

## Clarence Lewis Protin

Of Belgian nationality, I was born in Madrid on the 12th of August of 1977 of a Belgian father and a mother from Pennsylvania in the United States.

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## Education

- PhD in Mathematics from the IST (2008) under the supervision of Pedro Resende with a thesis entitled Quantales of Open Groupoids (approved unanimously). The area of my thesis consisted in the application of a categorical treatment of quantales and locales to the Noncommutative Geometry of Alain Connes.
- Passed PhD qualifying exams in Geometry and Topology and Mathematical Analysis at the IST (2005).
- I completed graduate level courses at the Instituto Superior Técnico (IST) in category theory, modal logic, non-conventional computation and Feynman integrals (2004-2005).
- Four-year PhD Scholarship from the Science and Technological Foundation (FCT) 2004-2008 (SFRH/BD/17823/2004)
- Four-year degree in Mathematics, concluded at the University of Lisbon in 2003 with an average of 18/20 on the final year. I took courses in mathematical logic, algebraic topology, algebraic geometry and universal algebra and lattice theory.

## Peer-Reviewed Publications

1. Quantales of Open Groupoids. J. Noncommut. Geom. 6 (2012), 199-247.  
doi: 10.4171/JNCG/90 <http://arxiv.org/abs/0811.4539> (with Pedro Resende).
2. Type-inhabitation of Atomic Polymorphism is Undecidable, Oxford Journal of Logic and Computation, Volume 31, Issue 2, March 2021.  
<https://academic.oup.com/logcom/advance-article-abstract/doi/10.1093/logcom/exaa090/6082839>
3. Typability and Type Inference in Atomic Polymorphism (with G. Ferreira), Logical Methods in Computer Science, Vol 18, Issue 3, 2022.  
<https://lmcs.episciences.org/9915>.
4. A Logic for Aristotle's Modal Syllogistic, History and Philosophy of Logic, 2022.  
<https://www.tandfonline.com/doi/full/10.1080/01445340.2022.2107382>  
<https://doi.org/10.1080/01445340.2022.2107382>

5. Continuity, Topos and Infinitesimals, La Part de l'Oeil, 2023 (to appear).

<https://arxiv.org/abs/2105.05889>

Paper 1 (with 23 citations according to Google Scholar) is an important contribution to the area of Alain Connes' Noncommutative Geometry and can be seen as furnishing the basis for a "noncommutative algebraic geometry" based on localic groupoids and a topos of modules over a quantale. Paper 2 solved a difficult problem in atomic polymorphism, a system of lambda calculus with important applications to the proof theory of intuitionistic propositional calculus. It is a result which has consequences for the theory of functional programming languages and for the study of fragments of second-order propositional logic. Paper 3 continues this line of research and studies the type theory of atomic polymorphism. Paper 4 deals with a novel algebraic logic style formalisation of Aristotle's theory of the modal syllogism.

Paper 5 is an exploration of the historical and philosophical origins of key concepts of modern topology and sheaf theory, in particular with reference to the work of Lawvere and Grothendieck.

## Communications

- A Constructive Proof of the Univalence Axiom, Mathematical Logic Webinar, 18th and 25th of May of 2022. [a-constructive-proof-of-the-univalence-axiom](#)
- Bealer's Intensional Logic, ALOPHIS seminar, 18th of May 2021. <https://people.unica.it/alophis/alophis-weekly-seminars/>
- Bealer's Intensional Logic, Logic Seminar of the University of Lisbon (2020) (2 talks)  
<https://ciencias.ulisboa.pt/pt/evento/12-10-2020/bealers-intensional-logic-part-i>
- On the undecidability of type inhabitation for atomic polymorphism, Logic Seminar of the University of Lisbon (2018)  
<https://ciencias.ulisboa.pt/sites/default/files/cmaficio-08out18.pdf>
- A Topos Theoretic Model for Intuitionistic Analysis, Grupo de Trabalho em Questões Lógicas of the Universidade de Lisboa (2010), Series of 5 lectures.  
[http://cmf.fc.ul.pt/arquivo/docs/seminarios/gtql/2010/2010\\_Maio\\_20.pdf](http://cmf.fc.ul.pt/arquivo/docs/seminarios/gtql/2010/2010_Maio_20.pdf)
- Quantales beyond étale groupoids, Category Theory Conference 2007, Carvoeiro, Portugal.  
<http://www.mat.uc.pt/~categ/ct2007/abstracts/Protin.pdf>
- Minimal realization for quantum automata, Quantum Computation and Information Seminar at the Instituto Superior Técnico (2004).  
<https://math.tecnico.ulisboa.pt/seminars/qci/index?action=show&id=943?action=show&id=943&lang=en>
- From a probabilistic SC institution to parainstitutions, Logic and Computation Seminar at the Instituto Superior Técnico (2004).  
<https://math.tecnico.ulisboa.pt/seminars/clc/index?action=show&id=989>

## Research centers and projects

- FCT project QUANTLOG (for 2004)
- PhD Student Member of the Centro de Lógica e Computação at the Instituto Superior Técnico (2004).
- External collaborator (2010 - ) of the Grupo de Lógica Matemática of the CMAF of the University of Lisbon.
- Collaborator of the Center for the Philosophy of Science of the University of Lisbon (CFCUL) (2020 - ) <https://cfcul.ciencias.ulisboa.pt/equipa/clarence-protin/>

## Survey articles

Notes for my talks on Bealer's intensional logic <https://arxiv.org/abs/2012.09846>.

## Work in preparation

- The PyLog Proof Assistant and Proof Checker. Written in Python, this is a proof checker and proof assistant which is based on natural deduction for the first-order predicate calculus expanded with an extension-forming operator  $\{x : A(x)\}$ . I have formalised and checked over ten thousand lines of proof related to the Kelley-Morse system of set theory. <https://owl77.github.io>. The main goal of PyLog is to formalise S. Simpson's book Subsystems of Second-Order Arithmetic.
- PyHott. This is a program similar to PyLog but for homotopy type theory.
- Ancient Natural Deduction (an essay on the relationship between ancient and modern logic) <https://arxiv.org/abs/2209.03388>
- A Topos for the Bounded Functional Interpretation.
- Towards a Formalisation of Aristotle's Topics.

## Interests

Philosophical logic, proof theory, type theory and category theory.

## Work as Editor

Subreviewer for an article that appeared in RAMICS 2020 <http://ramics18.gforge.inria.fr>

## Some Conferences attended

Days in Logic 2022

<https://daysinlogic2022.ualg.pt>

LanCog Workshop on Substructural Logics, September 26-27, 2019

<https://cful.letras.ulisboa.pt/events/workshop-on-substructural-logics/>

International Category Theory Conference 2007

<http://www.mat.uc.pt/~categ/ct2007/>

CombLog '04

<http://www.cs.math.ist.utl.pt/comblog04/>

## Employment and Experience

Present: (September 2022-): Tutor at the Universidade Aberta.

Past:

- Assistant Professor of Mathematics at the Universidade Lusófona de Humanidades e Tecnologias from 2009 to 2011.
- During the first semester I taught an average of 10 hours weekly and during the third semester I taught 13 hours weekly. During these two years I taught Linear Algebra, Mathematical Analysis I, Mathematical Analysis II and Mathematical Analysis III to students of various engineering degrees.
- Private Tutor (University and advanced high-school level) 2012 - 2022. I taught Linear Algebra, Calculus in one and several variables, Numerical Analysis, Probability and Statistics and Econometrics.
- German, Portuguese and English Translator

## IT Skills

Machine code and x86 assembly, the Linux command line, C, OCaml, Python, Java and Web programming languages (HTML/CSS/PHP/Javascript). Learning Agda.

## Languages

- My native tongue is English.
- I can read and understand French, German and Spanish.
- I am studying Dutch and Flemish.

- I can understand, speak and write Portuguese.
- I took a one semester of Mandarin at the Centro Cultural e Científico de Macau (2009).
- I have knowledge of classical Latin, ancient Greek and some classical Chinese.

## Other activities and hobbies

- Classical piano. I studied music for eleven years (1984-1995) at the Escola de Música e Belas Artes Luisa Todi in Setúbal having reached level 6 on the piano.