

컴퓨터 비전 세미나

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Review

Q. What do Linear and Non-Linear mean?

- the output is directly proportional to the input
- the resulting system subjected to a complex input can be described as a sum of responses to simpler inputs
- Because linear systems are so much easier to analyze, predict and solve than nonlinear ones, much research is devoted to finding linear approximations of nonlinear phenomena.

Q. Why Convolutional-NN is not called Correlation-NN ?

- They are equivalent because the weights are initialized and updated in the same way.
- Using "convolution" in the name emphasizes the ties to signal processing and traditional image filtering methods.

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More neighborhood operators

Fourier transform

Geometric transformations

Non-linear filtering

- The filters we have looked at so far have all been linear.
- In many cases, better performance can be obtained by using a non-linear combination of neighboring pixels.

Median filtering

- selects the median value from each pixel's neighborhood
- it selects only one input pixel value to replace each output pixel, it is not as efficient at averaging away regular Gaussian noise

1	2	1	2	4
2	1	3	5	8
1	3	7	6	9
3	4	8	6	7
4	5	7	8	9

(a) median = 4

alpha-trimmed mean

- averages together all of the pixels except for the fraction

1	2	1	2	4
2	1	3	5	8
1	3	7	6	9
3	4	8	6	7
4	5	7	8	9

(b) α -mean = 4.6

weighted median

- [illegible]

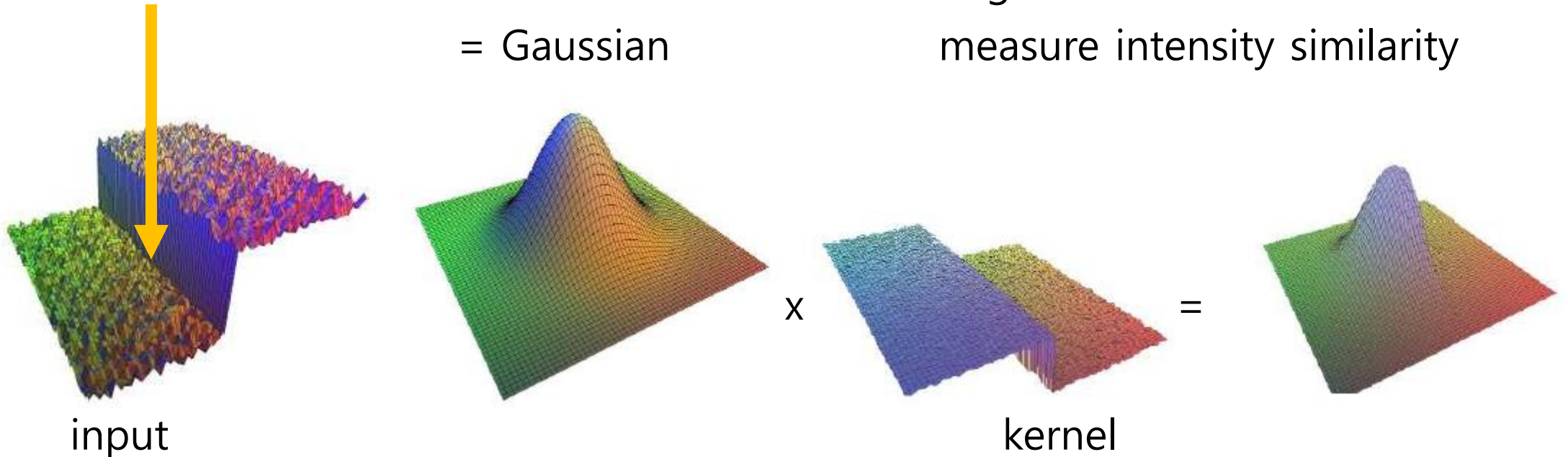
Bilateral filtering

- instead of rejecting a fixed percentage, bilateral filtering reject pixels whose values differ too much from the central pixel value

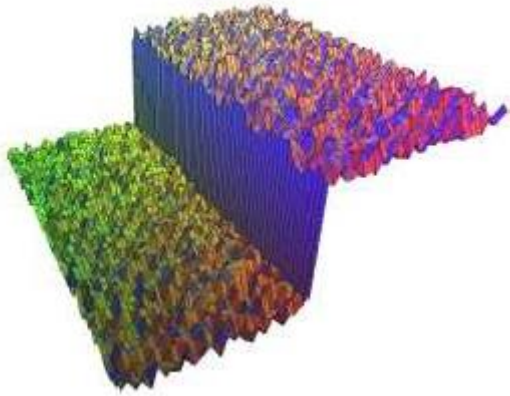
$$w(i, j, k, l) = \exp \left(-\frac{(i - k)^2 + (j - l)^2}{2\sigma_d^2} - \frac{\|\mathbf{f}(i, j) - \mathbf{f}(k, l)\|^2}{2\sigma_r^2} \right)$$

domain kernel
= Gaussian

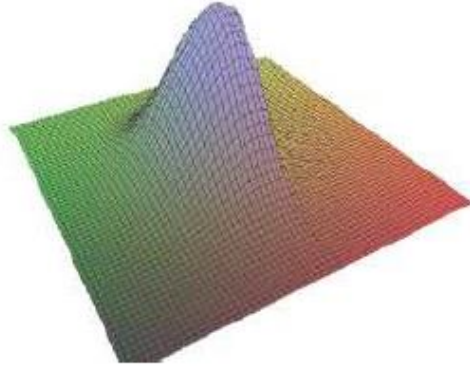
range kernel
measure intensity similarity



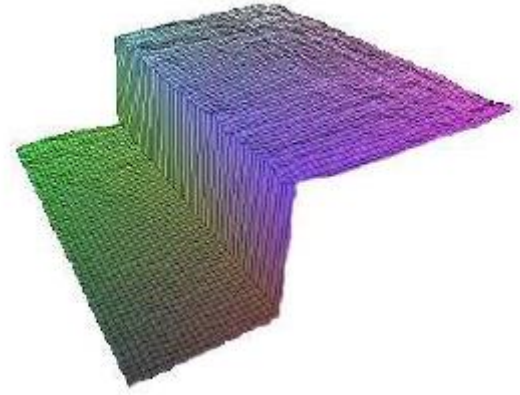
Bilateral filtering



input



kernel



output

- Since bilateral filtering is slow, a number of acceleration techniques have been developed

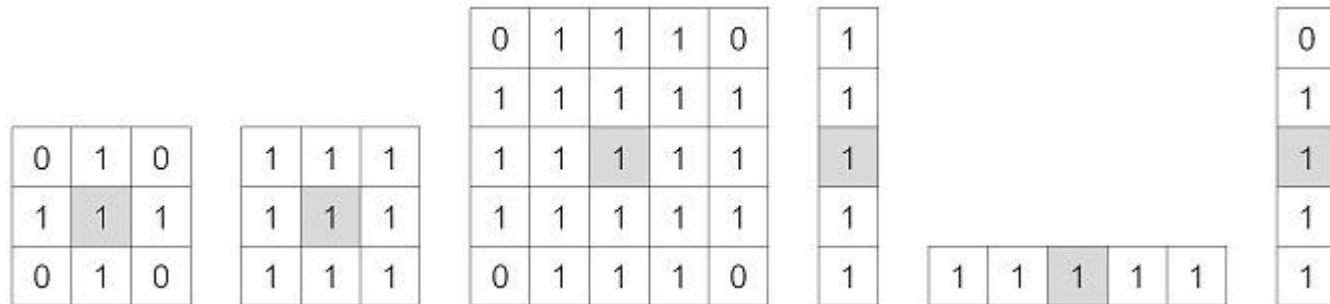
Binary image processing

- While non-linear filters are often used to enhance color images, they are also used extensively to process binary images.
- Such images often occur after a thresholding operation.

$$\theta(f, t) = \begin{cases} 1 & \text{if } f \geq t, \\ 0 & \text{else,} \end{cases}$$

Morphology

- Morphology changes the shape of the underlying binary objects.
- first convolve the binary image with a binary structuring element
- then select a binary output value depending on the thresholded result of the convolution
- The structuring element can be any shape, from a simple 3 x 3 box filter, to more complicated disc structures.



Morphology

- **dilation:** $\text{dilate}(f, s) = \theta(c, 1)$;
- **erosion:** $\text{erode}(f, s) = \theta(c, S)$;
- **majority:** $\text{maj}(f, s) = \theta(c, S/2)$;
- **opening:** $\text{open}(f, s) = \text{dilate}(\text{erode}(f, s), s)$;
- **closing:** $\text{close}(f, s) = \text{erode}(\text{dilate}(f, s), s)$.



original dilation erosion majority opening closing

Opening fails to eliminate the dot, since it is not wide enough.

- dilation grows objects
- erosion shrinks them
- majority smooth sharp corners
- opening and closing operations tend to remove small objects or holes

Distance transforms

distance transform $D(i, j)$ of a binary image $b(i, j)$, $d(k, l)$ is some distance metric

$$D(i, j) = \min_{k, l: b(k, l) = 0} d(i - k, j - l),$$

it is the distance to the nearest background pixel whose value is 0.

Manhattan distance

$$d_1(k, l) = |k| + |l|$$

Euclidean distance

$$d_2(k, l) = \sqrt{k^2 + l^2}.$$

Distance transforms

0	0	0	0	1	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	0	1	0	0	0	0
0	0	0	0	0	0	0

(a)

0	0	0	0	1	0	0
0	0	1	1	2	0	0
0	1	2	2	3	1	0
0	1	2	3			

(b)

0	0	0	0	1	0	0
0	0	1	1	2	0	0
0	1	2	2	3	1	0
0	1	2	2	1	1	0
0	1	2	1	0	0	0
0	0	1	0	0	0	0
0	0	0	0	0	0	0

(c)

0	0	0	0	1	0	0
0	0	1	1	1	0	0
0	1	2	2	2	1	0
0	1	2	2	1	1	0
0	1	2	1	0	0	0
0	0	1	0	0	0	0
0	0	0	0	0	0	0

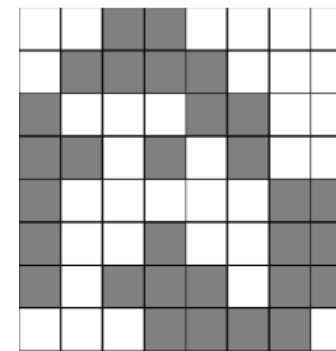
(d)



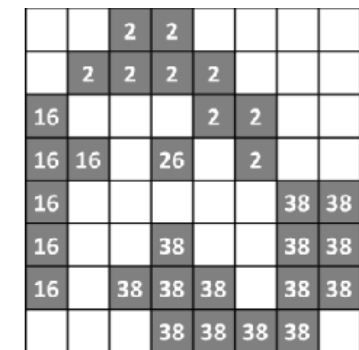
The ridges in the distance transform become the skeleton and consist of pixels that are of equal distance to their boundaries

Connected components

- finding connected components, which are defined as regions of adjacent pixels that have the same input value or label
- N4 adjacent(+), N8 adjacent(□)
- it is often useful to compute the area statistics for each individual region
 - the area (number of pixels)
 - the perimeter (number of boundary pixels)
 - the centroid (average x and y values)
 - the second moments
- DFS, stack



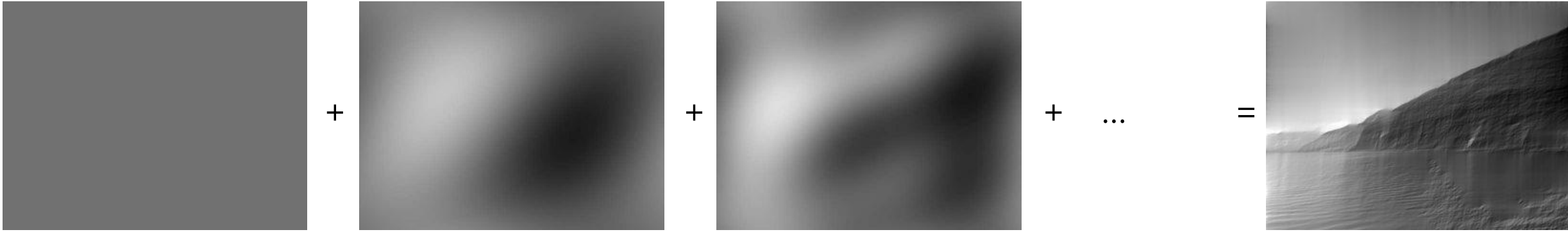
(a)



(b)

Image frequency

- The image is made up of various waves or frequencies



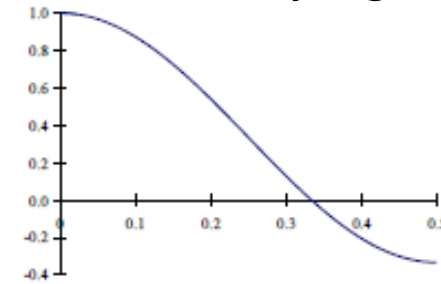
- The high frequency means rapid change of values which happens when there is sharp contrast in the image, such as edges.
- The low frequency means slow change in pixel values which corresponds to plain areas in images
- If an image has large values at high frequency components, then the data is changing rapidly on a short distance scale. e.g. a page of text, sharp image

Fourier transforms

- decomposes functions depending on space(2D) or time(1D) into functions depending on spatial or temporal frequency
- any signal can be represented as a sum of periodic components with varying frequencies

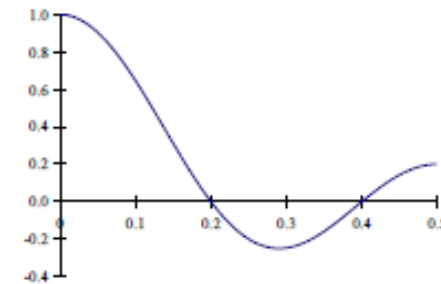
box-3 $\frac{1}{3} \begin{bmatrix} 1 & 1 & 1 \end{bmatrix}$

$$\frac{1}{3}(1 + 2 \cos \omega)$$



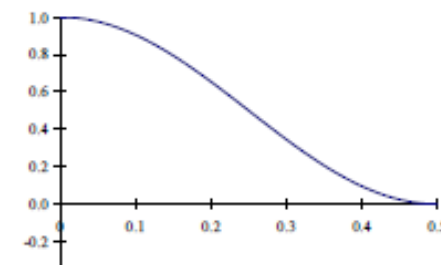
box-5 $\frac{1}{5} \begin{bmatrix} 1 & 1 & 1 & 1 & 1 \end{bmatrix}$

$$\frac{1}{5}(1 + 2 \cos \omega + 2 \cos 2\omega)$$

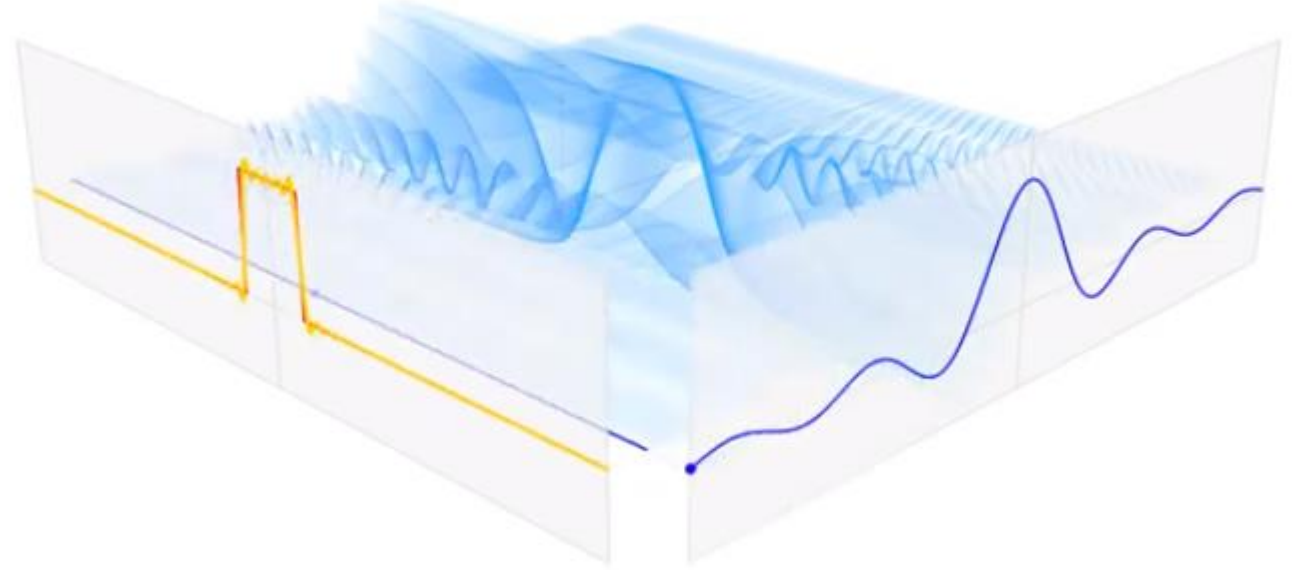


linear $\frac{1}{4} \begin{bmatrix} 1 & 2 & 1 \end{bmatrix}$

$$\frac{1}{2}(1 + \cos \omega)$$



Fourier transforms



$$f \star g \xrightarrow{\text{F.T.}} \mathcal{F} \cdot \mathcal{G}$$

Time domain
or Space domain

Frequency domain

Where $\mathcal{F} = \text{Fourier_Transform}(f)$

- Convolution of two functions corresponds to the product of them in frequency domain.

Wiener filter

- reduce the amount of noise present in a signal by comparison with an estimation of the desired noiseless signal
- The Wiener filter is based on a statistical approach, based on minimum mean square error (MMSE)
- assuming that an image is a sample from a correlated Gaussian random noise field combined with a statistical model of the measurement process yields an optimum restoration filter known as the Wiener filter

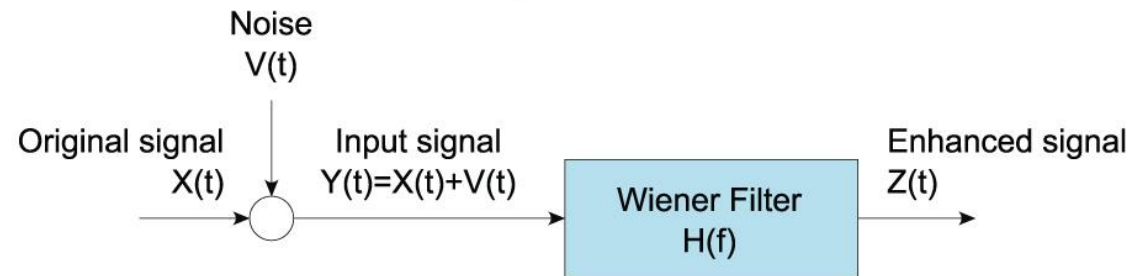
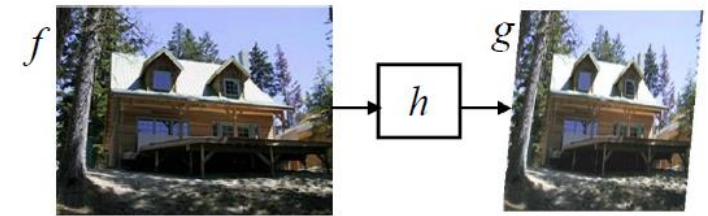


Figure 1. Optimal (Wiener) filtering signal flow

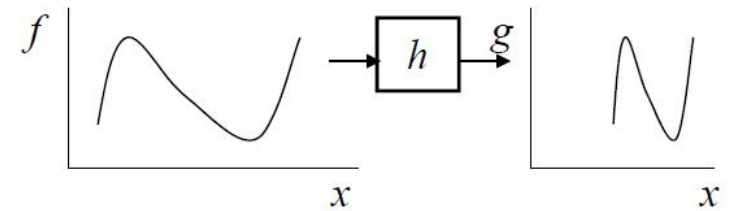
Geometric transformations

- more general transformations, such as image rotations or general warps
- In contrast to the point processes, which transform the range of the image, here we look at functions that transform the domain

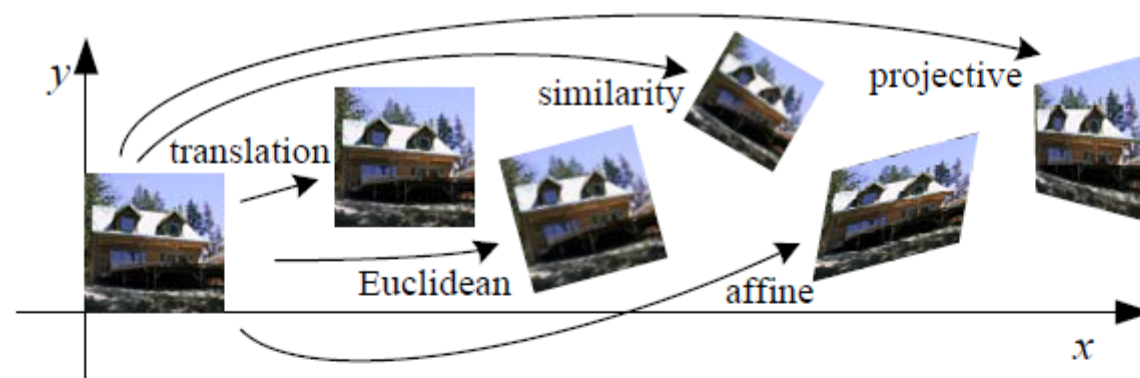


Parametric transformations

- global deformation to an image, where the behavior of the transformation is controlled by a small number of parameters



Parametric transformations



Transformation	Matrix	# DoF	Preserves	Icon
translation	$\begin{bmatrix} \mathbf{I} & \mathbf{t} \end{bmatrix}_{2 \times 3}$	2	orientation	
rigid (Euclidean)	$\begin{bmatrix} \mathbf{R} & \mathbf{t} \end{bmatrix}_{2 \times 3}$	3	lengths	
similarity	$\begin{bmatrix} s\mathbf{R} & \mathbf{t} \end{bmatrix}_{2 \times 3}$	4	angles	
affine	$\begin{bmatrix} \mathbf{A} \end{bmatrix}_{2 \times 3}$	6	parallelism	
projective	$\begin{bmatrix} \tilde{\mathbf{H}} \end{bmatrix}_{3 \times 3}$	8	straight lines	

Parametric transformations

- translation
$$\begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x + t_x \\ y + t_y \\ 1 \end{bmatrix}$$

- rigid
$$\begin{bmatrix} \cos(\theta) & -\sin(\theta) & t_x \\ \sin(\theta) & \cos(\theta) & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$

- similarity
$$\begin{bmatrix} s \cos(\theta) & -s \sin(\theta) & t_x \\ s \sin(\theta) & s \cos(\theta) & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$

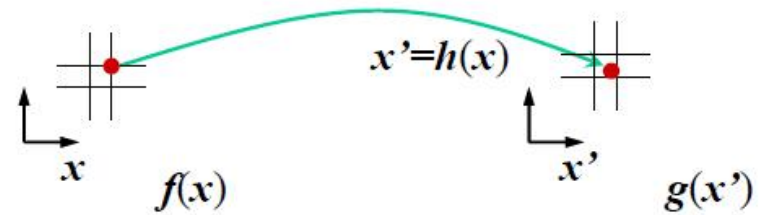
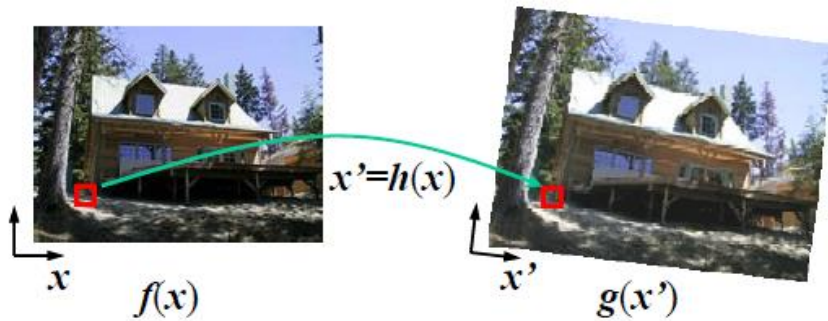
- affine
$$\begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} u \\ v \\ w \end{bmatrix}$$

- projective
$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} u \\ v \\ w \end{bmatrix}$$

- The 2 x 3 matrices are extended with a third $[0^T \ 1]$ row to form a full 3 x 3 matrix for homogeneous coordinate transformations.

Forward warping

- given a transformation specified by a formula $x' = h(x)$
- Compute the destination location $x' = h(x)$.
- Copy the pixel $f(x)$ to $g(x')$.

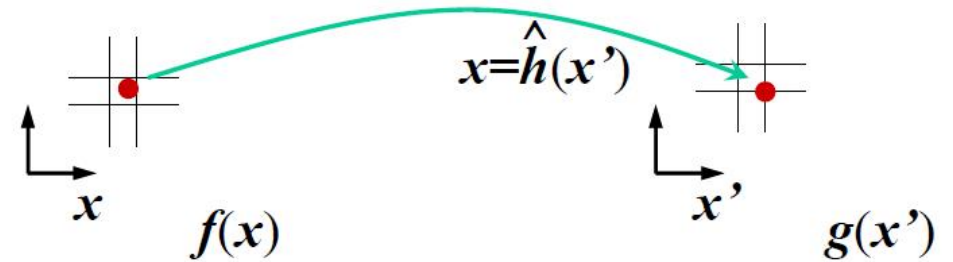
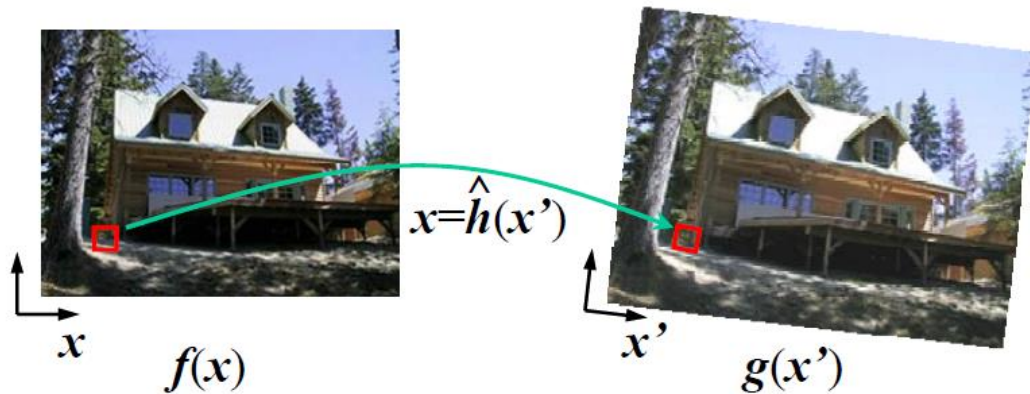


Forward warping

- this approach suffers from several limitations.
- copying a pixel $f(x)$ to a location x' in g is not well defined when x' has a non-integer value
- round the value of x' to the nearest integer coordinate and copy the pixel there
- distribute the value among its four nearest neighbors in a weighted fashion

Inverse warping

- $\hat{h}(x')$ is presumably defined for all pixels in $g(x')$
- $x = \hat{h}(x')$ can simply be computed as the inverse of $h(x)$
- Resample $f(x)$ at location x and copy to $g(x')$

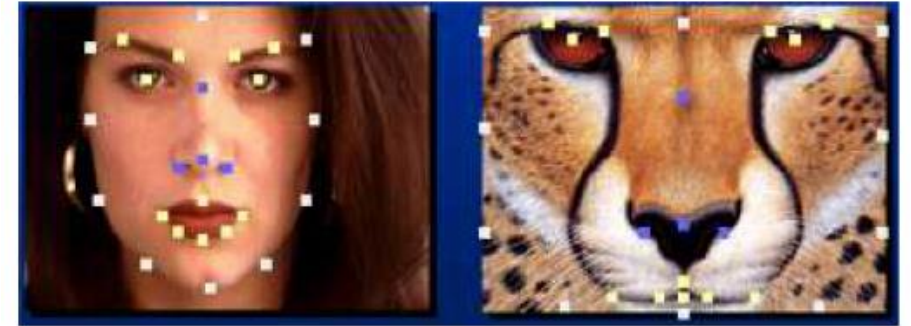


Mesh-based warping

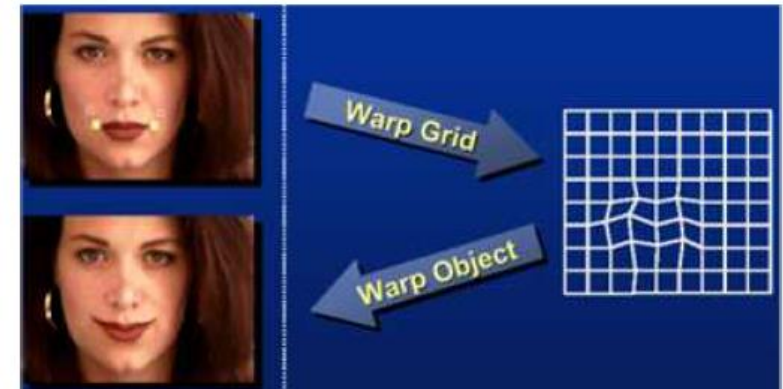
- changing the appearance of a face from a frown to a smile
- To perform such a transformation, different amounts of motion are required in different parts of the image.

Mesh-based warping

- first approach is to specify a sparse set of corresponding points
- displacement of these points can then be interpolated to a dense displacement field



- interpolating a sparse set of displacements include moving nearby quadrilateral mesh vertices
- If quadrilateral meshes are used, it may be desirable to interpolate displacements down to individual pixel values



Mesh-based warping

- second approach is specifying displacements for local deformations is to use corresponding oriented line segments
 - Each line segment correspondence specifies a translation, rotation, and scaling
 - Pixels along each line segment are transferred from source to destination exactly as specified
-
- final approach is using a mesh specifically adapted to the underlying image content
 - Once the two meshes have been specified, intermediate warps can be generated using linear interpolation and the displacements

