

HW 2 (due June 3 at etl.snu.ac.kr)

1. This problem is based on the Matlab example "Sliding Mode Control Design for a Robotic Manipulator" available at the following site :

<https://www.mathworks.com/help/slcontrol/ug/design-smc-controller-for-robotic-manipulator.html>

We would like to design a sliding mode controller (SMC) for a robotic manipulator with two actuated joints, whose dynamics is

$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) + F(\dot{q}) = \tau + \tau_d$$

where

- $q, \dot{q}, \ddot{q}$  are 2-by-1 vectors representing the joint angles, velocities, and accelerations, respectively.
- The control input  $\tau$  is 2-by-1 torque vector applied to the joints.
- The inertia matrix  $M(q)$ , Coriolis matrix  $C(q, \dot{q})$ , gravity vector  $G(q)$ , and friction vector  $F(\dot{q})$  encapsulate the dynamics of the manipulator
- $\tau_d$  represents the disturbance torques affecting the system, and the magnitude of its elements is upper-bounded by  $D = [10, 5]^T$ .

- (a) Given a desired trajectory  $q_d$ , design SMC so that  $q - q_d \rightarrow 0$ .
  - (b) Perform simulation with your choice of  $q_d$  and  $\tau_d$ , and observe the difference using "sign" function vs saturation function.
2. Design a nonlinear model predictive controller for the manipulator in No. 1. See if there is a difference between when  $\tau_d = 0$  and  $\tau_D \neq 0$ . You may refer to the Matlab example "Control Robot Manipulator Using Passivity-Based Nonlinear MPC" at the following site :  
<https://www.mathworks.com/help/mpc/ug/control-of-robot-manipulator-using-passivity-based-nonlinear-mpc.html>
  3. Design a backstepping control for the following system:

$$\begin{aligned}\dot{x} &= ax - x^3 + \xi \\ \dot{\xi} &= u\end{aligned}$$

- (a) Let  $a = 1$ , and design a backstepping control such that  $x(t) \rightarrow x_d(t)$ .
  - (b) Let  $a$  be an unknown constant, and design an adaptive backstepping control such that  $x(t) \rightarrow x_d(t)$ .
  - (c) Simulate (b) with your choice of  $x_d$ , and check the state/parameter convergence.
4. Consider the nonlinear system:

$$\begin{aligned}\dot{x}_1 &= x_1 + x_1x_2 - x_2^2 + u \\ \dot{x}_2 &= x_1x_2 - x_2^2 + u \\ \dot{x}_3 &= x_1 + x_1x_2 - x_2^2 - (x_3 - x_1)^3 + u \\ y &= x_1 - x_2\end{aligned}$$

- (a) Show that the system has relative degree two.
  - (b) Define the internal variable, and transform the system into the normal form.
  - (c) Show that the origin of the zero dynamics is globally asymptotically stable.
  - (d) Design a feedback law that achieves global asymptotic stability.
5. (Term project proposal) The course project may be:
    - A. an independent research project that can utilize any of the techniques covered in the course, or
    - B. a review of the literature in an area covered in or related to the course.
 You may choose a project related to your area of research, and/or you may choose to apply any of the techniques from class to a system that you are interested in.
    - In the case of an independent research project, you should submit a paper which summarizes related work, describes your problem and method, and presents your results.

- In the case of a literature review, you should submit a report which provides the background review, presents a clear description of the results presented in the papers that you are reviewing, and gives your own assessment of these results.
- The projects will be evaluated according to correctness and depth of your analysis or review, and your written presentation.
- Please prepare to give a brief ( $< 3$  min) proposal presentation on June 5, describing your topic and what you plan to accomplish in your project.
- The final course project papers or reports are due **11:59 pm, June 17**. Recommended length: 6–12 single-column pages, or 3–6 double-column pages.