

MEV - 11

$$E = U + K.E + P.E$$

$$E_2 - E_1 = (U_2 - U_1) + \frac{1}{2} m(V_2^2 - V_1^2) + mg(h_2 - h_1) \quad \left. \begin{array}{l} \text{Energy eq.} \\ \text{for finite changes} \end{array} \right\}$$

Heat in  $\Rightarrow$  +ive (absorb) (endothermic)

Work done by system  $\Rightarrow$  +ive

$$\text{Inst. rate } \dot{E}_{cv} = \dot{Q} - \dot{W} \quad \left. \begin{array}{l} \text{Energy eq.} \\ \text{for control mass/volume} \end{array} \right\}$$

$= +in - out$

$$\Delta U = Q - W$$

$$1^{st} \text{ law thermo. } \oint Q = \oint W$$

$$Q_{net \text{ in}} = W_{net \text{ out}}$$

Isobaric  $\Rightarrow$  P: same

Isothermal  $\Rightarrow$  T: same  $\Rightarrow$  Ideal gas law  $P_1 V_1 = P_2 V_2$

Insulated  $\Rightarrow Q = 0$

Adiabatic  $\Rightarrow$  No heat transfer  $\Rightarrow Q = 0$   
 Ideal gas under isothermal process  $\Rightarrow \Delta U = 0$

$$\Delta U = Q - W = -W$$

$$\eta = \frac{W_{net \text{ out}}}{Q_{net \text{ in}}} \times 100\%$$

$$\text{Work done (Ideal gas)} = W = nRT \ln\left(\frac{V_2}{V_1}\right) = P_1 V_1 \ln\left(\frac{V_2}{V_1}\right)$$

$$\delta W = F dx$$

$$\delta W = P dV = F \cdot ds$$

$$KE = \frac{1}{2} m V^2$$

$$W_2 = P(V_2 - V_1) = (P_2 - P_1)(V_2 - V_1) = m(P_2 - P_1)(v_2 - v_1)$$

Unit: Work  $\Rightarrow$  Joule (J)  $\left\{ \begin{array}{l} \text{Heat} \Rightarrow \text{Joule (J)} \end{array} \right.$

Power  $\Rightarrow$  Watt (W)

$$\dot{W}(\text{Power}) = T(\text{torque}) \omega(\text{ang. velocity})$$

$$\text{Spec. Work} \Rightarrow w = \frac{W}{m}$$

$$P \propto \frac{1}{V}, P \propto T, V \propto T$$

$$PV = RT$$

$$PV = mRT = n\bar{R}T$$

$$R = \frac{\bar{R}}{M}$$

$$n = \frac{m}{M}$$

$$P\dot{V} = \dot{m}RT = \dot{m}\bar{R}T$$

$$\dot{V} = \frac{dV}{dt} = \frac{DV}{Dt}$$

Steps:-

① Sketch (mass forces, heat flows, work)

② Control Mass/Volume

③ General laws (Energy Eq.)

④ Specific laws

⑤ Solve using diagrams/tables  $P, V, T - V$

⑥ Formulate

$$\Delta U + \Delta K.E + \Delta P.E = Q - W$$

$$Q_{Total} = \int \delta Q$$

$$\text{Spec. heat transfer: } q = \frac{Q}{m}$$

Conduction: due to collision of molecules (direct contact)

$$\dot{Q} = -kA \frac{dT}{dx} \quad \left. \begin{array}{l} \text{Fourier's Law} \\ \text{Conduction} \\ \text{thermal conductivity} \\ \text{Area} \\ \text{temperature gradient} \end{array} \right\}$$

k (metals): about  $100 \frac{W}{mK}$

k (insulators): upto  $0.01 \frac{W}{mK}$

Convection: due to moving fluid (liquid or gas)

$$\dot{Q} = hA\Delta T \quad \left. \begin{array}{l} \text{Newton's Law} \\ \text{of Cooling} \end{array} \right\}$$

convective heat transfer coeff.  $\left(\frac{W}{m^2K}\right)$

- ① Natural
- ② Forced

Radiation: due to electromagnetic waves

$$\dot{Q} = \epsilon \sigma A T_s^4 \quad \left. \begin{array}{l} \text{Stefan-Boltzmann Law} \\ \text{emissivity (0 to 1)} \\ \text{S-B const } (5.67 \times 10^{-8} \frac{W}{m^2 K^4}) \\ \text{surface area} \\ \text{surface temp. (could be } \Delta T_s^4) \end{array} \right\}$$

$$\text{Spec. internal energy: } u = \frac{U}{m} \Rightarrow U = um = mu$$

$$U = U_{liq} + U_{vap}$$

$$u = u_f + x u_{fg}$$

$$v = v_f + x v_{fg}$$

$x = 0 \Rightarrow \text{sat. liq}$   
 $x = 1 \Rightarrow \text{sat. vap}$

CL	SV
$P > P_{sat}$	$P < P_{sat}$
$T < T_{sat}$	$T > T_{sat}$
$V < v_f$	$V > v_g$
$h < h_f$	$h > h_g$
$u < u_f$	$u > u_g$
$\downarrow$ $v = v_f$ $s < s_{fg}$	$\downarrow$ $v = v_g$ $s > s_{fg}$

$v_f < v < v_g$   
 $u_f < u < u_g$   
 $h_f < h < h_g$   
 Two phase  $(0 \leq x \leq 1)$

$$m = \frac{V}{v} \Rightarrow m_{liq} = \frac{V_{liq}}{v_f} \Rightarrow m_{vap} = \frac{V_{vap}}{v_g}$$



$$W_{12} = P(V_2 - V_1)$$

$$U = Q - W$$

$$Q_{12} = (U_2 - U_1) + P(V_2 - V_1) \therefore Q = U + W$$

Enthalpy:  $H = U + PV$  Unit:  $\frac{kJ}{kg}$

$$Q_{12} = H_2 - H_1 \text{ (const. pressure)}$$

Spe. Enthalpy:  $h = H + PV$   
 $h = h - P v$

$$h = h_f + x h_{fg}$$

$$h = \frac{H}{m}$$

Eq. of Continuity  $\frac{dm_{cv}}{dt} = \sum \dot{m}_i - \sum \dot{m}_{out}$

if  $\frac{dm_{cv}}{dt} = 0$ , mass constant

Vol. flow rate  $\dot{V} = VA$  (velocity)

Mass. flow rate  $\dot{m} = \rho AV = \frac{AV}{v}$

Unit:  $kg/s$

Energy Eq. for control mass

$$E_2 - E_1 = Q_{12} - W_{12}$$

or  $\frac{dE_{c.m.}}{dt} = \dot{Q} - \dot{W}$

Work flow  $\dot{W} = FV = P\dot{V} = P\dot{m}v$

Energy Eq. for control volume

$$\frac{dE_{c.v.}}{dt} = \dot{Q}_{cv} - \dot{W}_{cv} + \sum \dot{m}_i \left( h_i + \frac{V_i^2}{2} + g z_i \right) - \sum \dot{m}_e \left( h_e + \frac{V_e^2}{2} + g z_e \right)$$

## Steady-State Process

- $\dot{m}_i$  &  $\dot{m}_e$ : constant
- Prop. of fluid in & out are constant
- Energy within control doesn't accumulate over time

Control volume: stationary

$\dot{m}_{cv} = 0$ ,  $\frac{dE_{c.v.}}{dt} = 0$

Rate of heat & work: constant

Continuity Eq.  $\sum \dot{m}_i = \sum \dot{m}_e$

Energy Eq.  $\dot{Q}_{cv} + \sum \dot{m}_i \left( h_i + \frac{V_i^2}{2} + g z_i \right) = \sum \dot{m}_e \left( h_e + \frac{V_e^2}{2} + g z_e \right) + \dot{W}_{cv}$

Continuity Eq.  $\dot{m}_i = \dot{m}_e = \dot{m}$

Energy Eq.  $\dot{Q}_{cv} + \dot{m} \left( h_i + \frac{V_i^2}{2} + g z_i \right) = \dot{m} \left( h_e + \frac{V_e^2}{2} + g z_e \right) + \dot{W}_{cv}$

$q = \frac{\dot{Q}_{cv}}{\dot{m}}$  Unit:  $kJ/kg$

heat transfer per unit mass

$w = \frac{\dot{W}_{cv}}{\dot{m}}$  Unit:  $kJ/kg$

work per unit mass

$$q + h_i + \frac{V_i^2}{2} + g z_i = h_e + \frac{V_e^2}{2} + g z_e + w$$

Heat Exchanger:  $Q \neq 0$ ,  $K.E. = 0$ ,  $P.E. = 0$ ,  $W = 0$

Nozzle:  $Q = 0$ ,  $W = 0$ ,  $P.E_i \approx P.E_e$ ,  $\dot{m} = \text{constant}$

Diffuser: Same as nozzle, but in opposite direction.  
 $K.E_i \uparrow$   $K.E_e \downarrow$   $h_i + \frac{V_i^2}{2} = h_e + \frac{V_e^2}{2}$

Throttle:  $K.E. = 0$ ,  $P.E. = 0$ ,  $W = 0$ ,  $Q = 0$

$$h_i = h_e$$

Turbines:  $P.E. = 0$ ,  $K.E_i = 0$ ,  $Q = 0$ ,  $K.E_e = 0$

Compressor/Pump:  $P.E. = 0$ ,  $K.E_i = 0$ ,  $K.E_e = 0$ ,  $Q = 0$

## MID-I

Total Energy =  $K.E. + P.E. + U$

$$\Delta U = Q - W = \frac{1}{2} m v^2 + m g h + U$$

- $\Rightarrow W \rightarrow +$ : on system
- $\Rightarrow W \rightarrow -$ : by system
- $\Rightarrow Q \rightarrow -$ : release (exo)
- $\Rightarrow Q \rightarrow +$ : absorb (endo)

Sp. Volume:  $v = \frac{V}{m}$

Sp. Density:  $\frac{m}{V} = \frac{1}{v} \Rightarrow \rho = \frac{m}{V}$

$P \propto \frac{1}{v}$   $P \propto T$   $V \propto T$

$$V_{fg} = V_g - V_f$$

$$V = V_f + x V_{fg}$$

$$V_{total} = V_{liq} + V_{vap} = m_{liq} V_f + m_{vap} V_g$$

$$x = \frac{m_{vap}}{m}$$

$$V_f \leq V < V_g$$

$\Rightarrow$  Two-phase

Ideal gas law holds

$\Rightarrow$  low press

$\Rightarrow$  high temp

$\Rightarrow$  low density

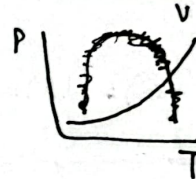
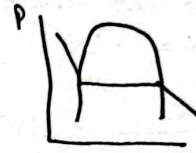
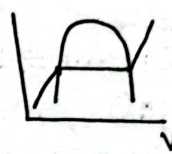
$$Z = \frac{PV}{RT}$$

$\Rightarrow PV = ZRT$   
 $Z = 1$ : ideal gas  
 $Z \neq 1$ : non-ideal gas  
 $Z < 1$ : attractive force  
 $Z > 1$ : repulsive force

$$P_r = \frac{P}{P_c} \quad T_r = \frac{T}{T_c}$$

$T > T_c$  } nearly ideal gas  
 $P < P_c$  }

$P \rightarrow P_c$ : non-ideal gas



Power unit:  $\frac{J}{s}$  (Watt)  $(W)$

For multiple flow streams

For single flow stream



## POST MID-II

$$\eta_{\text{thermal}} = \frac{W}{Q_H} = 1 - \frac{Q_L}{Q_H} \rightarrow \begin{matrix} \text{released} \\ \text{absorbed} \end{matrix}$$

Efficiency of real engine:  $W = Q_H - Q_L$

$$\text{COP: } \beta = \frac{Q_L}{W} = \frac{Q_L}{Q_H - Q_L} \text{ (refrigerator)}$$

$$\text{COP: } \beta' = \frac{Q_H}{W} = \frac{Q_H}{Q_H - Q_L} \text{ (heat pump)}$$

2<sup>nd</sup> Law KP:  $\eta_{\text{thermal}} < 100\%$

2<sup>nd</sup> Law C:  $\beta < \infty$

## Carnot Cycle

① Reversible Isothermal expansion ( $Q \neq W \neq 0$ )

② " Adiabatic expansion ( $Q=0, W \neq 0$ ) ( $Q_H = T_H \Delta S$ )

③ " Isothermal compression ( $W \neq 0$ )

④ " Adiabatic compression ( $Q=0, W \neq 0$ ) ( $Q_L = T_L \Delta S$ )

⑤ Isothermal expansion

$$\eta_{\text{Carnot}} = 1 - \frac{Q_L}{Q_H} = 1 - \frac{T_L}{T_H}$$

Propositions: ①  $\eta_{\text{any}} \leq \eta_{\text{reversible}}$

②  $\eta_{\text{rev1}} = \eta_{\text{rev2}}$

Entropy  $dS = \frac{\delta Q}{T} \Big|_{\text{rev}}$

$$\oint \delta Q = Q_H - Q_L$$

Entropy Change  $S_2 - S_1 = \int_1^2 \frac{\delta Q}{T} \Big|_{\text{rev}}$

Rev. Heat Engine:  $\oint \delta Q \geq 0$  ( $\oint \frac{\delta Q}{T} = 0$ )

Irrev. Heat Engine:  $\oint \delta Q \geq 0$  ( $\oint \frac{\delta Q}{T} < 0$ )

Rev. Refrigerator:  $\oint \delta Q \leq 0$  ( $\oint \frac{\delta Q}{T} = 0$ )

Irrev. Refrigerator:  $\oint \delta Q \leq 0$  ( $\oint \frac{\delta Q}{T} < 0$ )

$$S = (1-x)S_{fg} + xS_g \quad \text{spec entropy } s = \frac{S}{m} \left( \frac{\text{kJ}}{\text{kgK}} \right)$$

$$s = S_f + x S_{fg}$$

Entropy in Rev. process: (Carnot Cycle)

$$\text{① } S_2 - S_1 = \int_1^2 \frac{\delta Q}{T} \Big|_{\text{rev}} = \frac{Q_2}{T_H}$$

$$\text{② } dS = \frac{\delta Q}{T} \Big|_{\text{rev}} = 0 \text{ (isentropic)} \rightarrow \text{const. entropy}$$

$$\text{③ } S_4 - S_3 = \int_3^4 \frac{\delta Q}{T} \Big|_{\text{rev}} = -\frac{Q_4}{T_L}$$

$$\text{④ } dS = \frac{\delta Q}{T} \Big|_{\text{rev}} = 0 \text{ (isentropic)}$$

$$\eta_{\text{Ther}} = \frac{W_{\text{net}}}{Q_H} = \frac{\text{area } 1-2-3-4-1}{\text{area } 1-2-b-a-1}$$

$$S_2 - S_1 = \frac{Q_L}{T} = \frac{h_{fg}}{T}$$

Entropy of Solid/Liquid:  $ds \approx \frac{du}{T} \approx \frac{c}{T} dT \rightarrow S_2 - S_1 \approx C \ln \frac{T_2}{T_1}$

## Rankine Cycle

① (1-2): rev. adiabatic (addition) pumping process in boiler pump  $\left\{ \begin{matrix} \Delta S = 0 \\ Q = 0 \\ S \rightarrow \text{const.} \end{matrix} \right\}$  Isentropic

② (2-3): Const. pressure transfer of heat in boiler  $\left\{ \begin{matrix} P \rightarrow \text{const} \\ \text{Isobaric} \end{matrix} \right\}$   
 $\Rightarrow$  Comp. liq into vapor

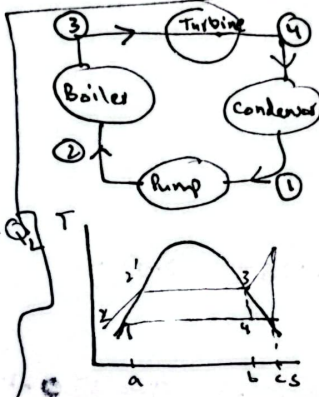
③ (3-4): Rev. adiabatic expansion in turbine  $\left\{ \begin{matrix} \Delta S = 0 \\ Q = 0 \\ S \rightarrow \text{const} \end{matrix} \right\}$  Isentropic  
 $\Rightarrow$  superheated vapor expand isentropically producing work

④ (4-1): Const. pressure transfer of heat in condenser (heat rejection)  $\left\{ \begin{matrix} P \rightarrow \text{const} \\ \text{Isobaric} \end{matrix} \right\}$   
 $\Rightarrow$  back to liquid (static)

$$\eta_{\text{th}} = \frac{W_{\text{net}}}{Q_H} = \frac{\text{area } 1-2-2'-3-4-1}{\text{area } a-2-2'-3-b-a}$$

$$K.E \approx 0, P.B \approx 0 = \frac{Q_H - Q_L}{Q_H}$$

$$\eta_{\text{Rankine}} < \eta_{\text{Carnot}}$$



Efficiency of Rankine Cycle:

- ① Lowering condenser pressure ( $P_4$ )  
 $\Rightarrow$  also increases turbine moisture content
- ② Superheating steam (boiler) ( $T_2$ )
- ③ Increasing boiler pressure ( $P_2$ )