

# Report on implementing a decision tree classifier

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In this assignment I designed, coded and evaluated a decision tree classifier in this report we'll take a look at the design decisions and we'll discuss the performance of the implementation.

## Content of the archive

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```
- benchmark.ipynb # a notebook that contains the code evaluating the model
- decision_tree.py # the source file of everything directly related to the
implementation of DecisionTree
- doc            # the sources of the report
- scratch.ipynb  # a notebook containing experiments and snippets of code used
during the conception
- utils.py       # the source file containing everything used in the
implementation that is not directly part of the implementation
```

## Designing and coding the decision tree

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### Guiding ideas

Here are some of the general ideas I wanted to follow designing the decision tree :

#### Python is slow but...

Python is slow. That being said it was still my choice to implement the tree because:

- it's simple
- it has a good datascience community
- numpy's `ndarray` negates part of the slowness of python
- rust wasn't one of the available languages

#### Prioritize numpy

Numpy, being implemented in c, allows us to get good performances when manipulating a large amount of data. So we are gonna try to prioritize the use of numpy even if it can complexify the code

```

ndarray = np.arange(20000000)
l = list(ndarray)
l = [2*x for x in l] # 2.5 seconds
ndarray = ndarray*2 # 0.9 seconds
# 3.9 seconds
lb = []
for i in l:
    lb.append(i*2)

```

## Tree = Recursive

Obviously when we talk about tree the first thought is **recursion**. So we'll use a recursive algorithm both for fitting the classifier and for the prediction. That being said repeated function call can be costly so we'll try to limit ourselves to one traversal.

## Design

Now I'll explain how we build the tree and then exploit it.

### The tree

Let's take a look at how tree is composed.

- `DecisionTree` the wrapper class that is used by the end user.
- `Node` an abstract class that describes a node of the decision tree
- `Leaf` the leaf node of the tree containing :
  - `label` : the majority label for the leaf
- `Branch` the branch node of the tree containing :
  - `feature` : the index of the feature along which the split has been done
  - `boundry` : the decision boundry of the split
  - `sup_branch:Node` & `inf_branch:Node` : the child node of the subtree
  - `_majority_label` : the majority label of the branch during training

### Building the tree

Most of the code that builds the tree is contained in the recursive function

```
DecisionTree._build_tree.
```

We first take care of the first two trivial cases : a uniform `y` and a uniform `x` and we create an appropriate list.

```
if np.all(y == y[0]):  
    # If every y are equal return a leaf  
    return Leaf(y[0])  
elif np.all(x == x[0]):  
    # If every x are equal then we return a leaf with the most common label  
    count = ut.count_vals(y)  
    return Leaf(ut.dict_max(count)[0])
```

If we're not in a trivial case it means we must create a split. To do so we will do a search of the best feature to split in terms of information gain.

```

else:
    # Infos about the best split found
    best_IG = 0
    best_feature = None
    best_split = None

    y_cached_split = [] # We can cache some of the work we already did
    cached_mask = None # trying to find the best split

    # Useful stuff to compute IG but doesnt change between features
    E_base = self.impurity_mesurement(y)
    n = len(y)

    for feat in range(x.shape[1]):
        # We split our classes along the mean of the feature
        split_plane = x[:, feat].mean()
        split_mask = x[:, feat] < split_plane
        ysubset1 = y[split_mask]
        ysubset2 = y[np.logical_not(split_mask)]

        # We compute the information gain for that feature
        E_s1 = self.impurity_mesurement(ysubset1)
        E_s2 = self.impurity_mesurement(ysubset2)
        E_s = (E_s1 * len(ysubset1) + E_s2 * len(ysubset2)) / n
        IG_s = E_base - E_s

        # If it is better than the previous IG save the split
        if IG_s >= best_IG:
            best_IG = IG_s
            best_feature = feat
            best_split = split_plane
            y_cached_split = [ysubset1, ysubset2]
            cached_mask = split_mask

    counts = ut.count_vals(y)
    majority_label = ut.dict_max(counts)[0]

    return Branch(
        best_feature,
        best_split,
        inf_branch=self._build_tree(x[cached_mask], y_cached_split[0]),
        sup_branch=self._build_tree(x[~cached_mask], y_cached_split[1]),
        majority_label=majority_label
    )

```

You can note that we keep some of the computed values cached so that we don't need to compute it again for the next call of the recursion.

We also store the majority label for the branch during training because it will be useful for the

## Pruning

The implementation of the pruning algorithm is spread across the iteration implementations of the function `Node.prune`.

The function `prune` returns the pruned tree and the number of positive hits achieved by the pruned tree on the pruning dataset. We do not use the accuracy because for our purpose it's equivalent to the number of positive hits. It's also easier to reuse the number of hits for the parent tree.

$$\begin{aligned} & accuracy_1 < accuracy_2 \\ \Leftrightarrow & \frac{positives_1}{N} < \frac{positives_2}{N} \\ \Leftrightarrow & positives_1 < positives_2 \end{aligned}$$

Apart from that no quirks in the implementation we just follow the algorithm described in the subject

## Inference

We just propagate the dataset in the tree and return a label when a  $x$  reaches a leaf.

The only thing that gives a bit of difficulty is that we need to keep the correspondence between the  $x$ s and the  $y$ s during that traversal of the tree. The problem is keeping the order is costly. So the solution we chose is to add the index of the  $x$  and then once the  $x$  reaches a leaf we return the index along the  $y$  and only sort the list at the end of the prediction

# Testing the Decision tree

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## Comparison

We'll compare our tree to scikit learn `DecisionTreeClassifier`. To make the comparison fair we'll add no limitation to the tree.

## Accuracy

Here's the validation accuracy of our model against scikit learn's.

	scikit learn	our implmentation
gini	0.808469	0.830342
entropy	0.806786	0.8682

We can see we get a slightly better accuracy which is probably due to the scikit learn implementation being more optimized for performance.

It also seems that we get better results with entropy.

**Sidenote** : I tested different value for the size of the pruning dataset but as it didnt seem to have an impact that is different from noise so I didnt include it in the `benchmark.ipynb`. The test can be seen in `scratch.ipynb`

I also tested an other regularisation parameter that would require a branch to have a `base_accuracy - accuracy_pruned > alpha` to not be pruned but it showed a negative impact on validation accuracy no matter the value of alpha so the idea was scratch

## Training time

I compared my implementation and scikit-learn on execution time on several randomly generated dataset and on the real dataset.

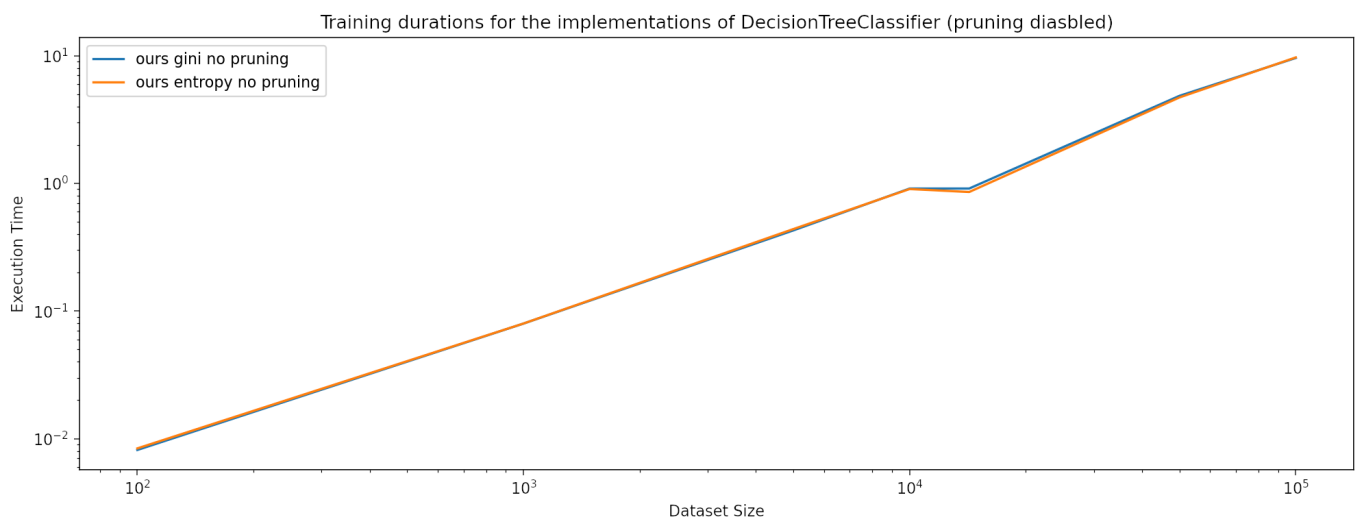
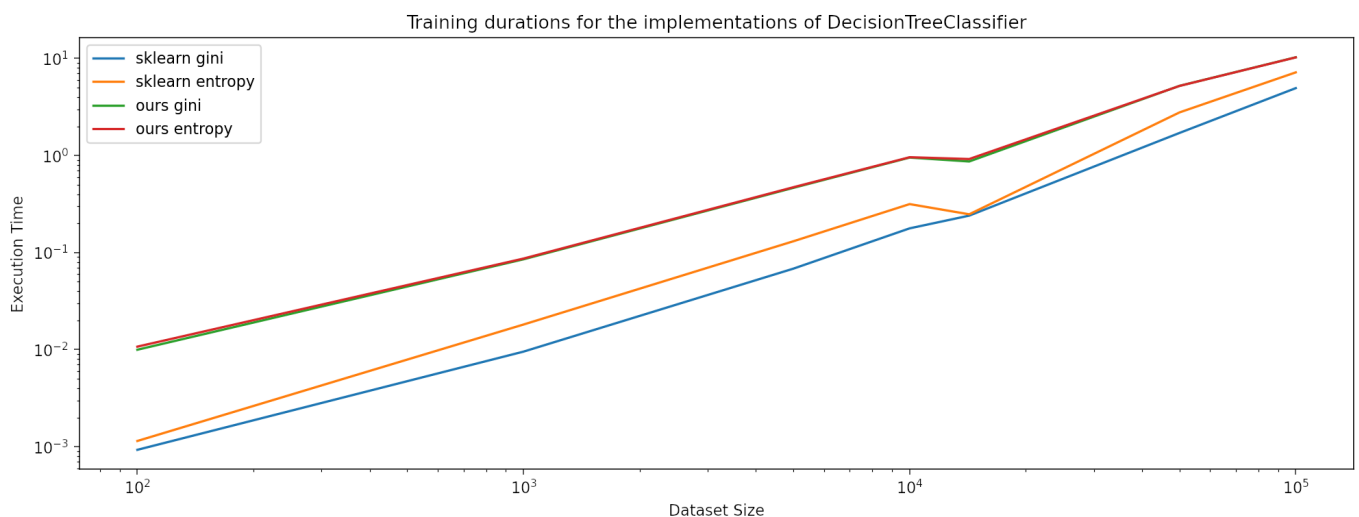
Here is the result of the benchmarck :

*with pruning :*

	sklearn gini	sklearn entropy	ours gini	ours entropy
Random(100)	0.00207186	0.00244713	0.0126264	0.0131702
Random(1000)	0.01739	0.0286255	0.0959089	0.0965569
Random(5000)	0.177305	0.291452	0.483316	0.482774
Random(10000)	0.396026	0.594108	1.05734	1.04421
Real Dataset(14265)	0.487228	0.501664	0.823519	0.824055
Random(50000)	4.08232	5.68392	5.36568	5.34775
Random(100000)	10.3493	16.0937	10.5132	10.4989

*without pruning :*

	ours gini no pruning	ours entropy no pruning
Random(100)	0.00815368	0.0083878
Random(1000)	0.0796692	0.0797589
Random(5000)	0.42792	0.438367
Random(10000)	0.909921	0.902353
Real Dataset(14265)	0.910468	0.855229
Random(50000)	4.84662	4.70836
Random(100000)	9.59238	9.68633
So that it is more readable we created graphs of the performance :		



We can observe several interesting things from that graph :

Although sklearn seems to have a better implementation in terms of speed my implmentation seems to grow with the same profile as the scikit learn implemntation. Which mean they share the same big-O notation. Which from the look of the graph might be  $O(e^n)$ .

Another thing that is intresting to see is that how noisy is the dataset has a big impact on the run time. Which makes sense considering that the algorithme as less chance to stop with big leafs if the dataset is noisy.

## inference time

I compared my implementation and scikit-learn on execution time on several randomly generated dataset and on the real dataset.

Here is the result of the benchmarck :

*with pruning :*

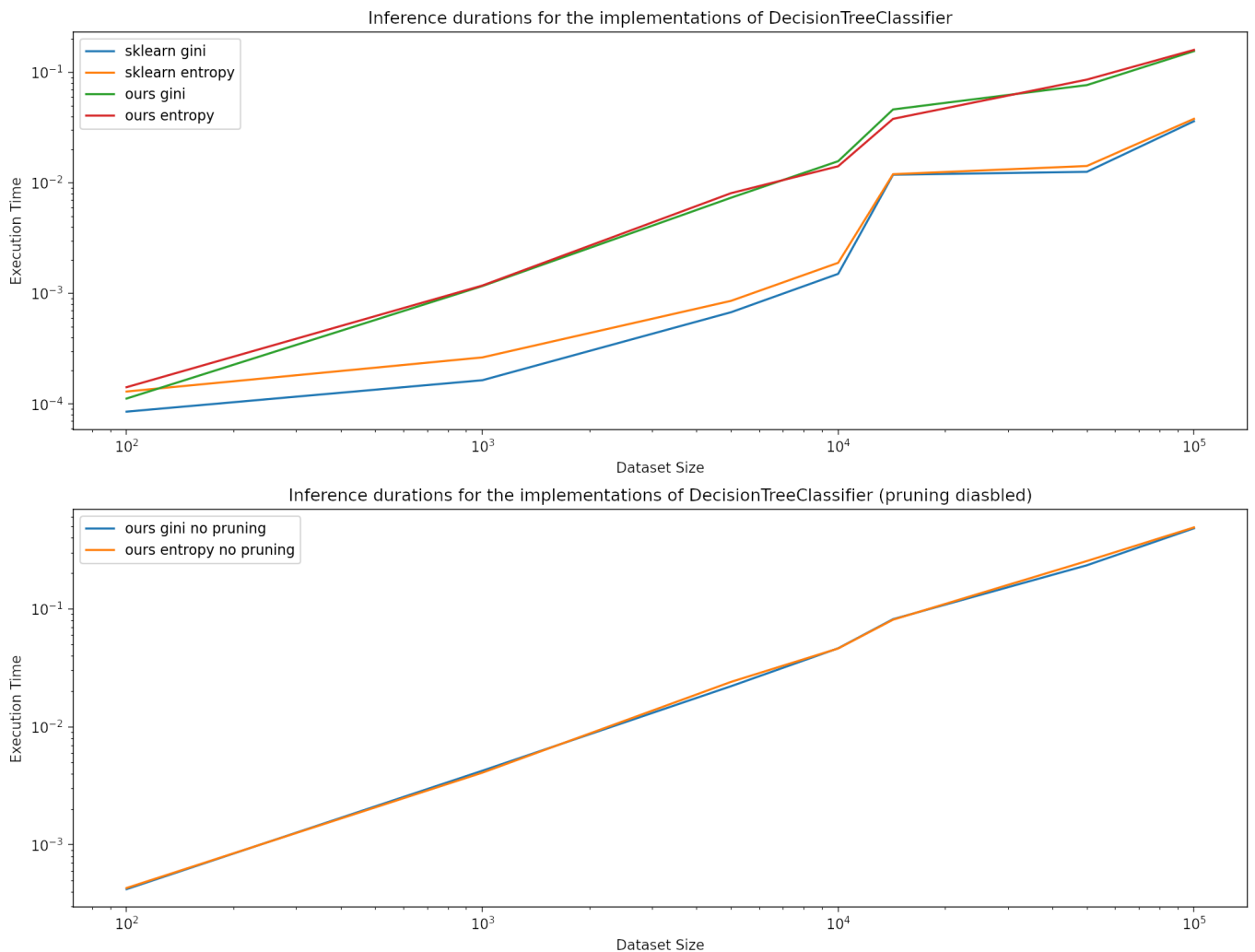
	sklearn gini	sklearn entropy	ours gini	ours entropy
Random(100)	8.53539e-05	0.000174284	0.000123501	0.000214815
Random(1000)	0.00019455	0.000413656	0.000883102	0.000960112
Random(5000)	0.000708342	0.000832319	0.00607967	0.00741029
Random(10000)	0.00194836	0.00193119	0.0137649	0.0142419
Real Dataset(14265)	0.0135095	0.00992227	0.0423906	0.0458436
Random(50000)	0.0125453	0.0138762	0.0780728	0.0743835
Random(100000)	0.0313737	0.034543	0.158311	0.162944

*without pruning*



	ours gini no pruning	ours entropy no pruning
Random(100)	0.000421047	0.000430584
Random(1000)	0.00424647	0.00408769
Random(5000)	0.0220993	0.024039
Random(10000)	0.0463181	0.0461442
Real Dataset(14265)	0.0817471	0.0809014
Random(50000)	0.233926	0.25408
Random(100000)	0.481616	0.489822

For the sake of readability we created graph for the inference time too



Here again we see the scikit learn implementation is faster than ours but we still are in the same class of algorithm.

What is odd is that the inference seems to be slower with real dataset. Which is surprising considering the tree should be smaller so quicker to traverse.

## Testing the selected model

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Since it was the best performing model on the validation model we picked my implementation with :

- 0.2 pruning size
- pruning enable
- entropy disorder measurement

And we obtained a 0.874 accuracy on the training test set.