

# Potential Energy Prediction with Persistence Images

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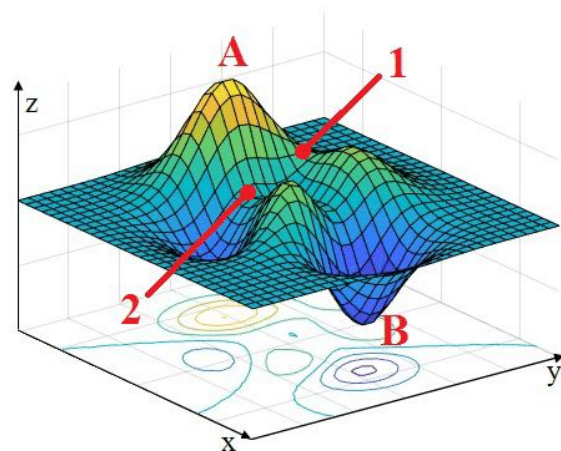
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# Problem Statement

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- Predict potential energy surface of a molecule
  - Ultimately, find lowest energy conformer of the molecule

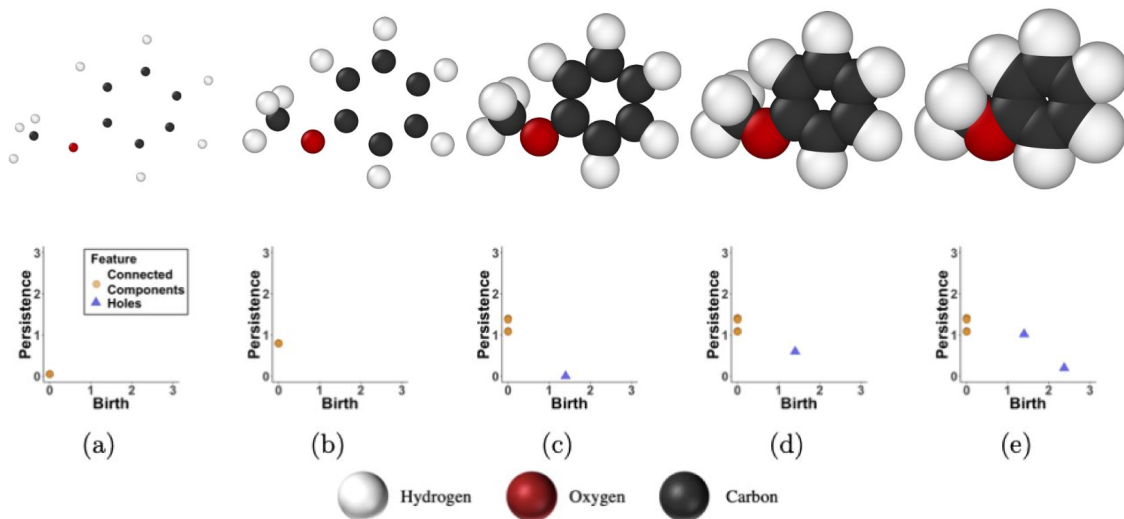


# Framing the Problem with ML

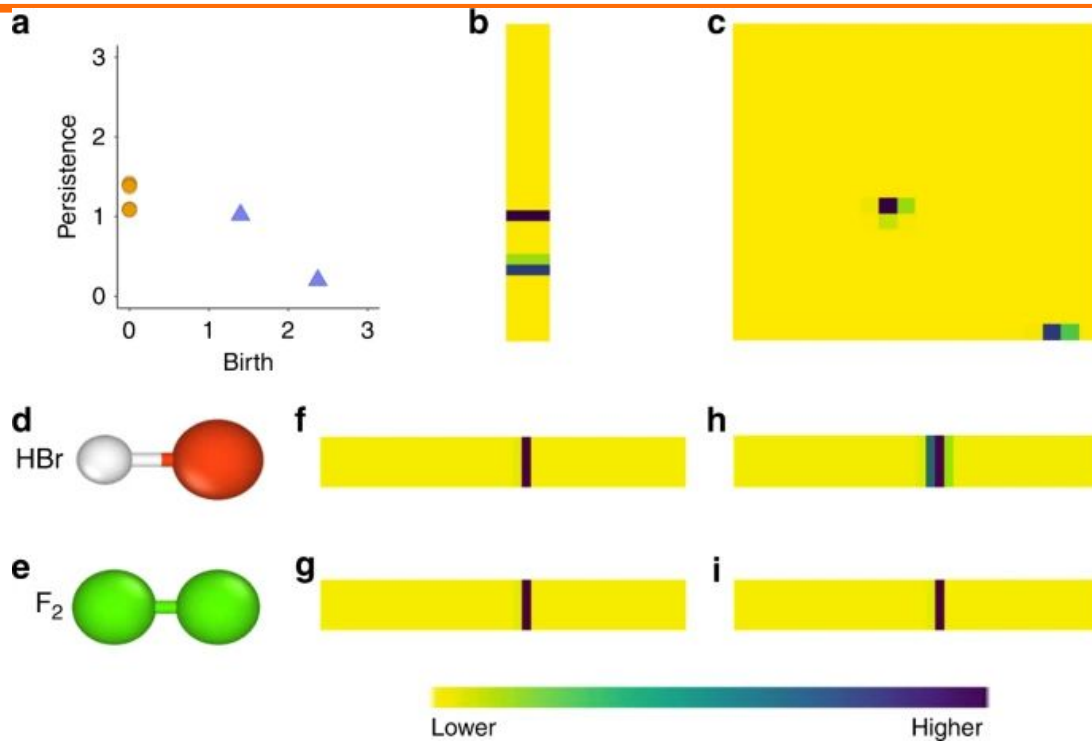
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- $\Delta$  geometry  $\rightarrow$   $\Delta$  energy
  - How to capture geometric perturbations?
- Need to solve...
  - Regression problem
  - Optimization problem

# Persistence Diagrams

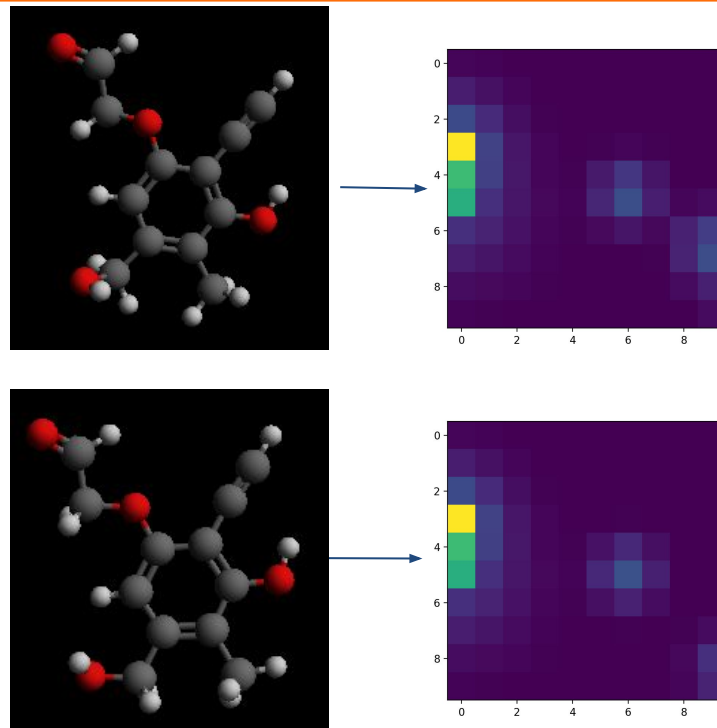


# Persistence Images



# Generating Conformations

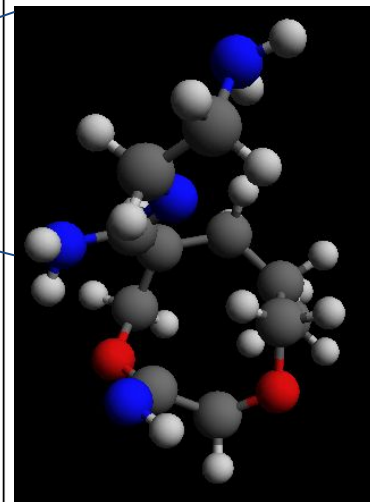
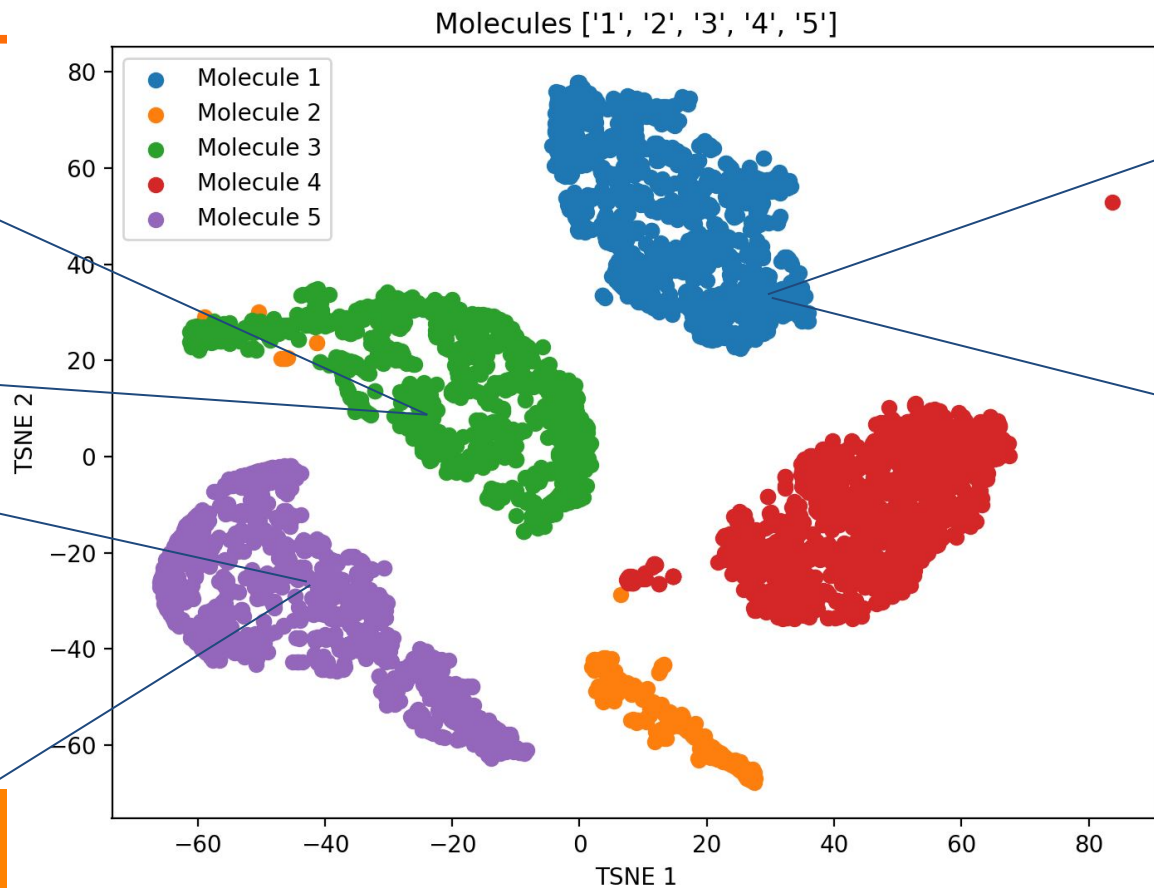
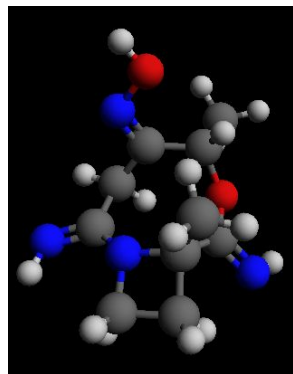
- Base structures from GDB-17 database<sup>1</sup>
- Conformations generated with XTB<sup>2</sup>
  - Uses molecular dynamics



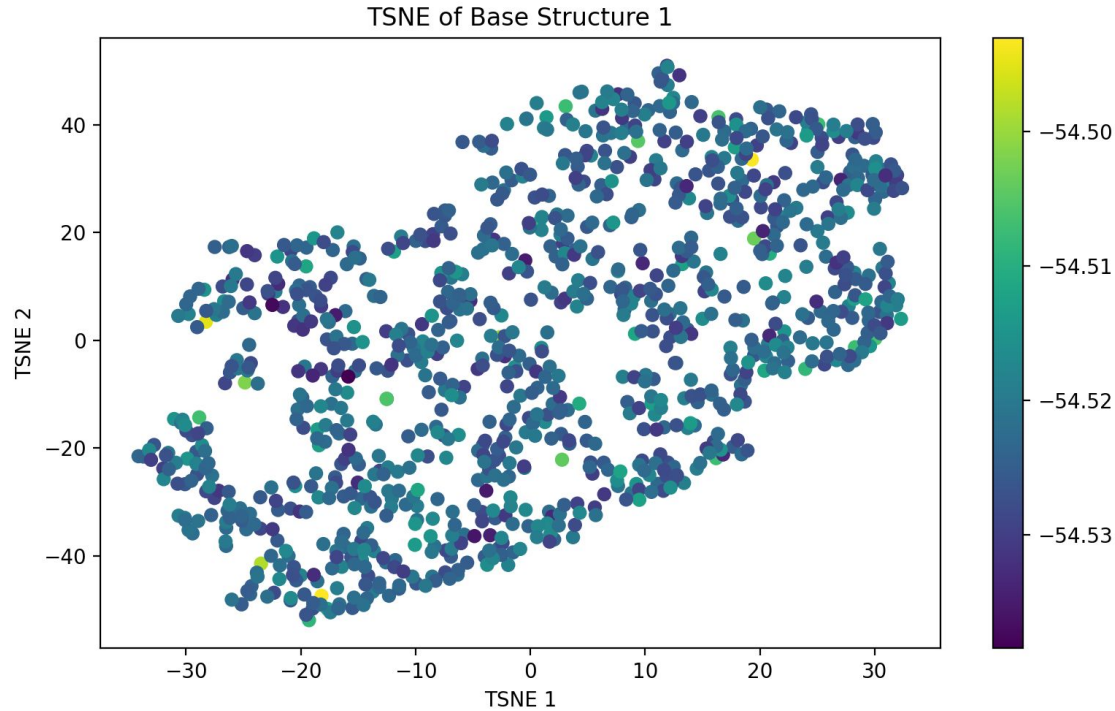
<sup>1</sup>L. Ruddigkeit, R. van Deursen, L. C. Blum, J. L. Reymond, *J. Chem. Inf. Model*, **2012**.

<sup>2</sup>C. Bannwarth et al., *WIREs Comp. Mol. Sci.*, **2020**.

# Distribution of PI's



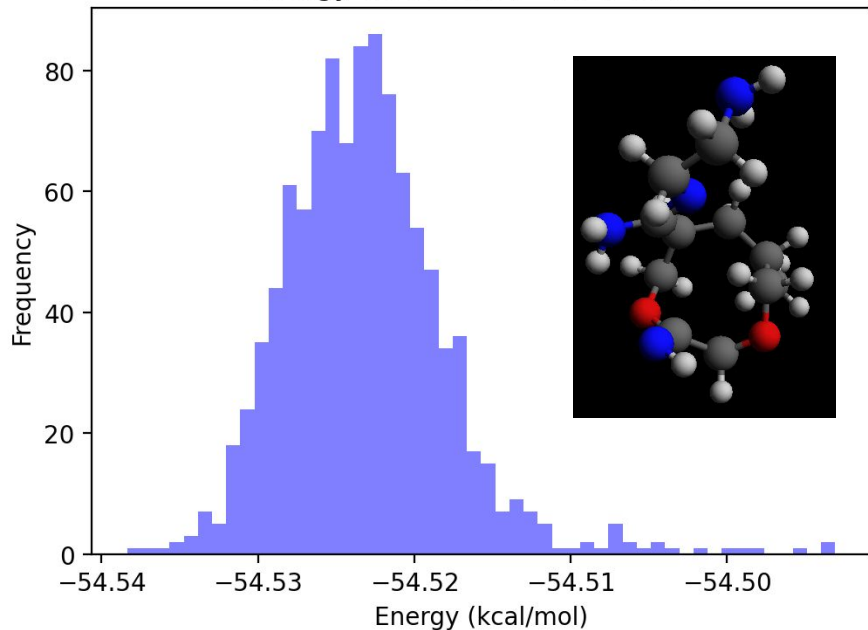
# Distribution of Energy per PI



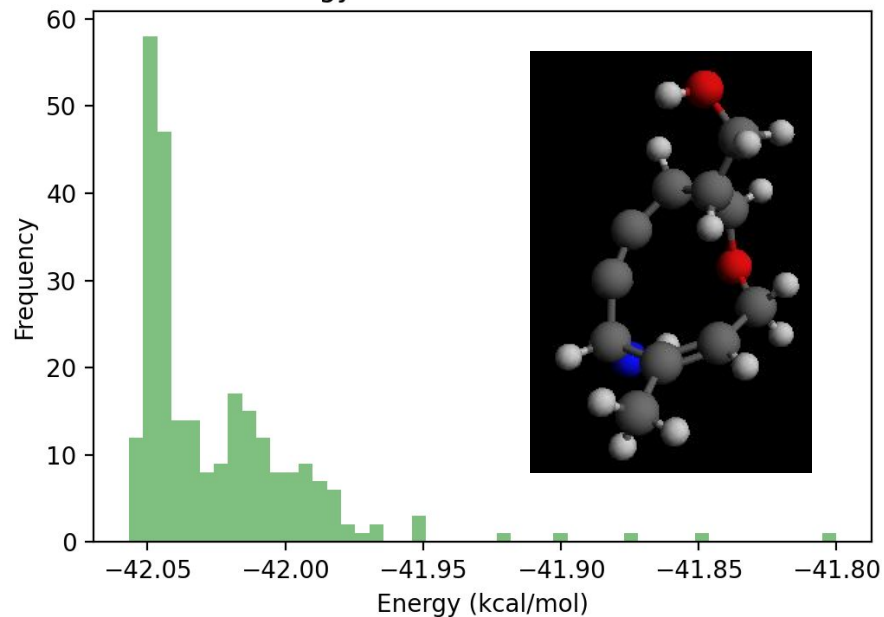


# Energy Distributions

Energy distribution - Molecule 1



Energy distribution - Molecule 2

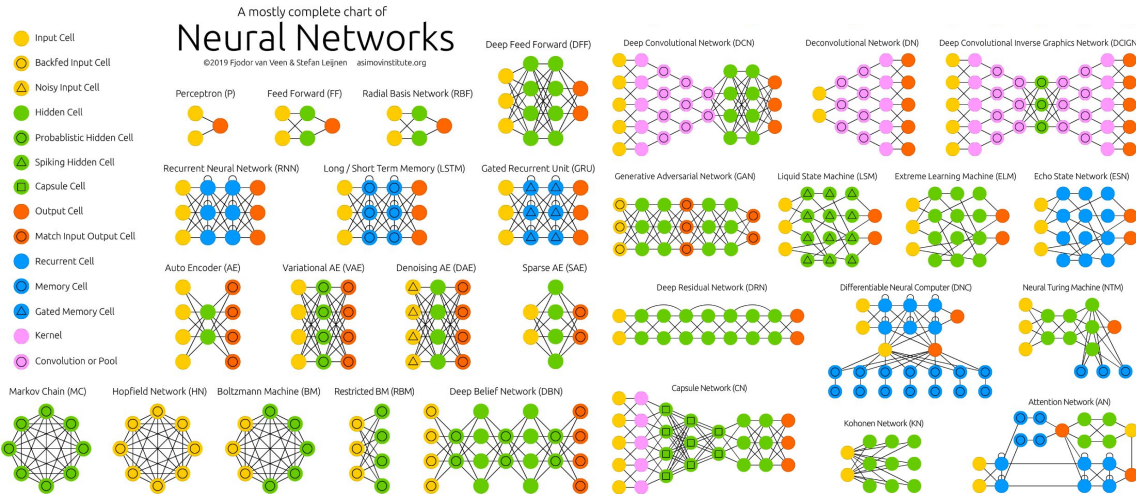


# ML Models

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- Non-deep learning
  - XGBoost, Kernel Ridge Regression, Support Vector Machine
- Deep learning
  - Convolutional neural network (CNN)
  - Recurrent Neural Network (RNN)

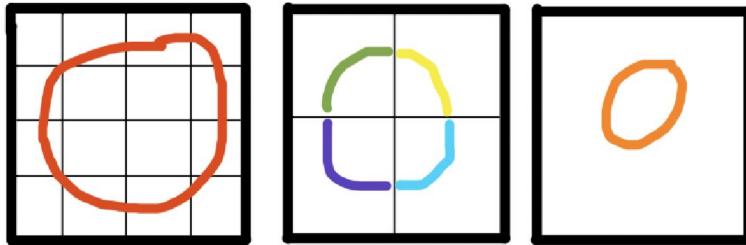
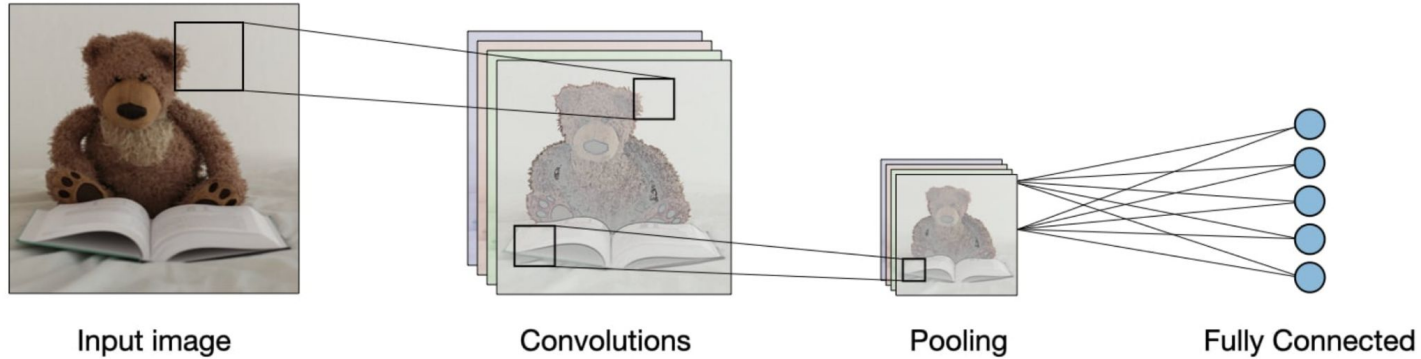
# Deep Learning Architectures



- Any architecture can learn anything (sorta)
- Goal is to find architecture that learns efficiently for given data
  - Image vs. Text
  - Sparse vs. Dense
  - Dynamic vs. Static
  - etc.

\*Image from Asimov Institute

# Convolutional Neural Networks

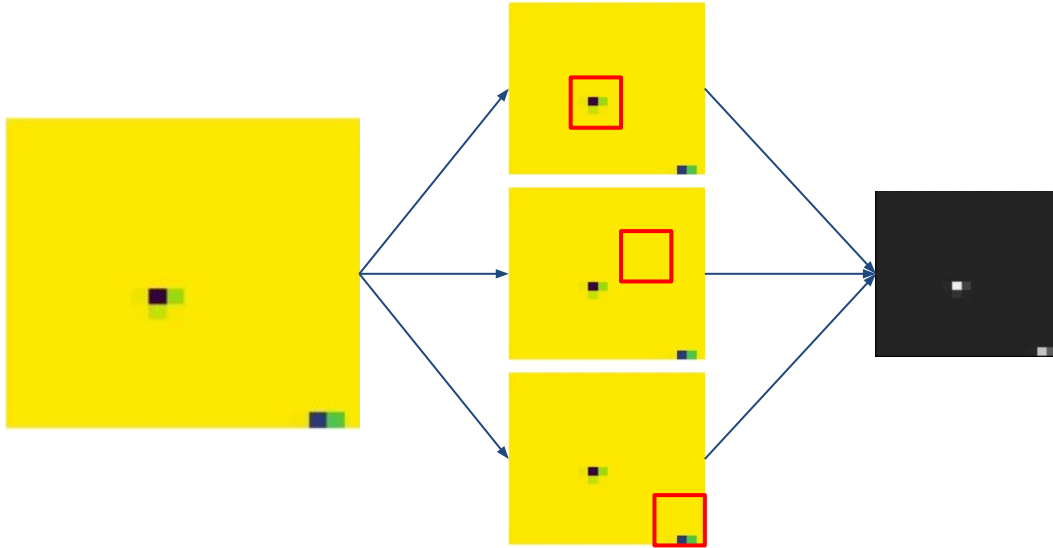


- Local Spatial Information, not global
- Combines features and downscales
- Good for learning hierarchical feature representations

\*Image from Shervine CS230 @ Stanford

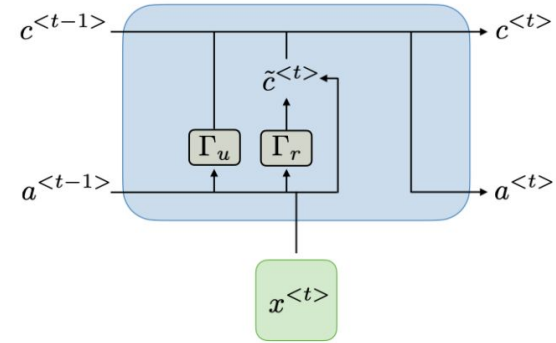
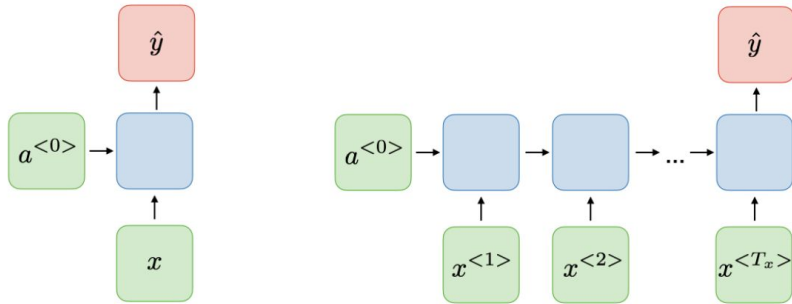
## Convolutional Neural Networks Cont.

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- Sparse data
- Global spatial information more important than feature shape

# Recurrent Neural Networks



- How does stored information affect interpretation of new observation
- How much of past stored information should be replaced with information from new observation

\*Images from Shervine CS230 @ Stanford

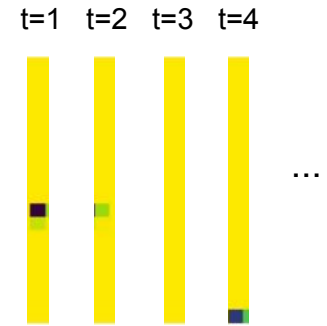
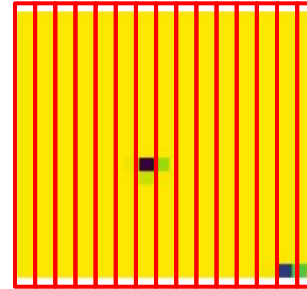
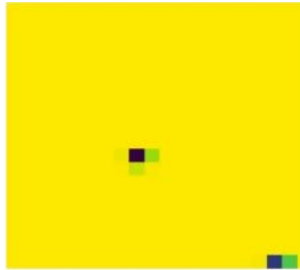
# Recurrent Neural Networks Cont.

## One Hot Encoding

Rome = [1, 0, 0, 0, 0, 0, ..., 0]  
Paris = [0, 1, 0, 0, 0, 0, ..., 0]  
Italy = [0, 0, 1, 0, 0, 0, ..., 0]  
France = [0, 0, 0, 1, 0, 0, ..., 0]

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## PI as Time Series Data



# Training Details

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- Split: 70% training, 30% testing
- Results reported in Mean Absolute Error (MAE)
- Regular ML: Sci-kit Learn
- CNN: PyTorch
  - Accuracy reported on lowest test loss observed during training
  - Trained on MAE as loss function
- Only trained/tested on conformers of Base Structure 1



# Results - One Structure

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Non-deep learning models (Mean Absolute Error kcal/mol)

- XGBoost: 0.0033107
- Kernel Ridge Regression: 0.0069986
- Support Vector Machine: 0.0076822

Deep Learning:

- CNN: ~0.004
- RNN: still in development

# Open Questions

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- How well do PIs work for this problem?
  - Can they capture subtleties in geometries?
- Which ML algorithms optimally capture information in PIs?
- How to optimize for lowest-energy conformation?

# Future Work

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- Graph neural networks (GNNs)
- Implement recurrent neural networks (RNNs)
- Autoencoders
- Transfer learning across molecules
- Using PIs as augmentation tool