

# libsvm code

## SMO 中变量 $\alpha$ 的选择

```
int Solver::select_working_set(int &out_i, int &out_j)
{
    double Gmax = -INF; // m(alpha) = max i in I_up -y_i delta f(alpha)
    double Gmax2 = -INF; // M(alpha) = min i in I_low -y_j delta f(alpha)
    int Gmax_idx = -1;
    int Gmin_idx = -1;
    double obj_diff_min = INF;

    for(int t=0; t<active_size; t++) // 更新 GMAX, m(alpha)
        if(y[t]==+1)
        {
            if(!is_upper_bound(t)) // y_t=1 and a_t<C
                if(-G[t] >= Gmax)
                {
                    Gmax = -G[t];
                    Gmax_idx = t;
                }
        }
        else
        {
            if(!is_lower_bound(t)) // y_t=-1 and a_t>0
                if(G[t] >= Gmax)
                {
                    Gmax = G[t];
                    Gmax_idx = t;
                }
        }
    int i = Gmax_idx;
    const Qfloat *Q_i = NULL;
    if(i != -1)
        Q_i = Q->get_Q(i, active_size);

    for(int j=0; j<active_size; j++) // 更新 GMAX2 M(alpha)
    {
        if(y[j]==+1)
        {
            if (!is_lower_bound(j))
            { // y_j=1 and a_j>0
                double grad_diff=Gmax+G[j];
```

```

        if (G[j] >= Gmax2) //求 max -M (alpha)
            Gmax2 = G[j];
        if (grad_diff > 0) //-y_j delta f(alpha) < -y_i delta f(alpha)
        {
            double obj_diff;
            double quad_coef = QD[i]+QD[j]-2.0*y[i]*Q_i[j];
            if (quad_coef > 0) //kii+kjj-2kij>0
                obj_diff = -(grad_diff*grad_diff)/quad_coef;
            else
                obj_diff = -(grad_diff*grad_diff)/TAU;

            if (obj_diff <= obj_diff_min) //取可以取到最小值的j
            {
                Gmin_idx=j;
                obj_diff_min = obj_diff;
            }
        }
    }
    else
    {
        if (!is_upper_bound(j))
        { //y_j=-1 and a_j>0
            double grad_diff= Gmax-G[j];
            if (-G[j] >= Gmax2)
                Gmax2 = -G[j];
            if (grad_diff > 0)
            {
                double obj_diff;
                double quad_coef = QD[i]+QD[j]+2.0*y[i]*Q_i[j];
                if (quad_coef > 0)
                    obj_diff = -(grad_diff*grad_diff)/quad_coef;
                else
                    obj_diff = -(grad_diff*grad_diff)/TAU;

                if (obj_diff <= obj_diff_min)
                {
                    Gmin_idx=j;
                    obj_diff_min = obj_diff;
                }
            }
        }
    }
}

if(Gmax+Gmax2 < eps || Gmin_idx == -1) // 停止条件
    return 1;

out_i = Gmax_idx; //寻找到的 SMO 的更新的「i, j」
out_j = Gmin_idx;
return 0;

```

```
}
```

## 变量 $\alpha$ 的更新

```
// 更新 alpha[i] and alpha[j]

const Qfloat *Q_i = Q.get_Q(i,active_size);
const Qfloat *Q_j = Q.get_Q(j,active_size);

double C_i = get_C(i);
double C_j = get_C(j);

double old_alpha_i = alpha[i];
double old_alpha_j = alpha[j];

if(y[i]!=y[j])//y_i!=y_j
{
    double quad_coef = QD[i]+QD[j]+2*Q_i[j];
    if (quad_coef <= 0)
        quad_coef = TAU;
    double delta = (-G[i]-G[j])/quad_coef;
    double diff = alpha[i] - alpha[j];

//更新
    alpha[i] += delta;
    alpha[j] += delta;

//修正 4种需要修正的情况
    if(diff > 0)
    {
        if(alpha[j] < 0)//region 3
        {
            alpha[j] = 0;
            alpha[i] = diff;
        }
    }
    else
    {
        if(alpha[i] < 0)//region 4
        {
            alpha[i] = 0;
            alpha[j] = -diff;
        }
    }
}
```

```

    if(diff > C_i - C_j)//region 1
    {
        if(alpha[i] > C_i)
        {
            alpha[i] = C_i;
            alpha[j] = C_i - diff;
        }
    }
    else
    {
        if(alpha[j] > C_j)////region 2
        {
            alpha[j] = C_j;
            alpha[i] = C_j + diff;
        }
    }
}

else//同理y_i==y_j 的情况
{
    double quad_coef = QD[i]+QD[j]-2*Q_i[j];
    if (quad_coef <= 0)
        quad_coef = TAU;
    double delta = (G[i]-G[j])/quad_coef;
    double sum = alpha[i] + alpha[j];
    alpha[i] -= delta;
    alpha[j] += delta;

    if(sum > C_i)
    {
        if(alpha[i] > C_i)
        {
            alpha[i] = C_i;
            alpha[j] = sum - C_i;
        }
    }
    else
    {
        if(alpha[j] < 0)
        {
            alpha[j] = 0;
            alpha[i] = sum;
        }
    }
    if(sum > C_j)
    {
        if(alpha[j] > C_j)
        {
            alpha[j] = C_j;
            alpha[i] = sum - C_j;
        }
    }
}

```

```

    }
    else
    {
        if(alpha[i] < 0)
        {
            alpha[i] = 0;
            alpha[j] = sum;
        }
    }
}

```

## 变量 $G$ 的更新

// update G

```

double delta_alpha_i = alpha[i] - old_alpha_i;
double delta_alpha_j = alpha[j] - old_alpha_j;

for(int k=0;k<active_size;k++)//只需要更新alpha_i 和alpha_j (其他的都没有改变)
{
    G[k] += Q_i[k]*delta_alpha_i + Q_j[k]*delta_alpha_j;
}

```