RS-HDMR-GPR Code Manual

 $Version\ 0.0.1$

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1 Installation Guide

rshdmrgpr package is installed as a Python package. Please install the 64-bit Python version on your Windows machine first. We also recommend the user install anaconda distribution. All examples and work done in this manual is performed on an interactive ipython notebook via Anaconda.

1.1 Windows Installation

On windows command prompt (or Anaconda prompt), create a virtual environment and install the package in a directory of your choosing.

```
C:\Users\new_user>python -m env env_name
C:\Users\new_user>env_name\Scripts\activate.bat
(env_name) C:\Users\new_user>pip install git+https://github.com/owen-ren0003/rshdmrgpr.git
```

After the package is installed, the user should be able to use it in terminal or any Python IDE with the correct environment setup.

```
(env_name) C:\Users\new_user>python
Python 3.7.4 (default, Aug 9 2019, 18:34:13) [MSC v.1915 64 bit (AMD64)]
    :: Anaconda, Inc. on win32
Type "help", "copyright", "credits" or "license" for more information.
>>> from rshdmrgpr import *
```

Users should consult pip and creating virtualenv for more detailed instructions and commands.

1.2 Anaconda Setup

Once Anaconda is installed, create a conda environment:

```
conda create -n env_name python=3.6
```

Activate the environment, which in this case is called 'env_name':

```
conda activate env_name
```

Install the rshdmrgpr package inside the conda environment:

```
pip install git+https://github.com/owen-ren0003/rshdmrgpr.git
```

Install jupyter lab:

```
conda install -c conda-forge jupyterlab
```

Finally, start jupyterlab to starting working interactively in a jupyter notebook:

jupyterlab

2 Python API

2.1 Helper function kernel_matrices

```
rshdmrgpr.kernel_matrices(order, dim, length_scale)
```

This function is used to create the RBF kernels and the matrix input for HDMR.

Parameters

- order: int The order of HDMR to use.
- dim: int The dimension of the feature space.
- length scale: float The length scale to use for the HDMR RBF kernels.

Returns

- list of 2D-numpy Array List of matrices, used to select the features to train the component functions. Has size (dim choose order).
- list of RBF kernels List of RBF kernels to use for training component function. Has size (dim choose order).

2.2 RSHDMRGPR class

```
class rshdmrgpr.RSHDMRGPR(num_models, matrices, kernels)
```

Bases: object

This class initializes the RS-HDMR-GPR model.

Parameters

- num_models: str The number of HDMR component functions to train.
- matrices: list of 2D numpy Array The matrices that define the HDMR component functions. Every matrix must have the same number of rows equaling the dimension of the feature space.
- **kernels:** list of **kernels** The list of sklearn.guassian_process.kernels to use for each HDMR component function.

2.2.1 RSHDMRGPR class methods

```
RSHDMRGPR.train(data, label='out', alphas=1e-7, cycles=50, scale_down=(0.5, 1), report_rmse=False)
```

Trains the component functions for the HDMR model.

Parameters

- data: pandas DataFrame The DataFrame containing both the features columns and label column.
- label: str The name of the label column in data.
- alphas: int or (list of int) The noise level to be set. If int, the noise level is the set to this for all cycles. To set different noise levels for different cycles, a list of int must be specified.
- cycles: int The number of self consistent cycles to use for training.
- **scale_down:** tuple Must be a tuple, say (s, e) of size two. Training predictions for each component function will be multiplied by min $\{s + \frac{(1-s)ec}{T}, 1\}$ on cycle c, where T denotes the total number of cycles.
- report_down: bool If True, returns a DataFrame containing the rmse of training predictions vs actuals for each cycle.

Returns self – The trained instance.

RSHDMRGPR.predict(test_data, return_std=False)

Predicts the results using the trained model parameters.

Parameters

- test_data: pandas DataFrame The DataFrame containing the features of the test set. Should have one less column than the data used for training.
- return_std: bool If True, the sum of all the component functions standard-deviation of the predictive distribution at the query points is returned along with the mean.

Returns

- **y_pred: 1D-numpy Array** Sum of the mean of predictive distribution at query points of all component functions.
- **y_std: 1D-numpy Array** Sum of the standard deviation of predictive distribution at query points of all component functions. Only returned when return_std=True.

RSHDMRGPR.get_models()

Returns the trained HDMR component functions.

Parameters

Returns list of GaussianProcessRegressor — List of GaussianProcessRegressor from the sklearn.gaussian_process library, their trained instances.

2.3 FirstOrderHDMRImpute class

class rshdmrgpr.FirstOrderHDMRImpute(models, division=1000)

Bases: object

This class is initialized by vectorizing the 1D HDMR component functions and creating a dictionary of output values with division subdivisions.

Parameters

- models: list of GaussianProcessRegressor list of trained GaussianProcessRegressor models which represents the hdmr component functions of first order. Must be of first order (each has 1 input and 1 output).
- division: int The number of divisions in the lookup table

2.3.1 FirstOrderHDMRImpute class methods

FirstOrderHDMRImpute.get_table()

Returns the lookup table for the component functions.

Parameters

Returns panda DataFrame - The lookup table for the HDMR component functions.

 $\verb|FirstOrderHDMRImpute.get_yi| (df_na)$

Modifies the DataFrame to contain the outputs of the first-order hdmr component functions. The output columns are concatenated past the last column of df_na.

Parameters

• **df_na:** pandas DataFrame - The DataFrame to impute. Must contain the output column and that column must be the last column.

Returns list - list of column indices for each row with missing df_na each corresponding to missing value column.

FirstOrderHDMRImpute.impute(df_na, get_candidates=False, threshold=0.001)

This function imputes the missing values given the input. Every single input row is expected to have at most one missing value.

Parameters

- **df_na:** pandas DataFrame The DataFrame to impute. It is expected to contain the columns corresponding to 1D hdmr outputs (i.e. as an output of the get_yi function).
- get_candidates: bool If True, returns all the candidates for imputation.
- threshold: float The threshold distance to set for selecting candidates from look-up table. Correspond to δ in the paper (Section 2.2).

Returns

- 1) pandas DataFrame The imputed DataFrame df_na if get_candidates=False.
- 2) pandas DataFrame, pandas Index, pandas Series, list of float The imputed DataFrame df_na, the index of rows with null entries, the column names (indexed by the index of null entries) containing the null entry, and a list of candidates for imputing that missing value if get_candidates=True.

3 rshdmrgpr Examples

This manual comes with a supplementary IPython notebook. Please see examples.ipynb in the package directory for complete worked out examples.