SUPERVISED LEARNING IN R: REGRESSION

Logistic regression to predict probabilities

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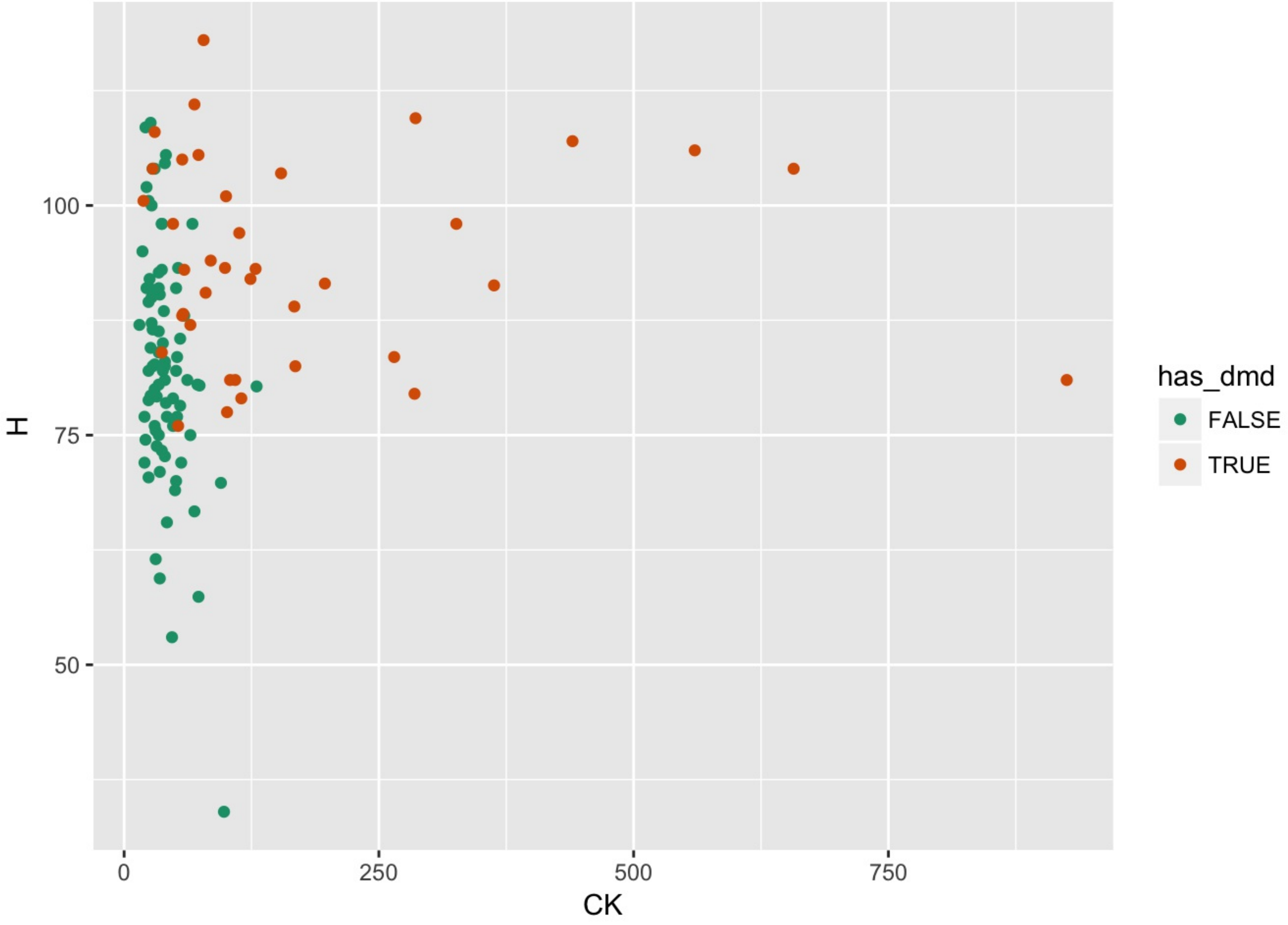
Predicting Probabilities

- Predicting *whether* an event occurs (yes/no): **classification**
- Predicting *the probability* that an event occurs: **regression**
- Linear regression: predicts values in $[-\infty, \infty]$
- Probabilities: limited to [0,1] interval
  - So we'll call it non-linear

Example: Predicting Duchenne Muscular Dystrophy (DMD)



- outcome: has_dmd
- inputs: CK, H

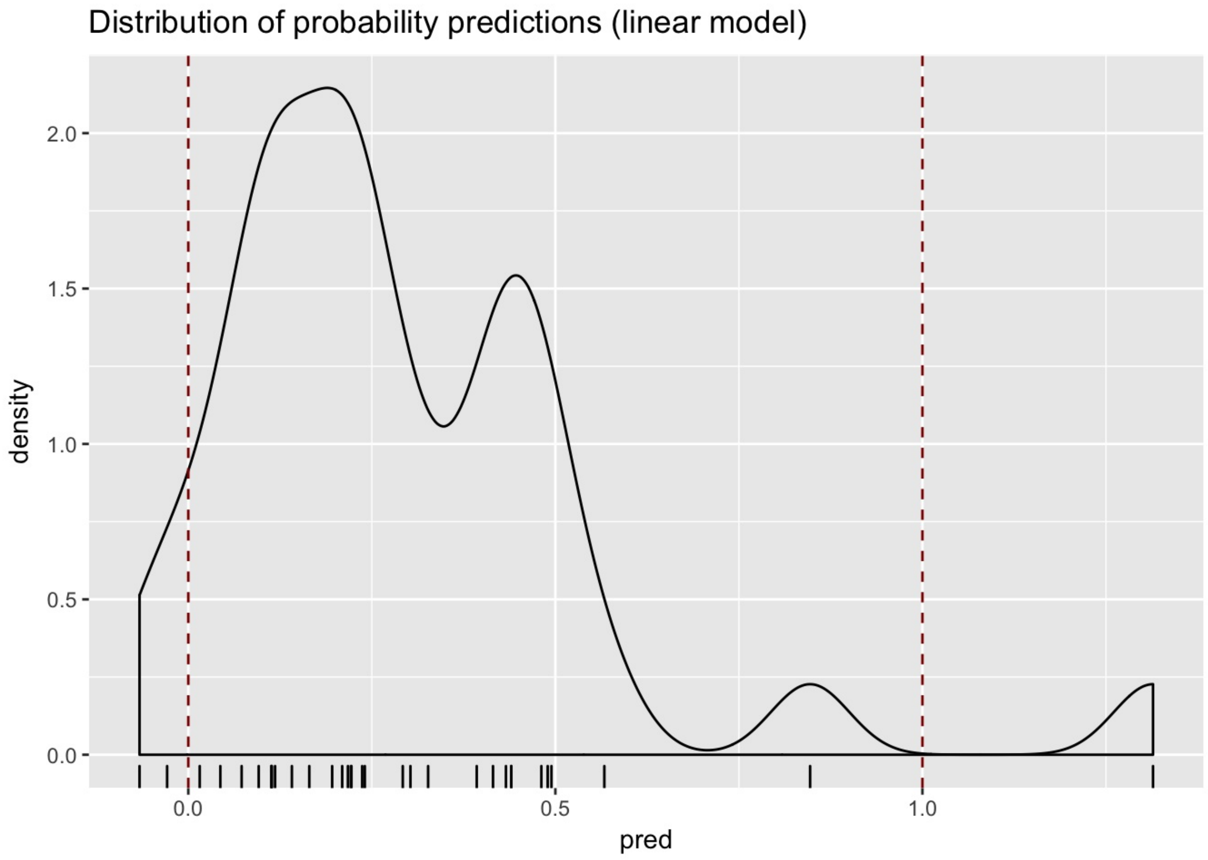
A Linear Regression Model

```
> model <- lm(has_dmd ~ CK + H,
+              data = train)

> test$pred <- predict(
+     model,
+     newdata = test
+ )
```

- outcome: has_dmd $\in$ {0,1}
  - 0: FALSE
  - 1: TRUE

Model predicts values outside the range [0:1]



Logistic Regression

$$log(\frac{p}{1-p}) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \ldots$$

```
glm(formula, data, family = binomial)
```

- Generalized linear model
- Assumes inputs additive, linear in *log-odds*: $log(p/(1-p))$
- family: describes error distribution of the model
    - logistic regression: *family = binomial*

DMD model

```
> model <- glm(has_dmd ~ CK + H, data = train, family = binomial)
```

- outcome: two classes, e.g. a and b
- model returns $Prob(b)$
  - Recommend: 0/1 or FALSE/TRUE

Interpreting Logistic Regression Models

```
> model

## Call:  glm(formula = has_dmd ~ CK + H, family = binomial, data = train)
##
## Coefficients:
## (Intercept)           CK            H
##   -16.22046      0.07128      0.12552
##
## Degrees of Freedom: 86 Total (i.e. Null);  84 Residual
## Null Deviance:       110.8
## Residual Deviance: 45.16     AIC: 51.16
```

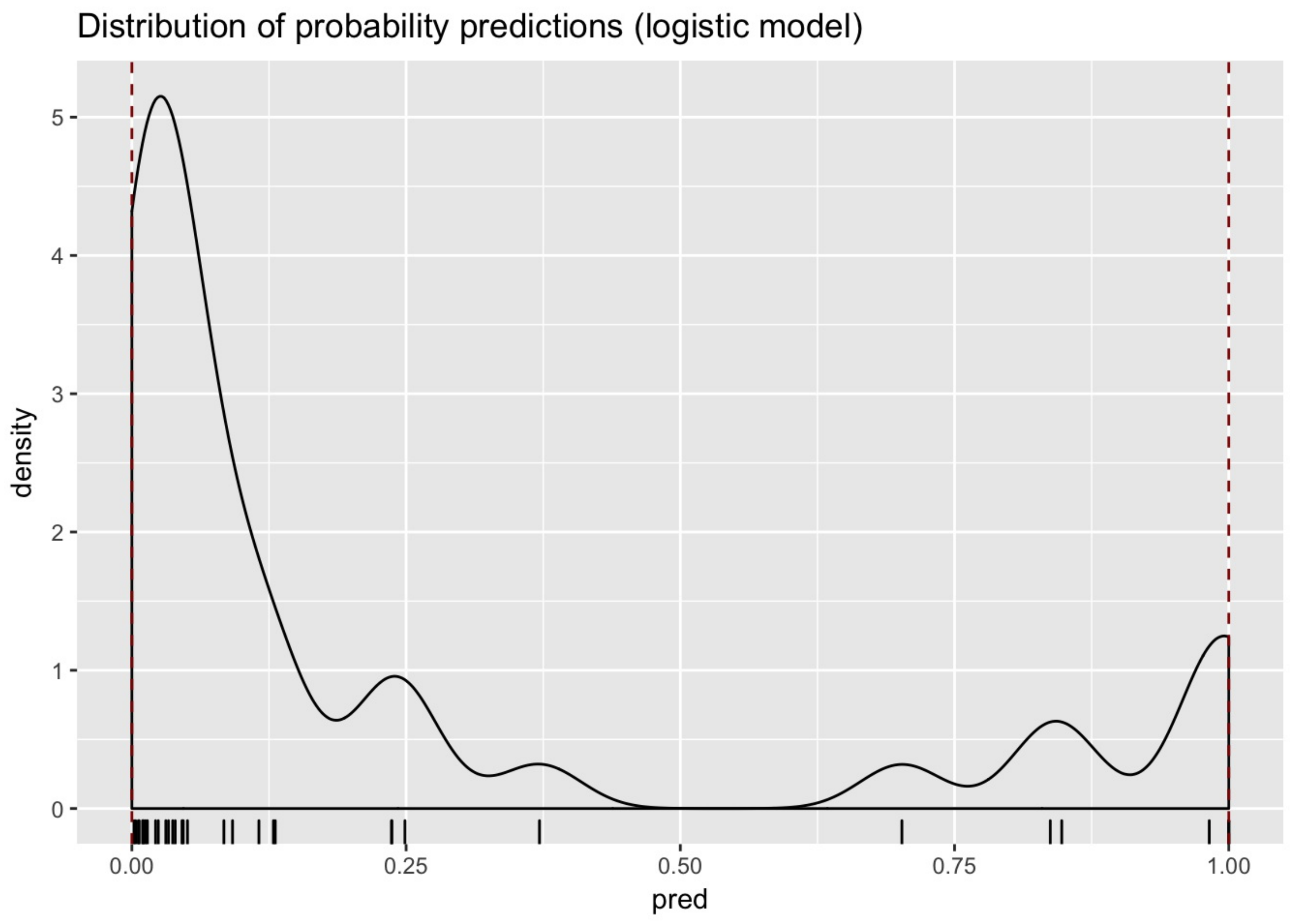
Predicting with a glm() model

```
predict(model, newdata, type = "response")
```

- newdata: by default, training data
- To get probabilities: use **type = "response"**
  - By default: returns log-odds

DMD Model

```
> model <- glm(has_dmd ~ CK + H, data = train, family = binomial)
> test$pred <- predict(model, newdata = test, type = "response")
```



Evaluating a logistic regression model: pseudo-R^2

$$R^2 = 1 - \frac{RSS}{SS_{Tot}}$$

$$pseudoR^2 = 1 - \frac{deviance}{null.deviance}$$

- Deviance: analogous to variance (RSS)
- Null deviance: Similar to SS_{Tot}
- pseudo R^2: Deviance explained

Pseudo-R^2 on Training data

Using broom::glance()

```
> glance(model) %>%
+     summarize(pR2 = 1 - deviance/null.deviance)

##    pseudoR2
## 1 0.5922402
```

Using sigr::wrapChiSqTest()

```
> wrapChiSqTest(model)

## "... pseudo-R2=0.59 ..."
```

Pseudo-R^2 on Test data

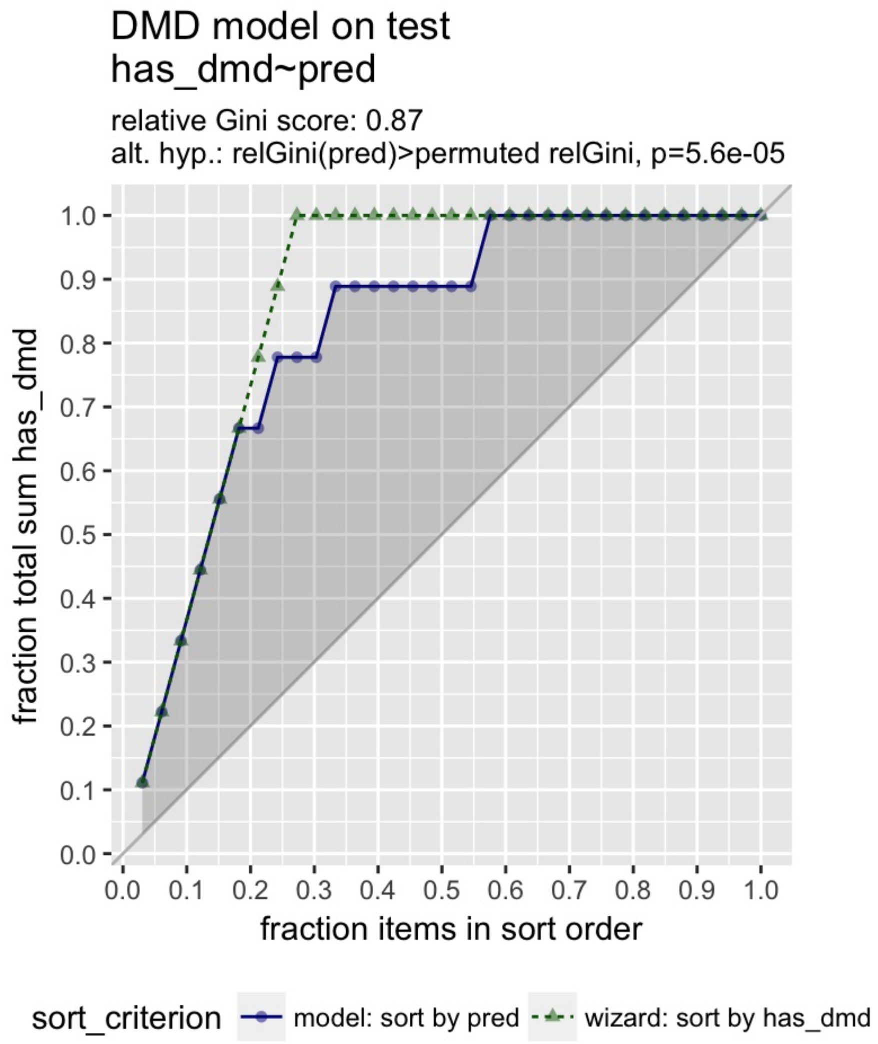
```
# Test data
> test %>%
+     mutate(pred = predict(model, newdata = test, type = "response")) %>%
+     wrapChiSqTest("pred", "has_dmd", TRUE)
```

Arguments:

- data frame
- prediction column name
- outcome column name
- target value (target event)

The Gain Curve Plot

```
> GainCurvePlot(test, "pred","has_dmd", "DMD model on test")
```



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Let's practice!

SUPERVISED LEARNING IN R: REGRESSION

Poisson and quasipoisson regression to predict counts

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Predicting Counts

- Linear regression: predicts values in $[-\infty, \infty]$
- Counts: integers in range $[0, \infty]$

Poisson/Quasipoisson Regression

```
glm(formula, data, family)
```

- family: either `poisson` or `quasipoisson`
- inputs additive and linear in log(count)

Poisson/Quasipoisson Regression

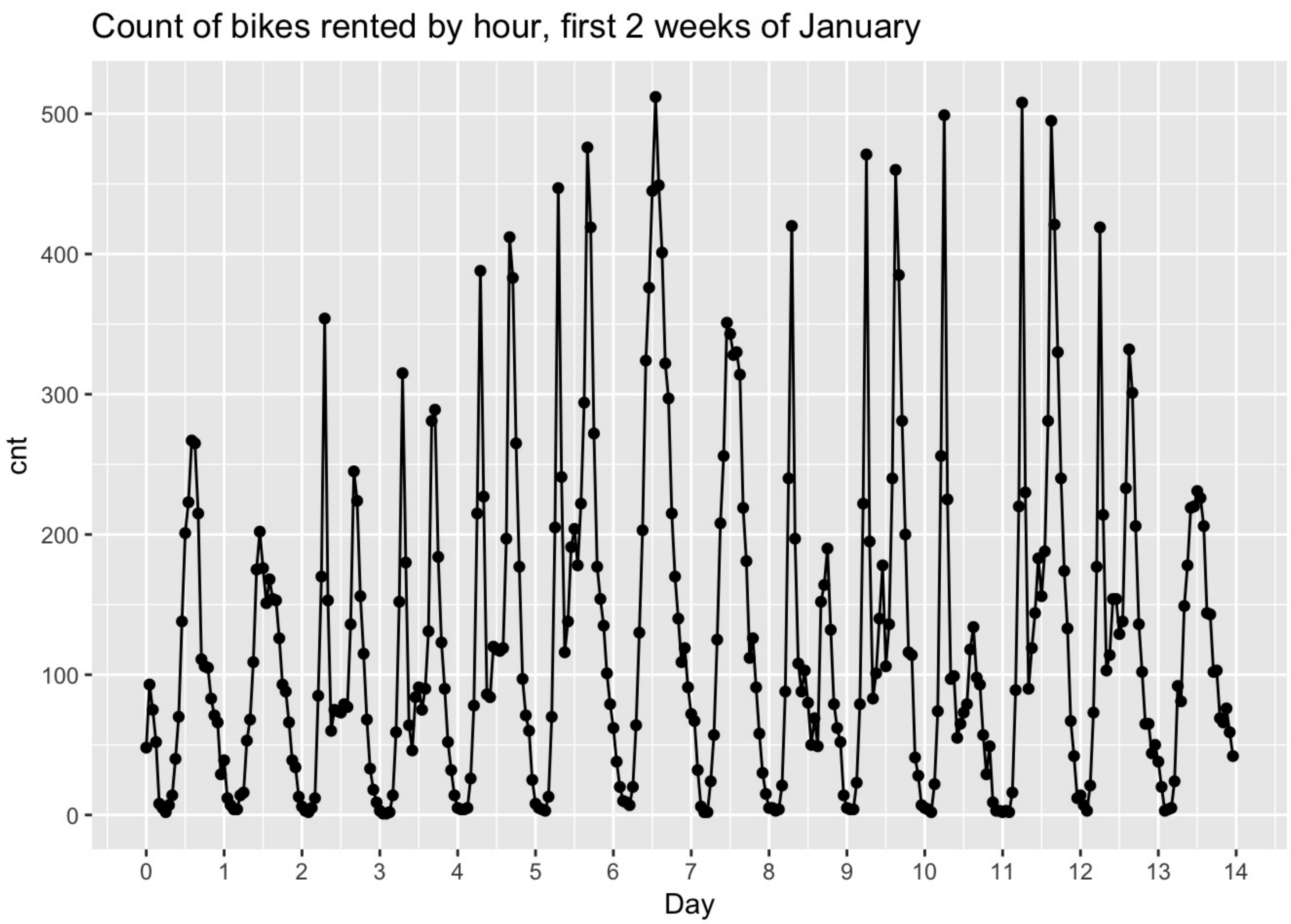
```
glm(formula, data, family)
```

- family: either `poisson` or `quasipoisson`
- inputs additive and linear in log(count)
- outcome: *integer*
  - counts: e.g. number of traffic tickets a driver gets
  - rates: e.g. number of website hits/day
- prediction: expected *rate* or *intensity* (not integral)
  - expected # traffic tickets; expected hits/day

Poisson vs. Quasipoisson

- Poisson assumes that `mean(y) = var(y)`
- If `var(y)` much different from `mean(y)` - quasipoisson
- Generally requires a large sample size
- If rates/counts >> 0 - regular regression is fine

Example: Predicting Bike Rentals



Fit the model

```
> bikesJan %>%
+     summarize(mean = mean(cnt), var = var(cnt))

##       mean      var
## 1 130.5587 14351.25
```

Since var(cnt) >> mean(cnt) $\rightarrow$ *use quasipoisson*

```
> fmla <- cnt ~ hr + holiday + workingday +
+     weathersit + temp + atemp + hum + windspeed

> model <- glm(fmla, data = bikesJan, family = quasipoisson)
```

Check model fit

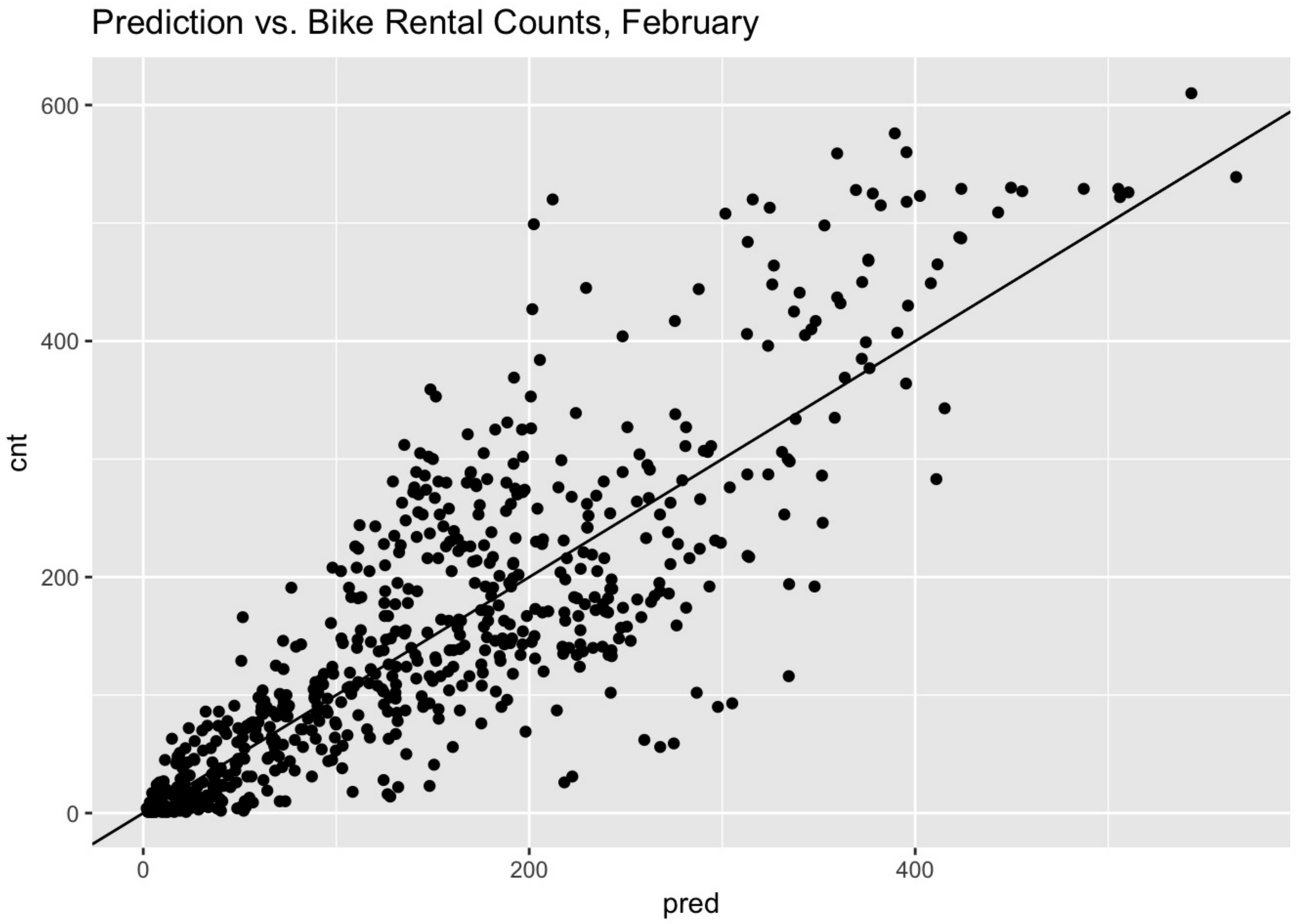
$$pseudoR^2 = 1 - \frac{deviance}{null.deviance}$$

```
> glance(model) %>%
+     summarize(pseudoR2 = 1 - deviance/null.deviance)

##    pseudoR2
## 1 0.7654358
```

Predicting from the model

```
> predict(model, newdata = bikesFeb, type = "response")
```



Evaluate the model

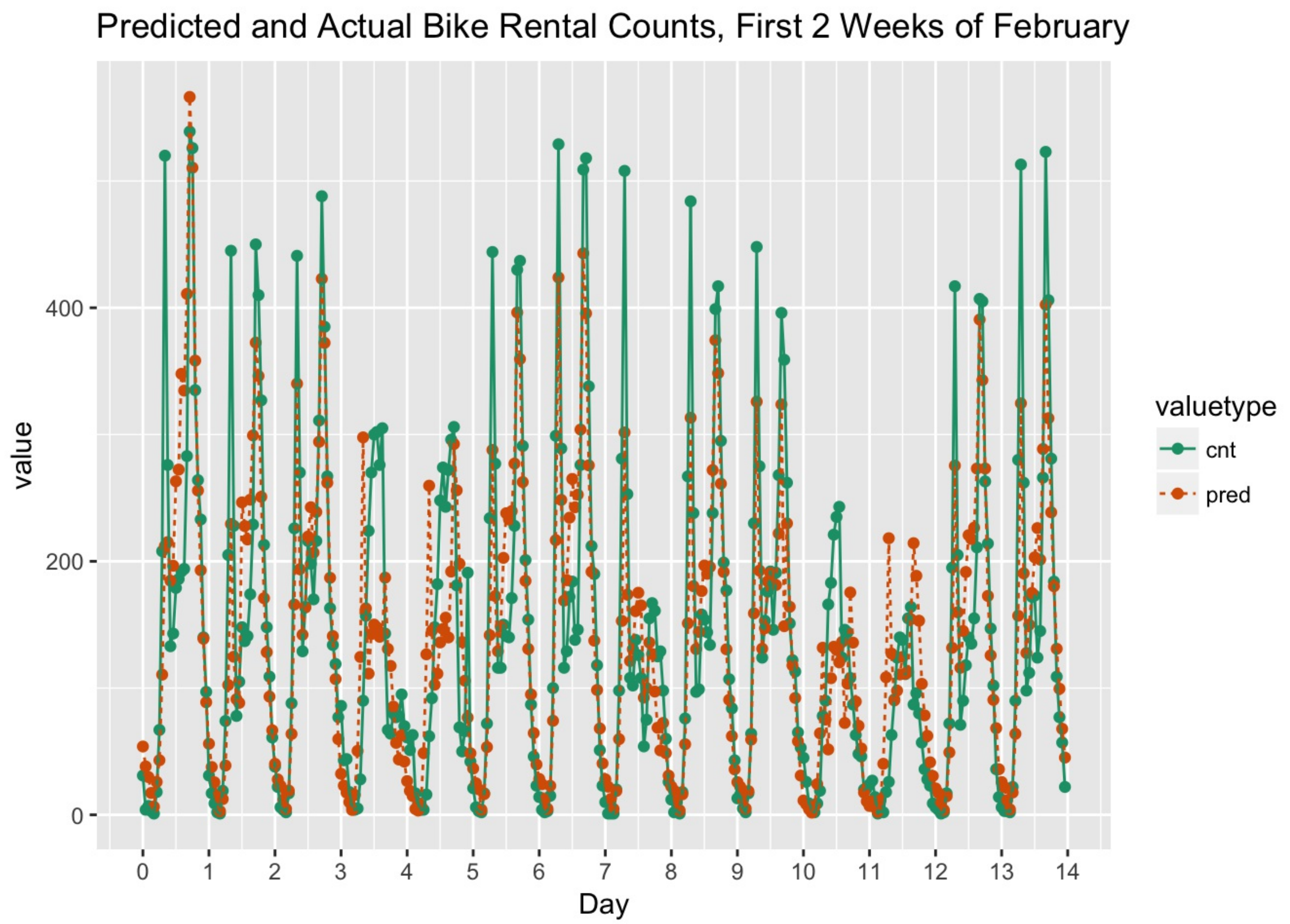
You can evaluate count models by RMSE

```
> bikesFeb %>%
+     mutate(residual = pred - cnt) %>%
+     summarize(rmse = sqrt(mean(residual^2)))

##       rmse
## 1 69.32869

> sd(bikesFeb$cnt)
[1] 134.2865
```

Compare Predictions and Actual Outcomes



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GAM to learn non-linear transformations

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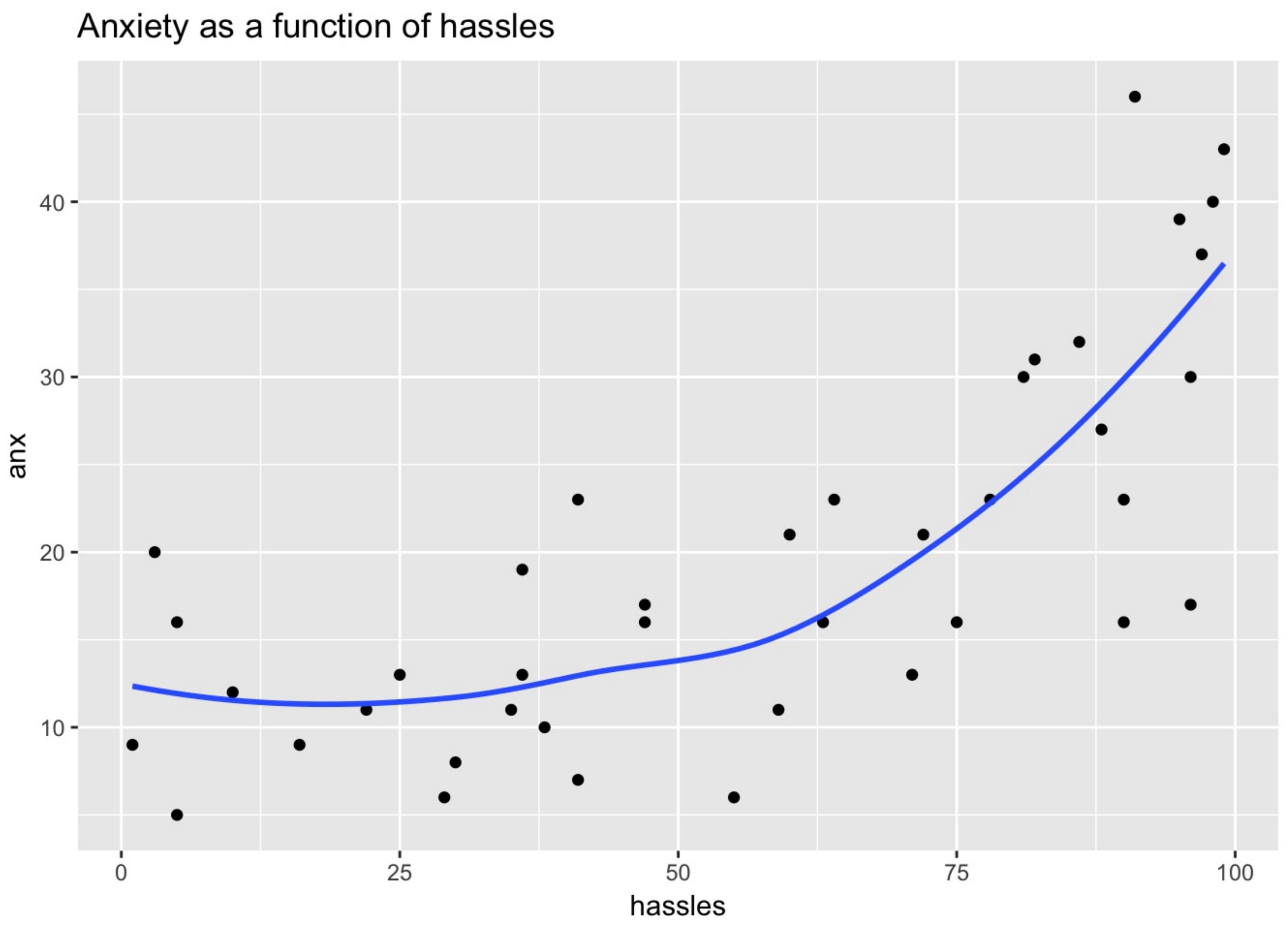
Generalized Additive Models (GAMs)

$$y \sim b0 + s1(x1) + s2(x2) + ...$$

Learning Non-linear Relationships



gam() in the mgcv package

```
gam(formula, family, data)
```

family:

- gaussian (default): "regular" regression
- binomial: probabilities
- poisson/quasipoisson: counts

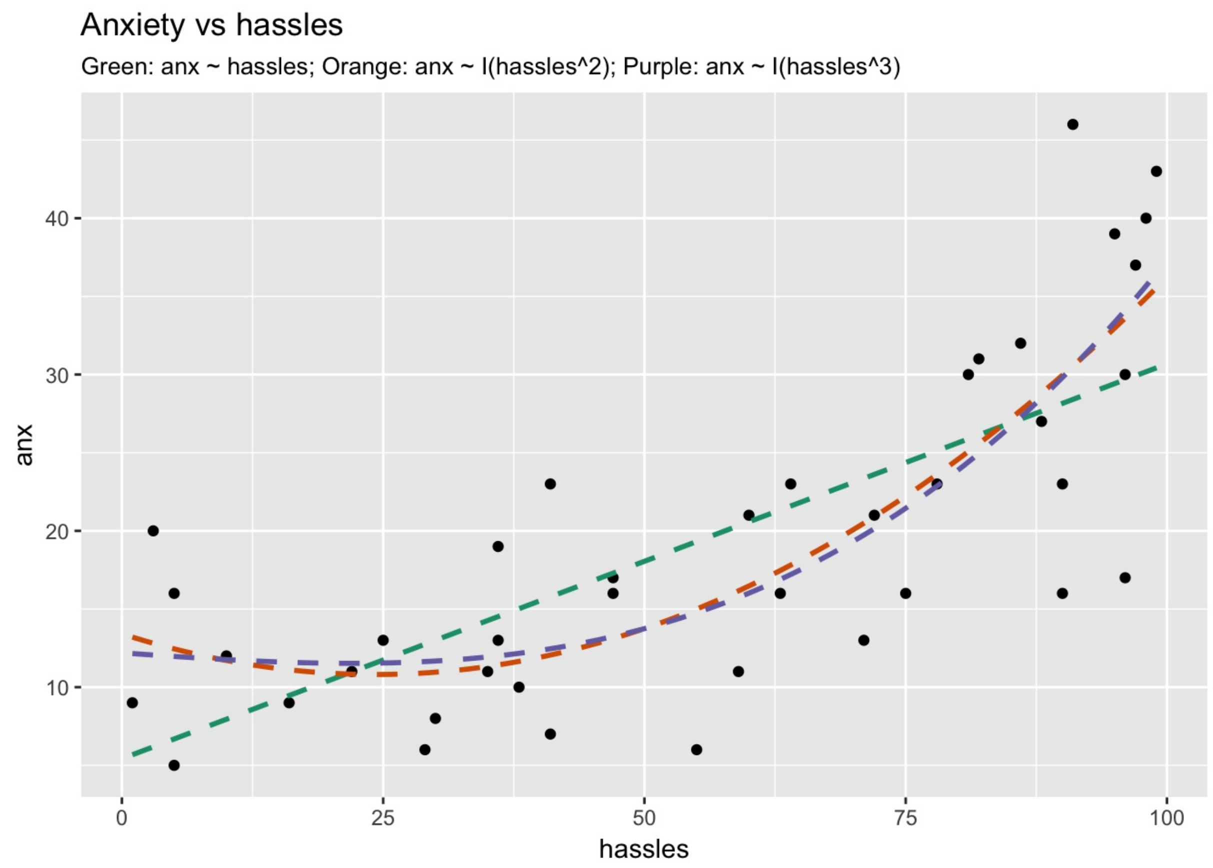
Best for larger data sets

The s() function

```
> anx ~ s(hassles)
```

- s() designates that variable should be non-linear
- Use s() with continuous variables
  - More than about 10 unique values

Revisit the hassles data



Model	RMSE (cross-val)	R^2 (training)
Linear ($hassles$)	7.69	0.53
Quadratic ($hassles^2$)	6.89	0.63
Cubic ($hassles^3$)	**6.70**	**0.65**

GAM of the hassles data

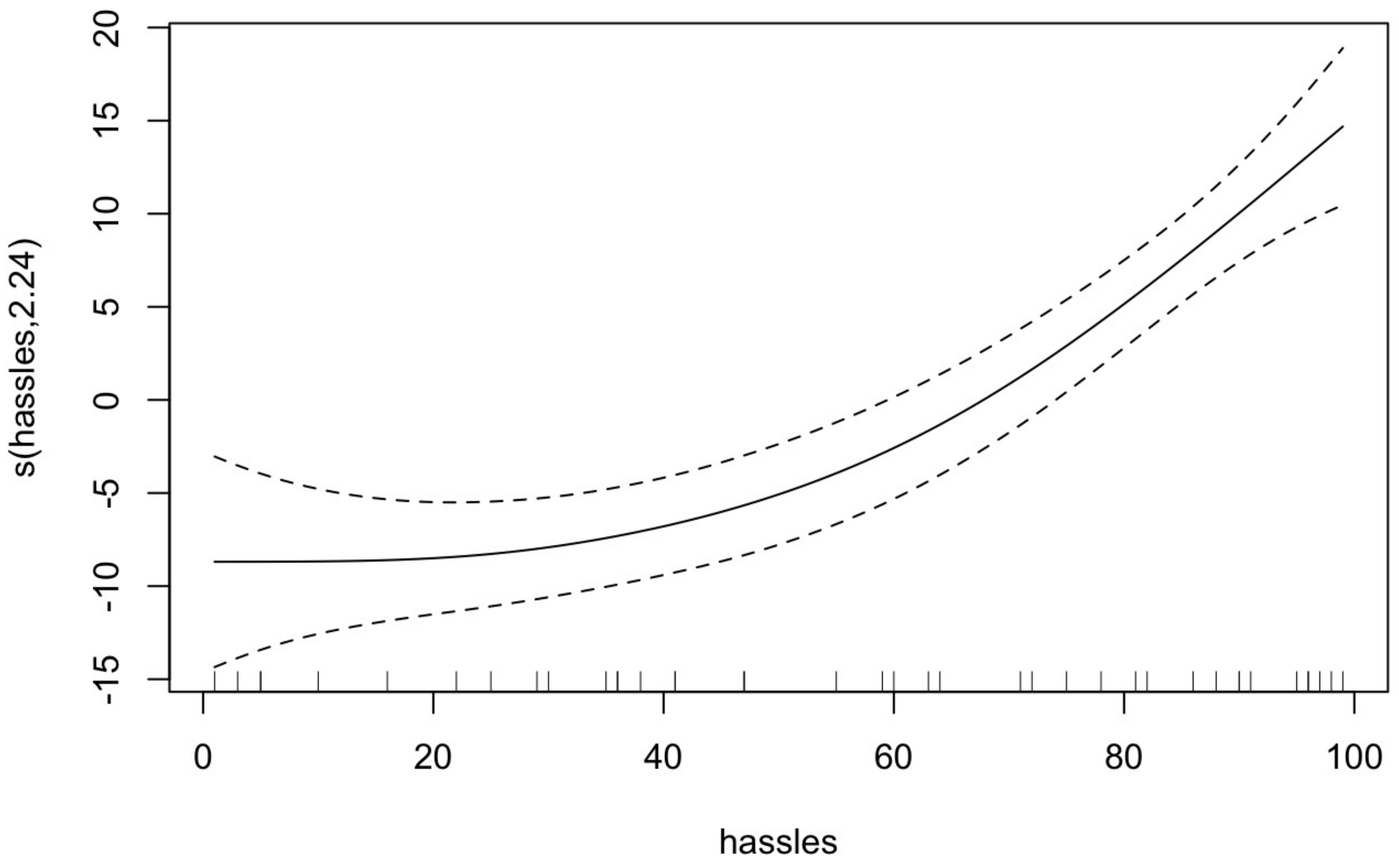
```
> model <- gam(anx ~ s(hassles), data = hassleframe, family = gaussian)

> summary(model)

## ...
##
## R-sq.(adj) =  0.619   Deviance explained = 64.1%
## GCV = 49.132  Scale est. = 45.153    n = 40
```

Examining the Transformations

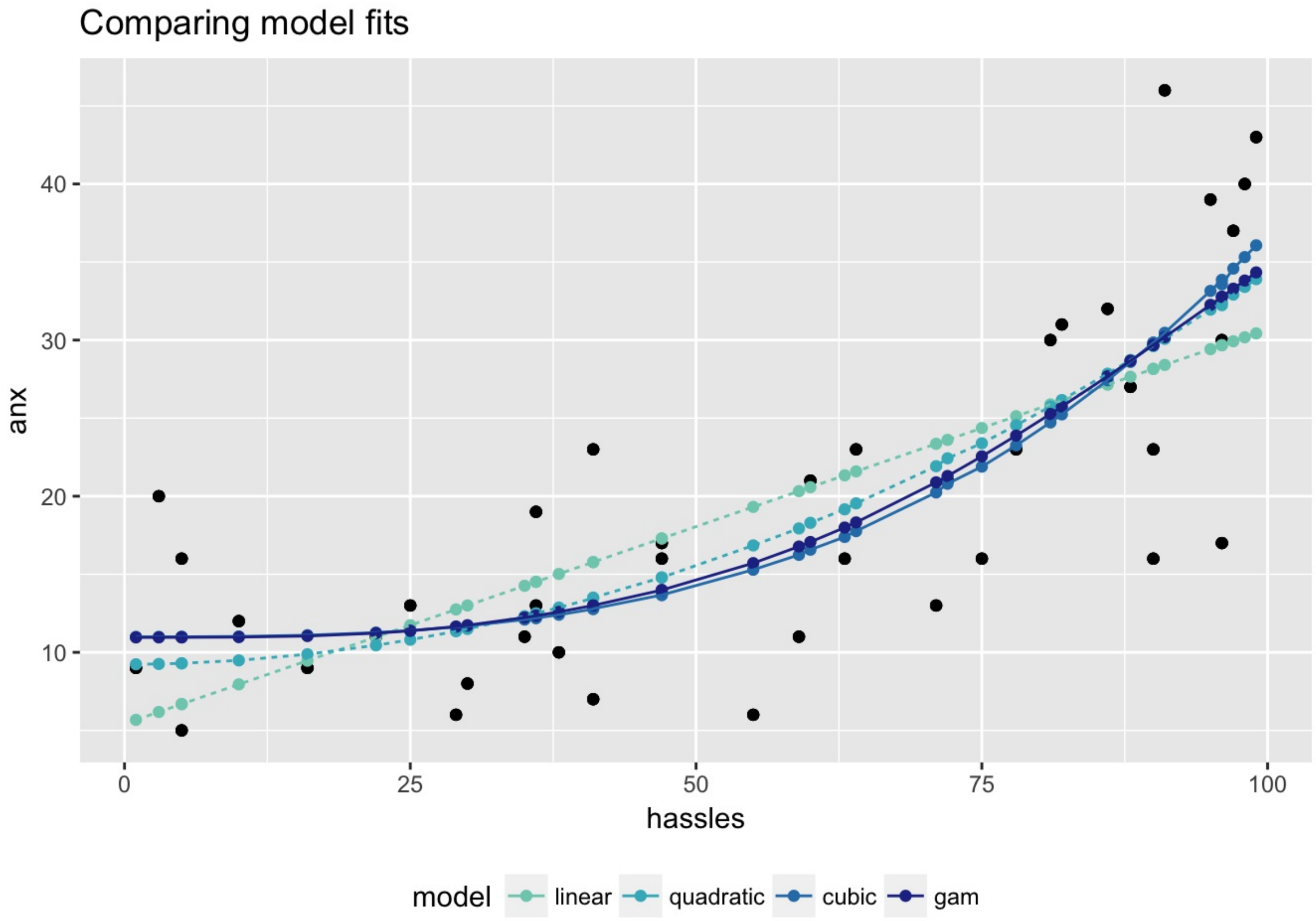
```
> plot(model)
```



y values: predict(model, type = "terms")

Predicting with the Model

```
> predict(model, newdata = hassleframe, type = "response")
```



Comparing out-of-sample performance

Knowing the correct transformation is best, but GAM is useful when transformation isn't known

Model	RMSE (cross-val)	R^2 (training)
Linear ($hassles$)	7.69	0.53
Quadratic ($hassles^2$)	6.89	0.63
Cubic ($hassles^3$)	6.70	0.65
GAM	**7.06**	0.64

- Small data set $\rightarrow$ noisier GAM

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