zero.



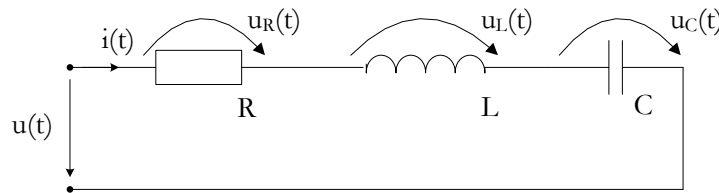
Problem 3-12

- 3-13** In the circuit below we know $R = 20\Omega$ and $L = 200\text{mH}$. If the voltage in the inductor is $u_L(t) = 200 \sin(314t - 60^\circ)$ V, find: a) the instantaneous value of the current, $i(t)$; b) the instantaneous value of the supplying voltage, $u(t)$.



Problem 3-13

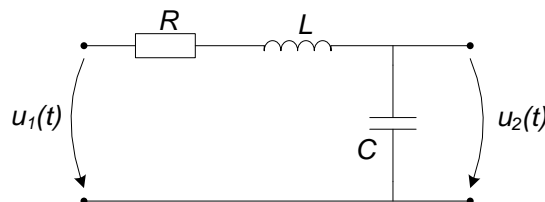
- 3-14** The circuit parameters for the RLC series circuit below are $R=20\Omega$, $L = 40\text{mH}$, $C = 50\mu\text{F}$, and the supplying voltage: $u(t) = 200 \sin(1000t - 30^\circ)$ V. Calculate: a) the inductive and capacitive reactances and the circuit impedance, X_L , X_C , Z ; b) the rms and the instantaneous value of the current, I , $i(t)$; c) the rms and the instantaneous value of resistance-voltage, U_R , $u_R(t)$; d) the rms and the instantaneous value of inductance-voltage, U_L , $u_L(t)$; e) the rms and the instantaneous value of capacitance-voltage, U_C , $u_C(t)$. Draw the circuit diagram.



Problem 3-14

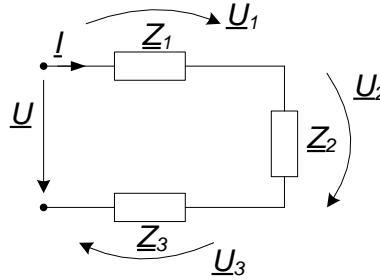
- 3-15** For an RLC series circuit we know $R = 30\Omega$, $X_L = \omega L = 80\Omega$, $X_C = \frac{1}{\omega C} 40\Omega$ and the supplying voltage $u(t) = 100\sqrt{2} \sin(100\pi t - 60^\circ)$ V. Calculate: a) the impedance in phasor form and the circuit impedance, \underline{Z} , Z ; b) the rms and the instantaneous value of circuit current, I , $i(t)$; c) the active, reactive and apparent power, P , Q , S . Verify the conservation of the active and the reactive power. Draw the circuit diagram.

- 3-16** For the circuit below we know $R = 10\Omega$, $X_L = \omega L = 5\Omega$, $X_C = \frac{1}{\omega C} = 15\Omega$ and the voltage $u_1(t) = 100\sqrt{2} \sin 100\pi t$ V. Find the output voltage, $u_2(t)$.



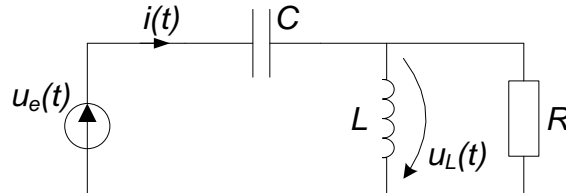
Problem 3-16

- 3-17** For the circuit below we know $\underline{Z}_1 = 3 + j4$, $\underline{Z}_2 = -j6$, $\underline{Z}_3 = 6 + j8$ and the rms current $I = 2\text{A}$. Find: a) the rms voltage on each impedance, U_1 , U_2 , U_3 ; the rms value of the supplying voltage, $u(t)$; c) the active, reactive and apparent power, P , Q , S .



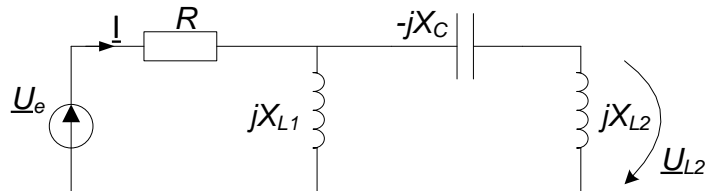
Problem 3-17

- 3-18** For the circuit below we know $R=10\Omega$, $L = \frac{3}{10\pi}\text{H}$, $C = \frac{1}{2.1\pi}\text{mF}$, and the supplying voltage: $u_e(t) = 100\sqrt{2}\sin(100\pi t - 60^\circ)\text{V}$. Calculate: a) the equivalent impedance and the circuit impedance regarding the source terminals, \underline{Z} , Z ; b) the rms value of the current, I ; c) the instantaneous value of the inductor-voltage, $u_L(t)$; d) the active, reactive and apparent power, P , Q , S . Verify the active and reactive power conservation.



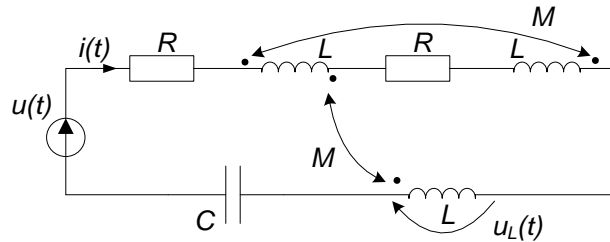
Problem 3-18

- 3-19** For the circuit below we know $R = 8\Omega$, $X_{L1} = \omega L_1 = 2\Omega$, $X_{L2} = \omega L_2 = 1\Omega$, $X_C = \frac{1}{\omega C} 40\Omega$ and the supplying voltage $u_e(t) = 100\sqrt{2}\sin(100\pi t - 60^\circ)\text{V}$. Calculate: a) the equivalent impedance and the circuit impedance regarding the source terminals, \underline{Z} , Z ; b) the rms value of the current, I ; c) the instantaneous value of the inductor-voltage indicated in figure, $u_{L2}(t)$; d) the active, reactive and apparent power, P , Q , S . Verify the active and reactive power conservation.



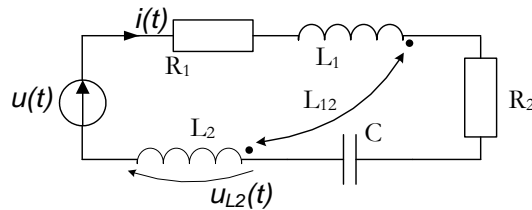
Problem 3-19

- 3-20** For the circuit below we know $R = 15\Omega$, $X_L = \omega L = 30\Omega$, $X_M = \omega M = 20\Omega$, $X_C = \frac{1}{\omega C} = 50\Omega$, and supplying voltage $u(t) = 100\sqrt{2} \sin(100\pi t + 60^\circ) V$. Determine: a) the phasor form of the equivalent impedance and the circuit impedance, \underline{Z} , Z ; b) the rms and the instantaneous value of the current, I , $i(t)$; the rms and the instantaneous voltage indicated in figure, U_L , $u_L(t)$.



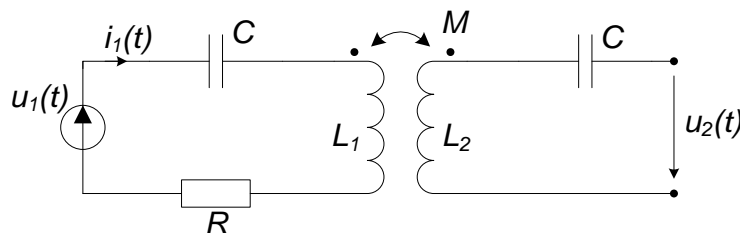
Problem 3-20

- 3-21** Determine the rms value of current, I , and the instantaneous value of the voltage drop on the inductance L_2 , $u_{L2}(t)$, for the circuit below. The circuit parameters are: $R_1 = 15\Omega$, $R_2 = 25\Omega$, $L_1 = L_2 = 2H$, $L_{12} = M = 1H$, $C = 2mF$, $u(t) = 100\sqrt{2} \sin 10t (V)$.



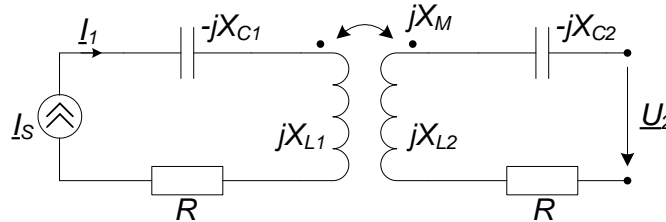
Problem 3-21

- 3-22** Determine the instantaneous value of current, $i_1(t)$, and the rms output-voltage U_2 for the circuit below. The circuit parameters are: $R = 40\Omega$, $X_{L1} = X_{L2} = 60\Omega$, $X_M = 30\Omega$, $X_C = 20\Omega$ and the supplying voltage $u_1(t) = 400 \sin(500t - 30^\circ) V$.



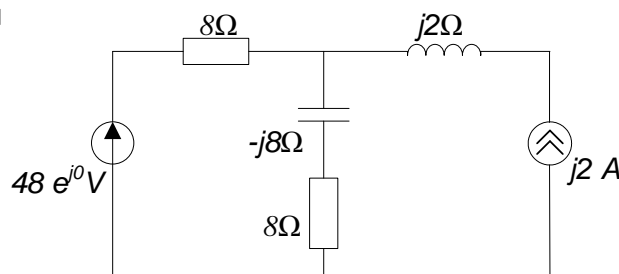
Problem 3-22

- 3-23** For the circuit below we know: $R_1 = R_2 = 50\Omega$, $X_{L1} = \omega L_1 = 10\Omega$, $X_{L2} = \omega L_2 = 40\Omega$, $X_M = \omega M = 20\Omega$, $X_{C1} = \frac{1}{\omega C} = 30\Omega$, $X_{C2} = \frac{1}{\omega C} = 10\Omega$, and current $i_s(t) = 3\sqrt{2} \sin(100\pi t + 30^\circ) V$. Determine: a) the rms value of voltage on the inductor L_1 , U_{L1} ; b) the instantaneous value of the outgoing voltage, $u_2(t)$.



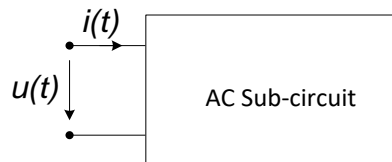
Problem 3-23

- 3-24** For the circuit below find the circuit currents. Verify the active and reactive power conservation.



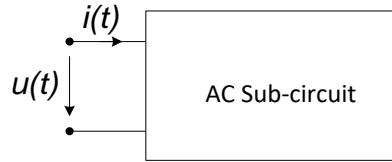
Problem 3-24

- 3-25** The voltage and the current absorbed by the sub-circuit below are: $u(t) = 200\sqrt{2} \sin(500t - 30^\circ) V$ and $i(t) = 5 \sin(500t + 60^\circ) A$. Write the voltage and current phasor operator, \underline{U} , \underline{I} . Find the impedance phasor operator, \underline{Z} , the circuit impedance, Z , the active power, P , and the reactive power, Q , removed by the sub-circuit.



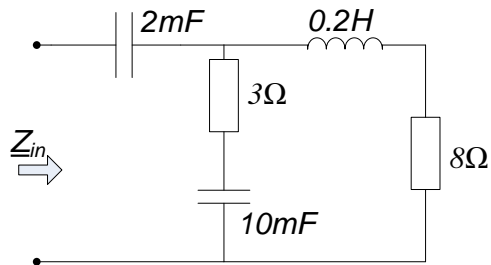
Problem 3-25

- 3-26** The terminals voltage and current absorbed by the sub-circuit below are: $u(t) = 100 \sin(100\pi t + 30^\circ)$ V and $i(t) = 2 \cos 100\pi t$ A. Determine: a) the phasor form of the supplying voltage and current, \underline{U} , \underline{I} ; b) the phasor impedance and sub-circuit impedance, \underline{Z} , Z ; c) the active, reactive and apparent power, P , Q , S .



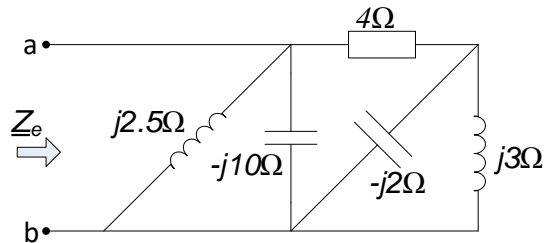
Problem 3-26

- 3-27** Find the input impedance of the circuit below. Assume that the circuit operates at $\omega = 50 \frac{\text{rad}}{\text{s}}$.



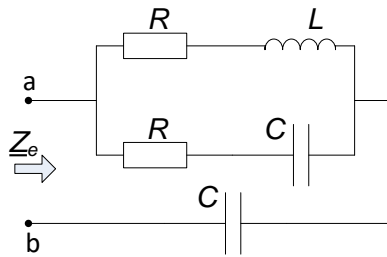
Problem 3-27

- 3-28** For the circuit below find the equivalent impedance \underline{Z}_e , regarding the terminals a and b.



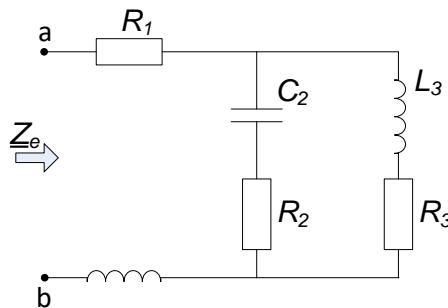
Problem 3-28

3-29 For the circuit below find the equivalent impedance \underline{Z}_e , regarding terminals a and b . The circuit parameters are $R=10\Omega$, $L = \frac{100}{\pi}\text{mH}$, $C = \frac{1}{\pi}\text{mF}$, and $f = 50\text{Hz}$.



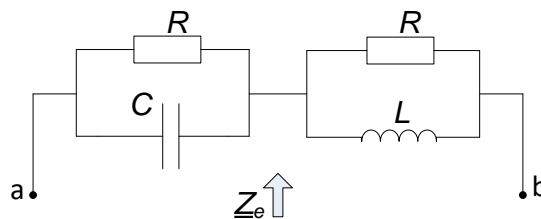
Problem 3-29

3-30 For the circuit below find the equivalent impedance \underline{Z}_e , regarding terminals a and b . The circuit parameters are $R_1 = R_2 = R_3 = 10\Omega$, $L_3 = \frac{20}{\pi}\text{mH}$, $C_2 = \frac{5}{\pi}\text{mF}$, and $f = 50\text{Hz}$.



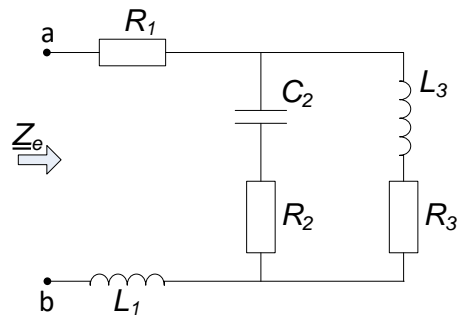
Problem 3-30

3-31 For the circuit below find the equivalent impedance \underline{Z}_e , regarding terminals a and b . The circuit parameters are $R=10\Omega$, $L = \frac{100}{\pi}\text{mH}$, $C = \frac{1}{\pi}\text{mF}$, and $f = 50\text{Hz}$.



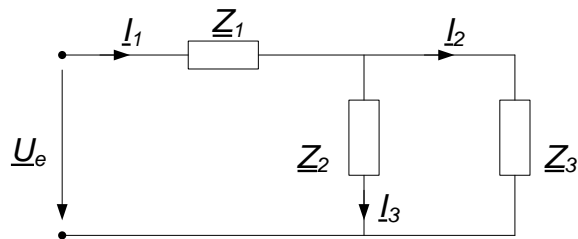
Problem 3-31

3-32 For the circuit below find the equivalent impedance \underline{Z}_e , regarding terminals a and b . The circuit parameters are $R_1 = 5\Omega$, $R_2 = R_3 = 10\Omega$, $L_1 = \frac{150}{\pi}\text{mH}$, $L_3 = \frac{100}{\pi}\text{mH}$, $C_2 = \frac{10^3}{\pi}\mu\text{F}$, and $f = 50\text{Hz}$.



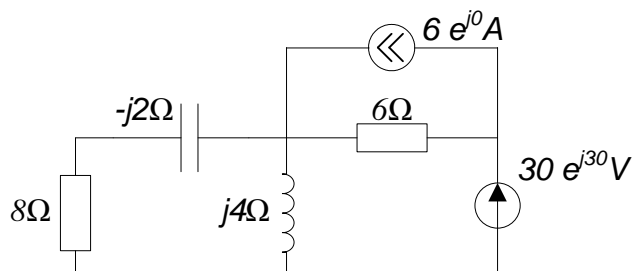
Problem 3-32

3-33 For the circuit below we know $\underline{Z}_1 = 10 + j40$, $\underline{Z}_2 = 20 - j20$, $\underline{Z}_3 = 20 + j20$ and rms current $I = 4\text{A}$. Find: a) the equivalent impedance regarding the source terminals; b) the rms and instantaneous value of supplying voltage, U_e , $u_e(t)$; the active, reactive and apparent power, P , Q , S .



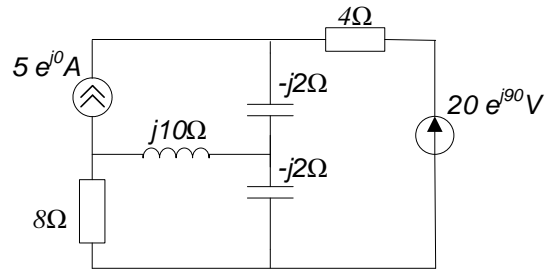
Problem 3-33

3-34 Determine current I_0 in the circuit below using the mesh analysis.



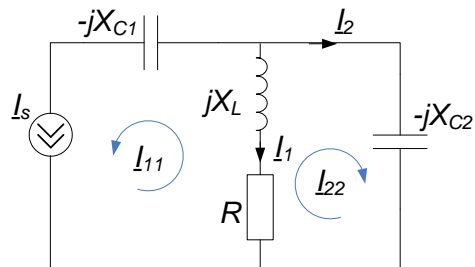
Problem 3-34

3-35 Determine current \underline{I}_0 in the circuit below using the mesh analysis.



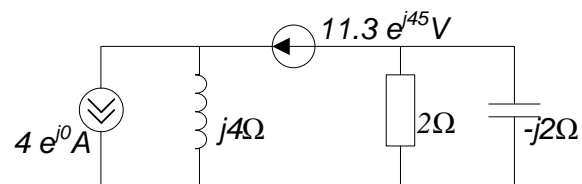
Problem 3-35

3-36 For the circuit below we know: $R=9.3\Omega$, $L=100\mu H$, $C_1=1.2nF$, $C_2=820pF$, $f=570KHz$, $\underline{I}_s = 3 e^{-j30^\circ}$. Using the loop analysis, determine currents \underline{I}_1 and \underline{I}_2 .



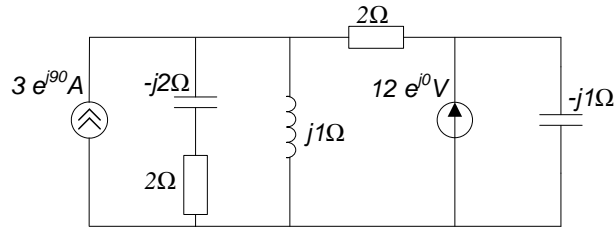
Problem 3-36

3-37 For the circuit below find the potentials of the circuit nodes. Calculate the circuit currents.



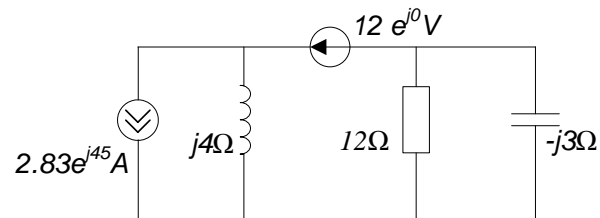
Problem 3-37

3-38 For the circuit below find the potentials of the circuit nodes. Calculate the circuit currents.



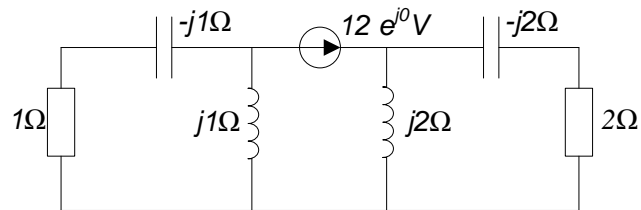
Problem 3-38

3-39 For the circuit below find the potentials of the circuit nodes. Calculate the circuit currents.



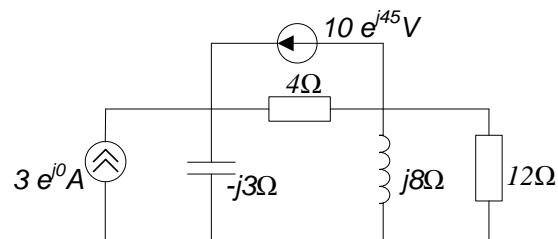
Problem 3-39

3-40 For the circuit below find the potentials of circuit nodes. Calculate the circuit currents.



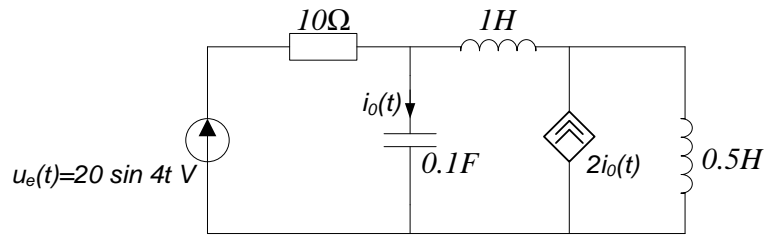
Problem 3-40

3-41 For the circuit below find the potentials of circuit nodes. Calculate the circuit currents.



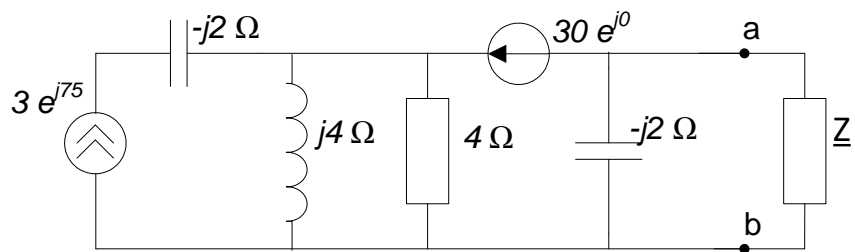
Problem 3-41

3-42 Find $i_o(t)$ in the circuit below using nodal analysis.



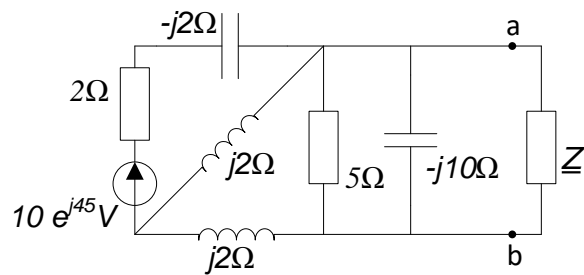
Problem 3-42

3-43 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



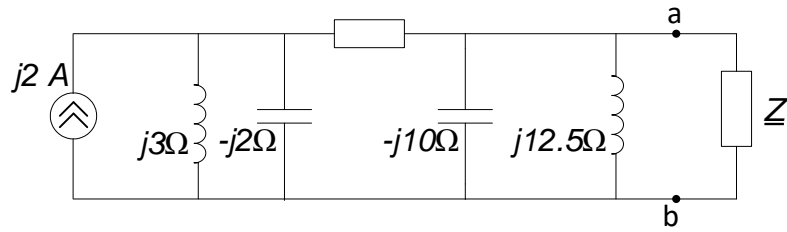
Problem 3-43

3-44 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



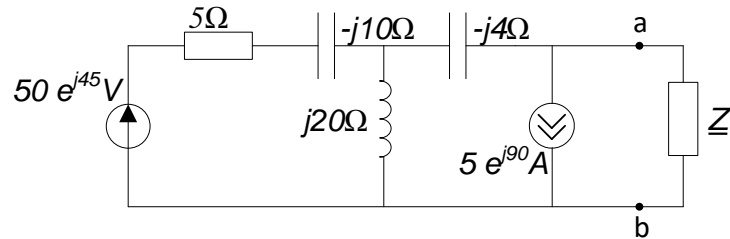
Problem 3-44

3-45 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



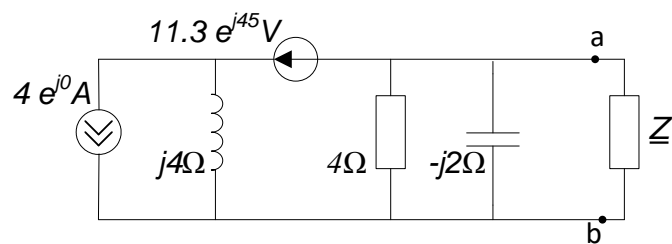
Problem 3-45

3-46 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



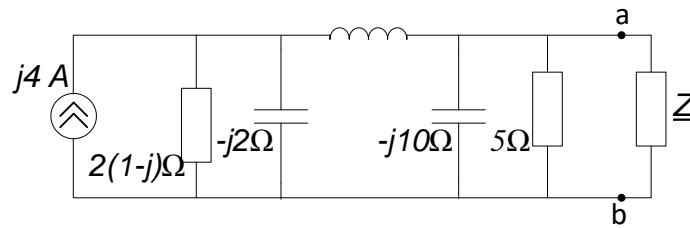
Problem 3-46

3-47 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



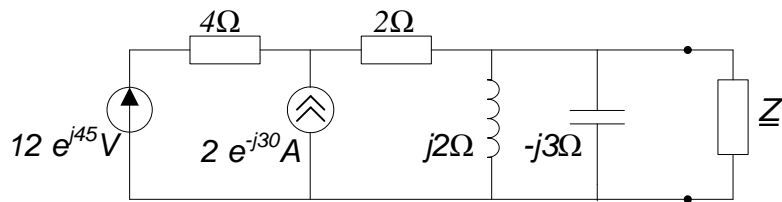
Problem 3-47

3-48 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



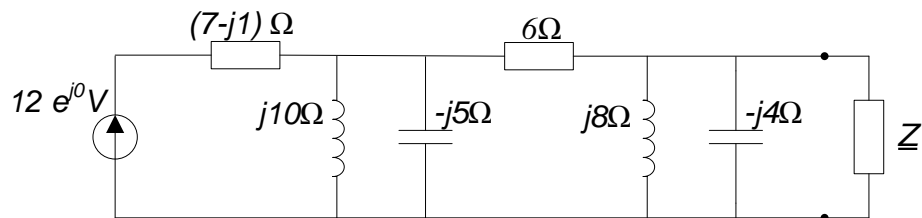
Problem 3-48

3-49 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



Problem 3-49

3-50 For the circuit below determine the impedance value \underline{Z} which will absorb the greatest power from the circuit.



Problem 3-50