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— MODULE utils —
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LOCAL INSTANCE Integers LOCAL INSTANCE Sequences
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\begin{aligned} \mathit{Max}(S) &\triangleq \\ &\text{ if } S = \{\} \text{ Then } 0 \\ &\text{ else choose } m \in S : \forall \, x \in S : m \geq x \end{aligned} \begin{aligned} \mathit{PruneLasts}(seq, \, n) &\triangleq \\ &\text{ if } n < 1 \text{ Then } \langle \rangle \\ &\text{ else if } n \geq \mathit{Len}(seq) \text{ Then } \mathit{seq} \\ &\text{ else } \mathit{SubSeq}(\mathit{seq}, \mathit{Len}(\mathit{seq}) - n + 1, \mathit{Len}(\mathit{seq})) \end{aligned} \begin{aligned} \mathit{PruneFirsts}(\mathit{seq}, \, n) &\triangleq \\ &\text{ if } n < 1 \text{ Then } \langle \rangle \\ &\text{ else if } n \geq \mathit{Len}(\mathit{seq}) \text{ Then } \mathit{seq} \\ &\text{ else } \mathit{SubSeq}(\mathit{seq}, 1, \mathit{Len}(\mathit{seq}) - n + 1) \end{aligned} \begin{aligned} \mathit{IsPrefix}(p, \, s) &\triangleq \\ &\wedge \mathit{Len}(p) \leq \mathit{Len}(s) \\ &\wedge \forall \, i \in 1 \ldots \mathit{Len}(p) : p[i] = s[i] \end{aligned}
```