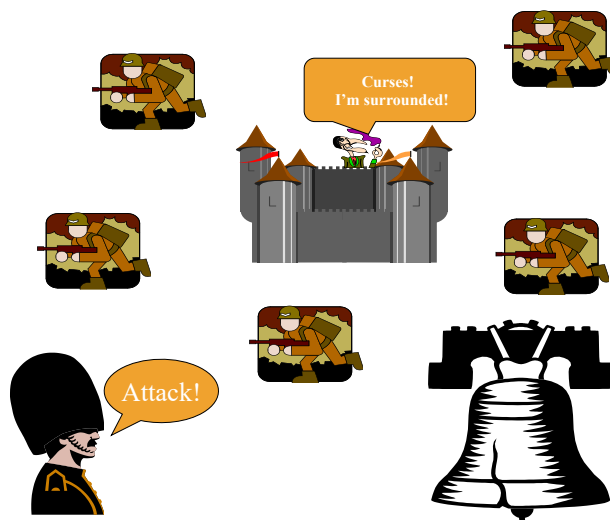


# BYZANTINE AGREEMENT

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## Byzantine Agreement



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## Byzantine Agreement

- Suppose 3 generals (A,B,C), one of whom may be traitor
- General A knows he's loyal
- Take majority vote?
- But traitor may be saying different things to A and other loyal general
- Lower bound: Need at least 4 generals if 1 traitor
- Generally: Need  $3f+1$  processors if  $f$  are faulty

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## Byzantine Agreement

- Assume wlog general sending orders to lieutenants
- Give commanders ability to sign their messages
- Assume no more than  $f$  failures, and  $f+2$  commanders

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## Protocol

- Round 1:
  - General broadcasts his order (true or false) to all lieutenants
- Round  $i$ , for loyal commander:
  - Consider any *messages* with  $i-1$  signatures received in previous round
  - Record any *orders* signed by the general
  - Commander adds his signature to each *message*, and broadcasts result to all other processes
  - Repeat this round  $f$  times for total  $f+1$  rounds

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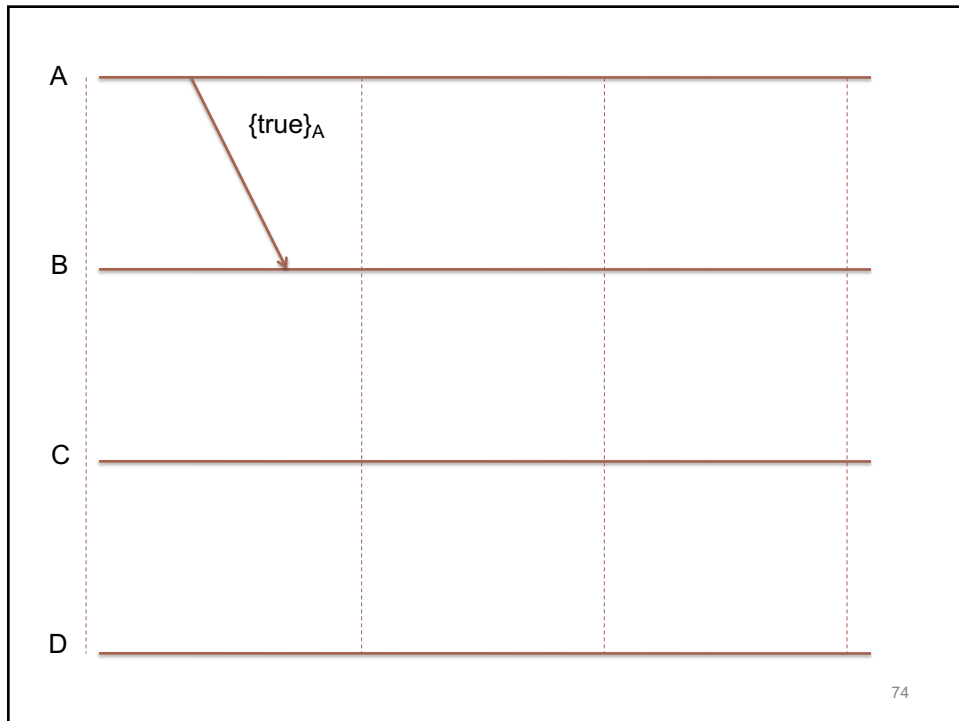
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## Protocol

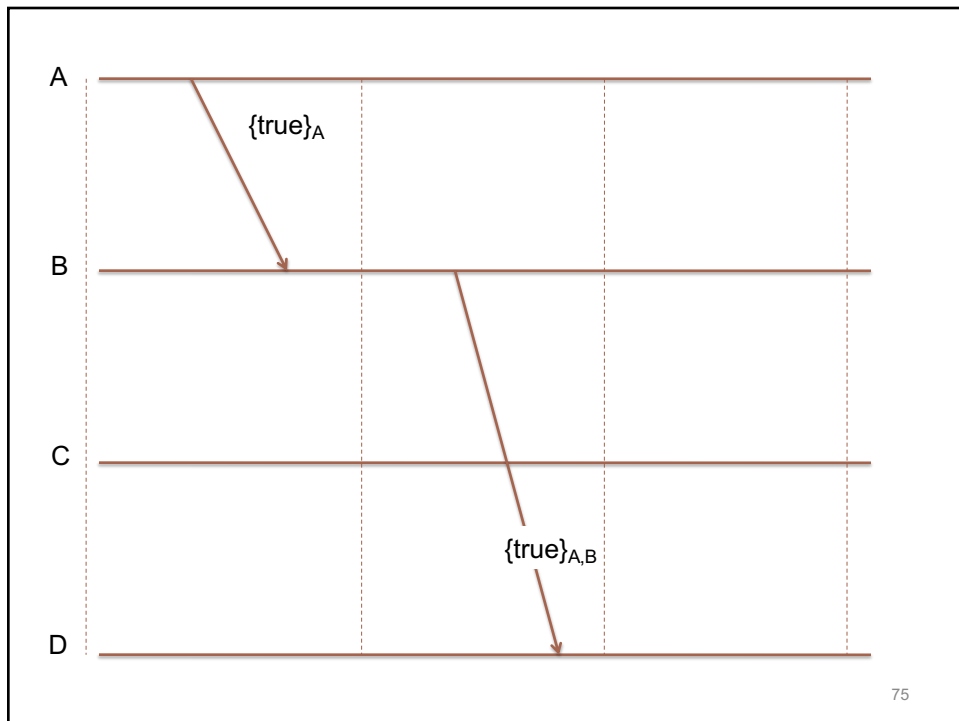
- After  $f+1$  rounds, each loyal commander considers the orders he has recorded:
  - If empty, or conflicting orders, then choose default decision
  - If exactly one order, then execute that order

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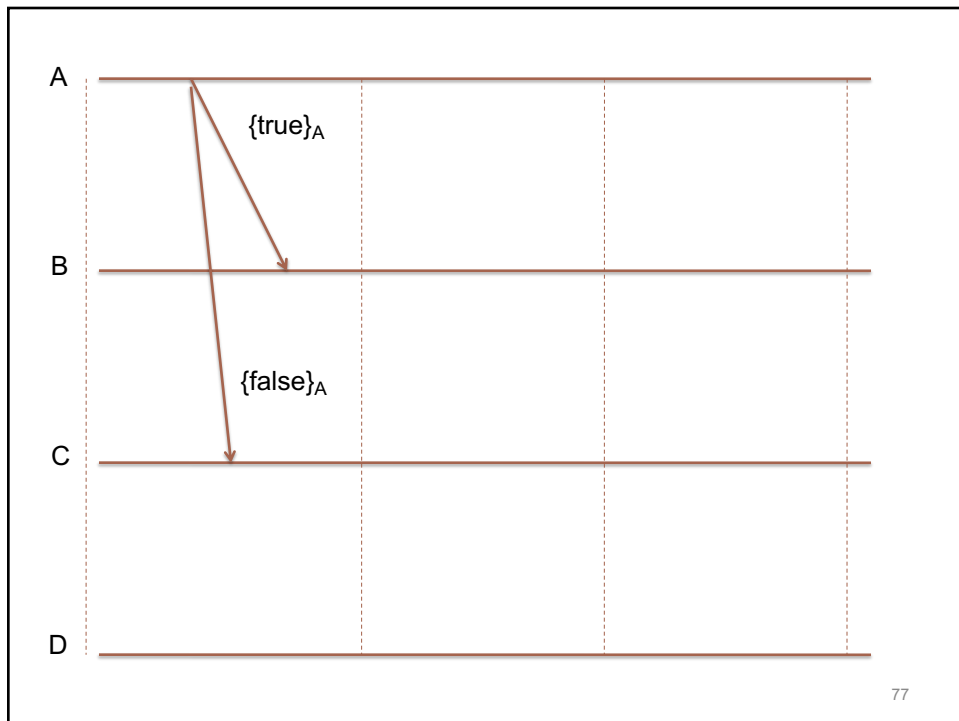
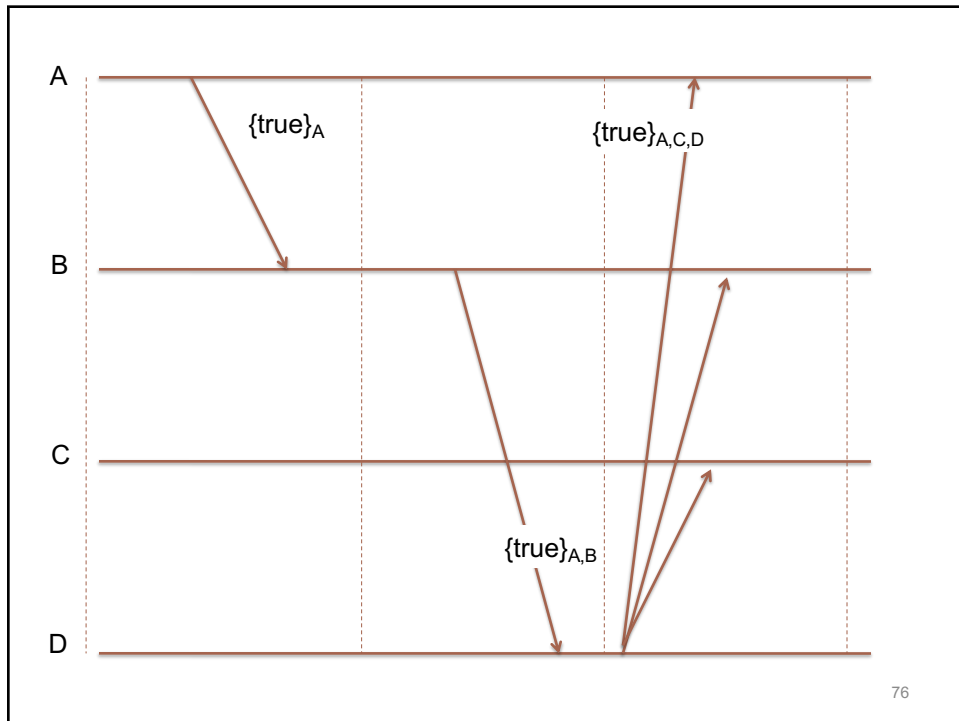
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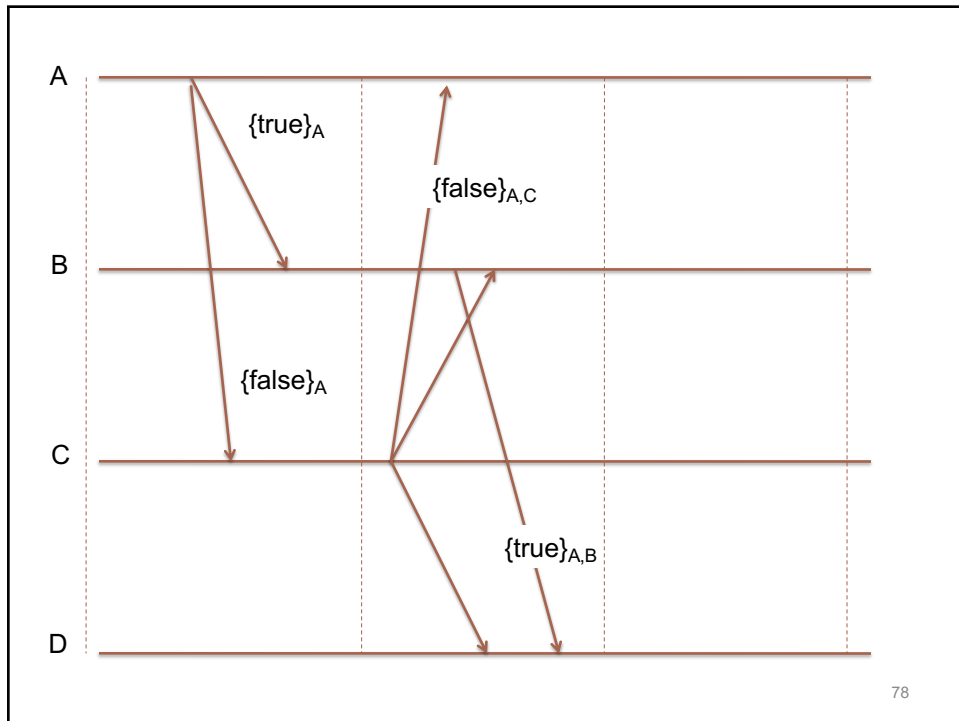


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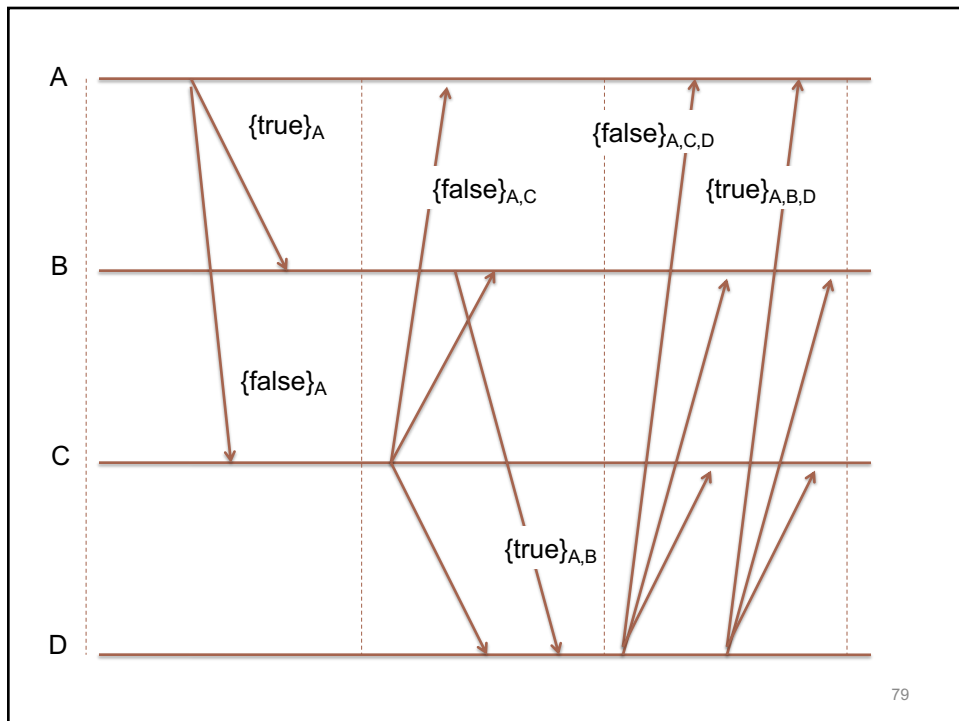


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## Why does this work?

- Suppose general is loyal
  - Broadcasts order in first round
  - But lieutenants do not know if he is loyal
  - Therefore run for  $f$  more rounds
- Disloyal general would:
  - Relay conflicting orders via disloyal lieutenants
  - Orders delivered to loyal lieutenants in last round
  - But protocol requires  $f+1$  rounds,  $f+1$  signatures
  - So orders relayed through at least one loyal lieutenant

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## Observations

- Complexity of protocol:
  - $O(N^2)$  messages on each round!
  - All Byzantine protocols are expensive
- Rabin: randomized protocols
  - Each process has a form of coin available to it
  - Can flip coin in each round
  - With randomness, very rapid agreement “with high probability” in very little time

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