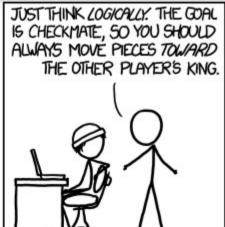
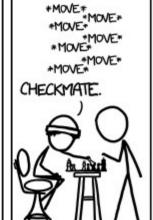
More on games (Ch. 5.4-5.6)















Alpha-beta pruning

Previously on CSci 4511...

We talked about how to modify the minimax algorithm to prune only bad searches (i.e. alpha-beta pruning)

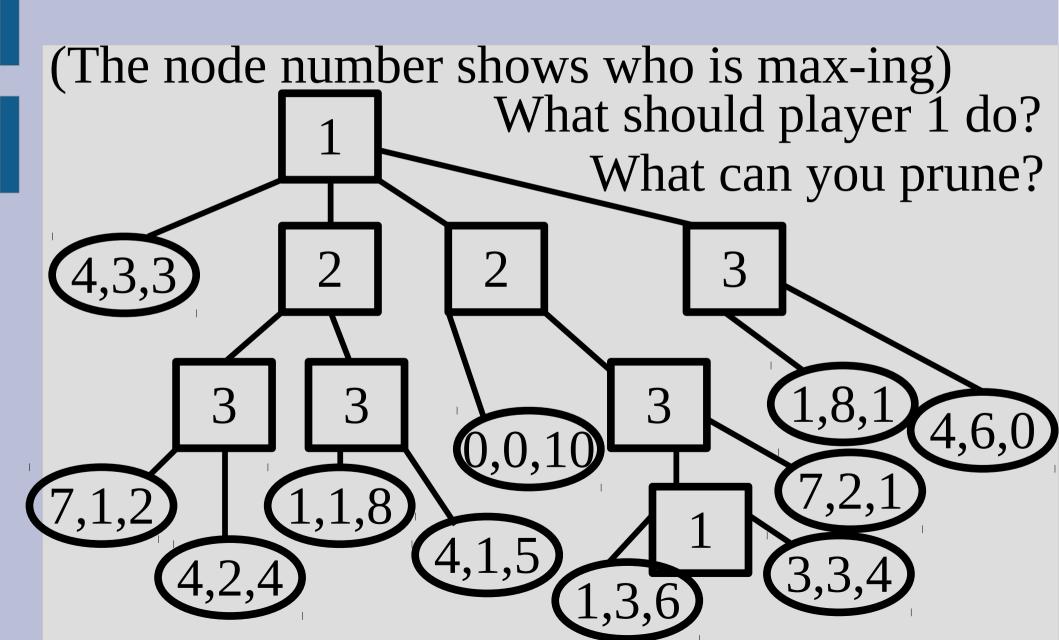
This rule of checking your parent's best/worst with the current value in the child only really works for two player games...

What about 3 player games?

For more than two player games, you need to provide values at every state for all the players

When it is the player's turn, they get to pick the action that maximizes their own value the most

(We will assume each agent is greedy and only wants to increase its own score... more on this next time)



How would you do alpha-beta pruning in a 3-player game?

How would you do alpha-beta pruning in a 3-player game?

TL;DR: Not easily

(also you cannot prune at all if there is no range on the values even in a zero sum game)

This is because one player could take a very low score for the benefit of the other two

So far we assumed that you have to reach a terminal state then propagate backwards (with possibly pruning)

More complex games (Go or Chess) it is hard to reach the terminal states as they are so far down the tree (and large branching factor)

Instead, we will estimate the value minimax would give without going all the way down

By using <u>mid-state evaluations</u> (not terminal) the "best" action can be found quickly

These mid-state evaluations need to be:

- 1. Based on current state only
- 2. Fast (and not just a recursive search)
- 3. Accurate (represents correct win/loss rate)

The quality of your final solution is highly correlated to the quality of your evaluation

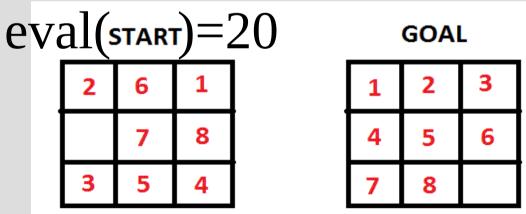
For searches, the heuristic only helps you find the goal faster (but A* will find the best solution as long as the heuristic is admissible)

There is no concept of "admissible" mid-state evaluations... and there is almost no guarantee that you will find the best/optimal solution

For this reason we only apply mid-state evals to problems that we cannot solve optimally

A common mid-state evaluation adds features of the state together

(we did this already for a heuristic...)



We summed the distances to the correct spots for all numbers

We then minimax (and prune) these mid-state evaluations as if they were the correct values

You can also weight features (i.e. getting the top row is more important in 8-puzzle)

A simple method in chess is to assign points for each piece: pawn=1, knight=4, queen=9... then sum over all pieces you have in play

What assumptions do you make if you use a weighted sum?

What assumptions do you make if you use a weighted sum?

A: The factors are independent (non-linear accumulation is common if the relationships have a large effect)

For example, a rook & queen have a synergy bonus for being together is non-linear, so queen=9, rook=5... but queen&rook = 16

There is also an issue with how deep should we look before making an evaluation?

There is also an issue with how deep should we look before making an evaluation?

A fixed depth? Problems if child's evaluation is overestimate and parent underestimate (or visa versa)

Ideally you would want to stop on states where the mid-state evaluation is most accurate

Mid-state evaluations also favor actions that "put off" bad results (i.e. they like stalling)

In go this would make the computer use up ko threats rather than give up a dead group

By evaluating only at a limited depth, you reward the computer for pushing bad news beyond the depth (but does not stop the bad news from eventually happening)

It is not easy to get around these limitations:

- 1. Push off bad news
- 2. How deep to evaluate?

A better mid-state evaluation can help compensate, but they are hard to find

They are normally found by mimicking what expert human players do, and there is no systematic good way to find one

Forward pruning

You can also use mid-state evaluations for alpha-beta type pruning

However as these evaluations are estimates, you might prune the optimal answer if the heuristic is not perfect (which it won't be)

In practice, this prospective pruning is useful as it allows you to prioritize spending more time exploring hopeful parts of the search tree

Forward pruning

You can also save time searching by using "expert knowledge" about the problem

For example, in both Go and Chess the start of the game has been very heavily analyzed over the years

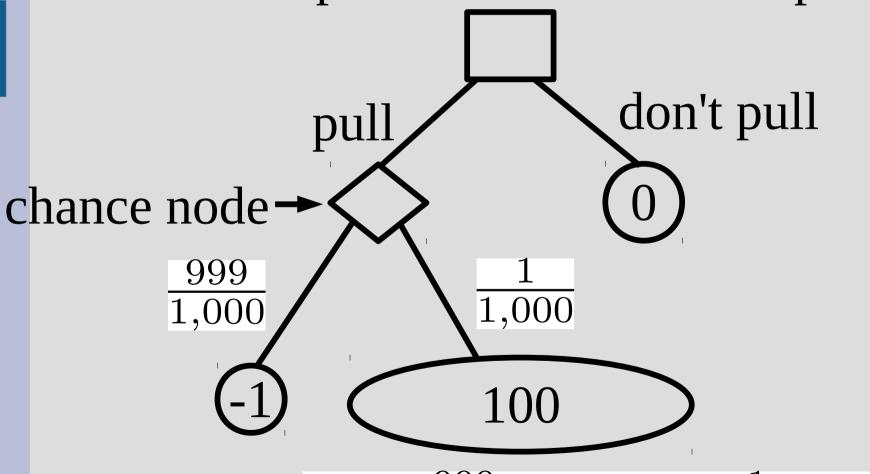
There is no reason to redo this search every time at the start of the game, instead we can just look up the "best" response

If we are playing a "game of chance", we can add chance nodes to the search tree

Instead of either player picking max/min, it takes the expected value of its children

This expected value is then passed up to the parent node which can choose to min/max this chance (or not)

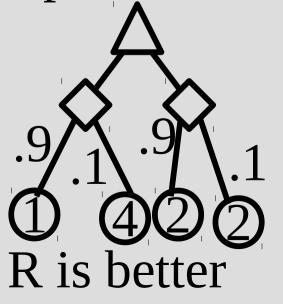
Here is a simple slot machine example:

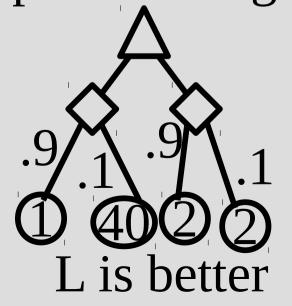


V(chance) =
$$-1 \cdot \frac{999}{1,000} + 100 \cdot \frac{1}{1,000} = -0.899$$

You might need to modify your mid-state evaluation if you add chance nodes

Minimax just cares about the largest/smallest, but expected value is an implicit average:





Some partially observable games (i.e. card games) can be searched with chance nodes

As there is a high degree of chance, often it is better to just assume full observability (i.e. you know the order of cards in the deck)

Then find which actions perform best over all possible chance outcomes (i.e. all possible deck orderings)

For example in blackjack, you can see what cards have been played and a few of the current cards in play

You then compute all possible decks that could lead to the cards in play (and used cards)

Then find the value of all actions (hit or stand) averaged over all decks (assumed equal chance of possible decks happening)

If there are too many possibilities for all the chance outcomes to "average them all", you can <u>sample</u>

This means you can search the chance-tree and just randomly select outcomes (based on probabilities) for each chance node

If you have a large number of samples, this should converge to the average

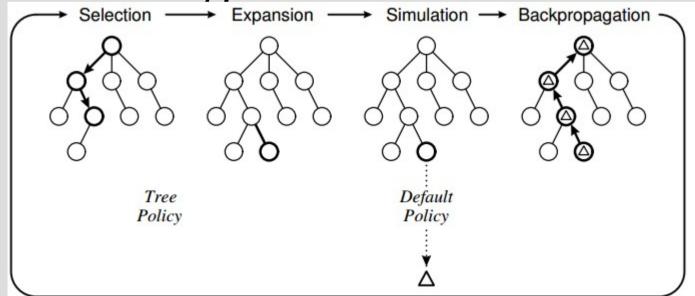
This idea of sampling a limited part of the tree to estimate values is common and powerful

In fact, in <u>monte-carlo tree search</u> there are no mid-state evaluations, just samples of terminal states

This means you do not need to create a good mid-state evaluation function, but instead you assume sampling is effective (might not be so)

MCTS has four steps:

- 1. Find the action which looks best (selection)
- 2. Add this new action sequence to a tree
- 3. Play randomly until over
- 4. Update how good this choice was



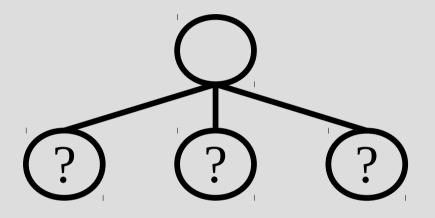
How to find which actions are "good"?

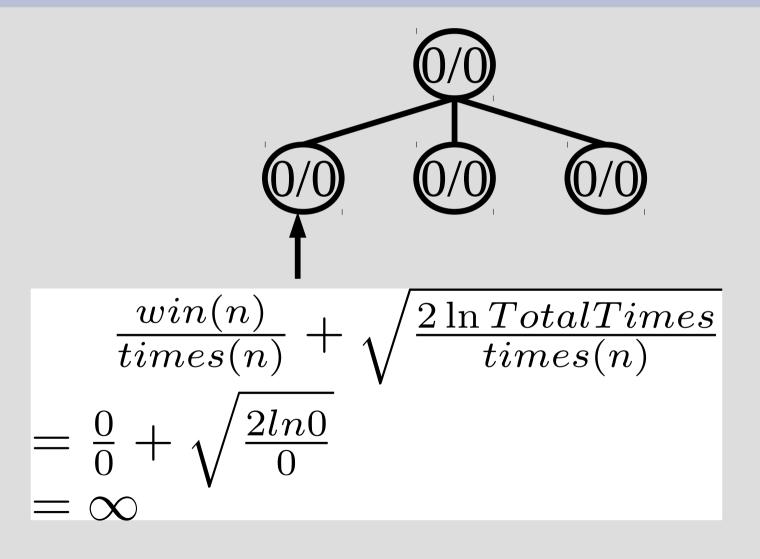
The "Upper Confidence Bound applied to Trees" UCT is commonly used:

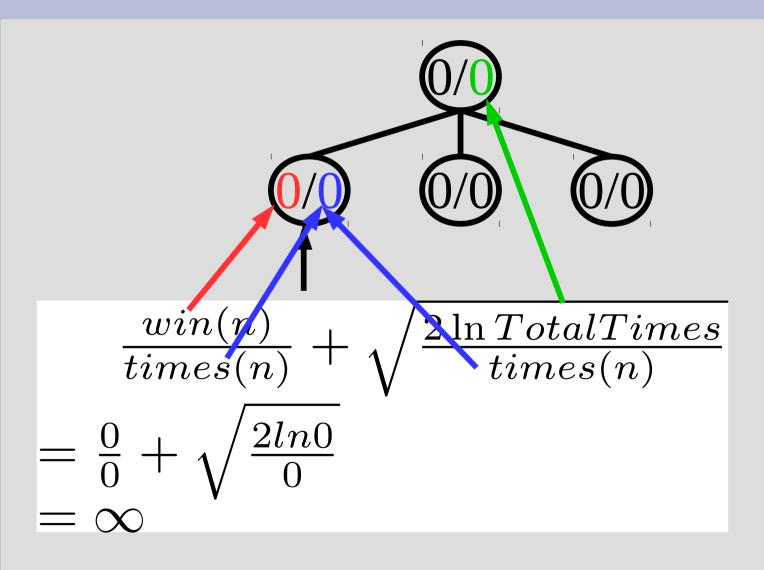
$$\max(\frac{win(n)}{times(n)} + \sqrt{\frac{2\ln TotalTimes}{times(n)}})$$

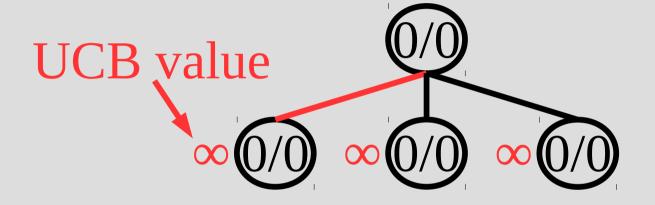
This ensures a trade off between checking branches you haven't explored much and exploring hopeful branches

(https://www.youtube.com/watch?v=Fbs4lnGLS8M)

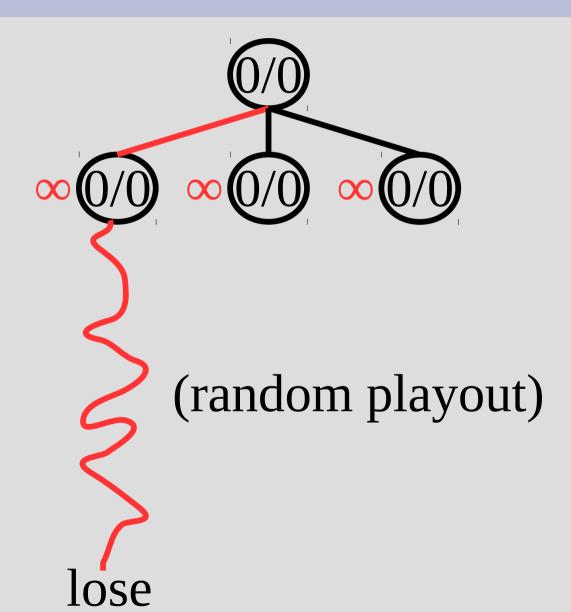


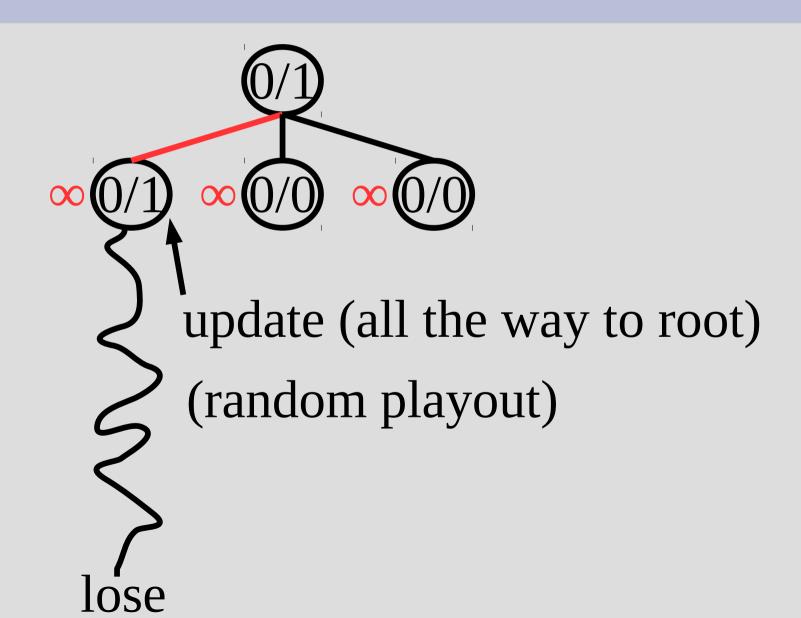


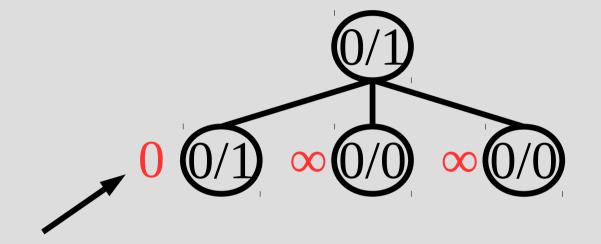




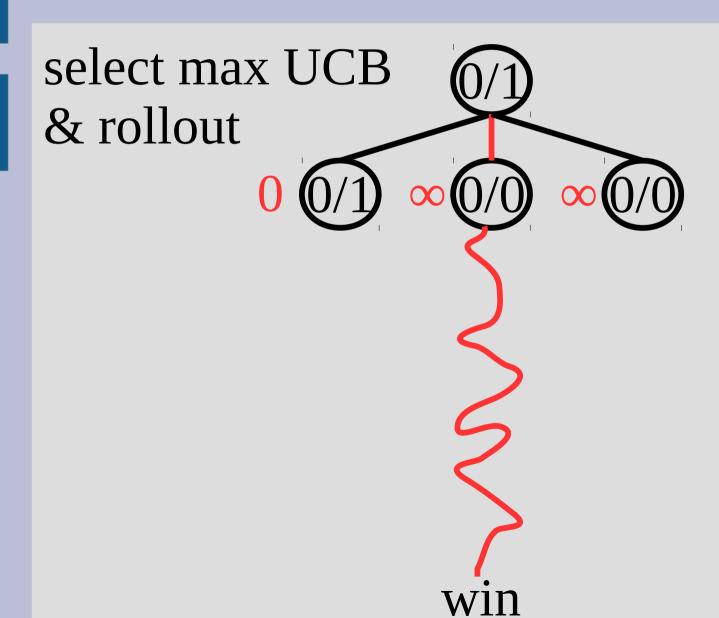
Pick max (I'll pick left-most)

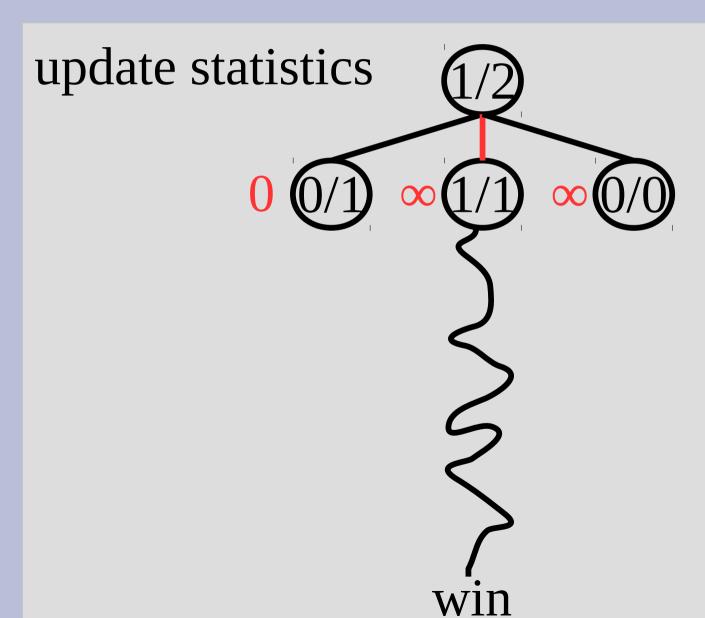


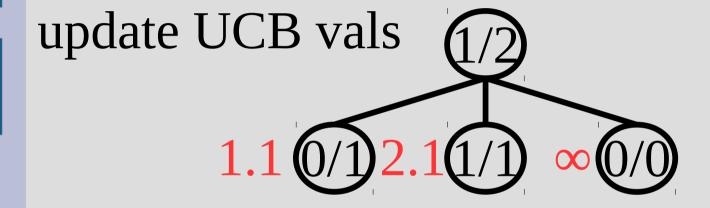


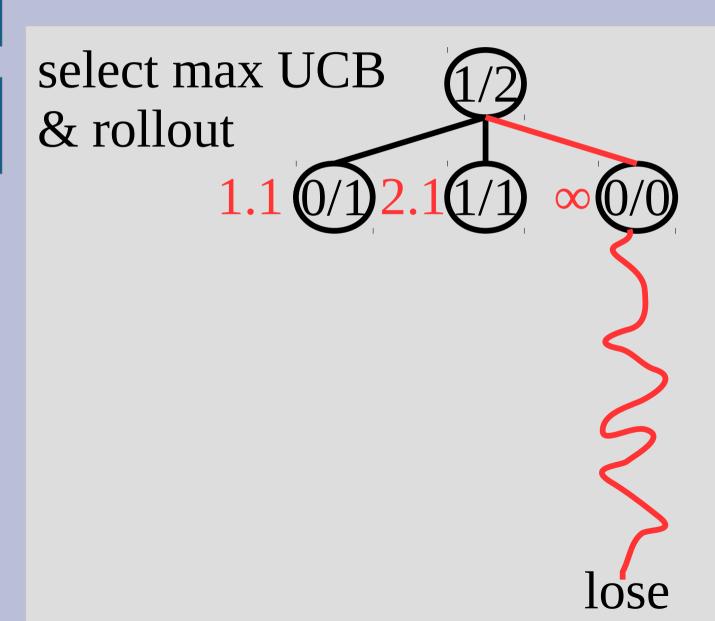


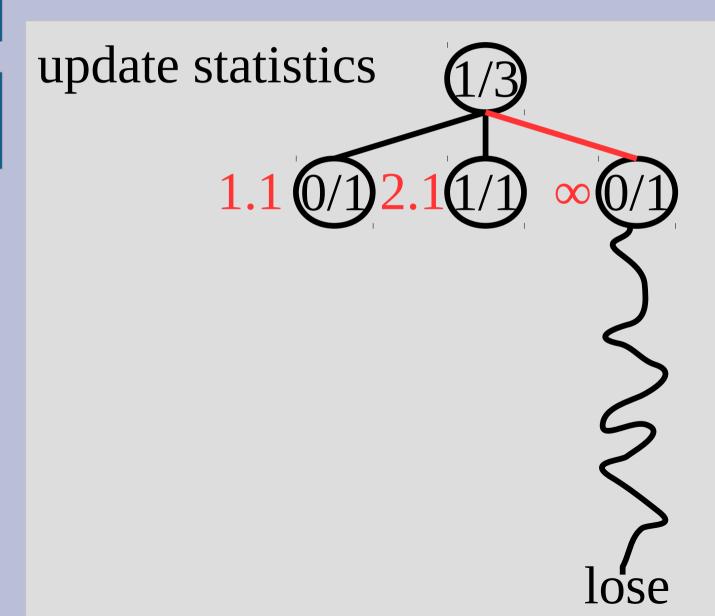
update UCB values (all nodes)

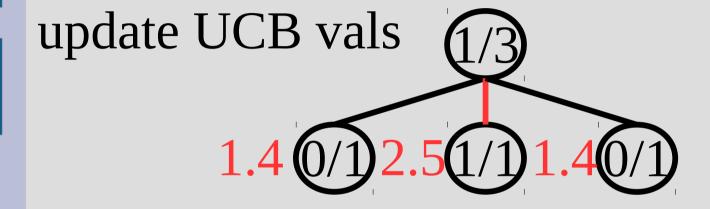


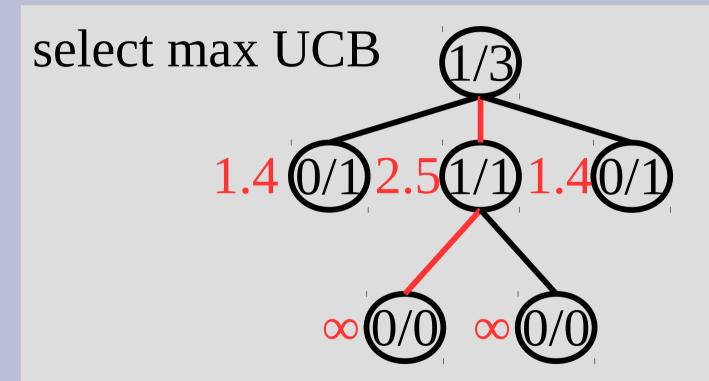




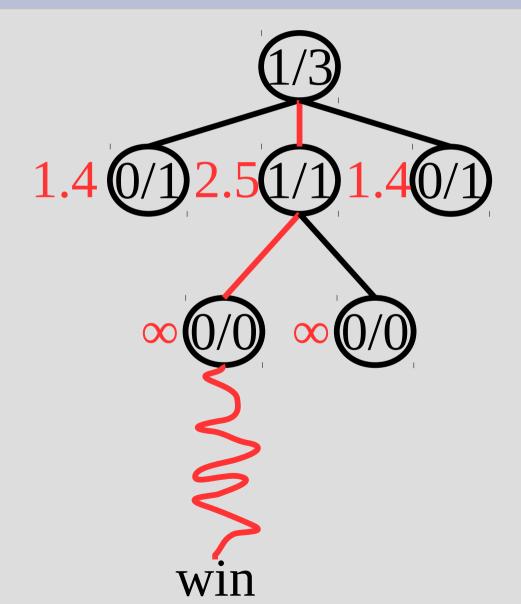


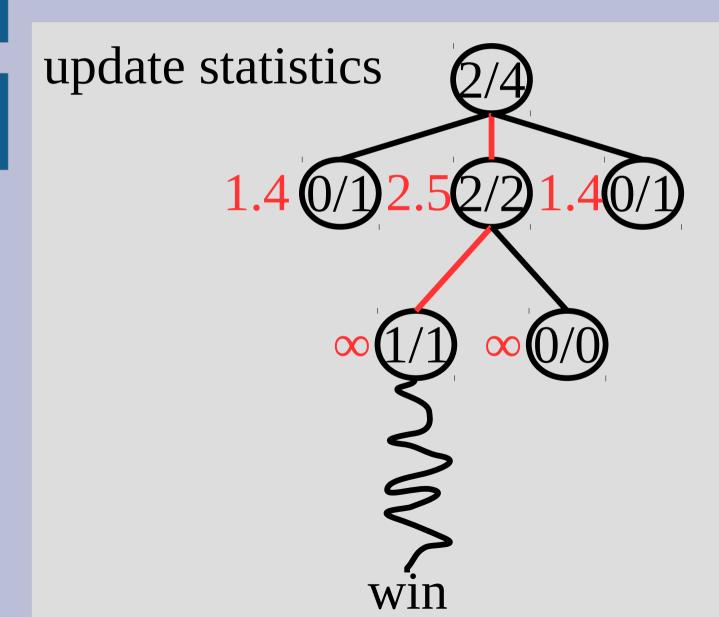


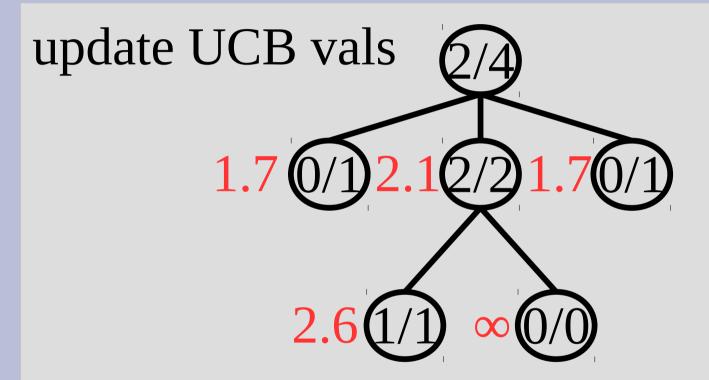




rollout







DIFFICULTY OF VARIOUS GAMES FOR COMPUTERS

HARD

EASY TIC-TAC-TOE < NIM SOLVED FOR ALL POSSIBLE POSITIONS (GHOST (1989) SOLVED CONNECT FOUR (1995) COMPUTERS CAN PLAY PERFECTLY SOLVED FOR (GOMOKU) STARTING POSITIONS (CHECKERS (2007) SCRABBLE COUNTERSTRIKE (UILL REVERSI) (BEER PONG (UILL ROBOT) COMPUTERS CAN FEBRUARY 10, 1996: FIRST WIN BY COMPUTER BEAT TOP HUMANS AGAINST TOP HUMAN CHESS NOVEMBER 21, 2005 LAST WIN BY HUMAN AGAINST TOP COMPUTER JEOPARDY! STARCRAFT POKER COMPUTERS STILL LOSE TO TOP HUMANS ARIMAA (BUT FOCUSED R&D **⟨**G0 COULD CHANGE THIS) SNAKES AND LADDERS <MAO COMPUTERS SEVEN MINUTES MAY NEVER IN HEAVEN OUTPLAY HUMANS CALVINBALL