GUROBI OPTIMIZER EXAMPLE TOUR



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Introduction

The GurobiTM distribution includes an extensive set of examples that illustrate commonly used features of the Gurobi libraries. Most examples have versions for C, C++, C#, Java, Visual Basic, and Python. A few, however, illustrate features that are specific to the Python interface.

This document provides a brief tour of these examples. We won't go through each example in detail. Instead, we'll start with an Overview of the set of tasks that you are likely to want to perform with the Gurobi Optimizer. Later sections will then describe how specific examples accomplish each of these tasks. We suggest that you browse the example source code (in a text editor, or in another browser window) while reading this document. This document includes Source Code for all of the examples, in all available languages. Source files are also available in the examples directory of the Gurobi distribution.

A brief note for users of the Gurobi MATLAB® and R interfaces: our interfaces to these languages are built around the assumption that you will use the rich matrix-oriented capabilities of the underlying languages to build your optimization models. Thus, our examples for these languages don't attempt to show you how to build models. We have instead chosen to provide a few simple examples that demonstrate how to pass matrices into our interface.

If you would like further details on any of the Gurobi routines used in these examples, please consult the Gurobi Reference Manual.

Example tour

This document provides a quick guided tour of the Gurobi examples; we will try to highlight some of the most important features of these examples. Full source code is provided in this document, so you are free to explore the examples in full detail.

Wherever possible, we try to discuss the examples in a manner that is independent of programming languages. We will refer to each example using a brief, language independent name. You will need to map this name to the specific source file name for your language. For example, the facility example corresponds to six different implementations, one in C (facility_c.c.), one in C++ (facility_c++.cpp), one in Java (Facility_java), one in C# (facility_cs.cs), one in Visual Basic (facility_vb.vb), and one in Python (facility.py). If you would like to look at the language implementation for a particular example, please refer to the appropriate example source file.

The Gurobi examples

The following is a list of all of the examples included in the Gurobi distribution. The source code for these examples can be found in the examples directory of the distribution, or in the Source Code section of this document.

- callback Demonstrates the use of Gurobi callbacks.
- dense Solves a model stored using dense matrices. We don't recommend that you use dense matrices for your models, but this example may be helpful if your data is already in this format.
- diet Builds and solves the classic diet problem. Demonstrates model construction and simple model modification after the initial model is solved, a constraint is added to limit the number of dairy servings.
- diet2, diet3, diet4, dietmodel Python-only variants of the diet example that illustrate model-data separation.
- facility Simple facility location model: given a set of plants and a set of warehouses, with transportation costs between them, this example finds the least expensive set of plants to open in order to satisfy product demand. This example demonstrates the use of MIP starts the example computes an initial, heuristic solution and passes that solution to the MIP solver.
- feasopt Reads a MIP model from a file, adds artificial slack variables to relax each constraint, and then minimizes the sum of the artificial variables. It then computes the same relaxation using the feasibility relaxation feature. The example demonstrates simple model modification by adding slack variables. It also demonstrates the feasibility relaxation feature.
- **fixanddive** Implements a simple MIP heuristic. It reads a MIP model from a file, relaxes the integrality conditions, and then solves the relaxation. It then chooses a set of integer variables that take integer or nearly integer values in the relaxation, fixes them to the nearest integer,

and solves the relaxation again. This process is repeated until the relaxation is either integer feasible or linearly infeasible. The example demonstrates different types of model modification (relaxing integrality conditions, changing variable bounds, etc.).

- lp A very simple example that reads a continuous model from a file, optimizes it, and writes the solution to a file. If the model is infeasible, it writes an Irreducible Inconsistent Subsystem (IIS) instead.
- **lpmethod** Demonstrates the use of different LP algorithms. Reads a continuous model from a file and solves it using multiple algorithms, reporting which is the quickest for that model.
- **lpmod** Demonstrates the use of advanced starts in LP. Reads a continuous model from a file, solves it, and then modifies one variable bound. The resulting model is then solved in two different ways: starting from the solution of the original model, or restarting from scratch.
- mip1 Builds a trivial MIP model, solves it, and prints the solution.
- mip2 Reads a MIP model from a file, optimizes it, and then solves the fixed version of the MIP model.
- netflow A Python-only example that solves a multi-commodity network flow model. It
 demonstrates the use of several Python modeling constructs, including dictionaries, tuples,
 and tuplelist objects.
- params Demonstrates the use of Gurobi parameters. Reads a MIP model from a file, and then spends 5 seconds solving the model with each of four different values of the MIPFocus parameter. It compares the optimality gaps for the four different runs, and continues with the MIPFocus value that produced the smallest gap.
- qp Builds a trivial QP model, solves it, converts it to an MIQP model, and solves it again.
- qcp Builds and solves a trivial QCP model.
- sensitivity MIP sensitivity analysis. Reads a MIP model, solves it, and then computes the objective impact of fixing each binary variable in the model to 0 or 1. Demonstrates simple MIP model modification by changing variable bounds.
- sos Builds and solves a trivial SOS models.
- **sudoku** Reads a Sudoku puzzle dataset from a file, builds a MIP model to solve that model, solves it, and prints the solution.
- tsp Solves a traveling salesman problem using lazy constraints.
- tune Uses the parameter tuning tool to search for improved parameter settings for a model.
- workforce1 Formulates and solves a workforce scheduling model. If the model is infeasible, the example computes and prints an Irreducible Inconsistent Subsystem (IIS).

- workforce2 An enhancement of workforce1. This example solves the same workforce scheduling model, but if the model is infeasible, it computes an IIS, removes one of the associated constraints from the model, and re-solves. This process is repeated until the model becomes feasible. Demonstrates constraint removal.
- workforce3 A different enhancement of workforce1. This example solves the same workforce scheduling model, but if the model is infeasible, it adds artificial variables to each constraint and minimizes the sum of the artificial variables. This corresponds to finding the minimum total change in the right-hand side vector required in order to make the model feasible. Demonstrates variable addition.
- workforce4 An enhancement of workforce3. This example solves the same workforce scheduling model, but it starts with artificial variables in each constraint. It first minimizes the sum of the artificial variables. Then, it introduces a new quadratic objective to balance the workload among the workers. Demonstrates optimization with multiple objective functions.

The example tour

The easiest place to start your introduction to the Gurobi examples is probably with the examples that load and solve a model from a file. These demonstrate the most basic capabilities of the Gurobi libraries. They also demonstrate the use of model attributes, which are an important concept in the Gurobi optimizer.

Once you are comfortable with these examples, you should move on to the examples that build a model from scratch. These show you how to create variables and constraints, and add them to an optimization model. They also illustrate the use of *lazy updates*, which you will need to understand in order to use the Gurobi libraries.

The next topic covered in this document is model modification. The Gurobi distribution includes examples that add and remove constraints, add variables, and change variable types, bounds and objective coefficients. You modify a model in much the same way that you build a model from scratch, but there are some important differences involving the use of the solution information.

Next, this document covers parameter changes. The params example shows you how to change parameters, and in particular how to use different parameter settings for different models.

On a related note, the tuning section demonstrates the use of our automated tuning tool. This tool searches for parameter settings that improve performance on a particular model.

The infeasibility section considers a few examples that cope with model infeasibility. Some use an Irreducible Inconsistent Subsystem (IIS) to handle the infeasibility, while others relax constraints.

One useful MIP feature that is worth understanding is MIP starts. A MIP start allows you to specify a known feasible solution to the MIP solver. The solution provides a bound on the objective of the best possible solution, which can help to limit the MIP search. The solution also provides a potential start point for the local search heuristics that are utilized by the Gurobi MIP solver.

It is possible to achieve model-data separation when using our Python interface, as is often done in modeling languages, but you need to make use of Python modules to do so. The model-data separation section provides an example of how this is done. It considers two versions of the diet example, which obtain model data from very different places. Both use the same file to formulate and solve the actual optimization model on that data.

The final topic we cover in this document is Gurobi callbacks. Callbacks allow the user to obtain periodic progress information related to the optimization.

2.1 Load and solve a model from a file

Examples: callback, feasopt, fixanddive, lp, lpmethod, lpmod, mip2, params, sensitivity

One of the most basic tasks you can perform with the Gurobi libraries is to read a model from a file, optimize it, and report the result. The lp (lp_c.c, lp_c++.cpp, lp_cs.cs, Lp.java, lp.py, lp_vb.vb) and mip2 (mip2_c.c, mip2_c++.cpp, mip2_cs.cs, Mip2.java, mip2.py, mip2_vb.vb) examples are simple illustratations of how this is done in the various supported Gurobi languages. While the specifics vary from one language to another, the basic structure remains the same for all languages.

After initializing the Gurobi environment, the examples begin by reading the model from the specified file. In C, you call the GRBreadmodel() function:

```
error = GRBreadmodel(masterenv, argv[1], &model);
In C++, this is done by constructing a GRBModel object:
    GRBModel model = GRBModel(env, argv[1]);
In C# and Java, this is also done by constructing a GRBModel object:
    GRBModel model = new GRBModel(env, args[0]);
In Python, this is done via the read global function:
    model = read(sys.argv[1])
    The next step is to invoke the Gurobi optimizer on the model. In C, you call GRBoptimize() on the model variable:
    error = GRBoptimize(model);
In C++, Java, and Python, this is accomplished by calling the optimize method on the model object:
    model.optimize();
In C#, the first letter of the method name is capitalized:
    model.Optimize();
```

A successful optimize call populates a set of solution attributes in the model. For example, once the call completes, the X variable attribute contains the solution value for each variable. Similarly, for continuous models, the Pi constraint attribute contains the dual value for each constraint.

The examples then retrieve the value of the model Status attribute to determine the result of the optimization. In the lp example, an optimal solution is written to a solution file (model.sol).

There are many other things you can do once you have read and solved the model. For example, lp checks the solution status — which is highly recommended. If the model is found to be infeasible, this example computes an Irreducible Inconsistent Subsystem (IIS) to isolate the source of the infeasibility.

2.2 Build a model

Examples: diet, facility, mip1, qcp, qp, sos, sudoku, workforce1, workforce2, workforce3, workforce4

Several of the Gurobi examples build models from scratch. We start by focusing on two, mip1 and sos, which build very simple models to illustrate the basic process.

Typically, the first step in building a model is to create an empty model. This is done using the GRBnewmodel function in C:

```
error = GRBnewmodel(env, &model, "mip1", 0, NULL, NULL, NULL, NULL);
```

You can optionally create a set of variables when you create the model, as well as specifying bounds, objective coefficients, and names for these variables. These examples add new variables separately.

In C++, C#, and Java, you create a new model using the GRBModel constructor. In Java, this looks like:

```
GRBModel model = new GRBModel(env);
```

In Python, the class is called Model, and its constructor is similar to the GRBModel constructor for C++ and Java.

Once the model has been created, the typical next step is to add variables. In C, you use the GRBaddvars function to add one or more variables:

```
error = GRBaddvars(model, 3, 0, NULL, NULL, NULL, obj, NULL, NULL, vtype, NULL);
```

In C++, Java, and Python, you use the addVar method on the Model object (AddVar in C#). In Java, this looks like:

```
GRBVar x = model.addVar(0.0, 1.0, -1.0, GRB.BINARY, "x");
```

The new variable's lower bound, upper bound, objective coefficient, type, and name are specified as arguments. In C++ and Python, you can omit these arguments and use default values; see the Gurobi Reference Manual for details.

After adding variables to the model, the next step is to call the update function (GRBupdatemodel() in C, model.update() in C++, Java, and Python, model.Update() in C#). Model modifications are performed in a *lazy* fashion in the Gurobi optimizer — they don't affect the model until the next update or optimize call. You *cannot* utilize the new variables (e.g., in constraints) until you call the update function.

The next step is to add constraints to the model. Linear constraints are added through the GRBaddconstr function in C:

```
error = GRBaddconstr(model, 3, ind, val, GRB_LESS_EQUAL, 4.0, "c0");
```

To add a linear constraint in C, you must specify a list of variable indices and coefficients for the left-hand side, a sense for the constraint (e.g., GRB_LESS_EQUAL), and a right-hand side constant. You can also give the constraint a name; if you omit the name, Gurobi will assign a default name for the constraint.

In C++, C#, Java, and Python, you build a linear constraint by first building linear expressions for the left- and right-hand sides. In Java, which doesn't support operator overloading, you build an expression as follows:

```
GRBLinExpr expr = new GRBLinExpr();
expr.addTerm(1.0, x); expr.addTerm(2.0, y); expr.addTerm(3.0, z);
```

You then use the addConstr method on the Model object to add a constraint using these linear expressions for the left- and right-hand sides:

```
model.addConstr(expr, GRB_LESS_EQUAL, 4.0, "c0");
```

For C++, C#, and Python, the standard mathematical operators such as +, *, <= have been overloaded so that the linear expression resembles a traditional mathematical expression. In C++:

```
model.addConstr(x + 2 * y + 3 * z \le 4, "c0");
```

Adding an special ordered set (SOS) constraint is similar. In C, you add one or more SOS constraint using the GRBaddsos function:

```
error = GRBaddsos(model, 1, 2, sostype, sosbeg, sosind, soswt);
```

For each SOS constraint, you must specify a list of members and a weight for each member.

In C++, C#, Java, and Python, you use the addSOS method on the Model object:

```
model.addSOS(sosv1, soswt1, GRB.SOS_TYPE1);
```

Once the model has been built, the typical next step is to optimize it (using GRBoptimize in C, model.optimize in C++, Java, and Python, or model.Optimize in C#). You can then query the X attribute on the variables to retrieve the solution (and the VarName attribute to retrieve the variable name for each variable). In C, the X attribute is retrieved as follows:

```
error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, 3, sol);
In C++:
cout << x.get(GRB_StringAttr_VarName) << " "</pre>
     << x.get(GRB_DoubleAttr_X) << endl;
cout << y.get(GRB_StringAttr_VarName) << " "</pre>
     << y.get(GRB_DoubleAttr_X) << endl;</pre>
cout << z.get(GRB_StringAttr_VarName) << " "</pre>
     << z.get(GRB_DoubleAttr_X) << endl;
In Java:
System.out.println(x.get(GRB.StringAttr.VarName) +
                    " " + x.get(GRB.DoubleAttr.X));
System.out.println(y.get(GRB.StringAttr.VarName) +
                    " " + y.get(GRB.DoubleAttr.X));
System.out.println(z.get(GRB.StringAttr.VarName) +
                    " " + z.get(GRB.DoubleAttr.X));
In C#:
```

When querying or modifying attribute values for an array of constraints or variables, it is generally more efficient to perform the action on the whole array at once. This is quite natural in the C interface, where most of the attribute routines take array arguments. In the C++, C#, and Java interface, you can use the **get** and **set** methods on the Model object to work directly with arrays of attribute values. In the **sudoku** Java example, this is done as follows:

```
double[][][] x = model.get(GRB.DoubleAttr.X, vars);
```

Note that the Python interface doesn't have array query routines. Python is an interpreted language, and overheads associated with queries on individual attributes are a small contributor to overall runtime.

2.3 Modify a model

Examples: diet, feasopt, fixanddive, lpmod, sensitivity, workforce3, workforce4

This section considers model modification. Modification can take many forms, including adding constraints or variables, deleting constraints or variables, modifying constraint and variable attributes, changing constraint coefficients, etc. Here is a sample of some types of model modification.

diet

This example builds a linear model that solves the classic diet problem: to find the minimum cost diet that satisfies a set of daily nutritional requirements. Once the model has been formulated and solved, the example adds an additional constraint to limit the number of servings of dairy products, and solves the model again. Let's focus on the model modification.

Adding constraints to a model that has already been solved is no different from adding constraints when constructing an initial model. In Python, we can introduce a limit of 6 dairy servings through the following constraint:

```
m.addConstr(buy[7] + buy[8] <= 6, "limit_dairy")</pre>
```

For linear models, the previously computed solution can be used as an efficient warm start for the modified model. The Gurobi solver retains the previous solution, so the next optimize call automatically starts from the previous solution.

Ipmod

Changing a variable bound is also straightforward. The 1pmod example changes a single variable bound, then re-solves the model in two different ways. A variable bound can be changed by modifying the UB or LB attribute of the variable. In C:

```
error = GRBsetdblattrelement(model, GRB_DBL_ATTR_UB, var, 0.0);
In Python:
    minVar.ub = 0
```

The model is re-solved simply by calling the optimize method again. For a continuous model, this starts the optimization from the previous solution. To illustrate the difference when solving the model from an initial, unsolved state, the lpmod example calls the reset function. In C:

```
error = GRBresetmodel(model);
In C++, Java, and Python:
   m.reset()
In C#:
   m.Reset()
```

When we call the optimize method after resetting the model, optimization starts from scratch. Although the difference in computation time is insignificant for this tiny example, the warm start can make a big difference for larger models.

fixanddive

The fixanddive example provides another example of bound modification. In this case, we repeatedly modify a set of variable bounds, utilizing warm starts each time. In C, variables are fixed as follows:

```
for (j = 0; j < nfix; ++j)
{
   fixval = floor(fractional[j].X + 0.5);
   error = GRBsetdblattrelement(model, "LB", fractional[j].index, fixval);
   if (error) goto QUIT;
   error = GRBsetdblattrelement(model, "UB", fractional[j].index, fixval);
   if (error) goto QUIT;
}
In Python, they are fixed as follows:
   for i in range(nfix):
        v = fractional[i]
        fixval = int(v.x + 0.5)
        v.lb = fixval
        v.ub = fixval</pre>
```

Again, the subsequent call to optimize starts from the previous solution.

sensitivity

The sensitivity example computes the amount by which the optimal objective changes if each binary variable is fixed at either 0 or 1. For each binary variable, the example creates and solves a copy of the model with new upper and lower bounds. This example is a MIP, so Gurobi can not make use of advanced start information. As a result, the model is solved from scratch after each bound modification.

feasopt

The last modification example we consider is feasopt, which adds variables to existing constraints and also changes the optimization objective. Setting the objective to zero is straightforward: simply call setObjective with a zero argument:

```
m.setObjective(0)
```

Adding new variables is somewhat more complex. In the example, we want to add artificial variable(s) to each constraint in order to allow the constraint to be relaxed. We use two artificial variables for equality constraints and one for all other constraints. The Python code for adding a single artificial variable to constraint c is:

```
feasModel.addVar(obj=1.0, name="ArtP_" + c.Constrname, column=Column([1], [c]))
```

We use the column argument of the addVar method to specify the set of constraints in which the new variable participates, as well as the associated coefficients. In this example, the new variable only participates in the constraint to be relaxed. Default values are used here for all variables attributes except the objective and the variable name.

2.4 Change parameters

Examples: callback, fixanddive, lp, lpmethod, mip2, params, sensitivity

This section illustrates the use of Gurobi parameters. Example params reads a MIP model from a file, then solves the model using four different values of the MIPFocus parameter, running for five seconds per value (MIPFocus chooses the high-level strategy that the MIP solver uses to solve the problem). It then chooses the parameter value that produced the smallest MIP gap, and continues solving the model until it achieves optimality.

The mechanics of setting a parameter are quite simple. To set the MIPFocus parameter in C, do the following:

```
GRBsetintparam(GRBgetenv(model), GRB_INT_PAR_MIPFOCUS, i);
In C++:
  model.getEnv().set(GRB_IntParam_MIPFocus, i);
In Java:
  model.getEnv().set(GRB.IntParam.MIPFocus, i);
In C#:
  model.GetEnv().Set(GRB.IntParam.MIPFocus, i);
```

In Python:

```
model.params.MIPFocus = i
```

Note how parameter settings affect the behavior of the different models. When we set the TimeLimit parameter on the base model, then make a copy of that model, the parameter setting is carried over to the copy. The copy gets its own environment that is a copy of the original. When we set the MIPFocus parameter on the copy, that parameter change has no effect on the other copies, nor on the original model.

2.5 Automated Parameter Tuning

Example: tune

The next example we consider is **tune**, which demonstrates the use of our automated parameter tuning tool. This tool searches for parameter settings that improve performance on a model. While you would typically invoke the tool through the command line, using our **grbtune** program, it can also be invoked from our APIs. We'll provide only a cursory description of the tool here. We recommend that you consult the *Parameter Tuning Tool* section of the Gurobi Reference Manual for more precise details.

Our tuning example demonstrates a typical use of the tuning tool. You would start by invoking the tool on a model. In C:

```
error = GRBtunemodel(model);
In Java:
  model.tune();
```

This routine solves the model multiple times, with different parameter settings, to find settings that improve performance.

Once tuning is complete, you would then use GetTuneResult to retrieve the result. In C:

```
error = GRBgettuneresult(model, 0);
In Java:
  model.getTuneResult(0);
```

The numerical argument indicates which tuning result to retrieve (0 is the best result, 1 is the second-best, etc.). This routine loads the requested parameter set into the environment associated with the argument model.

Once the tune parameter settings have been loaded into the model, you can then call <code>Optimize</code> to use these parameters to solve the model, or you can call <code>Write</code> to write these parameters to a .prm file.

2.6 Diagnose and cope with infeasibility

Examples: feasopt, lp, workforce1, workforce2, workforce3, workforce4

When solving optimization models, there are some situations where the specified constraints cannot be satisfied. When this happens, you often need to either identify and repair the root cause

of the infeasibility, or alternatively find a set of constraints to relax in order to obtain a feasible model. The workforce1, workforce2, and workforce3 illustrate these different strategies.

Starting with the simplest of the three examples, workforce1 formulates a simple workforce scheduling model and solves it. If the model is infeasible, it computes an Irreducible Inconsistent Subsystem (IIS). The user can then inspect this information to understand and hopefully address the source of the infeasibility in the model.

Example workforce2 is similar, except that if the model is infeasible, the example repeatedly identifies an IIS and removes one of the associated constraints from the model until the model becomes feasible. Note that it is sufficient to remove one constraint from the IIS to address that source of infeasibility, but that one IIS may not capture all sources of infeasibility. It is therefore necessary to repeat the process until the model is feasible.

Example workforce3 takes a different approach to addressing infeasibility. Rather than identifying and removing IIS members, it allows the constraints of the model to be relaxed. Like the feasopt example, an artificial variable is added to each constraint. The example sets the objective on the original variables to zero, and then solves a model that minimizes the total magnitude of the constraint relaxation.

The feasopt example demonstrates another approach to relaxing an infeasible model. It computes a *feasibility relaxation* for the infeasible model. A feasibility relaxation is a model that, when solved, minimizes the amount by which the solution violates the bounds and linear constraints of the original model. This method is invoked as follows:

```
In C:
```

The arguments to this method select the objective function for the relaxed model, the specific set of bounds and constraints that are allowed to be relaxed, and the penalties for relaxing specific bounds and constraints.

2.7 MIP starts

Example: facility

A MIP modeler often knows how to compute a feasible solution to their problem. In cases where the MIP solver is slow in finding an initial feasible solution, it can helpful for the modeler to provide a feasible solution along with the model itself. This is done through the Start attribute on the variables. This is illustrated in the facility example.

The facility example solves a simple facility location problem. The model contains a set of warehouses, and a set of plants that produce the products required in the warehouses. Each plant has a maximum production capacity and a fixed operating cost. Additionally, there is a cost associated with shipping products from a plant to a warehouse. The goal is to decide which plants should satisfy the demand for the product, given the associated capacities and costs.

The example uses a simple heuristic for choosing an initial solution: it closes the plant with the highest fixed cost. The associated solution may not be optimal, but it could produce a reasonable starting solution for the MIP optimization. The MIP start is passed to the MIP solver by setting the Start attribute before the optimization begins. In C, we set the start attribute to open all plants using the following code:

```
for (p = 0; p < nPlants; ++p)
{
   error = GRBsetdblattrelement(model, "Start", opencol(p), 1.0);
   if (error) goto QUIT;
}
In Python:
   for p in range(nPlants):
      open[p].start = 1.0</pre>
```

When you run the example, the MIP solver reports that the start produced a feasible initial solution:

Loaded MIP start with objective 210500

This initial solution turns out to be optimal for the sample data. Although the computation difference is insignificant for this tiny example, providing a good starting solution can sometimes help for more difficult models.

Note that the MIP start in this example only specifies values for some of the variables – the variables that determine which plants to leave open and which plants to close. The Gurobi MIP solve uses whatever start information is provided to try to construct a complete solution.

2.8 Model-Data Separation in Python

Examples: diet2.py, diet3.py, diet4.py

When building an optimization model in a modeling language, it is typical to separate the optimization model itself from the data used to create an instance of the model. These two model ingredients are often stored in completely different files. We show how a similar result can be achieved in our Python interface with our diet2.py, diet3.py, and diet4.py examples. These examples illustrate alternate approaches to providing data to the optimization model: diet2.py embeds the data in the source file, diet3.py reads the data from an SQL database (using the Python sqlite3 package), and diet4.py reads the data from an Excel spreadsheet (using the Python xlrd package). dietmodel.py contains the optimization model itself. The same model is used by diet2.py, diet3.py, and diet4.py.

The key construct that enables the separation of the model from the data is the Python module. A module is simply a set of functions and variables, stored in a file. You import a module into a program using the import statement. diet2.py, diet3.py, and diet4.py all populate a set of variables, and then pass them to the solve function of the dietmodel module using the following pair of statements:

```
import dietmodel
dietmodel.solve(categories, minNutrition, maxNutrition, foods, cost, nutritionValues)
```

The first statement imports the dietmodel module, which must be stored in file dietmodel.py in the current directory. The second passes the model data to the solve function in the newly imported module.

2.9 Callbacks

Example: callback

The final example we consider is callback, which demonstrates the use of Gurobi callbacks. Callbacks are used to report on the progress of the optimization or to modify the behavior of the Gurobi solver. To use a callback, the user writes a routine that implements the desired behavior. The routine is passed to the Gurobi optimizer when optimization begins, and the routine is called regularly during the optimization process. One argument of the user routine is a where value, which indicates from where in the optimization process the callback is invoked. The user callback routine can call the optimization library to query certain values. We refer the reader to the callback section of the Gurobi Reference Manual for more precise details.

Our callback example implements a simple termination scheme: the user passes a node count into the callback, and the callback asks the optimizer to terminate when that node count is reached. This is implemented in C as follows:

```
GRBcbget(cbdata, where, GRB_CB_MIP_NODCNT, &nodecnt);
if (nodecnt > limit)
   GRBterminate(model);

In Python, this is implemented as:
  nodecnt = model.cbGet(GRB.callback.MIP_NODCNT)
  if nodecnt > model._mynodelimit:
    model.terminate()
```

To obtain the current node count, the user routine calls the cbget routine (the GRBcbget function in C, or the cbGet method on the model object in C++, C#, Java, and Python).

Our callback example also prints progress information. In C:

```
GRBcbget(cbdata, where, GRB_CB_MIP_NODCNT, &nodecnt);
if (nodecnt - mydata->lastmsg >= 100) {
    ...
    printf("%7.0f ...", nodecnt, ...);
}
```

In Python:

```
nodecnt = model.cbGet(GRB.callback.MIP_NODCNT)
if nodecnt % 100 == 0:
    print int(nodecnt), ...
```

Again, the user callback calls the cbGet routine to query the state of the optimization.

We have included source code for all of the distributed examples in this section. The identical example source code is included in the examples directory in the Gurobi distribution.

3.1 C Examples

This section includes source code for all of the Gurobi C examples. The same source code can be found in the examples/c directory of the Gurobi distribution.

callback c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP or a MIP from a file, sets a callback
   to monitor the optimization progress and to output some progress
   information to the screen and to a log file. If it is a MIP and 10%
   gap is reached, then it aborts */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
/* Define structure to pass my data to the callback function */
struct callback_data {
  double lastnode;
  double lastiter;
 FILE
         *logfile;
  double *solution;
};
int __stdcall
mycallback(GRBmodel *model,
           void
                    *cbdata,
                     where,
           int
                    *usrdata)
           void
  struct callback_data *mydata = (struct callback_data *) usrdata;
  char *msg;
```

```
if (where == GRB_CB_POLLING) {
  /* Ignore polling callback */
} else if (where == GRB_CB_MESSAGE) {
  GRBcbget(cbdata, where, GRB_CB_MSG_STRING, &msg);
  fprintf(mydata->logfile, "%s", msg);
} else if (where == GRB_CB_SIMPLEX) {
  double pinf, dinf, obj, itrcnt;
  int
         ispert;
  char
         ch;
  GRBcbget(cbdata, where, GRB_CB_SPX_ITRCNT, &itrcnt);
  if (itrcnt - mydata->lastiter >= 100) {
    mydata->lastiter = itrcnt;
    GRBcbget(cbdata, where, GRB_CB_SPX_ISPERT, &ispert);
    GRBcbget(cbdata, where, GRB_CB_SPX_OBJVAL, &obj);
    GRBcbget(cbdata, where, GRB_CB_SPX_PRIMINF, &pinf);
    GRBcbget(cbdata, where, GRB_CB_SPX_DUALINF, &dinf);
            (ispert == 0) ch = ', ';
    else if (ispert == 1) ch = 'S';
                          ch = 'P':
    else
    printf("%7.0f %14.7e%c %13.6e %13.6e\n", itrcnt, obj, ch, pinf, dinf);
} else if (where == GRB_CB_PRESOLVE) {
  int cdels, rdels;
  GRBcbget(cbdata, where, GRB_CB_PRE_COLDEL, &cdels);
  GRBcbget(cbdata, where, GRB_CB_PRE_ROWDEL, &rdels);
  if (cdels || rdels) {
    printf("%7d columns and %7d rows are removed\n", cdels, rdels);
} else if (where == GRB_CB_MIP) {
  double objbst, objbnd, nodecnt, actnodes, itrcnt;
         cutcnt, solcnt;
  GRBcbget(cbdata, where, GRB_CB_MIP_NODCNT, &nodecnt);
  if (nodecnt - mydata->lastnode >= 100) {
    mydata->lastnode = nodecnt;
    GRBcbget(cbdata, where, GRB_CB_MIP_OBJBST, &objbst);
    GRBcbget(cbdata, where, GRB_CB_MIP_OBJBND, &objbnd);
    /* if gap is small, then quit */
    if (fabs(objbst - objbnd) < 0.1 * (1.0 + fabs(objbst))) {
      printf("Stop early - 10%% gap achieved\n");
      GRBterminate(model);
    }
    GRBcbget(cbdata, where, GRB_CB_MIP_NODLFT, &actnodes);
    GRBcbget(cbdata, where, GRB_CB_MIP_ITRCNT, &itrcnt);
    GRBcbget(cbdata, where, GRB_CB_MIP_SOLCNT, &solcnt);
```

```
GRBcbget(cbdata, where, GRB_CB_MIP_CUTCNT, &cutcnt);
     printf("%7.0f %7.0f %8.0f %13.6e %13.6e %7d %7d\n",
             nodecnt, actnodes, itrcnt, objbst, objbnd, solcnt, cutcnt);
  } else if (where == GRB_CB_MIPSOL) {
    double obj, nodecnt;
    int solcnt;
    GRBcbget(cbdata, where, GRB_CB_MIPSOL_OBJ, &obj);
    GRBcbget(cbdata, where, GRB_CB_MIPSOL_NODCNT, &nodecnt);
    GRBcbget(cbdata, where, GRB_CB_MIPSOL_SOLCNT, &solcnt);
    GRBcbget(cbdata, where, GRB_CB_MIPSOL_SOL, mydata->solution);
    printf("**** New solution at node %.0f, obj %g, sol %d, x[0] = %.2f **** n",
           nodecnt, obj, solcnt, mydata->solution[0]);
  } else if (where == GRB_CB_BARRIER) {
    double primobj, dualobj, priminf, dualinf, compl;
    int iter;
    GRBcbget(cbdata, where, GRB_CB_BARRIER_ITRCNT,
    GRBcbget(cbdata, where, GRB_CB_BARRIER_PRIMOBJ, &primobj);
    GRBcbget(cbdata, where, GRB_CB_BARRIER_DUALOBJ, &dualobj);
    GRBcbget(cbdata, where, GRB_CB_BARRIER_PRIMINF, &priminf);
    GRBcbget(cbdata, where, GRB_CB_BARRIER_DUALINF, &dualinf);
    GRBcbget(cbdata, where, GRB_CB_BARRIER_COMPL,
                                                    &compl);
    printf("Barrier iter: %d %.4e %.4e %.4e %.4e %.4e \n",
           iter, primobj, dualobj, priminf, dualinf, compl);
  }
 return 0;
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env
                = NULL;
  GRBmodel *model = NULL;
  int
            error = 0;
  int
            vars, optimstatus;
  double
            objval;
  struct callback_data mydata;
 mydata.lastnode = -GRB_INFINITY;
 mydata.lastiter = -GRB_INFINITY;
 mydata.logfile = NULL;
 mydata.solution = NULL;
```

}

```
if (argc < 2) {
  fprintf(stderr, "Usage: callback_c filename\n");
  goto QUIT;
}
mydata.logfile = fopen("cb.log", "w");
if (!mydata.logfile) {
  fprintf(stderr, "Cannot open cb.log for callback message\n");
  goto QUIT;
}
/* Create environment */
error = GRBloadenv(&env, NULL);
if (error) goto QUIT;
/* Turn off display */
error = GRBsetintparam(env, GRB_INT_PAR_OUTPUTFLAG, 0);
if (error) goto QUIT;
/* Read model from file */
error = GRBreadmodel(env, argv[1], &model);
if (error) goto QUIT;
/* Allocate space for solution */
error = GRBgetintattr(model, GRB_INT_ATTR_NUMVARS, &vars);
if (error) goto QUIT;
mydata.solution = malloc(vars*sizeof(double));
if (mydata.solution == NULL) {
  fprintf(stderr, "Failed to allocate memory\n");
  exit(1);
}
/* Set callback function */
error = GRBsetcallbackfunc(model, mycallback, (void *) &mydata);
if (error) goto QUIT;
/* Solve model */
```

```
error = GRBoptimize(model);
  if (error) goto QUIT;
  /* Capture solution information */
  error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
  if (error) goto QUIT;
  error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
  if (error) goto QUIT;
 printf("\nOptimization complete\n");
  if (optimstatus == GRB_OPTIMAL)
   printf("Optimal objective: %.4e\n", objval);
  else if (optimstatus == GRB_INF_OR_UNBD)
   printf("Model is infeasible or unbounded\n");
    printf("Optimization was stopped early\n");
 printf("\n");
QUIT:
 /* Error reporting */
  if (error) {
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
 /* Close file */
  if (mydata.logfile)
   fclose(mydata.logfile);
  /* Free solution */
  if (mydata.solution)
    free(mydata.solution);
  /* Free model */
 GRBfreemodel(model);
  /* Free environment */
```

```
GRBfreeenv(env);
return 0;
}
```

```
dense c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                 x + y + x^2 + x*y + y^2 + y*z + z^2
     subject to x + 2y + 3z >= 4
                 x + y
                               >= 1
  The example illustrates the use of dense matrices to store A and Q
   (and dense vectors for the other relevant data). We don't recommend
  that you use dense matrices, but this example may be helpful if you
  already have your data in this format.
*/
#include <stdlib.h>
#include <stdio.h>
#include "gurobi_c.h"
/*
  Solve an LP/QP/MILP/MIQP represented using dense matrices. This
 routine assumes that A and Q are both stored in row-major order.
 It returns 1 if the optimization succeeds. When successful,
  it returns the optimal objective value in 'objvalP', and the
  optimal solution vector in 'solution'.
*/
static int
dense_optimize(GRBenv *env,
               int
                      rows,
               int
                       cols.
                             /* linear portion of objective function */
               double *c,
               double *Q,
                             /* quadratic portion of objective function */
               double *A,
                             /* constraint matrix */
                      *sense, /* constraint senses */
               double *rhs, /* RHS vector */
                             /* variable lower bounds */
               double *lb,
               double *ub,
                             /* variable upper bounds */
                      *vtype, /* variable types (continuous, binary, etc.) */
               double *solution,
               double *objvalP)
{
  GRBmodel *model = NULL;
  int
            i, j, optimstatus;
            error = 0;
  int
```

```
success = 0;
int
/* Create an empty model */
error = GRBnewmodel(env, &model, "dense", cols, c, lb, ub, vtype, NULL);
if (error) goto QUIT;
error = GRBaddconstrs(model, rows, 0, NULL, NULL, NULL, sense, rhs, NULL);
if (error) goto QUIT;
/* Integrate new rows and columns */
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* Populate A matrix */
for (i = 0; i < rows; i++) {
  for (j = 0; j < cols; j++) {
    if (A[i*cols+j] != 0) {
      error = GRBchgcoeffs(model, 1, &i, &j, &A[i*cols+j]);
      if (error) goto QUIT;
    }
  }
}
/* Populate Q matrix */
if (Q) {
  for (i = 0; i < cols; i++) {
    for (j = 0; j < cols; j++) {
      if (Q[i*cols+j] != 0) {
        error = GRBaddqpterms(model, 1, &i, &j, &Q[i*cols+j]);
        if (error) goto QUIT;
      }
    }
  }
}
/* Integrate new coefficients */
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* Write model to 'dense.lp' */
```

```
error = GRBwrite(model, "dense.lp");
  if (error) goto QUIT;
  /* Optimize model */
  error = GRBoptimize(model);
  if (error) goto QUIT;
  /* Capture solution information */
  error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
  if (error) goto QUIT;
  if (optimstatus == GRB_OPTIMAL) {
    error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, objvalP);
    if (error) goto QUIT;
    error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, cols, solution);
    if (error) goto QUIT;
    success = 1;
  }
QUIT:
  /* Error reporting */
  if (error) {
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  /* Free model */
  GRBfreemodel(model);
  return success;
}
int
main(int
           argc,
     char *argv[])
{
```

```
GRBenv *env
                  = NULL;
  int
          error
                  = 0;
                  = \{1, 1, 0\};
  double
          c[]
  double
          Q[3][3] = \{\{1, 1, 0\}, \{0, 1, 1\}, \{0, 0, 1\}\};
          A[2][3] = \{\{1, 2, 3\}, \{1, 1, 0\}\};
          sense[] = {'>', '>'};
  char
  double rhs[]
                  = \{4, 1\};
                  = \{0, 0, 0\};
  double lb[]
  double sol[3];
  int
          solved;
  double objval;
  /* Create environment */
  error = GRBloadenv(&env, "dense.log");
  if (error) goto QUIT;
  /* Solve the model */
  solved = dense_optimize(env, 2, 3, c, &Q[0][0], &A[0][0], sense, rhs, lb,
                           NULL, NULL, sol, &objval);
  if (solved)
    printf("Solved: x=\%.4f, y=\%.4f, z=\%.4f n", sol[0], sol[1], sol[2]);
QUIT:
  /* Free environment */
  GRBfreeenv(env);
  return 0;
```

}

```
diet c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve the classic diet model, showing how to add constraints
   to an existing model. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
int printSolution(GRBmodel* model, int nCategories, int nFoods);
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env
                = NULL;
  GRBmodel *model = NULL;
  int
            error = 0;
  int
           i, j;
  int
           *cbeg, *cind, idx;
           *cval, *rhs;
  double
  char
           *sense;
  /* Nutrition guidelines, based on
     USDA Dietary Guidelines for Americans, 2005
     http://www.health.gov/DietaryGuidelines/dga2005/ */
  const int nCategories = 4;
  char *Categories[] =
    { "calories", "protein", "fat", "sodium" };
  double minNutrition[] = { 1800, 91, 0, 0 };
  double maxNutrition[] = { 2200, GRB_INFINITY, 65, 1779 };
  /* Set of foods */
  const int nFoods = 9;
  char* Foods[] =
    { "hamburger", "chicken", "hot dog", "fries",
      "macaroni", "pizza", "salad", "milk", "ice cream" };
    { 2.49, 2.89, 1.50, 1.89, 2.09, 1.99, 2.49, 0.89, 1.59 };
  /* Nutrition values for the foods */
```

```
double nutritionValues[][4] = {
                                 { 410, 24, 26, 730 },
                                 { 420, 32, 10, 1190 },
                                 { 560, 20, 32, 1800 },
                                 { 380, 4, 19, 270 },
                                 { 320, 12, 10, 930 },
                                 { 320, 15, 12, 820 },
                                 { 320, 31, 12, 1230 },
                                 { 100, 8, 2.5, 125 },
                                 { 330, 8, 10, 180 }
                              };
/* Create environment */
error = GRBloadenv(&env, "diet.log");
if (error) goto QUIT;
/* Create initial model */
error = GRBnewmodel(env, &model, "diet", nFoods + nCategories,
                    NULL, NULL, NULL, NULL, NULL);
if (error) goto QUIT;
/* Initialize decision variables for the foods to buy */
for (j = 0; j < nFoods; ++j)
{
  error = GRBsetdblattrelement(model, "Obj", j, cost[j]);
  if (error) goto QUIT;
  error = GRBsetstrattrelement(model, "VarName", j, Foods[j]);
  if (error) goto QUIT;
}
/* Initialize decision variables for the nutrition information,
   which we limit via bounds */
for (j = 0; j < nCategories; ++j)</pre>
  error = GRBsetdblattrelement(model, "LB", j + nFoods, minNutrition[j]);
  if (error) goto QUIT;
  error = GRBsetdblattrelement(model, "UB", j + nFoods, maxNutrition[j]);
  if (error) goto QUIT;
  error = GRBsetstrattrelement(model, "VarName", j + nFoods, Categories[j]);
  if (error) goto QUIT;
}
/* The objective is to minimize the costs */
error = GRBsetintattr(model, "ModelSense", 1);
if (error) goto QUIT;
```

```
/* Nutrition constraints */
cbeg = malloc(sizeof(int) * nCategories);
if (!cbeg) goto QUIT;
cind = malloc(sizeof(int) * nCategories * (nFoods + 1));
if (!cind) goto QUIT;
cval = malloc(sizeof(double) * nCategories * (nFoods + 1));
if (!cval) goto QUIT;
rhs = malloc(sizeof(double) * nCategories);
if (!rhs) goto QUIT;
sense = malloc(sizeof(char) * nCategories);
if (!sense) goto QUIT;
idx = 0;
for (i = 0; i < nCategories; ++i)</pre>
  cbeg[i] = idx;
  rhs[i] = 0.0;
  sense[i] = GRB_EQUAL;
  for (j = 0; j < nFoods; ++j)
    cind[idx] = j;
    cval[idx++] = nutritionValues[j][i];
  cind[idx] = nFoods + i;
  cval[idx++] = -1.0;
}
error = GRBaddconstrs(model, nCategories, idx, cbeg, cind, cval, sense,
                      rhs, Categories);
if (error) goto QUIT;
/* Solve */
error = GRBoptimize(model);
if (error) goto QUIT;
error = printSolution(model, nCategories, nFoods);
if (error) goto QUIT;
printf("\nAdding constraint: at most 6 servings of dairy\n");
cind[0] = 7;
cval[0] = 1.0;
cind[1] = 8;
cval[1] = 1.0;
error = GRBaddconstr(model, 2, cind, cval, GRB_LESS_EQUAL, 6.0,
                     "limit_dairy");
if (error) goto QUIT;
```

```
/* Solve */
  error = GRBoptimize(model);
  if (error) goto QUIT;
  error = printSolution(model, nCategories, nFoods);
  if (error) goto QUIT;
QUIT:
  /* Error reporting */
  if (error)
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free data */
  free(cbeg);
  free(cind);
  free(cval);
  free(rhs);
  free(sense);
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
  return 0;
}
int printSolution(GRBmodel* model, int nCategories, int nFoods)
  int error, status, i, j;
  double obj, x;
  char* vname;
  error = GRBgetintattr(model, "Status", &status);
```

```
if (error) return error;
if (status == GRB_OPTIMAL)
  error = GRBgetdblattr(model, "ObjVal", &obj);
  if (error) return error;
  printf("\nCost: %f\n\nBuy:\n", obj);
  for (j = 0; j < nFoods; ++j)
    error = GRBgetdblattrelement(model, "X", j, &x);
    if (error) return error;
    if (x > 0.0001)
    {
      error = GRBgetstrattrelement(model, "VarName", j, &vname);
      if (error) return error;
      printf("%s %f\n", vname, x);
    }
  }
  printf("\nNutrition:\n");
  for (i = 0; i < nCategories; ++i)</pre>
    error = GRBgetdblattrelement(model, "X", i + nFoods, &x);
    if (error) return error;
    error = GRBgetstrattrelement(model, "VarName", i + nFoods, &vname);
    if (error) return error;
    printf("%s %f\n", vname, x);
  }
}
else
  printf("No solution\n");
return 0;
```

}

facility c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Facility location: a company currently ships its product from 5 plants
  to 4 warehouses. It is considering closing some plants to reduce
  costs. What plant(s) should the company close, in order to minimize
  transportation and fixed costs?
  Based on an example from Frontline Systems:
  http://www.solver.com/disfacility.htm
  Used with permission.
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
#define opencol(p)
#define transportcol(w,p) nPlants*(w+1)+p
#define MAXSTR
                           128
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env = NULL;
  GRBmodel *model = NULL;
  int
          error = 0;
  int
           p, w, col;
           *cbeg = NULL;
  int
  int
          *cind = NULL;
           idx, rowct;
  int
  double
          *cval = NULL;
  double
           *rhs = NULL;
  char
           *sense = NULL;
  char
           vname[MAXSTR];
  int
           cnamect = 0;
  char
         **cname = NULL;
  double
           maxFixed = -GRB_INFINITY, sol, obj;
  /* Number of plants and warehouses */
  const int nPlants = 5;
  const int nWarehouses = 4;
```

```
/* Warehouse demand in thousands of units */
double Demand[] = { 15, 18, 14, 20 };
/* Plant capacity in thousands of units */
double Capacity[] = { 20, 22, 17, 19, 18 };
/* Fixed costs for each plant */
double FixedCosts[] =
  { 12000, 15000, 17000, 13000, 16000 };
// Transportation costs per thousand units
double TransCosts[4][5] = {
                            { 4000, 2000, 3000, 2500, 4500 },
                            { 2500, 2600, 3400, 3000, 4000 },
                            { 1200, 1800, 2600, 4100, 3000 },
                            { 2200, 2600, 3100, 3700, 3200 }
                          };
/* Create environment */
error = GRBloadenv(&env, "facility.log");
if (error) goto QUIT;
/* Create initial model */
error = GRBnewmodel(env, &model, "facility", nPlants * (nWarehouses + 1),
                    NULL, NULL, NULL, NULL, NULL);
if (error) goto QUIT;
/* Initialize decision variables for plant open variables */
for (p = 0; p < nPlants; ++p)
{
  col = opencol(p);
  error = GRBsetcharattrelement(model, "VType", col, GRB_BINARY);
  if (error) goto QUIT;
  error = GRBsetdblattrelement(model, "Obj", col, FixedCosts[p]);
  if (error) goto QUIT;
  sprintf(vname, "Open%i", p);
  error = GRBsetstrattrelement(model, "VarName", col, vname);
  if (error) goto QUIT;
}
/* Initialize decision variables for transportation decision variables:
   how much to transport from a plant p to a warehouse w */
for (w = 0; w < nWarehouses; ++w)</pre>
{
```

```
for (p = 0; p < nPlants; ++p)
    col = transportcol(w, p);
    error = GRBsetdblattrelement(model, "Obj", col, TransCosts[w][p]);
    if (error) goto QUIT;
    sprintf(vname, "Trans%i.%i", p, w);
    error = GRBsetstrattrelement(model, "VarName", col, vname);
    if (error) goto QUIT;
  }
}
/* The objective is to minimize the total fixed and variable costs */
error = GRBsetintattr(model, "ModelSense", 1);
if (error) goto QUIT;
/* Make space for constraint data */
rowct = (nPlants > nWarehouses) ? nPlants : nWarehouses;
cbeg = malloc(sizeof(int) * rowct);
if (!cbeg) goto QUIT;
cind = malloc(sizeof(int) * (nPlants * (nWarehouses + 1)));
if (!cind) goto QUIT;
cval = malloc(sizeof(double) * (nPlants * (nWarehouses + 1)));
if (!cval) goto QUIT;
rhs = malloc(sizeof(double) * rowct);
if (!rhs) goto QUIT;
sense = malloc(sizeof(char) * rowct);
if (!sense) goto QUIT;
cname = calloc(rowct, sizeof(char*));
if (!cname) goto QUIT;
/* Production constraints
   Note that the limit sets the production to zero if
   the plant is closed */
idx = 0;
for (p = 0; p < nPlants; ++p)
  cbeg[p] = idx;
  rhs[p] = 0.0;
  sense[p] = GRB_LESS_EQUAL;
  cname[p] = malloc(sizeof(char) * MAXSTR);
  if (!cname[p]) goto QUIT;
  cnamect++;
  sprintf(cname[p], "Capacity%i", p);
  for (w = 0; w < nWarehouses; ++w)
  {
```

```
cind[idx] = transportcol(w, p);
    cval[idx++] = 1.0;
  cind[idx] = opencol(p);
  cval[idx++] = -Capacity[p];
}
error = GRBaddconstrs(model, nPlants, idx, cbeg, cind, cval, sense,
                      rhs, cname);
if (error) goto QUIT;
/* Demand constraints */
idx = 0;
for (w = 0; w < nWarehouses; ++w)
  cbeg[w] = idx;
  sense[w] = GRB_EQUAL;
  sprintf(cname[w], "Demand%i", w);
  for (p = 0; p < nPlants; ++p)
  {
    cind[idx] = transportcol(w, p);
    cval[idx++] = 1.0;
}
error = GRBaddconstrs(model, nWarehouses, idx, cbeg, cind, cval, sense,
                      Demand, cname);
if (error) goto QUIT;
/* Guess at the starting point: close the plant with the highest
   fixed costs; open all others */
/* First, open all plants */
for (p = 0; p < nPlants; ++p)
{
  error = GRBsetdblattrelement(model, "Start", opencol(p), 1.0);
  if (error) goto QUIT;
}
/* Now close the plant with the highest fixed cost */
printf("Initial guess:\n");
for (p = 0; p < nPlants; ++p)
  if (FixedCosts[p] > maxFixed)
    maxFixed = FixedCosts[p];
```

```
}
for (p = 0; p < nPlants; ++p)
  if (FixedCosts[p] == maxFixed)
  {
    error = GRBsetdblattrelement(model, "Start", opencol(p), 0.0);
    if (error) goto QUIT;
    printf("Closing plant %i\n\n", p);
    break;
  }
}
/* Use barrier to solve root relaxation */
error = GRBsetintparam(GRBgetenv(model),
                       GRB_INT_PAR_METHOD,
                       GRB_METHOD_BARRIER);
if (error) goto QUIT;
/* Solve */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Print solution */
error = GRBgetdblattr(model, "ObjVal", &obj);
if (error) goto QUIT;
printf("\nTOTAL COSTS: %f\n", obj);
printf("SOLUTION:\n");
for (p = 0; p < nPlants; ++p)
  error = GRBgetdblattrelement(model, "X", opencol(p), &sol);
  if (error) goto QUIT;
  if (sol == 1.0)
    printf("Plant %i open:\n", p);
    for (w = 0; w < nWarehouses; ++w)
      error = GRBgetdblattrelement(model, "X", transportcol(w, p), &sol);
      if (error) goto QUIT;
      if (sol > 0.0001)
        printf(" Transport %f units to warehouse %i\n", sol, w);
      }
    }
  }
  else
```

```
printf("Plant %i closed!\n", p);
    }
  }
QUIT:
  /* Error reporting */
  if (error)
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  /* Free data */
  free(cbeg);
  free(cind);
  free(cval);
  free(rhs);
  free(sense);
  for (p = 0; p < cnamect; ++p) {
    free(cname[p]);
  free(cname);
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
 return 0;
}
```

feasopt c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, adds artificial
   variables to each constraint, and then minimizes the sum of the
   artificial variables. A solution with objective zero corresponds
   to a feasible solution to the input model.
   We can also use FeasRelax feature to do it. In this example, we
   use minrelax=1, i.e. optimizing the returned model finds a solution
   that minimizes the original objective, but only from among those
   solutions that minimize the sum of the artificial variables. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
 GRBenv
                      = NULL;
           *env
                      = NULL;
  GRBmodel *model
  GRBmodel *feasmodel = NULL;
  double *rhspen
                        = NULL;
            error = 0;
  int
  int
            i, j;
  int
           numvars, numconstrs;
  char
            sense;
  int
            vind[1];
  double
            vval[1];
  double
            feasobj;
            *cname, *vname;
  char
  if (argc < 2)
   fprintf(stderr, "Usage: feasopt_c filename\n");
    exit(1);
  }
  error = GRBloadenv(&env, "feasopt.log");
  if (error) goto QUIT;
  error = GRBreadmodel(env, argv[1], &model);
```

```
if (error) goto QUIT;
/* Create a copy to use FeasRelax feature later */
feasmodel = GRBcopymodel(model);
if (error) goto QUIT;
/* clear objective */
error = GRBgetintattr(model, "NumVars", &numvars);
if (error) goto QUIT;
for (j = 0; j < numvars; ++j)
{
  error = GRBsetdblattrelement(model, "Obj", j, 0.0);
  if (error) goto QUIT;
/* add slack variables */
error = GRBgetintattr(model, "NumConstrs", &numconstrs);
if (error) goto QUIT;
for (i = 0; i < numconstrs; ++i)</pre>
  error = GRBgetcharattrelement(model, "Sense", i, &sense);
  if (error) goto QUIT;
  if (sense != '>')
  ₹
    error = GRBgetstrattrelement(model, "ConstrName", i, &cname);
    if (error) goto QUIT;
    vname = malloc(sizeof(char) * (6 + strlen(cname)));
    if (!vname) goto QUIT;
    strcpy(vname, "ArtN_");
    strcat(vname, cname);
    vind[0] = i;
    vval[0] = -1.0;
    error = GRBaddvar(model, 1, vind, vval, 1.0, 0.0, GRB_INFINITY,
                      GRB_CONTINUOUS, vname);
    if (error) goto QUIT;
    free(vname);
  if (sense != '<')
    error = GRBgetstrattrelement(model, "ConstrName", i, &cname);
    if (error) goto QUIT;
    vname = malloc(sizeof(char) * (6 + strlen(cname)));
    if (!vname) goto QUIT;
    strcpy(vname, "ArtP_");
```

```
strcat(vname, cname);
    vind[0] = i;
    vval[0] = 1.0;
    error = GRBaddvar(model, 1, vind, vval, 1.0, 0.0, GRB_INFINITY,
                      GRB_CONTINUOUS, vname);
    if (error) goto QUIT;
    free(vname);
}
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* optimize modified model */
error = GRBwrite(model, "feasopt.lp");
if (error) goto QUIT;
error = GRBoptimize(model);
if (error) goto QUIT;
/* Use FeasRelax feature */
rhspen = (double *) malloc(numconstrs*sizeof(double));
if (rhspen == NULL) {
  printf("ERROR: out of memory\n");
  goto QUIT;
}
/* set penalties for artificial variables */
for (i = 0; i < numconstrs; i++) rhspen[i] = 1;</pre>
/* create a FeasRelax model with the original objective recovered
   and enforcement on minimum of aretificial variables */
error = GRBfeasrelax(feasmodel, GRB_FEASRELAX_LINEAR, 1,
                     NULL, NULL, rhspen, &feasobj);
if (error) goto QUIT;
/* optimize FeasRelax model */
error = GRBwrite(feasmodel, "feasopt1.lp");
if (error) goto QUIT;
error = GRBoptimize(feasmodel);
if (error) goto QUIT;
```

QUIT:

```
/* Error reporting */
if (error)
{
   printf("ERROR: %s\n", GRBgeterrormsg(env));
   exit(1);
}

/* Free models, env and etc. */
if (rhspen) free(rhspen);

GRBfreemodel(model);
GRBfreemodel(feasmodel);

GRBfreeenv(env);

return 0;
}
```

fixanddive c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Implement a simple MIP heuristic. Relax the model,
   sort variables based on fractionality, and fix the 25% of
   the fractional variables that are closest to integer variables.
   Repeat until either the relaxation is integer feasible or
   linearly infeasible. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
typedef struct
  int index;
  double X;
}
var_t ;
int vcomp(const void* v1, const void* v2);
int
main(int
           argc,
     char *argv[])
  GRBenv
                  = NULL, *modelenv = NULL;
           *env
 GRBmodel *model = NULL;
           error = 0;
  int
  int
            j, iter, nfix;
  int
           numvars, numintvars, numfractional;
           *intvars = NULL;
  int
  int
            status;
  char
           vtype, *vname;
  double
           sol, obj, fixval;
 var_t
           *fractional = NULL;
  if (argc < 2)
    fprintf(stderr, "Usage: fixanddive_c filename\n");
    exit(1);
  }
```

```
error = GRBloadenv(&env, "fixanddive.log");
if (error) goto QUIT;
/* Read model */
error = GRBreadmodel(env, argv[1], &model);
if (error) goto QUIT;
/* Collect integer variables and relax them */
error = GRBgetintattr(model, "NumVars", &numvars);
if (error) goto QUIT;
error = GRBgetintattr(model, "NumIntVars", &numintvars);
if (error) goto QUIT;
intvars = malloc(sizeof(int) * numintvars);
if (!intvars) goto QUIT;
fractional = malloc(sizeof(var_t) * numintvars);
if (!fractional) goto QUIT;
numfractional = 0;
for (j = 0; j < numvars; j++)
{
  error = GRBgetcharattrelement(model, "VType", j, &vtype);
  if (error) goto QUIT;
  if (vtype != GRB_CONTINUOUS)
    intvars[numfractional++] = j;
    error = GRBsetcharattrelement(model, "VType", j, GRB_CONTINUOUS);
    if (error) goto QUIT;
  }
}
modelenv = GRBgetenv(model);
if (!modelenv) goto QUIT;
error = GRBsetintparam(modelenv, "OutputFlag", 0);
if (error) goto QUIT;
error = GRBoptimize(model);
if (error) goto QUIT;
/* Perform multiple iterations. In each iteration, identify the first
   quartile of integer variables that are closest to an integer value
   in the relaxation, fix them to the nearest integer, and repeat. */
for (iter = 0; iter < 1000; ++iter)
{
  /* create a list of fractional variables, sorted in order of
     increasing distance from the relaxation solution to the nearest
```

```
integer value */
numfractional = 0;
for (j = 0; j < numintvars; ++j)
  error = GRBgetdblattrelement(model, "X", intvars[j], &sol);
  if (error) goto QUIT;
  if (fabs(sol - floor(sol + 0.5)) > 1e-5)
    fractional[numfractional].index = intvars[j];
    fractional[numfractional++].X = sol;
 }
}
error = GRBgetdblattr(model, "ObjVal", &obj);
if (error) goto QUIT;
printf("Iteration %i, obj %f, fractional %i\n",
       iter, obj, numfractional);
if (numfractional == 0)
 printf("Found feasible solution - objective %f\n", obj);
 break;
/* Fix the first quartile to the nearest integer value */
qsort(fractional, numfractional, sizeof(var_t), vcomp);
nfix = numfractional / 4;
nfix = (nfix > 1) ? nfix : 1;
for (j = 0; j < nfix; ++j)
 fixval = floor(fractional[j].X + 0.5);
  error = GRBsetdblattrelement(model, "LB", fractional[j].index, fixval);
  if (error) goto QUIT;
  error = GRBsetdblattrelement(model, "UB", fractional[j].index, fixval);
  if (error) goto QUIT;
  error = GRBgetstrattrelement(model, "VarName",
                               fractional[j].index, &vname);
  if (error) goto QUIT;
 printf(" Fix %s to %f ( rel %f )\n", vname, fixval, fractional[j].X);
}
error = GRBoptimize(model);
if (error) goto QUIT;
```

```
/* Check optimization result */
    error = GRBgetintattr(model, "Status", &status);
    if (error) goto QUIT;
    if (status != GRB_OPTIMAL)
      printf("Relaxation is infeasible\n");
      break;
    }
  }
QUIT:
  /* Error reporting */
  if (error)
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free data */
  free(intvars);
  free(fractional);
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
  return 0;
}
int vcomp(const void* v1, const void* v2)
  double sol1, sol2, frac1, frac2;
  sol1 = fabs(((var_t *)v1)->X);
  sol2 = fabs(((var_t *)v2)->X);
  frac1 = fabs(sol1 - floor(sol1 + 0.5));
```

```
frac2 = fabs(sol2 - floor(sol2 + 0.5));
return (frac1 < frac2) ? -1 : ((frac1 == frac2) ? 0 : 1);
}</pre>
```

```
lp_c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
   If the model is infeasible or unbounded, the example turns off
   presolve and solves the model again. If the model is infeasible,
   the example computes an Irreducible Infeasible Subsystem (IIS),
   and writes it to a file */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
{
  GRBenv
           *masterenv = NULL;
  GRBmodel *model
                      = NULL;
  GRBenv
           *modelenv = NULL;
  int
            error
                      = 0;
  int
            optimstatus;
  double
            objval;
  if (argc < 2) {
    fprintf(stderr, "Usage: lp_c filename\n");
    exit(1);
  }
  /* Create environment */
  error = GRBloadenv(&masterenv, "lp.log");
  if (error) goto QUIT;
  /* Read model from file */
  error = GRBreadmodel(masterenv, argv[1], &model);
  if (error) goto QUIT;
  /* Solve model */
  error = GRBoptimize(model);
```

if (error) goto QUIT;

```
/* Capture solution information */
error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
if (error) goto QUIT;
/* If model is infeasible or unbounded, turn off presolve and resolve */
if (optimstatus == GRB_INF_OR_UNBD) {
 modelenv = GRBgetenv(model);
  if (!modelenv) {
    fprintf(stderr, "Error: could not get model environment\n");
   goto QUIT;
  }
  /* Change parameter on model environment. The model now has
     a copy of the master environment, so changing the master will
     no longer affect the model. */
  error = GRBsetintparam(modelenv, "PRESOLVE", 0);
  if (error) goto QUIT;
  error = GRBoptimize(model);
  if (error) goto QUIT;
  error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
  if (error) goto QUIT;
}
if (optimstatus == GRB_OPTIMAL) {
  error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
  if (error) goto QUIT;
  printf("Optimal objective: %.4e\n\n", objval);
} else if (optimstatus == GRB_INFEASIBLE) {
  printf("Model is infeasible\n\n");
  error = GRBcomputeIIS(model);
  if (error) goto QUIT;
  error = GRBwrite(model, "model.ilp");
  if (error) goto QUIT;
} else if (optimstatus == GRB_UNBOUNDED) {
  printf("Model is unbounded\n\n");
} else {
  printf("Optimization was stopped with status = %d\n\n", optimstatus);
```

QUIT: /* Error reporting */ if (error) { printf("ERROR: %s\n", GRBgeterrormsg(masterenv)); exit(1); } /* Free model */ GRBfreemodel(model); /* Free environment */ GRBfreeenv(masterenv); return 0; }

Ipmethod c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve a model with different values of the Method parameter;
   show which value gives the shortest solve time. */
#include <stdlib.h>
#include <stdio.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env = NULL, *menv;
 GRBmodel *m = NULL;
  int
            error = 0;
  int
            i;
            optimstatus;
  int
  int
            bestMethod = -1;
  double
            bestTime;
  if (argc < 2)
  {
    fprintf(stderr, "Usage: lpmethod_c filename\n");
    exit(1);
  }
  error = GRBloadenv(&env, "lpmethod.log");
  if (error) goto QUIT;
  /* Read model */
  error = GRBreadmodel(env, argv[1], &m);
  if (error) goto QUIT;
 menv = GRBgetenv(m);
  error = GRBgetdblparam(menv, "TimeLimit", &bestTime);
  if (error) goto QUIT;
  /* Solve the model with different values of Method */
 for (i = 0; i \le 2; ++i)
  {
    error = GRBresetmodel(m);
    if (error) goto QUIT;
    error = GRBsetintparam(menv, "Method", i);
    if (error) goto QUIT;
```

```
error = GRBoptimize(m);
    if (error) goto QUIT;
    error = GRBgetintattr(m, "Status", &optimstatus);
    if (error) goto QUIT;
    if (optimstatus == GRB_OPTIMAL) {
      error = GRBgetdblattr(m, "Runtime", &bestTime);
      if (error) goto QUIT;
      bestMethod = i;
      /* Reduce the TimeLimit parameter to save time
         with other methods */
      error = GRBsetdblparam(menv, "TimeLimit", bestTime);
      if (error) goto QUIT;
   }
  }
  /* Report which method was fastest */
  if (bestMethod == -1) {
   printf("Unable to solve this model\n");
 } else {
   printf("Solved in %f seconds with Method: %i\n",
           bestTime, bestMethod);
  }
QUIT:
 /* Error reporting */
  if (error)
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
 /* Free model */
 GRBfreemodel(m);
  /* Free environment */
 GRBfreeenv(env);
 return 0;
}
```

lpmod c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
   If the model can be solved, then it finds the smallest positive variable,
   sets its upper bound to zero, and resolves the model two ways:
   first with an advanced start, then without an advanced start
   (i.e. 'from scratch'). */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
{
  GRBenv
           *env
                = NULL;
  GRBmodel *model = NULL;
  int
            error = 0;
  int
            j;
  int
            numvars, isMIP, status, minVar = 0;
  double
            minVal = GRB_INFINITY, sol, 1b;
  char
           *varname;
  double
            warmCount, warmTime, coldCount, coldTime;
  if (argc < 2)
    fprintf(stderr, "Usage: lpmod_c filename\n");
    exit(1);
  }
  error = GRBloadenv(&env, "lpmod.log");
  if (error) goto QUIT;
  /* Read model and determine whether it is an LP */
  error = GRBreadmodel(env, argv[1], &model);
  if (error) goto QUIT;
  error = GRBgetintattr(model, "IsMIP", &isMIP);
  if (error) goto QUIT;
  if (isMIP)
   printf("The model is not a linear program\n");
```

```
goto QUIT;
}
error = GRBoptimize(model);
if (error) goto QUIT;
error = GRBgetintattr(model, "Status", &status);
if (error) goto QUIT;
if ((status == GRB_INF_OR_UNBD) || (status == GRB_INFEASIBLE) ||
    (status == GRB_UNBOUNDED))
{
  printf("The model cannot be solved because it is ");
  printf("infeasible or unbounded\n");
  goto QUIT;
}
if (status != GRB_OPTIMAL)
{
  printf("Optimization was stopped with status %i\n", status);
  goto QUIT;
}
/* Find the smallest variable value */
error = GRBgetintattr(model, "NumVars", &numvars);
if (error) goto QUIT;
for (j = 0; j < numvars; ++j)
{
  error = GRBgetdblattrelement(model, "X", j, &sol);
  if (error) goto QUIT;
  error = GRBgetdblattrelement(model, "LB", j, &lb);
  if (error) goto QUIT;
  if ((sol > 0.0001) && (sol < minVal) &&
      (1b == 0.0))
    minVal = sol;
    minVar = j;
  }
}
error = GRBgetstrattrelement(model, "VarName", minVar, &varname);
if (error) goto QUIT;
printf("\n*** Setting %s from %f to zero ***\n", varname, minVal);
error = GRBsetdblattrelement(model, "LB", minVar, 0.0);
if (error) goto QUIT;
```

```
/* Solve from this starting point */
  error = GRBoptimize(model);
  if (error) goto QUIT;
  /* Save iteration & time info */
  error = GRBgetdblattr(model, "IterCount", &warmCount);
  if (error) goto QUIT;
  error = GRBgetdblattr(model, "Runtime", &warmTime);
  if (error) goto QUIT;
  /* Reset the model and resolve */
 printf("\n*** Resetting and solving ");
 printf("without an advanced start ***\n\n");
  error = GRBresetmodel(model);
  if (error) goto QUIT;
  error = GRBoptimize(model);
  if (error) goto QUIT;
  /* Save iteration & time info */
  error = GRBgetdblattr(model, "IterCount", &coldCount);
  if (error) goto QUIT;
  error = GRBgetdblattr(model, "Runtime", &coldTime);
  if (error) goto QUIT;
 printf("\n*** Warm start: %f iterations, %f seconds\n",
         warmCount, warmTime);
 printf("*** Cold start: %f iterations, %f seconds\n",
         coldCount, coldTime);
QUIT:
 /* Error reporting */
  if (error)
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  /* Free model */
 GRBfreemodel(model);
```

```
/* Free environment */
GRBfreeenv(env);
return 0;
}
```

```
mip1 c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple MIP model:
     maximize
                 x +
                       y + 2 z
     subject to x + 2y + 3z \le 4
                 x + y
                               >= 1
     x, y, z binary
*/
#include <stdlib.h>
#include <stdio.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
{
  GRBenv
           *env
                = NULL;
  GRBmodel *model = NULL;
  int
            error = 0;
  double
           sol[3];
  int
           ind[3];
  double
           val[3];
  double
            obj[3];
  char
            vtype[3];
  int
            optimstatus;
  double
            objval;
  /* Create environment */
  error = GRBloadenv(&env, "mip1.log");
  if (error) goto QUIT;
  /* Create an empty model */
  error = GRBnewmodel(env, &model, "mip1", 0, NULL, NULL, NULL, NULL, NULL);
  if (error) goto QUIT;
  /* Add variables */
  obj[0] = 1; obj[1] = 1; obj[2] = 2;
  vtype[0] = GRB_BINARY; vtype[1] = GRB_BINARY; vtype[2] = GRB_BINARY;
```

```
error = GRBaddvars(model, 3, 0, NULL, NULL, NULL, obj, NULL, NULL, vtype,
                   NULL);
if (error) goto QUIT;
/* Change objective sense to maximization */
error = GRBsetintattr(model, GRB_INT_ATTR_MODELSENSE, GRB_MAXIMIZE);
if (error) goto QUIT;
/* Integrate new variables */
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* First constraint: x + 2 y + 3 z \le 4 */
ind[0] = 0; ind[1] = 1; ind[2] = 2;
val[0] = 1; val[1] = 2; val[2] = 3;
error = GRBaddconstr(model, 3, ind, val, GRB_LESS_EQUAL, 4.0, "c0");
if (error) goto QUIT;
/* Second constraint: x + y >= 1 */
ind[0] = 0; ind[1] = 1;
val[0] = 1; val[1] = 1;
error = GRBaddconstr(model, 2, ind, val, GRB_GREATER_EQUAL, 1.0, "c1");
if (error) goto QUIT;
/* Optimize model */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Write model to 'mip1.lp' */
error = GRBwrite(model, "mip1.lp");
if (error) goto QUIT;
/* Capture solution information */
error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
if (error) goto QUIT;
```

```
error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
  if (error) goto QUIT;
  error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, 3, sol);
  if (error) goto QUIT;
  printf("\nOptimization complete\n");
  if (optimstatus == GRB_OPTIMAL) {
    printf("Optimal objective: %.4e\n", objval);
    printf(" x=\%.0f, y=\%.0f, z=\%.0f\n", sol[0], sol[1], sol[2]);
  } else if (optimstatus == GRB_INF_OR_UNBD) {
    printf("Model is infeasible or unbounded\n");
    printf("Optimization was stopped early\n");
QUIT:
  /* Error reporting */
  if (error) {
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
  return 0;
}
```

```
mip2 c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, solves it and
   prints the objective values from all feasible solutions
   generated while solving the MIP. Then it creates the fixed
   model and solves that model. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
{
  GRBenv
                  = NULL;
           *env
  GRBmodel *model = NULL;
  GRBmodel *fixed = NULL;
  int
            error = 0;
  int
            ismip;
            j, k, solcount, numvars;
  int
  double
            objn, vobj, xn;
  int
            optimstatus, foptimstatus;
  double
            objval, fobjval;
  char
            *varname;
  double
            x;
  /* To change settings for a loaded model, we need to get
     the model environment, which will be freed when the model
     is freed. */
 {\tt GRBenv}
           *menv, *fenv;
  if (argc < 2) {
   fprintf(stderr, "Usage: mip2_c filename\n");
    exit(1);
  }
 /* Create environment */
  error = GRBloadenv(&env, "mip2.log");
  if (error) goto QUIT;
```

```
/* Read model from file */
error = GRBreadmodel(env, argv[1], &model);
if (error) goto QUIT;
error = GRBgetintattr(model, "IsMIP", &ismip);
if (error) goto QUIT;
if (ismip == 0) {
  printf("Model is not a MIP\n");
  goto QUIT;
/* Get model environment */
menv = GRBgetenv(model);
if (!menv) {
  fprintf(stderr, "Error: could not get model environment\n");
  goto QUIT;
}
/* Solve model */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Capture solution information */
error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
if (error) goto QUIT;
printf("\nOptimization complete\n");
if (optimstatus == GRB_OPTIMAL) {
  error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
  if (error) goto QUIT;
  printf("Optimal objective: %.4e\n\n", objval);
} else if (optimstatus == GRB_INF_OR_UNBD) {
  printf("Model is infeasible or unbounded\n\n");
  goto QUIT;
} else if (optimstatus == GRB_INFEASIBLE) {
  printf("Model is infeasible\n\n");
  goto QUIT;
} else if (optimstatus == GRB_UNBOUNDED) {
  printf("Model is unbounded\n\n");
  goto QUIT;
```

```
} else {
  printf("Optimization was stopped with status = %d\n\n", optimstatus);
  goto QUIT;
/* Iterate over the solutions and compute the objectives */
error = GRBsetintparam(menv, "OutputFlag", 0);
if (error) goto QUIT;
error = GRBgetintattr(model, "SolCount", &solcount);
if (error) goto QUIT;
error = GRBgetintattr(model, "NumVars", &numvars);
if (error) goto QUIT;
printf("\n");
for (k = 0; k < solcount; ++k) {
  error = GRBsetintparam(menv, "SolutionNumber", k);
  objn = 0.0;
  for ( j = 0; j < numvars; ++j ) {
    error = GRBgetdblattrelement(model, "Obj", j, &vobj);
    if (error) goto QUIT;
    error = GRBgetdblattrelement(model, "Xn", j, &xn);
    if (error) goto QUIT;
    objn += vobj * xn;
  printf("Solution %i has objective: %f\n", k, objn);
}
printf("\n");
error = GRBsetintparam(menv, "OutputFlag", 1);
if (error) goto QUIT;
/* Create a fixed model, turn off presolve and solve */
fixed = GRBfixedmodel(model);
if (!fixed) {
  fprintf(stderr, "Error: could not create fixed model\n");
  goto QUIT;
}
fenv = GRBgetenv(fixed);
if (!fenv) {
  fprintf(stderr, "Error: could not get fixed model environment\n");
  goto QUIT;
}
```

```
error = GRBsetintparam(fenv, "PRESOLVE", 0);
  if (error) goto QUIT;
  error = GRBoptimize(fixed);
  if (error) goto QUIT;
  error = GRBgetintattr(fixed, GRB_INT_ATTR_STATUS, &foptimstatus);
  if (error) goto QUIT;
  if (foptimstatus != GRB_OPTIMAL) {
    fprintf(stderr, "Error: fixed model isn't optimal\n");
    goto QUIT;
  }
  error = GRBgetdblattr(fixed, GRB_DBL_ATTR_OBJVAL, &fobjval);
  if (error) goto QUIT;
  if (fabs(fobjval - objval) > 1.0e-6 * (1.0 + fabs(objval))) {
    fprintf(stderr, "Error: objective values are different\n");
  }
  /* Print values of nonzero variables */
 for (j = 0; j < numvars; ++j) {
    error = GRBgetstrattrelement(fixed, "VarName", j, &varname);
    if (error) goto QUIT;
    error = GRBgetdblattrelement(fixed, "X", j, &x);
    if (error) goto QUIT;
    if (x != 0.0) {
     printf("%s %f\n", varname, x);
  }
QUIT:
 /* Error reporting */
  if (error) {
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free models */
```

```
GRBfreemodel(model);
GRBfreemodel(fixed);

/* Free environment */
GRBfreeenv(env);
return 0;
}
```

params c.c /* Copyright 2013, Gurobi Optimization, Inc. */ /* Use parameters that are associated with a model. A MIP is solved for 5 seconds with different sets of parameters. The one with the smallest MIP gap is selected, and the optimization is resumed until the optimal solution is found. */ #include <stdlib.h> #include <stdio.h> #include <math.h> #include "gurobi_c.h" int gap(GRBmodel*, double*); int main(int argc, char *argv[]) = NULL, *baseenv = NULL, *menv = NULL, *bestenv = NULL; GRBenv GRBmodel *base = NULL, *m = NULL, *bestModel = NULL; int error = 0;int i; int ismip; mipfocus; int bestGap = GRB_INFINITY, currGap; double if (argc < 2)fprintf(stderr, "Usage: params_c filename\n"); exit(1); } error = GRBloadenv(&env, "params.log"); if (error) goto QUIT; /* Read model and verify that it is a MIP */ error = GRBreadmodel(env, argv[1], &base); if (error) goto QUIT; error = GRBgetintattr(base, "IsMIP", &ismip); if (error) goto QUIT;

if (ismip == 0)

{

```
printf("The model is not an integer program\n");
  goto QUIT;
/* Set a 5 second time limit */
baseenv = GRBgetenv(base);
if (!baseenv) goto QUIT;
error = GRBsetdblparam(baseenv, "TimeLimit", 5);
if (error) goto QUIT;
/* Now solve the model with different values of MIPFocus */
for (i = 0; i \le 3; ++i)
  m = GRBcopymodel(base);
  if (!m) goto QUIT;
  menv = GRBgetenv(m);
  if (!menv) goto QUIT;
  error = GRBsetintparam(menv, "MIPFocus", i);
  if (error) goto QUIT;
  error = GRBoptimize(m);
  if (error) goto QUIT;
  error = gap(m, &currGap);
  if (error) goto QUIT;
  if (bestModel == NULL || bestGap > currGap)
  {
    GRBfreemodel(bestModel);
    bestModel = m;
    bestGap = currGap;
  }
  else
    GRBfreemodel(m);
}
/* Finally, reset the time limit and continue to solve the
   best model to optimality */
bestenv = GRBgetenv(bestModel);
if (!bestenv) goto QUIT;
error = GRBsetdblparam(bestenv, "TimeLimit", GRB_INFINITY);
if (error) goto QUIT;
error = GRBoptimize(bestModel);
if (error) goto QUIT;
error = GRBgetintparam(bestenv, "MIPFocus", &mipfocus);
if (error) goto QUIT;
```

```
printf("Solved with MIPFocus: %i\n", mipfocus);
QUIT:
  /* Error reporting */
  if (error)
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  /* Free models */
 GRBfreemodel(bestModel);
 GRBfreemodel(base);
 /* Free environment */
 GRBfreeenv(env);
 return 0;
/* Simple function to determine the MIP gap */
int gap(GRBmodel *model, double *gap)
 int error;
  int solcount;
 double objval, objbound;
  error = GRBgetintattr(model, "SolCount", &solcount);
  if (error) return error;
  error = GRBgetdblattr(model, "ObjVal", &objval);
  if (error) return error;
 if ((solcount == 0) || (fabs(objval) < 1e-6))</pre>
    *gap = GRB_INFINITY;
   return 0;
  error = GRBgetdblattr(model, "ObjBound", &objbound);
  if (error) return error;
```

```
*gap = fabs(objbound - objval) / fabs(objval);
return 0;
}
```

```
qcp c.c
```

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QCP model:
     maximize
     subject to x + y + z = 1
                 x^2 + y^2 \le z^2 (second-order cone)
                 x^2 <= yz (rotated second-order cone)
*/
#include <stdlib.h>
#include <stdio.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env
                = NULL;
  GRBmodel *model = NULL;
  int
           error = 0;
  double sol[3];
  int
           ind[3];
  double val[3];
  double
           obj[] = \{1, 0, 0\};
  int
            qrow[3];
            qcol[3];
  int
  double
           qval[3];
  int
            optimstatus;
  double
            objval;
  /* Create environment */
  error = GRBloadenv(&env, "qcp.log");
  if (error) goto QUIT;
  /* Create an empty model */
  error = GRBnewmodel(env, &model, "qcp", 0, NULL, NULL, NULL, NULL, NULL);
  if (error) goto QUIT;
  /* Add variables */
```

```
error = GRBaddvars(model, 3, 0, NULL, NULL, NULL, obj, NULL, NULL, NULL,
                   NULL);
if (error) goto QUIT;
/* Change sense to maximization */
error = GRBsetintattr(model, GRB_INT_ATTR_MODELSENSE, GRB_MAXIMIZE);
if (error) goto QUIT;
/* Integrate new variables */
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* Linear constraint: x + y + z = 1 */
ind[0] = 0; ind[1] = 1; ind[2] = 2;
val[0] = 1; val[1] = 1; val[2] = 1;
error = GRBaddconstr(model, 3, ind, val, GRB_EQUAL, 1.0, "c0");
if (error) goto QUIT;
/* Cone: x^2 + y^2 <= z^2 */
qrow[0] = 0; qcol[0] = 0; qval[0] = 1.0;
qrow[1] = 1; qcol[1] = 1; qval[1] = 1.0;
qrow[2] = 2; qcol[2] = 2; qval[2] = -1.0;
error = GRBaddqconstr(model, 0, NULL, NULL, 3, qrow, qcol, qval,
                      GRB_LESS_EQUAL, 0.0, "qc0");
if (error) goto QUIT;
/* Rotated cone: x^2 \le yz */
qrow[0] = 0; qcol[0] = 0; qval[0] = 1.0;
qrow[1] = 1; qcol[1] = 2; qval[1] = -1.0;
error = GRBaddqconstr(model, 0, NULL, NULL, 2, qrow, qcol, qval,
                      GRB_LESS_EQUAL, 0.0, "qc1");
if (error) goto QUIT;
/* Optimize model */
error = GRBoptimize(model);
if (error) goto QUIT;
```

```
/* Write model to 'qcp.lp' */
  error = GRBwrite(model, "qcp.lp");
  if (error) goto QUIT;
  /* Capture solution information */
  error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
  if (error) goto QUIT;
  error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
  if (error) goto QUIT;
  error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, 3, sol);
  if (error) goto QUIT;
 printf("\nOptimization complete\n");
  if (optimstatus == GRB_OPTIMAL) {
   printf("Optimal objective: %.4e\n", objval);
    printf(" x=\%.2f, y=\%.2f, z=\%.2f\n", sol[0], sol[1], sol[2]);
 } else if (optimstatus == GRB_INF_OR_UNBD) {
   printf("Model is infeasible or unbounded\n");
 } else {
   printf("Optimization was stopped early\n");
  }
QUIT:
 /* Error reporting */
  if (error) {
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free model */
 GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
```

```
return 0;
```

```
qp_c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                 x^2 + x*y + y^2 + y*z + z^2 + z
     subject to x + 2 y + 3 z >= 4
                 x + y
                               >= 1
   It solves it once as a continuous model, and once as an integer model.
*/
#include <stdlib.h>
#include <stdio.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env
                = NULL;
  GRBmodel *model = NULL;
           error = 0;
  int
  double
           sol[3];
  int
            ind[3];
  double
           val[3];
  int
            qrow[5];
  int
            qcol[5];
  double
           qval[5];
  char
            vtype[3];
  int
            optimstatus;
  double
            objval;
  /* Create environment */
  error = GRBloadenv(&env, "qp.log");
  if (error) goto QUIT;
  /* Create an empty model */
  error = GRBnewmodel(env, &model, "qp", 0, NULL, NULL, NULL, NULL, NULL);
  if (error) goto QUIT;
  /* Add variables */
```

```
error = GRBaddvars(model, 3, 0, NULL, NULL, NULL, NULL, NULL, NULL, NULL,
                   NULL);
if (error) goto QUIT;
/* Integrate new variables */
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* Quadratic objective terms */
qrow[0] = 0; qrow[1] = 0; qrow[2] = 1; qrow[3] = 1; qrow[4] = 2;
qcol[0] = 0; qcol[1] = 1; qcol[2] = 1; qcol[3] = 2; qcol[4] = 2;
qval[0] = 1; qval[1] = 1; qval[2] = 1; qval[3] = 1; qval[4] = 1;
error = GRBaddqpterms(model, 5, qrow, qcol, qval);
if (error) goto QUIT;
/* Linear objective term */
error = GRBsetdblattrelement(model, GRB_DBL_ATTR_OBJ, 0, 2.0);
if (error) goto QUIT;
/* First constraint: x + 2 y + 3 z \le 4 */
ind[0] = 0; ind[1] = 1; ind[2] = 2;
val[0] = 1; val[1] = 2; val[2] = 3;
error = GRBaddconstr(model, 3, ind, val, GRB_GREATER_EQUAL, 4.0, "c0");
if (error) goto QUIT;
/* Second constraint: x + y >= 1 */
ind[0] = 0; ind[1] = 1;
val[0] = 1; val[1] = 1;
error = GRBaddconstr(model, 2, ind, val, GRB_GREATER_EQUAL, 1.0, "c1");
if (error) goto QUIT;
/* Optimize model */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Write model to 'qp.lp' */
```

```
error = GRBwrite(model, "qp.lp");
if (error) goto QUIT;
/* Capture solution information */
error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
if (error) goto QUIT;
error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
if (error) goto QUIT;
error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, 3, sol);
if (error) goto QUIT;
printf("\nOptimization complete\n");
if (optimstatus == GRB_OPTIMAL) {
  printf("Optimal objective: %.4e\n", objval);
  printf(" x=\%.4f, y=\%.4f, z=\%.4f\n", sol[0], sol[1], sol[2]);
} else if (optimstatus == GRB_INF_OR_UNBD) {
  printf("Model is infeasible or unbounded\n");
} else {
  printf("Optimization was stopped early\n");
}
/* Modify variable types */
vtype[0] = GRB_INTEGER; vtype[1] = GRB_INTEGER; vtype[2] = GRB_INTEGER;
error = GRBsetcharattrarray(model, GRB_CHAR_ATTR_VTYPE, 0, 3, vtype);
if (error) goto QUIT;
/* Optimize model */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Write model to 'qp2.lp' */
error = GRBwrite(model, "qp2.lp");
if (error) goto QUIT;
/* Capture solution information */
```

```
error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
  if (error) goto QUIT;
  error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
  if (error) goto QUIT;
  error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, 3, sol);
  if (error) goto QUIT;
 printf("\nOptimization complete\n");
  if (optimstatus == GRB_OPTIMAL) {
   printf("Optimal objective: %.4e\n", objval);
    printf(" x=\%.4f, y=\%.4f, z=\%.4f\n", sol[0], sol[1], sol[2]);
  } else if (optimstatus == GRB_INF_OR_UNBD) {
   printf("Model is infeasible or unbounded\n");
  } else {
   printf("Optimization was stopped early\n");
  }
QUIT:
 /* Error reporting */
  if (error) {
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  /* Free model */
 GRBfreemodel(model);
  /* Free environment */
 GRBfreeenv(env);
 return 0;
}
```

sensitivity c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Simple MIP sensitivity analysis example.
   For each integer variable, fix it to its lower and upper bound
   and check the impact on the objective. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env = NULL, *aenv;
  GRBmodel *a = NULL, *b = NULL;
  int
            error = 0;
  int
            i, numvars, status;
  char
           vtype, *vname;
           x, bnd, aobj, bobj, objchg;
  double
  if (argc < 2)
    fprintf(stderr, "Usage: sensitivity_c filename\n");
    exit(1);
  }
  error = GRBloadenv(&env, "sensitivity.log");
  if (error) goto QUIT;
  /* Read model */
  error = GRBreadmodel(env, argv[1], &a);
  if (error) goto QUIT;
  error = GRBoptimize(a);
  if (error) goto QUIT;
  error = GRBgetdblattr(a, "ObjVal", &aobj);
  if (error) goto QUIT;
  aenv = GRBgetenv(a);
  if (!aenv) goto QUIT;
  error = GRBsetintparam(aenv, "OutputFlag", 0);
  if (error) goto QUIT;
  /* Iterate over all variables */
```

```
error = GRBgetintattr(a, "NumVars", &numvars);
if (error) goto QUIT;
for (i = 0; i < numvars; ++i)</pre>
  error = GRBgetcharattrelement(a, "VType", i, &vtype);
  if (error) goto QUIT;
  if (vtype == GRB_BINARY)
    /* Create clone and fix variable */
    b = GRBcopymodel(a);
    if (!b) goto QUIT;
    error = GRBgetstrattrelement(a, "VarName", i, &vname);
    if (error) goto QUIT;
    error = GRBgetdblattrelement(a, "X", i, &x);
    if (error) goto QUIT;
    error = GRBgetdblattrelement(a, "LB", i, &bnd);
    if (error) goto QUIT;
    if (x - bnd < 0.5)
      error = GRBgetdblattrelement(b, "UB", i, &bnd);
      if (error) goto QUIT;
      error = GRBsetdblattrelement(b, "LB", i, bnd);
      if (error) goto QUIT;
    }
    else
      error = GRBgetdblattrelement(b, "LB", i, &bnd);
      if (error) goto QUIT;
      error = GRBsetdblattrelement(b, "UB", i, bnd);
      if (error) goto QUIT;
    }
    error = GRBoptimize(b);
    if (error) goto QUIT;
    error = GRBgetintattr(b, "Status", &status);
    if (error) goto QUIT;
    if (status == GRB_OPTIMAL)
    {
      error = GRBgetdblattr(b, "ObjVal", &bobj);
      if (error) goto QUIT;
      objchg = bobj - aobj;
      if (objchg < 0)
```

```
{
          objchg = 0;
        printf("Objective sensitivity for variable %s is %f\n", vname, objchg);
      }
      else
      {
        printf("Objective sensitivity for variable %s is infinite\n", vname);
      GRBfreemodel(b);
      b = NULL;
    }
  }
QUIT:
  /* Error reporting */
  if (error)
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free models */
  GRBfreemodel(a);
  GRBfreemodel(b);
  /* Free environment */
  GRBfreeenv(env);
  return 0;
}
```

```
sos c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example creates a very simple Special Ordered Set (SOS) model.
   The model consists of 3 continuous variables, no linear constraints,
   and a pair of SOS constraints of type 1. */
#include <stdlib.h>
#include <stdio.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
{
 GRBenv
           *env = NULL;
 GRBmodel *model = NULL;
  int
            error = 0;
  double
            x[3];
  double
            obj[3];
  double
            ub[3];
  int
            sostype[2];
  int
            sosbeg[2];
            sosind[4];
  int
  double
            soswt[4];
  int
            optimstatus;
  double
            objval;
  int
            zero = 0;
  /* Create environment */
  error = GRBloadenv(&env, "sos.log");
  if (error) goto QUIT;
  /* Create an empty model */
  error = GRBnewmodel(env, &model, "sos", O, NULL, NULL, NULL, NULL, NULL);
  if (error) goto QUIT;
  /* Add variables */
  obj[0] = -2; obj[1] = -1; obj[2] = -1;
 ub[0] = 1.0; ub[1] = 1.0; ub[2] = 2.0;
  error = GRBaddvars(model, 3, 0, NULL, NULL, NULL, obj, NULL, ub, NULL,
```

```
NULL);
if (error) goto QUIT;
/* Integrate new variables */
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* Build first SOS1: x0=0 or x1=0 */
sosind[0] = 0; sosind[1] = 1;
soswt[0] = 1.0; soswt[1] = 2.0;
sosbeg[0] = 0; sostype[0] = GRB_SOS_TYPE1;
/* Build second SOS1: x0=0 or x2=0 */
sosind[2] = 0; sosind[3] = 2;
soswt[2] = 1.0; soswt[3] = 2.0;
sosbeg[1] = 2; sostype[1] = GRB_SOS_TYPE1;
/* Add SOSs to model */
error = GRBaddsos(model, 2, 4, sostype, sosbeg, sosind, soswt);
if (error) goto QUIT;
/* Optimize model */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Write model to 'sos.lp' */
error = GRBwrite(model, "sos.lp");
if (error) goto QUIT;
/* Capture solution information */
error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
if (error) goto QUIT;
error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
if (error) goto QUIT;
error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, 3, x);
if (error) goto QUIT;
```

```
printf("\nOptimization complete\n");
  if (optimstatus == GRB_OPTIMAL) {
    printf("Optimal objective: %.4e\n", objval);
    printf(" x=\%.4f, y=\%.4f, z=\%.4f\n", x[0], x[1], x[2]);
  } else if (optimstatus == GRB_INF_OR_UNBD) {
    printf("Model is infeasible or unbounded\n");
  } else {
    printf("Optimization was stopped early\n");
  }
QUIT:
  /* Error reporting */
  if (error) {
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
  return 0;
}
```

```
sudoku c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
  Sudoku example.
 The Sudoku board is a 9x9 grid, which is further divided into a 3x3 grid
  of 3x3 grids. Each cell in the grid must take a value from 0 to 9.
 No two grid cells in the same row, column, or 3x3 subgrid may take the
  same value.
  In the MIP formulation, binary variables x[i,j,v] indicate whether
  cell <i,j> takes value 'v'. The constraints are as follows:
    1. Each cell must take exactly one value (sum_v x[i,j,v] = 1)
    2. Each value is used exactly once per row (sum_i x[i,j,v] = 1)
    3. Each value is used exactly once per column (sum_j x[i,j,v] = 1)
    4. Each value is used exactly once per 3x3 subgrid (sum_grid x[i,j,v] = 1)
  Input datasets for this example can be found in examples/data/sudoku*.
*/
#include <stdlib.h>
#include <stdio.h>
#include <string.h>
#include "gurobi_c.h"
#define SUBDIM 3
#define DIM
              (SUBDIM*SUBDIM)
int
main(int
           argc,
     char *argv[])
{
 FILE
           *fp
                  = NULL;
  GRBenv
                  = NULL;
           *env
  GRBmodel *model = NULL;
  int
            board[DIM] [DIM];
  char
            inputline[100];
  int
            ind[DIM];
  double
            val[DIM];
  double
            lb[DIM*DIM*DIM];
            vtype[DIM*DIM*DIM];
  char
           *names[DIM*DIM*DIM];
  char
  char
            namestorage[10*DIM*DIM*DIM];
  char
           *cursor;
  int
            optimstatus;
```

```
double
          objval;
int
          zero = 0;
int
          i, j, v, ig, jg, count;
          error = 0;
int
if (argc < 2) {
  fprintf(stderr, "Usage: sudoku_c datafile\n");
  exit(1);
}
fp = fopen(argv[1], "r");
if (fp == NULL) {
  fprintf(stderr, "Error: unable to open input file %s\n", argv[1]);
  exit(1);
}
for (i = 0; i < DIM; i++) {
  fgets(inputline, 100, fp);
  if (strlen(inputline) < 9) {</pre>
    fprintf(stderr, "Error: not enough board positions specified\n");
    exit(1);
  for (j = 0; j < DIM; j++) {
    board[i][j] = (int) inputline[j] - (int) '1';
    if (board[i][j] < 0 || board[i][j] >= DIM)
      board[i][j] = -1;
  }
}
/* Create an empty model */
cursor = namestorage;
for (i = 0; i < DIM; i++) {
  for (j = 0; j < DIM; j++) {
    for (v = 0; v < DIM; v++) {
      if (board[i][j] == v)
        lb[i*DIM*DIM+j*DIM+v] = 1;
        lb[i*DIM*DIM+j*DIM+v] = 0;
      vtype[i*DIM*DIM+j*DIM+v] = GRB_BINARY;
      names[i*DIM*DIM+j*DIM+v] = cursor;
      sprintf(names[i*DIM*DIM+j*DIM+v], "x[%d,%d,%d]", i, j, v+1);
      cursor += strlen(names[i*DIM*DIM+j*DIM+v]) + 1;
    }
```

```
}
}
/* Create environment */
error = GRBloadenv(&env, "sudoku.log");
if (error) goto QUIT;
/* Create new model */
error = GRBnewmodel(env, &model, "sudoku", DIM*DIM*DIM, NULL, lb, NULL,
                    vtype, names);
if (error) goto QUIT;
/* Each cell gets a value */
for (i = 0; i < DIM; i++) {
  for (j = 0; j < DIM; j++) {
    for (v = 0; v < DIM; v++) {
      ind[v] = i*DIM*DIM + j*DIM + v;
      val[v] = 1.0;
    }
    error = GRBaddconstr(model, DIM, ind, val, GRB_EQUAL, 1.0, NULL);
    if (error) goto QUIT;
  }
}
/* Each value must appear once in each row */
for (v = 0; v < DIM; v++) {
  for (j = 0; j < DIM; j++) {
   for (i = 0; i < DIM; i++) {
      ind[i] = i*DIM*DIM + j*DIM + v;
      val[i] = 1.0;
    }
    error = GRBaddconstr(model, DIM, ind, val, GRB_EQUAL, 1.0, NULL);
    if (error) goto QUIT;
  }
}
/* Each value must appear once in each column */
for (v = 0; v < DIM; v++) {
```

```
for (i = 0; i < DIM; i++) {
    for (j = 0; j < DIM; j++) {
      ind[j] = i*DIM*DIM + j*DIM + v;
      val[j] = 1.0;
    }
    error = GRBaddconstr(model, DIM, ind, val, GRB_EQUAL, 1.0, NULL);
    if (error) goto QUIT;
  }
}
/* Each value must appear once in each subgrid */
for (v = 0; v < DIM; v++) {
  for (ig = 0; ig < SUBDIM; ig++) {</pre>
    for (jg = 0; jg < SUBDIM; jg++) {
      count = 0;
      for (i = ig*SUBDIM; i < (ig+1)*SUBDIM; i++) {
        for (j = jg*SUBDIM; j < (jg+1)*SUBDIM; j++) {
          ind[count] = i*DIM*DIM + j*DIM + v;
          val[count] = 1.0;
          count++;
        }
      }
      error = GRBaddconstr(model, DIM, ind, val, GRB_EQUAL, 1.0, NULL);
      if (error) goto QUIT;
    }
  }
}
/* Optimize model */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Write model to 'sudoku.lp' */
error = GRBwrite(model, "sudoku.lp");
if (error) goto QUIT;
/* Capture solution information */
error = GRBgetintattr(model, GRB_INT_ATTR_STATUS, &optimstatus);
if (error) goto QUIT;
```

```
error = GRBgetdblattr(model, GRB_DBL_ATTR_OBJVAL, &objval);
  if (error) goto QUIT;
  printf("\nOptimization complete\n");
  if (optimstatus == GRB_OPTIMAL)
    printf("Optimal objective: %.4e\n", objval);
  else if (optimstatus == GRB_INF_OR_UNBD)
    printf("Model is infeasible or unbounded\n");
  else
    printf("Optimization was stopped early\n");
  printf("\n");
QUIT:
  /* Error reporting */
  if (error) {
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
  return 0;
}
```

```
tsp c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/*
  Solve a traveling salesman problem on a randomly generated set of
 points using lazy constraints.
                                  The base MIP model only includes
  'degree-2' constraints, requiring each node to have exactly
 two incident edges. Solutions to this model may contain subtours -
 tours that don't visit every node. The lazy constraint callback
  adds new constraints to cut them off.
*/
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
/* Define structure to pass data to the callback function */
struct callback_data {
  int n;
};
/* Given an integer-feasible solution 'sol', find the smallest
  sub-tour. Result is returned in 'tour', and length is
  returned in 'tourlenP'. */
static void
findsubtour(int
                    n,
            double *sol,
            int
                   *tourlenP,
                   *tour)
            int
  int i, node, len, start;
  int bestind, bestlen;
  int *seen = NULL;
  seen = (int *) malloc(n*sizeof(int));
  if (seen == NULL) {
    fprintf(stderr, "Out of memory\n");
    exit(1);
  }
```

```
for (i = 0; i < n; i++)
    seen[i] = 0;
  start = 0;
  bestlen = n+1;
  bestind = -1;
  while (start < n) {</pre>
    for (node = 0; node < n; node++)
      if (seen[node] == 0)
        break;
    if (node == n)
      break;
    for (len = 0; len < n; len++) {
      tour[start+len] = node;
      seen[node] = 1;
      for (i = 0; i < n; i++) {
        if (sol[node*n+i] > 0.5 \&\& !seen[i]) {
          node = i;
          break;
        }
      }
      if (i == n) {
        len++;
        if (len < bestlen) {</pre>
          bestlen = len;
          bestind = start;
        }
        start += len;
        break;
      }
    }
  for (i = 0; i < bestlen; i++)
    tour[i] = tour[bestind+i];
  *tourlenP = bestlen;
  free(seen);
}
/* Subtour elimination callback. Whenever a feasible solution is found,
   find the shortest subtour, and add a subtour elimination constraint
   if that tour doesn't visit every node. */
```

```
int __stdcall
subtourelim(GRBmodel *model,
                     *cbdata,
            void
            int
                      where,
            void
                     *usrdata)
  struct callback_data *mydata = (struct callback_data *) usrdata;
  int n = mydata -> n;
  int *tour = NULL;
 double *sol = NULL;
  int i, j, len, nz;
  int error = 0;
  if (where == GRB_CB_MIPSOL) {
    sol = (double *) malloc(n*n*sizeof(double));
    tour = (int *)
                      malloc(n*sizeof(int));
    if (sol == NULL || tour == NULL) {
      fprintf(stderr, "Out of memory\n");
      exit(1);
   }
    GRBcbget(cbdata, where, GRB_CB_MIPSOL_SOL, sol);
    findsubtour(n, sol, &len, tour);
    if (len < n) {
             *ind = NULL;
      int
      double *val = NULL;
      ind = (int *)
                       malloc(len*(len-1)/2*sizeof(int));
      val = (double *) malloc(len*(len-1)/2*sizeof(double));
      if (ind == NULL || val == NULL) {
        fprintf(stderr, "Out of memory\n");
        exit(1);
      }
      /* Add subtour elimination constraint */
      nz = 0;
      for (i = 0; i < len; i++)
        for (j = i+1; j < len; j++)
          ind[nz++] = tour[i]*n+tour[j];
      for (i = 0; i < nz; i++)
        val[i] = 1.0;
```

```
error = GRBcblazy(cbdata, nz, ind, val, GRB_LESS_EQUAL, len-1);
      free(ind);
      free(val);
    }
    free(sol);
    free(tour);
  }
  return error;
}
/* Euclidean distance between points 'i' and 'j'. */
static double
distance(double *x,
         double *y,
         int
                 i,
         int
                 j)
  double dx = x[i] - x[j];
  double dy = y[i] - y[j];
 return sqrt(dx*dx + dy*dy);
}
int
main(int
           argc,
     char *argv[])
{
  GRBenv
           *env
                = NULL;
  GRBmodel *model = NULL;
           i, j, len, n, solcount;
  int
  int
           error = 0;
  char
           name[100];
  double
           *x = NULL;
  double
           *y = NULL;
  int
           *ind = NULL;
  double
           *val = NULL;
  struct callback_data mydata;
  if (argc < 2) {
    fprintf(stderr, "Usage: tsp_c size\n");
```

```
exit(1);
}
n = atoi(argv[1]);
if (n == 0) {
  fprintf(stderr, "Argument must be a positive integer.\n");
} else if (n > 100) {
  printf("It will be a challenge to solve a TSP this large.\n");
}
    = (double *) malloc(n*sizeof(double));
y = (double *) malloc(n*sizeof(double));
ind = (int *)
                 malloc(n*sizeof(int));
val = (double *) malloc(n*sizeof(double));
if (x == NULL \mid | y == NULL \mid | ind == NULL \mid | val == NULL) {
  fprintf(stderr, "Out of memory\n");
  exit(1);
}
/* Create random points */
for (i = 0; i < n; i++) {
  x[i] = ((double) rand())/RAND_MAX;
  y[i] = ((double) rand())/RAND_MAX;
}
/* Create environment */
error = GRBloadenv(&env, "tsp.log");
if (error) goto QUIT;
/* Create an empty model */
error = GRBnewmodel(env, &model, "tsp", 0, NULL, NULL, NULL, NULL, NULL);
if (error) goto QUIT;
/* Add variables - one for every pair of nodes */
/* Note: If edge from i to j is chosen, then x[i*n+j] = x[j*n+i] = 1. */
/* The cost is split between the two variables. */
for (i = 0; i < n; i++) {
  for (j = 0; j < n; j++) {
    sprintf(name, "x_{d_{d_{i,j}}}d_{i,j});
```

```
error = GRBaddvar(model, 0, NULL, NULL, distance(x, y, i, j)/2,
                      0.0, 1.0, GRB_BINARY, name);
    if (error) goto QUIT;
  }
}
/* Integrate new variables */
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* Degree-2 constraints */
for (i = 0; i < n; i++) {
  for (j = 0; j < n; j++) {
    ind[j] = i*n+j;
   val[j] = 1.0;
  sprintf(name, "deg2_%d", i);
  error = GRBaddconstr(model, n, ind, val, GRB_EQUAL, 2, name);
  if (error) goto QUIT;
}
/* Forbid edge from node back to itself */
for (i = 0; i < n; i++) {
  error = GRBsetdblattrelement(model, GRB_DBL_ATTR_UB, i*n+i, 0);
  if (error) goto QUIT;
}
/* Symmetric TSP */
for (i = 0; i < n; i++) {
  for (j = 0; j < i; j++) {
    ind[0] = i*n+j;
    ind[1] = i+j*n;
    val[0] = 1;
    val[1] = -1;
    error = GRBaddconstr(model, 2, ind, val, GRB_EQUAL, 0, NULL);
    if (error) goto QUIT;
}
```

```
/* Set callback function */
mydata.n = n;
error = GRBsetcallbackfunc(model, subtourelim, (void *) &mydata);
if (error) goto QUIT;
/* Must set LazyConstraints parameter when using lazy constraints */
error = GRBsetintparam(GRBgetenv(model), GRB_INT_PAR_LAZYCONSTRAINTS, 1);
if (error) goto QUIT;
/* Optimize model */
error = GRBoptimize(model);
if (error) goto QUIT;
/* Extract solution */
error = GRBgetintattr(model, GRB_INT_ATTR_SOLCOUNT, &solcount);
if (error) goto QUIT;
if (solcount > 0) {
  int *tour = NULL;
  double *sol = NULL;
  sol = (double *) malloc(n*n*sizeof(double));
  tour = (int *) malloc(n*sizeof(int));
  if (sol == NULL || tour == NULL) {
    fprintf(stderr, "Out of memory\n");
    exit(1);
  }
  error = GRBgetdblattrarray(model, GRB_DBL_ATTR_X, 0, n*n, sol);
  if (error) goto QUIT;
  /* Print tour */
  findsubtour(n, sol, &len, tour);
  printf("Tour: ");
  for (i = 0; i < len; i++)
    printf("%d ", tour[i]);
  printf("\n");
```

```
free(tour);
    free(sol);
 }
QUIT:
  /* Free data */
 free(x);
  free(y);
  free(ind);
 free(val);
 /* Error reporting */
 if (error) {
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
 return 0;
}
```

```
tune c.c
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a model from a file and tunes it.
   It then writes the best parameter settings to a file
   and solves the model using these parameters. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
int
main(int
           argc,
     char *argv[])
  GRBenv
                = NULL;
           *env
  GRBmodel *model = NULL;
  int
            tuneresultcount;
  int
            error = 0;
  if (argc < 2) {
    fprintf(stderr, "Usage: tune_c filename\n");
    exit(1);
  }
  /* Create environment */
  error = GRBloadenv(&env, "tune_c.log");
  if (error) goto QUIT;
  /* Read model from file */
  error = GRBreadmodel(env, argv[1], &model);
  if (error) goto QUIT;
  /* Set the TuneResults parameter to 1 */
  error = GRBsetintparam(GRBgetenv(model), GRB_INT_PAR_TUNERESULTS, 1);
  if (error) goto QUIT;
  /* Tune the model */
  error = GRBtunemodel(model);
  if (error) goto QUIT;
```

```
/* Get the number of tuning results */
  error = GRBgetintattr(model, GRB_INT_ATTR_TUNE_RESULTCOUNT, &tuneresultcount);
  if (error) goto QUIT;
  if (tuneresultcount > 0) {
   /* Load the best tuned parameters into the model's environment */
    error = GRBgettuneresult(model, 0);
    if (error) goto QUIT;
   /* Write tuned parameters to a file */
    error = GRBwrite(model, "tune.prm");
    if (error) goto QUIT;
   /* Solve the model using the tuned parameters */
   error = GRBoptimize(model);
    if (error) goto QUIT;
  }
QUIT:
 /* Error reporting */
  if (error) {
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
 /* Free model */
 GRBfreemodel(model);
  /* Free environment */
 GRBfreeenv(env);
 return 0;
}
```

workforce1 c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, use IIS to find a set of
  conflicting constraints. Note that there may be additional conflicts
  besides what is reported via IIS. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include "gurobi_c.h"
#define xcol(w,s) nShifts*w+s
#define MAXSTR
                   128
int
main(int
          argc,
     char *argv[])
 GRBenv
                = NULL;
           *env
 GRBmodel *model = NULL;
  int
          error = 0, status;
  int
          s, w, col;
          *cbeg = NULL;
  int
          *cind = NULL;
  int
  int
           idx;
 double *cval = NULL;
          *sense = NULL;
  char
  char
           vname[MAXSTR];
  double
            obj;
  int
            i, iis, numconstrs;
  char
           *cname;
  /* Sample data */
  const int nShifts = 14;
  const int nWorkers = 7;
  /* Sets of days and workers */
  char* Shifts[] =
    { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
      "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
      "Sun14" };
```

```
char* Workers[] =
  { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
/* Number of workers required for each shift */
double shiftRequirements[] =
  \{3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5\};
/* Amount each worker is paid to work one shift */
double pay[] = { 10, 12, 10, 8, 8, 9, 11 };
/* Worker availability: 0 if the worker is unavailable for a shift */
double availability[][14] =
  { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
    \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\},\
    { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
    { 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1 },
    { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
    { 1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1 },
    { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
/* Create environment */
error = GRBloadenv(&env, "workforce1.log");
if (error) goto QUIT;
/* Create initial model */
error = GRBnewmodel(env, &model, "workforce1", nWorkers * nShifts,
                    NULL, NULL, NULL, NULL, NULL);
if (error) goto QUIT;
/* Initialize assignment decision variables:
   x[w][s] == 1 if worker w is assigned
   to shift s. Since an assignment model always produces integer
   solutions, we use continuous variables and solve as an LP. */
for (w = 0; w < nWorkers; ++w)
  for (s = 0; s < nShifts; ++s)
    col = xcol(w, s);
    sprintf(vname, "%s.%s", Workers[w], Shifts[s]);
    error = GRBsetdblattrelement(model, "UB", col, availability[w][s]);
    if (error) goto QUIT;
    error = GRBsetdblattrelement(model, "Obj", col, pay[w]);
    if (error) goto QUIT;
    error = GRBsetstrattrelement(model, "VarName", col, vname);
    if (error) goto QUIT;
```

```
}
}
/* The objective is to minimize the total pay costs */
error = GRBsetintattr(model, "ModelSense", 1);
if (error) goto QUIT;
/* Make space for constraint data */
cbeg = malloc(sizeof(int) * nShifts);
if (!cbeg) goto QUIT;
cind = malloc(sizeof(int) * nShifts * nWorkers);
if (!cind) goto QUIT;
cval = malloc(sizeof(double) * nShifts * nWorkers);
if (!cval) goto QUIT;
sense = malloc(sizeof(char) * nShifts);
if (!sense) goto QUIT;
/* Constraint: assign exactly shiftRequirements[s] workers
   to each shift s */
idx = 0;
for (s = 0; s < nShifts; ++s)
  cbeg[s] = idx;
  sense[s] = GRB_EQUAL;
  for (w = 0; w < nWorkers; ++w)
    cind[idx] = xcol(w, s);
    cval[idx++] = 1.0;
  }
}
error = GRBaddconstrs(model, nShifts, idx, cbeg, cind, cval, sense,
                      shiftRequirements, Shifts);
if (error) goto QUIT;
/* Optimize */
error = GRBoptimize(model);
if (error) goto QUIT;
error = GRBgetintattr(model, "Status", &status);
if (error) goto QUIT;
if (status == GRB_UNBOUNDED)
 printf("The model cannot be solved because it is unbounded\n");
  goto QUIT;
if (status == GRB_OPTIMAL)
```

```
{
    error = GRBgetdblattr(model, "ObjVal", &obj);
    if (error) goto QUIT;
   printf("The optimal objective is %f\n", obj);
   goto QUIT;
  if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
   printf("Optimization was stopped with status %i\n", status);
   goto QUIT;
  }
  /* do IIS */
 printf("The model is infeasible; computing IIS\n");
  error = GRBcomputeIIS(model);
  if (error) goto QUIT;
 printf("\nThe following constraint(s) cannot be satisfied:\n");
  error = GRBgetintattr(model, "NumConstrs", &numconstrs);
  if (error) goto QUIT;
 for (i = 0; i < numconstrs; ++i)</pre>
    error = GRBgetintattrelement(model, "IISConstr", i, &iis);
    if (error) goto QUIT;
    if (iis)
    ₹
      error = GRBgetstrattrelement(model, "ConstrName", i, &cname);
      if (error) goto QUIT;
      printf("%s\n", cname);
  }
QUIT:
  /* Error reporting */
  if (error)
  {
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free data */
```

```
free(cbeg);
free(cind);
free(cval);
free(sense);

/* Free model */

GRBfreemodel(model);

/* Free environment */

GRBfreeenv(env);

return 0;
```

workforce2_c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, use IIS iteratively to
  find all conflicting constraints. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include "gurobi_c.h"
#define xcol(w,s) nShifts*w+s
#define MAXSTR
                   128
int
main(int
           argc,
     char *argv[])
 GRBenv
           *env = NULL;
 GRBmodel *model = NULL;
  int
           error = 0, status;
  int
           s, w, col;
           *cbeg = NULL;
  int
           *cind = NULL;
  int
  int
           idx;
 double *cval = NULL;
          *sense = NULL;
  char
           vname[MAXSTR];
  char
  double
            i, iis, numconstrs, numremoved = 0;
  int
  char
           *cname;
  char
          **removed = NULL;
  /* Sample data */
  const int nShifts = 14;
  const int nWorkers = 7;
 /* Sets of days and workers */
  char* Shifts[] =
    { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
      "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
```

```
"Sun14" };
char* Workers[] =
  { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
/* Number of workers required for each shift */
double shiftRequirements[] =
  \{3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5\};
/* Amount each worker is paid to work one shift */
double pay[] = { 10, 12, 10, 8, 8, 9, 11 };
/* Worker availability: 0 if the worker is unavailable for a shift */
double availability[][14] =
  { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
    { 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 },
    { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
    { 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, },
    { 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1 },
    \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
    { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
/* Create environment */
error = GRBloadenv(&env, "workforce2.log");
if (error) goto QUIT;
/* Create initial model */
error = GRBnewmodel(env, &model, "workforce2", nWorkers * nShifts,
                    NULL, NULL, NULL, NULL, NULL);
if (error) goto QUIT;
/* Initialize assignment decision variables:
   x[w][s] == 1 if worker w is assigned
   to shift s. Since an assignment model always produces integer
   solutions, we use continuous variables and solve as an LP. */
for (w = 0; w < nWorkers; ++w)
  for (s = 0; s < nShifts; ++s)
    col = xcol(w, s);
    sprintf(vname, "%s.%s", Workers[w], Shifts[s]);
    error = GRBsetdblattrelement(model, "UB", col, availability[w][s]);
    if (error) goto QUIT;
    error = GRBsetdblattrelement(model, "Obj", col, pay[w]);
    if (error) goto QUIT;
    error = GRBsetstrattrelement(model, "VarName", col, vname);
```

```
if (error) goto QUIT;
  }
}
/* The objective is to minimize the total pay costs */
error = GRBsetintattr(model, "ModelSense", 1);
if (error) goto QUIT;
/* Make space for constraint data */
cbeg = malloc(sizeof(int) * nShifts);
if (!cbeg) goto QUIT;
cind = malloc(sizeof(int) * nShifts * nWorkers);
if (!cind) goto QUIT;
cval = malloc(sizeof(double) * nShifts * nWorkers);
if (!cval) goto QUIT;
sense = malloc(sizeof(char) * nShifts);
if (!sense) goto QUIT;
/* Constraint: assign exactly shiftRequirements[s] workers
   to each shift s */
idx = 0;
for (s = 0; s < nShifts; ++s)
  cbeg[s] = idx;
  sense[s] = GRB_EQUAL;
  for (w = 0; w < nWorkers; ++w)
    cind[idx] = xcol(w, s);
    cval[idx++] = 1.0;
  }
error = GRBaddconstrs(model, nShifts, idx, cbeg, cind, cval, sense,
                      shiftRequirements, Shifts);
if (error) goto QUIT;
/* Optimize */
error = GRBoptimize(model);
if (error) goto QUIT;
error = GRBgetintattr(model, "Status", &status);
if (error) goto QUIT;
if (status == GRB_UNBOUNDED)
{
  printf("The model cannot be solved because it is unbounded\n");
  goto QUIT;
```

```
if (status == GRB_OPTIMAL)
  error = GRBgetdblattr(model, "ObjVal", &obj);
  if (error) goto QUIT;
  printf("The optimal objective is %f\n", obj);
  goto QUIT;
}
if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
  printf("Optimization was stopped with status %i\n", status);
  goto QUIT;
}
/* do IIS */
printf("The model is infeasible; computing IIS\n");
/* Loop until we reduce to a model that can be solved */
error = GRBgetintattr(model, "NumConstrs", &numconstrs);
if (error) goto QUIT;
removed = calloc(numconstrs, sizeof(char*));
if (!removed) goto QUIT;
while (1)
  error = GRBcomputeIIS(model);
  if (error) goto QUIT;
  printf("\nThe following constraint cannot be satisfied:\n");
  for (i = 0; i < numconstrs; ++i)</pre>
    error = GRBgetintattrelement(model, "IISConstr", i, &iis);
    if (error) goto QUIT;
    if (iis)
    {
      error = GRBgetstrattrelement(model, "ConstrName", i, &cname);
      if (error) goto QUIT;
      printf("%s\n", cname);
      /* Remove a single constraint from the model */
      removed[numremoved] = malloc(sizeof(char) * (1+strlen(cname)));
      if (!removed[numremoved]) goto QUIT;
      strcpy(removed[numremoved++], cname);
      cind[0] = i;
      error = GRBdelconstrs(model, 1, cind);
      if (error) goto QUIT;
      break;
    }
  }
```

```
printf("\n");
    error = GRBoptimize(model);
    if (error) goto QUIT;
    error = GRBgetintattr(model, "Status", &status);
    if (error) goto QUIT;
    if (status == GRB_UNBOUNDED)
      printf("The model cannot be solved because it is unbounded\n");
     goto QUIT;
    if (status == GRB_OPTIMAL)
     break;
    if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
      printf("Optimization was stopped with status %i\n", status);
      goto QUIT;
   }
  }
 printf("\nThe following constraints were removed to get a feasible LP:\n");
 for (i = 0; i < numremoved; ++i)</pre>
   printf("%s ", removed[i]);
  }
 printf("\n");
QUIT:
 /* Error reporting */
  if (error)
   printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
 /* Free data */
 free(cbeg);
 free(cind);
```

```
free(cval);
free(sense);
for (i=0; i<numremoved; ++i) {
   free(removed[i]);
}
free(removed);

/* Free model */

GRBfreemodel(model);

/* Free environment */

GRBfreeenv(env);

return 0;
}</pre>
```

workforce3_c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
   particular day. If the problem cannot be solved, add slack variables
   to determine which constraints cannot be satisfied, and how much
   they need to be relaxed. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include "gurobi_c.h"
#define xcol(w,s) nShifts*w+s
#define MAXSTR
                   128
int
main(int
           argc,
     char *argv[])
  GRBenv
           *env = NULL;
  GRBmodel *model = NULL;
  int
           error = 0, status;
            s, w, col;
  int
  int
           *cbeg = NULL;
  int
           *cind = NULL;
  int
            idx;
  double
           *cval = NULL;
           *sense = NULL;
  char
  char
            vname[MAXSTR];
  double
            obj;
  int
            i, j, numvars, numconstrs;
  int
           *vbeg = NULL;
  int
           *vind = NULL;
  double
           *vval = NULL;
  double
           *vobj = NULL;
  double
            sol;
           *cname, *sname;
  char
            varnamesct = 0;
  int
  char
          **varnames = NULL;
  /* Sample data */
```

```
const int nShifts = 14;
const int nWorkers = 7;
/* Sets of days and workers */
char* Shifts[] =
  { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
    "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
    "Sun14" }:
char* Workers[] =
  { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
/* Number of workers required for each shift */
double shiftRequirements[] =
  { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
/* Amount each worker is paid to work one shift */
double pay[] = { 10, 12, 10, 8, 8, 9, 11 };
/* Worker availability: 0 if the worker is unavailable for a shift */
double availability[][14] =
  { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
    \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\},\
    { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
   { 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1 },
   \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
    { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
/* Create environment */
error = GRBloadenv(&env, "workforce3.log");
if (error) goto QUIT;
/* Create initial model */
error = GRBnewmodel(env, &model, "workforce3", nWorkers * nShifts,
                   NULL, NULL, NULL, NULL, NULL);
if (error) goto QUIT;
/* Initialize assignment decision variables:
   x[w][s] == 1 if worker w is assigned
   to shift s. Since an assignment model always produces integer
   solutions, we use continuous variables and solve as an LP. */
for (w = 0; w < nWorkers; ++w)
 for (s = 0; s < nShifts; ++s)
  {
```

```
col = xcol(w, s);
    sprintf(vname, "%s.%s", Workers[w], Shifts[s]);
    error = GRBsetdblattrelement(model, "UB", col, availability[w][s]);
    if (error) goto QUIT;
    error = GRBsetdblattrelement(model, "Obj", col, pay[w]);
    if (error) goto QUIT;
    error = GRBsetstrattrelement(model, "VarName", col, vname);
    if (error) goto QUIT;
  }
}
/* The objective is to minimize the total pay costs */
error = GRBsetintattr(model, "ModelSense", 1);
if (error) goto QUIT;
/* Make space for constraint data */
cbeg = malloc(sizeof(int) * nShifts);
if (!cbeg) goto QUIT;
cind = malloc(sizeof(int) * nShifts * nWorkers);
if (!cind) goto QUIT;
cval = malloc(sizeof(double) * nShifts * nWorkers);
if (!cval) goto QUIT;
sense = malloc(sizeof(char) * nShifts);
if (!sense) goto QUIT;
/* Constraint: assign exactly shiftRequirements[s] workers
   to each shift s */
idx = 0;
for (s = 0; s < nShifts; ++s)
  cbeg[s] = idx;
  sense[s] = GRB_EQUAL;
  for (w = 0; w < nWorkers; ++w)
    cind[idx] = xcol(w, s);
    cval[idx++] = 1.0;
  }
}
error = GRBaddconstrs(model, nShifts, idx, cbeg, cind, cval, sense,
                      shiftRequirements, Shifts);
if (error) goto QUIT;
/* Optimize */
error = GRBoptimize(model);
if (error) goto QUIT;
```

```
error = GRBgetintattr(model, "Status", &status);
if (error) goto QUIT;
if (status == GRB_UNBOUNDED)
  printf("The model cannot be solved because it is unbounded\n");
  goto QUIT;
}
if (status == GRB_OPTIMAL)
  error = GRBgetdblattr(model, "ObjVal", &obj);
  if (error) goto QUIT;
  printf("The optimal objective is f^n, obj);
  goto QUIT;
}
if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
  printf("Optimization was stopped with status %i\n", status);
  goto QUIT;
}
/* Add slack variables to make the model feasible */
printf("The model is infeasible; adding slack variables\n");
/* Determine the matrix size before adding the slacks */
error = GRBgetintattr(model, "NumVars", &numvars);
if (error) goto QUIT;
error = GRBgetintattr(model, "NumConstrs", &numconstrs);
if (error) goto QUIT;
/* Set original objective coefficients to zero */
for (j = 0; j < numvars; ++j)
  error = GRBsetdblattrelement(model, "Obj", j, 0.0);
  if (error) goto QUIT;
}
/* Add a new slack variable to each shift constraint so that the shifts
   can be satisfied */
vbeg = malloc(sizeof(int) * numconstrs);
if (!vbeg) goto QUIT;
vind = malloc(sizeof(int) * numconstrs);
if (!vind) goto QUIT;
vval = malloc(sizeof(double) * numconstrs);
if (!vval) goto QUIT;
vobj = malloc(sizeof(double) * numconstrs);
```

```
if (!vobj) goto QUIT;
varnames = calloc(numconstrs, sizeof(char*));
if (!varnames) goto QUIT;
for (i = 0; i < numconstrs; ++i)</pre>
{
  vbeg[i] = i;
  vind[i] = i;
  vval[i] = 1.0;
  vobj[i] = 1.0;
  error = GRBgetstrattrelement(model, "ConstrName", i, &cname);
  if (error) goto QUIT;
  varnames[i] = malloc(sizeof(char*) * (6 + strlen(cname)));
  if (!varnames[i]) goto QUIT;
  varnamesct++;
  strcpy(varnames[i], cname);
  strcat(varnames[i], "Slack");
}
error = GRBaddvars(model, numconstrs, numconstrs,
                   vbeg, vind, vval, vobj, NULL, NULL, NULL, varnames);
if (error) goto QUIT;
error = GRBupdatemodel(model);
if (error) goto QUIT;
/* Solve the model with slacks */
error = GRBoptimize(model);
if (error) goto QUIT;
error = GRBgetintattr(model, "Status", &status);
if (error) goto QUIT;
if ((status == GRB_INF_OR_UNBD) || (status == GRB_INFEASIBLE) ||
    (status == GRB_UNBOUNDED))
{
  printf("The model with slacks cannot be solved "
         "because it is infeasible or unbounded\n");
  goto QUIT;
if (status != GRB_OPTIMAL)
  printf("Optimization was stopped with status %i\n", status);
  goto QUIT;
}
printf("\nSlack values:\n");
for (j = numvars; j < numvars + numconstrs; ++j)</pre>
```

```
error = GRBgetdblattrelement(model, "X", j, &sol);
    if (error) goto QUIT;
    if (sol > 1e-6)
      error = GRBgetstrattrelement(model, "VarName", j, &sname);
      if (error) goto QUIT;
      printf("%s = %f\n", sname, sol);
  }
QUIT:
  /* Error reporting */
  if (error)
    printf("ERROR: %s\n", GRBgeterrormsg(env));
    exit(1);
  }
  /* Free data */
  free(cbeg);
  free(cind);
  free(cval);
  free(sense);
  free(vbeg);
  free(vind);
  free(vval);
  free(vobj);
  for (i = 0; i < varnamesct; ++i)
    free(varnames[i]);
  free(varnames);
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
```

```
return 0;
}
```

workforce4 c.c

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. We use Pareto optimization to solve the model:
  first, we minimize the linear sum of the slacks. Then, we constrain
  the sum of the slacks, and we minimize a quadratic objective that
  tries to balance the workload among the workers. */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include "gurobi_c.h"
int solveAndPrint(GRBmodel* model,
                  int nShifts, int nWorkers, char** Workers,
                  int* status);
#define xcol(w,s)
                          nShifts*w+s
#define slackcol(s)
                          nShifts*nWorkers+s
#define totSlackcol
                          nShifts*(nWorkers+1)
#define totShiftscol(w)
                         nShifts*(nWorkers+1)+1+w
#define avgShiftscol
                         (nShifts+1)*(nWorkers+1)
#define diffShiftscol(w) (nShifts+1)*(nWorkers+1)+1+w
#define MAXSTR
                   128
int
main(int
          argc,
     char *argv[])
{
 GRBenv
           *env = NULL;
  GRBmodel *model = NULL;
  int
            error = 0, status;
  int
           s, w, col;
  int
           *cbeg = NULL;
  int
           *cind = NULL;
  int
           idx;
  double
          *cval = NULL;
           *sense = NULL;
  char
           vname[MAXSTR], cname[MAXSTR];
  char
  double
           val;
```

```
/* Sample data */
const int nShifts = 14;
const int nWorkers = 7;
/* Sets of days and workers */
char* Shifts[] =
  { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
    "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
    "Sun14" };
char* Workers[] =
  { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
/* Number of workers required for each shift */
double shiftRequirements[] =
  {3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5};
/* Worker availability: 0 if the worker is unavailable for a shift */
double availability[][14] =
  { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
    { 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 },
   { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
   \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
   { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
/* Create environment */
error = GRBloadenv(&env, "workforce4.log");
if (error) goto QUIT;
/* Create initial model */
error = GRBnewmodel(env, &model, "workforce4",
                   (nShifts + 1) * (nWorkers + 1),
                   NULL, NULL, NULL, NULL, NULL);
if (error) goto QUIT;
/* Initialize assignment decision variables:
  x[w][s] == 1 if worker w is assigned to shift s.
  This is no longer a pure assignment model, so we must
  use binary variables. */
for (w = 0; w < nWorkers; ++w)
  for (s = 0; s < nShifts; ++s)
   col = xcol(w, s);
```

```
sprintf(vname, "%s.%s", Workers[w], Shifts[s]);
    error = GRBsetcharattrelement(model, "VType", col, GRB_BINARY);
    if (error) goto QUIT;
    error = GRBsetdblattrelement(model, "UB", col, availability[w][s]);
    if (error) goto QUIT;
    error = GRBsetstrattrelement(model, "VarName", col, vname);
    if (error) goto QUIT;
}
/* Initialize slack decision variables */
for (s = 0; s < nShifts; ++s)
  sprintf(vname, "%sSlack", Shifts[s]);
  error = GRBsetstrattrelement(model, "VarName", slackcol(s), vname);
  if (error) goto QUIT;
}
/* Initialize total slack decision variable */
error = GRBsetstrattrelement(model, "VarName", totSlackcol, "totSlack");
if (error) goto QUIT;
/* Initialize variables to count the total shifts worked by each worker */
for (w = 0; w < nWorkers; ++w)
{
  sprintf(vname, "%sTotShifts", Workers[w]);
  error = GRBsetstrattrelement(model, "VarName", totShiftscol(w), vname);
  if (error) goto QUIT;
/* The objective is to minimize the sum of the slacks */
error = GRBsetintattr(model, "ModelSense", 1);
if (error) goto QUIT;
error = GRBsetdblattrelement(model, "Obj", totSlackcol, 1.0);
if (error) goto QUIT;
/* Make space for constraint data */
cbeg = malloc(sizeof(int) * nShifts);
if (!cbeg) goto QUIT;
cind = malloc(sizeof(int) * nShifts * (nWorkers + 1));
if (!cind) goto QUIT;
cval = malloc(sizeof(double) * nShifts * (nWorkers + 1));
if (!cval) goto QUIT;
sense = malloc(sizeof(char) * nShifts);
if (!sense) goto QUIT;
```

```
/* Constraint: assign exactly shiftRequirements[s] workers
   to each shift s, plus the slack */
idx = 0;
for (s = 0; s < nShifts; ++s)
  cbeg[s] = idx;
  sense[s] = GRB_EQUAL;
  for (w = 0; w < nWorkers; ++w)
    cind[idx] = xcol(w, s);
    cval[idx++] = 1.0;
  cind[idx] = slackcol(s);
  cval[idx++] = 1.0;
}
error = GRBaddconstrs(model, nShifts, idx, cbeg, cind, cval, sense,
                      shiftRequirements, Shifts);
if (error) goto QUIT;
/* Constraint: set totSlack column equal to the total slack */
idx = 0;
for (s = 0; s < nShifts; ++s)
  cind[idx] = slackcol(s);
  cval[idx++] = 1.0;
cind[idx] = totSlackcol;
cval[idx++] = -1.0;
error = GRBaddconstr(model, idx, cind, cval, GRB_EQUAL,
                     0.0, "totSlack");
if (error) goto QUIT;
/* Constraint: compute the total number of shifts for each worker */
for (w = 0; w < nWorkers; ++w)
  idx = 0;
  for (s = 0; s < nShifts; ++s)
    cind[idx] = xcol(w,s);
    cval[idx++] = 1.0;
  sprintf(cname, "totShifts%s", Workers[w]);
  cind[idx] = totShiftscol(w);
  cval[idx++] = -1.0;
```

```
error = GRBaddconstr(model, idx, cind, cval, GRB_EQUAL, 0.0, cname);
  if (error) goto QUIT;
}
/* Optimize */
error = solveAndPrint(model, nShifts, nWorkers, Workers, &status);
if (error) goto QUIT;
if (status != GRB_OPTIMAL) goto QUIT;
/* Constrain the slack by setting its upper and lower bounds */
error = GRBgetdblattrelement(model, "X", totSlackcol, &val);
if (error) goto QUIT;
error = GRBsetdblattrelement(model, "UB", totSlackcol, val);
if (error) goto QUIT;
error = GRBsetdblattrelement(model, "LB", totSlackcol, val);
if (error) goto QUIT;
/* Variable to count the average number of shifts worked */
error = GRBaddvar(model, 0, NULL, NULL, 0, 0, GRB_INFINITY, GRB_CONTINUOUS,
                  "avgShifts");
if (error) goto QUIT;
/* Variables to count the difference from average for each worker;
   note that these variables can take negative values. */
error = GRBaddvars(model, nWorkers, O, NULL, NULL, NULL, NULL, NULL, NULL,
                   NULL, NULL);
if (error) goto QUIT;
error = GRBupdatemodel(model);
if (error) goto QUIT;
for (w = 0; w < nWorkers; ++w)
  sprintf(vname, "%sDiff", Workers[w]);
  error = GRBsetstrattrelement(model, "VarName", diffShiftscol(w), vname);
  if (error) goto QUIT;
  error = GRBsetdblattrelement(model, "LB", diffShiftscol(w), -GRB_INFINITY);
  if (error) goto QUIT;
}
/* Constraint: compute the average number of shifts worked */
idx = 0;
for (w = 0; w < nWorkers; ++w) {
  cind[idx] = totShiftscol(w);
  cval[idx++] = 1.0;
```

```
}
  cind[idx] = avgShiftscol;
  cval[idx++] = -nWorkers;
  error = GRBaddconstr(model, idx, cind, cval, GRB_EQUAL, 0.0, "avgShifts");
  if (error) goto QUIT;
 // Constraint: compute the difference from the average number of shifts
 for (w = 0; w < nWorkers; ++w) {
    cind[0] = totShiftscol(w);
    cval[0] = 1.0;
    cind[1] = avgShiftscol;
    cval[1] = -1.0;
    cind[2] = diffShiftscol(w);
    cval[2] = -1.0;
    sprintf(cname, "%sDiff", Workers[w]);
    error = GRBaddconstr(model, 3, cind, cval, GRB_EQUAL, 0.0, cname);
    if (error) goto QUIT;
  }
  /* Objective: minimize the sum of the square of the difference from the
     average number of shifts worked */
  error = GRBsetdblattrelement(model, "Obj", totSlackcol, 0.0);
  if (error) goto QUIT;
 for (w = 0; w < nWorkers; ++w)
    cind[w] = diffShiftscol(w);
    cval[w] = 1.0;
  error = GRBaddqpterms(model, nWorkers, cind, cind, cval);
  if (error) goto QUIT;
  /* Optimize */
  error = solveAndPrint(model, nShifts, nWorkers, Workers, &status);
  if (error) goto QUIT;
  if (status != GRB_OPTIMAL) goto QUIT;
QUIT:
 /* Error reporting */
  if (error)
   printf("ERROR: %s\n", GRBgeterrormsg(env));
```

```
exit(1);
  /* Free data */
  free(cbeg);
  free(cind);
  free(cval);
  free(sense);
  /* Free model */
  GRBfreemodel(model);
  /* Free environment */
  GRBfreeenv(env);
  return 0;
}
int solveAndPrint(GRBmodel* model,
                  int nShifts, int nWorkers, char** Workers,
                  int* status)
{
  int error, w;
  double val;
  error = GRBoptimize(model);
  if (error) return error;
  error = GRBgetintattr(model, "Status", status);
  if (error) return error;
  if ((*status == GRB_INF_OR_UNBD) || (*status == GRB_INFEASIBLE) ||
      (*status == GRB_UNBOUNDED))
    printf("The model cannot be solved "
           "because it is infeasible or unbounded\n");
   return 0;
  }
  if (*status != GRB_OPTIMAL)
    printf("Optimization was stopped with status %i\n", *status);
```

```
return 0;
}

/* Print total slack and the number of shifts worked for each worker */
error = GRBgetdblattrelement(model, "X", totSlackcol, &val);
if (error) return error;

printf("\nTotal slack required: %f\n", val);
for (w = 0; w < nWorkers; ++w)
{
   error = GRBgetdblattrelement(model, "X", totShiftscol(w), &val);
   if (error) return error;
   printf("%s worked %f shifts\n", Workers[w], val);
}
printf("\n");
return 0;
}</pre>
```

3.2 C++ Examples

This section includes source code for all of the Gurobi C++ examples. The same source code can be found in the examples/c++ directory of the Gurobi distribution.

```
callback c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP or a MIP from a file, sets a callback
   to monitor the optimization progress and to output some progress
   information to the screen and to a log file. If it is a MIP and 10%
   gap is reached, then it aborts */
#include "gurobi_c++.h"
#include <cmath>
using namespace std;
class mycallback: public GRBCallback
 public:
    GRBVar* vars;
    int numvars;
   double lastnode;
    double lastiter;
    mycallback(GRBVar* xvars, int xnumvars) {
      vars = xvars;
      numvars = xnumvars;
      lastnode = lastiter = -1;
 protected:
    void callback () {
      try {
        if (where == GRB_CB_MESSAGE) {
          // Message callback
          string msg = getStringInfo(GRB_CB_MSG_STRING);
          cout << msg;</pre>
        } else if (where == GRB_CB_PRESOLVE) {
          // Presolve callback
          int cdels = getIntInfo(GRB_CB_PRE_COLDEL);
          int rdels = getIntInfo(GRB_CB_PRE_ROWDEL);
          cout << cdels << " columns and " << rdels</pre>
               << " rows are removed" << endl;
        } else if (where == GRB_CB_SIMPLEX) {
          // Simplex callback
          double itcnt = getDoubleInfo(GRB_CB_SPX_ITRCNT);
```

```
if (itcnt - lastiter >= 100) {
      lastiter = itcnt;
      double obj = getDoubleInfo(GRB_CB_SPX_OBJVAL);
      double pinf = getDoubleInfo(GRB_CB_SPX_PRIMINF);
      double dinf = getDoubleInfo(GRB_CB_SPX_DUALINF);
      int ispert = getIntInfo(GRB_CB_SPX_ISPERT);
      char ch;
      if (ispert == 0)
                         ch = ', ';
      else if (ispert == 1) ch = 'S';
                            ch = 'P';
      cout << itcnt << " " << obj << ch << " " << pinf
           << " " << dinf << endl;
  } else if (where == GRB_CB_MIP) {
    // General MIP callback
    double nodecnt = getDoubleInfo(GRB_CB_MIP_NODCNT);
    if (nodecnt - lastnode >= 100) {
      lastnode = nodecnt;
      double objbst = getDoubleInfo(GRB_CB_MIP_OBJBST);
      double objbnd = getDoubleInfo(GRB_CB_MIP_OBJBND);
      if (fabs(objbst - objbnd) < 0.1 * (1.0 + fabs(objbst)))
        abort();
      int actnodes = (int) getDoubleInfo(GRB_CB_MIP_NODLFT);
      int itcnt = (int) getDoubleInfo(GRB_CB_MIP_ITRCNT);
      int solcnt = getIntInfo(GRB_CB_MIP_SOLCNT);
      int cutcnt = getIntInfo(GRB_CB_MIP_CUTCNT);
      cout << nodecnt << " " << actnodes << " " << itcnt << " "
           << objbst << " " << objbnd << " " << solcnt << " "
           << cutcnt << endl;
    }
  } else if (where == GRB_CB_MIPSOL) {
    // MIP solution callback
    double obj
                   = getDoubleInfo(GRB_CB_MIPSOL_OBJ);
           nodecnt = (int) getDoubleInfo(GRB_CB_MIPSOL_NODCNT);
    double* x = getSolution(vars, numvars);
    cout << "**** New solution at node " << nodecnt << ", obj "</pre>
                       << obj << ", x[0] = " << x[0] << "****" << endl;
   delete[] x;
  }
} catch (GRBException e) {
  cout << "Error number: " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
} catch (...) {
  cout << "Error during callback" << endl;</pre>
```

}

```
}
};
int
main(int
           argc,
     char *argv[])
  if (argc < 2) {
    cout << "Usage: callback_c++ filename" << endl;</pre>
    return 1;
 }
 GRBEnv *env = 0;
 GRBVar *vars = 0;
 try {
    env = new GRBEnv();
    GRBModel model = GRBModel(*env, argv[1]);
    model.getEnv().set(GRB_IntParam_OutputFlag, 0);
    int numvars = model.get(GRB_IntAttr_NumVars);
    vars = model.getVars();
    // Create a callback object and associate it with the model
    mycallback cb = mycallback(vars, numvars);
    model.setCallback(&cb);
    model.optimize();
    for (int j = 0; j < numvars; j++) {
      GRBVar v = vars[j];
      cout << v.get(GRB_StringAttr_VarName) << " "</pre>
           << v.get(GRB_DoubleAttr_X) << endl;</pre>
  } catch (GRBException e) {
    cout << "Error number: " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
 } catch (...) {
    cout << "Error during optimization" << endl;</pre>
  }
  delete[] vars;
  delete env;
```

```
return 0;
}
```

```
dense c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                x + y + x^2 + x*y + y^2 + y*z + z^2
     subject to x + 2y + 3z >= 4
                x + y
                              >= 1
  The example illustrates the use of dense matrices to store A and Q
   (and dense vectors for the other relevant data). We don't recommend
  that you use dense matrices, but this example may be helpful if you
  already have your data in this format.
*/
#include "gurobi_c++.h"
using namespace std;
static bool
dense_optimize(GRBEnv* env,
                      rows,
               int
               int
                       cols,
                             /* linear portion of objective function */
               double* c,
                             /* quadratic portion of objective function */
              double* Q,
              double* A,
                             /* constraint matrix */
                       sense, /* constraint senses */
               double* rhs, /* RHS vector */
                            /* variable lower bounds */
               double* lb,
                            /* variable upper bounds */
              double* ub.
                     vtype, /* variable types (continuous, binary, etc.) */
               double* solution,
               double* objvalP)
{
  GRBModel model = GRBModel(*env);
  int i, j;
  bool success = false;
  /* Add variables to the model */
 GRBVar* vars = model.addVars(lb, ub, NULL, vtype, NULL, cols);
 model.update();
 /* Populate A matrix */
 for (i = 0; i < rows; i++) {
```

```
GRBLinExpr lhs = 0;
    for (j = 0; j < cols; j++)
      if (A[i*cols+j] != 0)
        lhs += A[i*cols+j]*vars[j];
    model.addConstr(lhs, sense[i], rhs[i]);
  }
  GRBQuadExpr obj = 0;
  for (j = 0; j < cols; j++)
    obj += c[j]*vars[j];
  for (i = 0; i < cols; i++)
    for (j = 0; j < cols; j++)
      if (Q[i*cols+j] != 0)
        obj += Q[i*cols+j]*vars[i]*vars[j];
  model.setObjective(obj);
  model.update();
  model.write("dense.lp");
  model.optimize();
  if (model.get(GRB_IntAttr_Status) == GRB_OPTIMAL) {
    *objvalP = model.get(GRB_DoubleAttr_ObjVal);
    for (i = 0; i < cols; i++)
      solution[i] = vars[i].get(GRB_DoubleAttr_X);
    success = true;
  delete[] vars;
  return success;
int
main(int
           argc,
     char *argv[])
  GRBEnv* env = 0;
  try {
    env = new GRBEnv();
    double c[] = \{1, 1, 0\};
    double Q[3][3] = \{\{1, 1, 0\}, \{0, 1, 1\}, \{0, 0, 1\}\};
    double A[2][3] = \{\{1, 2, 3\}, \{1, 1, 0\}\};
```

}

{

```
sense[] = {'>', '>'};
    char
    double rhs[]
                   = \{4, 1\};
    double lb[]
                     = \{0, 0, 0\};
    bool
            success;
    double objval, sol[3];
    success = dense_optimize(env, 2, 3, c, &Q[0][0], &A[0][0], sense, rhs,
                              lb, NULL, NULL, sol, &objval);
    cout << "x: " << sol[0] << " y: " << sol[1] << " z: " << sol[2] << endl;</pre>
  } catch(GRBException e) {
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  } catch(...) {
    cout << "Exception during optimization" << endl;</pre>
  }
  delete env;
  return 0;
}
```

```
diet c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve the classic diet model, showing how to add constraints
  to an existing model. */
#include "gurobi_c++.h"
using namespace std;
void printSolution(GRBModel& model, int nCategories, int nFoods,
                   GRBVar* buy, GRBVar* nutrition) throw(GRBException);
int
main(int argc,
     char *argv[])
  GRBEnv* env = 0;
  GRBVar* nutrition = 0;
 GRBVar* buy = 0;
 try
  {
   // Nutrition guidelines, based on
    // USDA Dietary Guidelines for Americans, 2005
    // http://www.health.gov/DietaryGuidelines/dga2005/
    const int nCategories = 4;
    string Categories[] =
      { "calories", "protein", "fat", "sodium" };
    double minNutrition[] = { 1800, 91, 0, 0 };
    double maxNutrition[] = { 2200, GRB_INFINITY, 65, 1779 };
    // Set of foods
    const int nFoods = 9;
    string Foods[] =
      { "hamburger", "chicken", "hot dog", "fries",
        "macaroni", "pizza", "salad", "milk", "ice cream" };
    double cost[] =
      { 2.49, 2.89, 1.50, 1.89, 2.09, 1.99, 2.49, 0.89, 1.59 };
    // Nutrition values for the foods
    double nutritionValues[][nCategories] = {
                      { 410, 24, 26, 730 },
                                               // hamburger
                      { 420, 32, 10, 1190 },
                                               // chicken
                      { 560, 20, 32, 1800 }, // hot dog
                      { 380, 4, 19, 270 },
                                               // fries
```

```
// macaroni
                  { 320, 12, 10, 930 },
                  { 320, 15, 12, 820 },
                                          // pizza
                  { 320, 31, 12, 1230 }, // salad
                  { 100, 8, 2.5, 125 },
                                           // milk
                  { 330, 8, 10, 180 }
                                           // ice cream
                };
// Model
env = new GRBEnv();
GRBModel model = GRBModel(*env);
model.set(GRB_StringAttr_ModelName, "diet");
// Create decision variables for the nutrition information,
// which we limit via bounds
nutrition = model.addVars(minNutrition, maxNutrition, 0, 0,
                          Categories, nCategories);
// Create decision variables for the foods to buy
buy = model.addVars(0, 0, cost, 0, Foods, nFoods);
// The objective is to minimize the costs
model.set(GRB_IntAttr_ModelSense, 1);
// Update model to integrate new variables
model.update();
// Nutrition constraints
for (int i = 0; i < nCategories; ++i)</pre>
 GRBLinExpr ntot = 0;
 for (int j = 0; j < nFoods; ++j)
   ntot += nutritionValues[j][i] * buy[j];
 model.addConstr(ntot == nutrition[i], Categories[i]);
// Solve
model.optimize();
printSolution(model, nCategories, nFoods, buy, nutrition);
cout << "\nAdding constraint: at most 6 servings of dairy" << endl;</pre>
model.addConstr(buy[7] + buy[8] <= 6.0, "limit_dairy");</pre>
// Solve
```

```
model.optimize();
    printSolution(model, nCategories, nFoods, buy, nutrition);
  }
  catch (GRBException e)
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  }
  catch (...)
    cout << "Exception during optimization" << endl;</pre>
  delete[] nutrition;
  delete[] buy;
  delete env;
  return 0;
}
void printSolution(GRBModel& model, int nCategories, int nFoods,
                    GRBVar* buy, GRBVar* nutrition) throw(GRBException)
  if (model.get(GRB_IntAttr_Status) == GRB_OPTIMAL)
  {
    cout << "\nCost: " << model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
    cout << "\nBuy:" << endl;</pre>
    for (int j = 0; j < nFoods; ++j)
      if (buy[j].get(GRB_DoubleAttr_X) > 0.0001)
        cout << buy[j].get(GRB_StringAttr_VarName) << " " <<</pre>
        buy[j].get(GRB_DoubleAttr_X) << endl;</pre>
      }
    }
    cout << "\nNutrition:" << endl;</pre>
    for (int i = 0; i < nCategories; ++i)</pre>
      cout << nutrition[i].get(GRB_StringAttr_VarName) << " " <<</pre>
      nutrition[i].get(GRB_DoubleAttr_X) << endl;</pre>
    }
  }
  else
    cout << "No solution" << endl;</pre>
```

} }

```
facility c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Facility location: a company currently ships its product from 5 plants
  to 4 warehouses. It is considering closing some plants to reduce
  costs. What plant(s) should the company close, in order to minimize
  transportation and fixed costs?
  Based on an example from Frontline Systems:
  http://www.solver.com/disfacility.htm
  Used with permission.
#include "gurobi_c++.h"
#include <sstream>
using namespace std;
int
main(int argc,
     char *argv[])
  GRBEnv* env = 0;
 GRBVar* open = 0;
 GRBVar** transport = 0;
  int transportCt = 0;
 try
  {
    // Number of plants and warehouses
    const int nPlants = 5;
    const int nWarehouses = 4;
    // Warehouse demand in thousands of units
    double Demand[] = { 15, 18, 14, 20 };
    // Plant capacity in thousands of units
    double Capacity[] = { 20, 22, 17, 19, 18 };
    // Fixed costs for each plant
    double FixedCosts[] =
      { 12000, 15000, 17000, 13000, 16000 };
    // Transportation costs per thousand units
    double TransCosts[][nPlants] = {
                                     { 4000, 2000, 3000, 2500, 4500 },
```

```
{ 2500, 2600, 3400, 3000, 4000 },
                                  { 1200, 1800, 2600, 4100, 3000 },
                                 { 2200, 2600, 3100, 3700, 3200 }
                                };
// Model
env = new GRBEnv();
GRBModel model = GRBModel(*env);
model.set(GRB_StringAttr_ModelName, "facility");
// Plant open decision variables: open[p] == 1 if plant p is open.
open = model.addVars(nPlants, GRB_BINARY);
model.update();
int p;
for (p = 0; p < nPlants; ++p)
  ostringstream vname;
  vname << "Open" << p;</pre>
  open[p].set(GRB_DoubleAttr_Obj, FixedCosts[p]);
  open[p].set(GRB_StringAttr_VarName, vname.str());
}
// Transportation decision variables: how much to transport from
// a plant p to a warehouse w
transport = new GRBVar* [nWarehouses];
int w;
for (w = 0; w < nWarehouses; ++w)
 transport[w] = model.addVars(nPlants);
 transportCt++;
 model.update();
 for (p = 0; p < nPlants; ++p)
  {
    ostringstream vname;
    vname << "Trans" << p << "." << w;</pre>
   transport[w][p].set(GRB_DoubleAttr_Obj, TransCosts[w][p]);
    transport[w][p].set(GRB_StringAttr_VarName, vname.str());
 }
}
// The objective is to minimize the total fixed and variable costs
model.set(GRB_IntAttr_ModelSense, 1);
// Update model to integrate new variables
model.update();
```

```
// Production constraints
// Note that the right-hand limit sets the production to zero if
// the plant is closed
for (p = 0; p < nPlants; ++p)
  GRBLinExpr ptot = 0;
  for (w = 0; w < nWarehouses; ++w)</pre>
    ptot += transport[w][p];
  }
  ostringstream cname;
  cname << "Capacity" << p;</pre>
  model.addConstr(ptot <= Capacity[p] * open[p], cname.str());</pre>
// Demand constraints
for (w = 0; w < nWarehouses; ++w)
{
  GRBLinExpr dtot = 0;
  for (p = 0; p < nPlants; ++p)
    dtot += transport[w][p];
  ostringstream cname;
  cname << "Demand" << w;</pre>
  model.addConstr(dtot == Demand[w], cname.str());
}
// Guess at the starting point: close the plant with the highest
// fixed costs; open all others
// First, open all plants
for (p = 0; p < nPlants; ++p)
  open[p].set(GRB_DoubleAttr_Start, 1.0);
}
// Now close the plant with the highest fixed cost
cout << "Initial guess:" << endl;</pre>
double maxFixed = -GRB_INFINITY;
for (p = 0; p < nPlants; ++p)
  if (FixedCosts[p] > maxFixed)
  {
```

```
maxFixed = FixedCosts[p];
    }
  }
  for (p = 0; p < nPlants; ++p)
    if (FixedCosts[p] == maxFixed)
      open[p].set(GRB_DoubleAttr_Start, 0.0);
      cout << "Closing plant " << p << endl << endl;</pre>
      break;
    }
  }
  // Use barrier to solve root relaxation
  model.getEnv().set(GRB_IntParam_Method, GRB_METHOD_BARRIER);
  // Solve
  model.optimize();
  // Print solution
  cout << "\nTOTAL COSTS: " << model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
  cout << "SOLUTION:" << endl;</pre>
  for (p = 0; p < nPlants; ++p)
    if (open[p].get(GRB_DoubleAttr_X) == 1.0)
      cout << "Plant " << p << " open:" << endl;</pre>
      for (w = 0; w < nWarehouses; ++w)
        if (transport[w][p].get(GRB_DoubleAttr_X) > 0.0001)
        {
          cout << " Transport " <<</pre>
          transport[w][p].get(GRB_DoubleAttr_X) <<</pre>
          " units to warehouse " << w << endl;
        }
      }
    }
    else
    {
      cout << "Plant " << p << " closed!" << endl;</pre>
    }
  }
}
catch (GRBException e)
```

```
{
   cout << "Error code = " << e.getErrorCode() << endl;
   cout << e.getMessage() << endl;
}
catch (...)
{
   cout << "Exception during optimization" << endl;
}

delete[] open;
for (int i = 0; i < transportCt; ++i) {
   delete[] transport[i];
}
delete[] transport;
delete env;
return 0;
}</pre>
```

```
feasopt c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, adds artificial
   variables to each constraint, and then minimizes the sum of the
   artificial variables. A solution with objective zero corresponds
   to a feasible solution to the input model.
   We can also use FeasRelax feature to do it. In this example, we
   use minrelax=1, i.e. optimizing the returned model finds a solution
   that minimizes the original objective, but only from among those
   solutions that minimize the sum of the artificial variables. */
#include "gurobi_c++.h"
using namespace std;
int
main(int argc,
     char *argv[])
 if (argc < 2)
    cout << "Usage: feasopt_c++ filename" << endl;</pre>
   return 1;
  }
  GRBEnv* env = 0;
 GRBConstr* c = 0;
 try
  {
    env = new GRBEnv();
   GRBModel feasmodel = GRBModel(*env, argv[1]);
    // Create a copy to use FeasRelax feature later */
    GRBModel feasmodel1 = GRBModel(feasmodel);
    // clear objective
    feasmodel.setObjective(GRBLinExpr(0.0));
   // add slack variables
    c = feasmodel.getConstrs();
    for (int i = 0; i < feasmodel.get(GRB_IntAttr_NumConstrs); ++i)</pre>
      char sense = c[i].get(GRB_CharAttr_Sense);
      if (sense != '>')
```

```
double coef = -1.0;
      feasmodel.addVar(0.0, GRB_INFINITY, 1.0, GRB_CONTINUOUS, 1,
                        &c[i], &coef, "ArtN_" +
                        c[i].get(GRB_StringAttr_ConstrName));
    }
    if (sense != '<')
      double coef = 1.0;
      feasmodel.addVar(0.0, GRB_INFINITY, 1.0, GRB_CONTINUOUS, 1,
                        &c[i], &coef, "ArtP_" +
                        c[i].get(GRB_StringAttr_ConstrName));
    }
  }
  feasmodel.update();
  // optimize modified model
  feasmodel.write("feasopt.lp");
  feasmodel.optimize();
  // use FeasRelax feature */
  feasmodel1.feasRelax(GRB_FEASRELAX_LINEAR, true, false, true);
  feasmodel1.write("feasopt1.lp");
  feasmodel1.optimize();
}
catch (GRBException e)
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
}
catch (...)
  cout << "Error during optimization" << endl;</pre>
delete[] c;
delete env;
return 0;
```

fixanddive c++.cpp /* Copyright 2013, Gurobi Optimization, Inc. */ /* Implement a simple MIP heuristic. Relax the model, sort variables based on fractionality, and fix the 25% of the fractional variables that are closest to integer variables. Repeat until either the relaxation is integer feasible or linearly infeasible. */ #include "gurobi_c++.h" #include <algorithm> #include <cmath> #include <deque> using namespace std; bool vcomp(GRBVar*, GRBVar*) throw(GRBException); int main(int argc, char *argv[]) if (argc < 2){ cout << "Usage: fixanddive_c++ filename" << endl;</pre> return 1; } GRBEnv* env = 0;GRBVar* x = 0;try { // Read model env = new GRBEnv(); GRBModel model = GRBModel(*env, argv[1]); // Collect integer variables and relax them // Note that we use GRBVar* to copy variables deque<GRBVar*> intvars; x = model.getVars(); for (int j = 0; j < model.get(GRB_IntAttr_NumVars); ++j)</pre> if (x[j].get(GRB_CharAttr_VType) != GRB_CONTINUOUS) intvars.push_back(&x[j]); x[j].set(GRB_CharAttr_VType, GRB_CONTINUOUS);

```
}
}
model.getEnv().set(GRB_IntParam_OutputFlag, 0);
model.optimize();
// Perform multiple iterations. In each iteration, identify the first
// quartile of integer variables that are closest to an integer value
// in the relaxation, fix them to the nearest integer, and repeat.
for (int iter = 0; iter < 1000; ++iter)</pre>
{
  // create a list of fractional variables, sorted in order of
  // increasing distance from the relaxation solution to the nearest
  // integer value
 deque<GRBVar*> fractional;
  for (size_t j = 0; j < intvars.size(); ++j)</pre>
    double sol = fabs(intvars[j]->get(GRB_DoubleAttr_X));
    if (fabs(sol - floor(sol + 0.5)) > 1e-5)
      fractional.push_back(intvars[j]);
    }
  }
  cout << "Iteration " << iter << ", obj " <<
 model.get(GRB_DoubleAttr_ObjVal) << ", fractional " <</pre>
  fractional.size() << endl;</pre>
  if (fractional.size() == 0)
  {
    cout << "Found feasible solution - objective " <<</pre>
    model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
    break;
  }
 // Fix the first quartile to the nearest integer value
  sort(fractional.begin(), fractional.end(), vcomp);
  int nfix = fractional.size() / 4;
 nfix = (nfix > 1) ? nfix : 1;
  for (int i = 0; i < nfix; ++i)</pre>
  {
    GRBVar* v = fractional[i];
```

```
double fixval = floor(v->get(GRB_DoubleAttr_X) + 0.5);
        v->set(GRB_DoubleAttr_LB, fixval);
        v->set(GRB_DoubleAttr_UB, fixval);
        cout << " Fix " << v->get(GRB_StringAttr_VarName) << " to " <</pre>
        fixval << " ( rel " << v->get(GRB_DoubleAttr_X) << " )" <<
        endl;
      }
      model.optimize();
      // Check optimization result
      if (model.get(GRB_IntAttr_Status) != GRB_OPTIMAL)
        cout << "Relaxation is infeasible" << endl;</pre>
        break;
      }
    }
  catch (GRBException e)
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  }
  catch (...)
    cout << "Error during optimization" << endl;</pre>
 delete[] x;
 delete env;
 return 0;
bool vcomp(GRBVar* v1,
           GRBVar* v2) throw(GRBException)
{
  double sol1 = fabs(v1->get(GRB_DoubleAttr_X));
  double sol2 = fabs(v2->get(GRB_DoubleAttr_X));
  double frac1 = fabs(sol1 - floor(sol1 + 0.5));
 double frac2 = fabs(sol2 - floor(sol2 + 0.5));
 return (frac1 < frac2);</pre>
```

```
lp_c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
   If the model is infeasible or unbounded, the example turns off
   presolve and solves the model again. If the model is infeasible,
   the example computes an Irreducible Infeasible Subsystem (IIS),
   and writes it to a file */
#include "gurobi_c++.h"
using namespace std;
int
main(int
           argc,
     char *argv[])
  if (argc < 2) {
    cout << "Usage: lp_c++ filename" << endl;</pre>
    return 1;
  }
 try {
    GRBEnv env = GRBEnv();
    GRBModel model = GRBModel(env, argv[1]);
    model.optimize();
    int optimstatus = model.get(GRB_IntAttr_Status);
    if (optimstatus == GRB_INF_OR_UNBD) {
      model.getEnv().set(GRB_IntParam_Presolve, 0);
      model.optimize();
      optimstatus = model.get(GRB_IntAttr_Status);
    }
    if (optimstatus == GRB_OPTIMAL) {
      double objval = model.get(GRB_DoubleAttr_ObjVal);
      cout << "Optimal objective: " << objval << endl;</pre>
    } else if (optimstatus == GRB_INFEASIBLE) {
      cout << "Model is infeasible" << endl;</pre>
      // compute and write out IIS
      model.computeIIS();
      model.write("model.ilp");
```

Ipmethod c++.cpp /* Copyright 2013, Gurobi Optimization, Inc. */ /* Solve a model with different values of the Method parameter; show which value gives the shortest solve time. */ #include "gurobi_c++.h" using namespace std; int main(int argc, char *argv[]) if (argc < 2)cout << "Usage: lpmethod_c++ filename" << endl;</pre> return 1; } try { // Read model GRBEnv env = GRBEnv(); GRBModel m = GRBModel(env, argv[1]); GRBEnv menv = m.getEnv(); // Solve the model with different values of Method bestMethod = -1;double bestTime = menv.get(GRB_DoubleParam_TimeLimit); for (int i = 0; $i \le 2$; ++i) { m.reset(); menv.set(GRB_IntParam_Method, i); m.optimize(); if (m.get(GRB_IntAttr_Status) == GRB_OPTIMAL) { bestTime = m.get(GRB_DoubleAttr_Runtime); bestMethod = i; // Reduce the TimeLimit parameter to save time // with other methods menv.set(GRB_DoubleParam_TimeLimit, bestTime); } } $\ensuremath{//}$ Report which method was fastest if (bestMethod == -1) {

cout << "Unable to solve this model" << endl;</pre>

```
Ipmod c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
   If the model can be solved, then it finds the smallest positive variable,
   sets its upper bound to zero, and resolves the model two ways:
   first with an advanced start, then without an advanced start
   (i.e. 'from scratch'). */
#include "gurobi_c++.h"
using namespace std;
int
main(int argc,
     char *argv[])
  if (argc < 2)
    cout << "Usage: lpmod_c++ filename" << endl;</pre>
    return 1;
  }
 GRBEnv* env = 0;
 GRBVar* v = 0;
 try
 {
    // Read model and determine whether it is an LP
    env = new GRBEnv();
    GRBModel model = GRBModel(*env, argv[1]);
    if (model.get(GRB_IntAttr_IsMIP) != 0)
      cout << "The model is not a linear program" << endl;</pre>
      return 1;
    model.optimize();
    int status = model.get(GRB_IntAttr_Status);
    if ((status == GRB_INF_OR_UNBD) || (status == GRB_INFEASIBLE) ||
        (status == GRB_UNBOUNDED))
      cout << "The model cannot be solved because it is "</pre>
      << "infeasible or unbounded" << endl;</pre>
      return 1;
```

```
}
if (status != GRB_OPTIMAL)
  cout << "Optimization was stopped with status " << status << endl;</pre>
  return 0;
}
// Find the smallest variable value
double minVal = GRB_INFINITY;
int minVar = 0;
v = model.getVars();
for (int j = 0; j < model.get(GRB_IntAttr_NumVars); ++j)</pre>
  double sol = v[j].get(GRB_DoubleAttr_X);
  if ((sol > 0.0001) && (sol < minVal) &&
      (v[j].get(GRB_DoubleAttr_LB) == 0.0))
  {
    minVal = sol;
    minVar = j;
  }
}
cout << "\n*** Setting " << v[minVar].get(GRB_StringAttr_VarName)</pre>
<< " from " << minVal << " to zero ***" << endl << endl;
v[minVar].set(GRB_DoubleAttr_UB, 0.0);
// Solve from this starting point
model.optimize();
// Save iteration & time info
double warmCount = model.get(GRB_DoubleAttr_IterCount);
double warmTime = model.get(GRB_DoubleAttr_Runtime);
// Reset the model and resolve
cout << "\n*** Resetting and solving "</pre>
<< "without an advanced start ***\n" << endl;</pre>
model.reset();
model.optimize();
// Save iteration & time info
double coldCount = model.get(GRB_DoubleAttr_IterCount);
double coldTime = model.get(GRB_DoubleAttr_Runtime);
cout << "\n*** Warm start: " << warmCount << " iterations, " <<
```

```
warmTime << " seconds" << endl;
  cout << "*** Cold start: " << coldCount << " iterations, " <<
  coldTime << " seconds" << endl;

}
catch (GRBException e)
{
  cout << "Error code = " << e.getErrorCode() << endl;
  cout << e.getMessage() << endl;
}
catch (...)
{
  cout << "Error during optimization" << endl;
}
delete[] v;
delete env;
return 0;
}</pre>
```

```
mip1 c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple MIP model:
     maximize
                 x +
                       y + 2z
     subject to x + 2y + 3z \le 4
                               >= 1
                 x +
                     У
     x, y, z binary
*/
#include "gurobi_c++.h"
using namespace std;
int
main(int
           argc,
     char *argv[])
{
  try {
    GRBEnv env = GRBEnv();
    GRBModel model = GRBModel(env);
    // Create variables
    GRBVar x = model.addVar(0.0, 1.0, 0.0, GRB_BINARY, "x");
    GRBVar y = model.addVar(0.0, 1.0, 0.0, GRB_BINARY, "y");
    GRBVar z = model.addVar(0.0, 1.0, 0.0, GRB_BINARY, "z");
    // Integrate new variables
    model.update();
    // Set objective: maximize x + y + 2z
    model.setObjective(x + y + 2 * z, GRB\_MAXIMIZE);
    // Add constraint: x + 2 y + 3 z \le 4
    model.addConstr(x + 2 * y + 3 * z \le 4, "c0");
    // Add constraint: x + y >= 1
    model.addConstr(x + y >= 1, "c1");
```

```
// Optimize model
    model.optimize();
    cout << x.get(GRB_StringAttr_VarName) << " "</pre>
          << x.get(GRB_DoubleAttr_X) << endl;</pre>
    cout << y.get(GRB_StringAttr_VarName) << " "</pre>
          << y.get(GRB_DoubleAttr_X) << endl;</pre>
    cout << z.get(GRB_StringAttr_VarName) << " "</pre>
          << z.get(GRB_DoubleAttr_X) << endl;</pre>
    cout << "Obj: " << model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
  } catch(GRBException e) {
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  } catch(...) {
    cout << "Exception during optimization" << endl;</pre>
  }
  return 0;
}
```

```
mip2 c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, solves it and
   prints the objective values from all feasible solutions
   generated while solving the MIP. Then it creates the fixed
   model and solves that model. */
#include "gurobi_c++.h"
#include <cmath>
using namespace std;
int
main(int
           argc,
     char *argv[])
  if (argc < 2) {
    cout << "Usage: mip2_c++ filename" << endl;</pre>
    return 1;
  }
  GRBEnv *env = 0;
  GRBVar *vars = 0, *fvars = 0;
  try {
    env = new GRBEnv();
    GRBModel model = GRBModel(*env, argv[1]);
    if (model.get(GRB_IntAttr_IsMIP) == 0) {
      throw GRBException("Model is not a MIP");
    model.optimize();
    int optimstatus = model.get(GRB_IntAttr_Status);
    cout << "Optimization complete" << endl;</pre>
    double objval = 0;
    if (optimstatus == GRB_OPTIMAL) {
      objval = model.get(GRB_DoubleAttr_ObjVal);
      cout << "Optimal objective: " << objval << endl;</pre>
    } else if (optimstatus == GRB_INF_OR_UNBD) {
      cout << "Model is infeasible or unbounded" << endl;</pre>
      return 0;
    } else if (optimstatus == GRB_INFEASIBLE) {
      cout << "Model is infeasible" << endl;</pre>
```

```
return 0;
} else if (optimstatus == GRB_UNBOUNDED) {
  cout << "Model is unbounded" << endl;</pre>
 return 0;
} else {
  cout << "Optimization was stopped with status = "</pre>
       << optimstatus << endl;
 return 0;
/* Iterate over the solutions and compute the objectives */
int numvars = model.get(GRB_IntAttr_NumVars);
vars = model.getVars();
model.getEnv().set(GRB_IntParam_OutputFlag, 0);
cout << endl;</pre>
for ( int k = 0; k < model.get(GRB_IntAttr_SolCount); ++k ) {</pre>
 model.getEnv().set(GRB_IntParam_SolutionNumber, k);
 double objn = 0.0;
 for (int j = 0; j < numvars; j++) {
    GRBVar v = vars[j];
    objn += v.get(GRB_DoubleAttr_Obj) * v.get(GRB_DoubleAttr_Xn);
  }
 cout << "Solution " << k << " has objective: " << objn << endl;</pre>
}
cout << endl;
model.getEnv().set(GRB_IntParam_OutputFlag, 1);
/* Create a fixed model, turn off presolve and solve */
GRBModel fixed = model.fixedModel();
fixed.getEnv().set(GRB_IntParam_Presolve, 0);
fixed.optimize();
int foptimstatus = fixed.get(GRB_IntAttr_Status);
if (foptimstatus != GRB_OPTIMAL) {
  cerr << "Error: fixed model isn't optimal" << endl;</pre>
 return 0;
}
```

```
double fobjval = fixed.get(GRB_DoubleAttr_ObjVal);
  if (fabs(fobjval - objval) > 1.0e-6 * (1.0 + fabs(objval))) {
    cerr << "Error: objective values are different" << endl;</pre>
    return 0;
  }
  /* Print values of nonzero variables */
  fvars = fixed.getVars();
  for (int j = 0; j < numvars; j++) {
    GRBVar v = fvars[j];
    if (v.get(GRB_DoubleAttr_X) != 0.0) {
      cout << v.get(GRB_StringAttr_VarName) << " "</pre>
            << v.get(GRB_DoubleAttr_X) << endl;</pre>
    }
  }
} catch(GRBException e) {
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
} catch (...) {
  cout << "Error during optimization" << endl;</pre>
delete[] fvars;
delete[] vars;
delete env;
return 0;
```

```
params c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Use parameters that are associated with a model.
   A MIP is solved for 5 seconds with different sets of parameters.
   The one with the smallest MIP gap is selected, and the optimization
   is resumed until the optimal solution is found.
*/
#include "gurobi_c++.h"
#include <cmath>
using namespace std;
double gap(GRBModel *model) throw(GRBException);
int
main(int argc,
     char *argv[])
 if (argc < 2)
    cout << "Usage: params_c++ filename" << endl;</pre>
   return 1;
  }
 GRBEnv* env = 0;
  GRBModel *bestModel = 0, *m = 0;
 try
  {
   // Read model and verify that it is a MIP
    env = new GRBEnv();
    GRBModel base = GRBModel(*env, argv[1]);
    if (base.get(GRB_IntAttr_IsMIP) == 0)
      cout << "The model is not an integer program" << endl;</pre>
      return 1;
    }
    // Set a 5 second time limit
    base.getEnv().set(GRB_DoubleParam_TimeLimit, 5);
    // Now solve the model with different values of MIPFocus,
    // using a pointer to save the best model
    double bestGap = GRB_INFINITY;
```

```
for (int i = 0; i \le 3; ++i)
    {
      m = new GRBModel(base);
      m->getEnv().set(GRB_IntParam_MIPFocus, i);
      m->optimize();
      if (bestModel == 0 || bestGap > gap(m))
        delete bestModel;
        bestModel = m;
        m = 0;
        bestGap = gap(bestModel);
      }
      else
        delete m;
        m = 0;
      }
    }
    // Finally, reset the time limit and continue to solve the
    // best model to optimality
    bestModel->getEnv().set(GRB_DoubleParam_TimeLimit, GRB_INFINITY);
    bestModel->optimize();
    cout << "Solved with MIPFocus: " <<</pre>
    bestModel->getEnv().get(GRB_IntParam_MIPFocus) << endl;</pre>
  }
  catch (GRBException e)
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  }
  catch (...)
    cout << "Error during optimization" << endl;</pre>
 delete bestModel;
 delete m;
 delete env;
 return 0;
// Simple function to determine the MIP gap
double gap(GRBModel *model) throw(GRBException)
```

```
sensitivity_c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Simple MIP sensitivity analysis example.
   For each integer variable, fix it to its lower and upper bound
   and check the impact on the objective. */
#include "gurobi_c++.h"
using namespace std;
int
main(int argc,
     char *argv[])
  if (argc < 2)
  {
    cout << "Usage: sensitivity_c++ filename" << endl;</pre>
    return 1;
  }
  GRBEnv* env = 0;
  GRBVar* avars = 0;
  GRBVar* bv = 0;
  try
    // Read model
    env = new GRBEnv();
    GRBModel a = GRBModel(*env, argv[1]);
    a.optimize();
    a.getEnv().set(GRB_IntParam_OutputFlag, 0);
    // Extract variables from model
    avars = a.getVars();
    for (int i = 0; i < a.get(GRB_IntAttr_NumVars); ++i)</pre>
      GRBVar v = avars[i];
      if (v.get(GRB_CharAttr_VType) == GRB_BINARY)
      {
        // Create clone and fix variable
        GRBModel b = GRBModel(a);
        bv = b.getVars();
        if (v.get(GRB_DoubleAttr_X) - v.get(GRB_DoubleAttr_LB) < 0.5)</pre>
```

```
bv[i].set(GRB_DoubleAttr_LB, bv[i].get(GRB_DoubleAttr_UB));
      }
      else
        bv[i].set(GRB_DoubleAttr_UB, bv[i].get(GRB_DoubleAttr_LB));
      delete[] bv;
      bv = 0;
      b.optimize();
      if (b.get(GRB_IntAttr_Status) == GRB_OPTIMAL)
        double objchg =
          b.get(GRB_DoubleAttr_ObjVal) - a.get(GRB_DoubleAttr_ObjVal);
        if (objchg < 0)
        {
          objchg = 0;
        cout << "Objective sensitivity for variable " <<</pre>
        v.get(GRB_StringAttr_VarName) << " is " << objchg << endl;</pre>
      }
      else
      {
        cout << "Objective sensitivity for variable " <<</pre>
        v.get(GRB_StringAttr_VarName) << " is infinite" << endl;</pre>
      }
    }
  }
catch (GRBException e)
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
}
catch (...)
  cout << "Error during optimization" << endl;</pre>
}
delete[] avars;
delete[] bv;
delete env;
```

```
return 0;
}
```

```
qcp c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QCP model:
     maximize
     subject to x + y + z = 1
                 x^2 + y^2 \le z^2 (second-order cone)
                 x^2 \ll yz
                                 (rotated second-order cone)
*/
#include "gurobi_c++.h"
using namespace std;
int
main(int
           argc,
     char *argv[])
{
  try {
    GRBEnv env = GRBEnv();
    GRBModel model = GRBModel(env);
    // Create variables
    GRBVar x = model.addVar(0.0, GRB_INFINITY, 0.0, GRB_CONTINUOUS, "x");
    GRBVar y = model.addVar(0.0, GRB_INFINITY, 0.0, GRB_CONTINUOUS, "y");
    GRBVar z = model.addVar(0.0, GRB_INFINITY, 0.0, GRB_CONTINUOUS, "z");
    // Integrate new variables
    model.update();
    // Set objective
    GRBLinExpr obj = x;
    model.setObjective(obj, GRB_MAXIMIZE);
    // Add linear constraint: x + y + z = 1
    model.addConstr(x + y + z == 1, "c0");
    // Add second-order cone: x^2 + y^2 \le z^2
    model.addQConstr(x*x + y*y <= z*z, "qc0");</pre>
```

```
// Add rotated cone: x^2 \le yz
    model.addQConstr(x*x <= y*z, "qc1");</pre>
    // Optimize model
    model.optimize();
    cout << x.get(GRB_StringAttr_VarName) << " "</pre>
          << x.get(GRB_DoubleAttr_X) << endl;</pre>
    cout << y.get(GRB_StringAttr_VarName) << " "</pre>
          << y.get(GRB_DoubleAttr_X) << endl;</pre>
    cout << z.get(GRB_StringAttr_VarName) << " "</pre>
          << z.get(GRB_DoubleAttr_X) << endl;</pre>
    cout << "Obj: " << model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
  } catch(GRBException e) {
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  } catch(...) {
    cout << "Exception during optimization" << endl;</pre>
  }
  return 0;
}
```

```
qp c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                x^2 + x*y + y^2 + y*z + z^2 + z
    subject to x + 2 y + 3 z >= 4
                 x + y
                               >= 1
  It solves it once as a continuous model, and once as an integer model.
*/
#include "gurobi_c++.h"
using namespace std;
int
main(int
           argc,
    char *argv[])
{
 try {
   GRBEnv env = GRBEnv();
   GRBModel model = GRBModel(env);
    // Create variables
    GRBVar x = model.addVar(0.0, 1.0, 0.0, GRB_CONTINUOUS, "x");
    GRBVar y = model.addVar(0.0, 1.0, 0.0, GRB_CONTINUOUS, "y");
    GRBVar z = model.addVar(0.0, 1.0, 0.0, GRB_CONTINUOUS, "z");
    // Integrate new variables
   model.update();
    // Set objective
    GRBQuadExpr obj = x*x + x*y + y*y + y*z + z*z + 2*x;
    model.setObjective(obj);
   // Add constraint: x + 2 y + 3 z >= 4
   model.addConstr(x + 2 * y + 3 * z >= 4, "c0");
    // Add constraint: x + y >= 1
```

```
model.addConstr(x + y >= 1, "c1");
  // Optimize model
  model.optimize();
  cout << x.get(GRB_StringAttr_VarName) << " "</pre>
       << x.get(GRB_DoubleAttr_X) << endl;
  cout << y.get(GRB_StringAttr_VarName) << " "</pre>
       << y.get(GRB_DoubleAttr_X) << endl;</pre>
  cout << z.get(GRB_StringAttr_VarName) << " "</pre>
       << z.get(GRB_DoubleAttr_X) << endl;</pre>
  cout << "Obj: " << model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
  // Change variable types to integer
  x.set(GRB_CharAttr_VType, GRB_INTEGER);
  y.set(GRB_CharAttr_VType, GRB_INTEGER);
  z.set(GRB_CharAttr_VType, GRB_INTEGER);
  // Optimize model
  model.optimize();
  cout << x.get(GRB_StringAttr_VarName) << " "</pre>
       << x.get(GRB_DoubleAttr_X) << endl;
  cout << y.get(GRB_StringAttr_VarName) << " "</pre>
       << y.get(GRB_DoubleAttr_X) << endl;</pre>
  cout << z.get(GRB_StringAttr_VarName) << " "</pre>
       << z.get(GRB_DoubleAttr_X) << endl;</pre>
  cout << "Obj: " << model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
} catch(GRBException e) {
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
} catch(...) {
  cout << "Exception during optimization" << endl;</pre>
return 0;
```

```
sos c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example creates a very simple Special Ordered Set (SOS) model.
   The model consists of 3 continuous variables, no linear constraints,
   and a pair of SOS constraints of type 1. */
#include "gurobi_c++.h"
using namespace std;
int
main(int
           argc,
     char *argv[])
  GRBEnv *env = 0;
  GRBVar *x = 0;
  try {
    env = new GRBEnv();
    GRBModel model = GRBModel(*env);
    // Create variables
    double ub[]
                   = \{1, 1, 2\};
    double obj[]
                   = \{-2, -1, -1\};
    string names[] = {"x0", "x1", "x2"};
    x = model.addVars(NULL, ub, obj, NULL, names, 3);
    // Integrate new variables
    model.update();
    // Add first SOS1: x0=0 or x1=0
    GRBVar sosv1[] = \{x[0], x[1]\};
    double soswt1[] = \{1, 2\};
    model.addSOS(sosv1, soswt1, 2, GRB_SOS_TYPE1);
    // Add second SOS1: x0=0 or x2=0 */
    GRBVar sosv2[] = \{x[0], x[2]\};
    double soswt2[] = \{1, 2\};
```

```
model.addSOS(sosv2, soswt2, 2, GRB_SOS_TYPE1);
    // Optimize model
    model.optimize();
    for (int i = 0; i < 3; i++)
      cout << x[i].get(GRB_StringAttr_VarName) << " "</pre>
           << x[i].get(GRB_DoubleAttr_X) << endl;
    cout << "Obj: " << model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
  } catch(GRBException e) {
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  } catch(...) {
    cout << "Exception during optimization" << endl;</pre>
  }
  delete[] x;
  delete env;
  return 0;
}
```

```
sudoku c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
  Sudoku example.
 The Sudoku board is a 9x9 grid, which is further divided into a 3x3 grid
  of 3x3 grids. Each cell in the grid must take a value from 0 to 9.
 No two grid cells in the same row, column, or 3x3 subgrid may take the
  same value.
  In the MIP formulation, binary variables x[i,j,v] indicate whether
  cell <i,j> takes value 'v'. The constraints are as follows:
    1. Each cell must take exactly one value (sum_v x[i,j,v] = 1)
    2. Each value is used exactly once per row (sum_i x[i,j,v] = 1)
    3. Each value is used exactly once per column (sum_j x[i,j,v] = 1)
    4. Each value is used exactly once per 3x3 subgrid (sum_grid x[i,j,v] = 1)
  Input datasets for this example can be found in examples/data/sudoku*.
*/
#include "gurobi_c++.h"
#include <sstream>
using namespace std;
#define sd 3
#define n (sd*sd)
string itos(int i) {stringstream s; s << i; return s.str(); }</pre>
int
main(int
           argc,
     char *argv[])
{
 try {
    GRBEnv env = GRBEnv();
    GRBModel model = GRBModel(env);
    GRBVar vars[n][n][n];
    int i, j, v;
    // Create 3-D array of model variables
    for (i = 0; i < n; i++) {
     for (j = 0; j < n; j++) {
        for (v = 0; v < n; v++) {
```

```
string s = "G_" + itos(i) + "_" + itos(j) + "_" + itos(v);
      vars[i][j][v] = model.addVar(0.0, 1.0, 0.0, GRB_BINARY, s);
    }
 }
}
// Integrate variables into model
model.update();
// Add constraints
// Each cell must take one value
for (i = 0; i < n; i++) {
  for (j = 0; j < n; j++) {
    GRBLinExpr expr = 0;
    for (v = 0; v < n; v++)
      expr += vars[i][j][v];
    string s = "V_" + itos(i) + "_" + itos(j);
    model.addConstr(expr, GRB_EQUAL, 1.0, s);
  }
}
// Each value appears once per row
for (i = 0; i < n; i++) {
  for (v = 0; v < n; v++) {
    GRBLinExpr expr = 0;
    for (j = 0; j < n; j++)
      expr += vars[i][j][v];
    string s = "R_" + itos(i) + "_" + itos(v);
    model.addConstr(expr == 1.0, s);
  }
}
// Each value appears once per column
for (j = 0; j < n; j++) {
  for (v = 0; v < n; v++) {
    GRBLinExpr expr = 0;
    for (i = 0; i < n; i++)
      expr += vars[i][j][v];
    string s = "C_" + itos(j) + "_" + itos(v);
    model.addConstr(expr == 1.0, s);
```

```
}
}
// Each value appears once per sub-grid
for (v = 0; v < n; v++) {
  for (int i0 = 0; i0 < sd; i0++) {
    for (int j0 = 0; j0 < sd; j0++) {
      GRBLinExpr expr = 0;
      for (int i1 = 0; i1 < sd; i1++) {
        for (int j1 = 0; j1 < sd; j1++) {
          expr += vars[i0*sd+i1][j0*sd+j1][v];
        }
      }
      string s = "Sub_" + itos(v) + "_" + itos(i0) + "_" + itos(j0);
      model.addConstr(expr == 1.0, s);
    }
 }
}
// Fix variables associated with pre-specified cells
char input[10];
for (i = 0; i < n; i++) {
  cin >> input;
  for (j = 0; j < n; j++) {
    int val = (int) input[j] - 48 - 1; // 0-based
    if (val >= 0)
      vars[i][j][val].set(GRB_DoubleAttr_LB, 1.0);
 }
}
// Optimize model
model.optimize();
// Write model to file
model.write("sudoku.lp");
cout << endl;</pre>
for (i = 0; i < n; i++) {
  for (j = 0; j < n; j++) {
```

```
for (v = 0; v < n; v++) {
           if (vars[i][j][v].get(GRB_DoubleAttr_X) > 0.5)
             cout << v+1;
        }
      }
      cout << endl;</pre>
    }
    cout << endl;</pre>
  } catch(GRBException e) {
    cout << "Error code = " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  } catch (...) {
    cout << "Error during optimization" << endl;</pre>
  }
 return 0;
}
```

```
tsp c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve a traveling salesman problem on a randomly generated set of
  points using lazy constraints.
                                    The base MIP model only includes
   'degree-2' constraints, requiring each node to have exactly
  two incident edges. Solutions to this model may contain subtours -
  tours that don't visit every node. The lazy constraint callback
  adds new constraints to cut them off. */
#include "gurobi_c++.h"
#include <cstdlib>
#include <cmath>
#include <sstream>
using namespace std;
string itos(int i) {stringstream s; s << i; return s.str(); }</pre>
double distance(double* x, double* y, int i, int j);
void findsubtour(int n, double** sol, int* tourlenP, int* tour);
// Subtour elimination callback. Whenever a feasible solution is found,
// find the smallest subtour, and add a subtour elimination constraint
// if the tour doesn't visit every node.
class subtourelim: public GRBCallback
{
 public:
    GRBVar** vars;
    int n:
    subtourelim(GRBVar** xvars, int xn) {
     vars = xvars;
           = xn;
    }
 protected:
    void callback() {
     try {
        if (where == GRB_CB_MIPSOL) {
          // Found an integer feasible solution - does it visit every node?
          double **x = new double*[n];
          int *tour = new int[n];
          int i, j, len;
          for (i = 0; i < n; i++)
            x[i] = getSolution(vars[i], n);
          findsubtour(n, x, &len, tour);
```

```
if (len < n) {
            // Add subtour elimination constraint
            GRBLinExpr expr = 0;
            for (i = 0; i < len; i++)
              for (j = 0; j < len; j++)
                 expr += vars[tour[i]][tour[j]];
            addLazy(expr <= len-1);</pre>
          for (i = 0; i < n; i++)
            delete[] x[i];
          delete[] x;
          delete[] tour;
      } catch (GRBException e) {
        cout << "Error number: " << e.getErrorCode() << endl;</pre>
        cout << e.getMessage() << endl;</pre>
      } catch (...) {
        cout << "Error during callback" << endl;</pre>
      }
};
// Given an integer-feasible solution 'sol', find the smallest
// sub-tour. Result is returned in 'tour', and length is
// returned in 'tourlenP'.
void
findsubtour(int
                      n,
            double** sol,
            int*
                      tourlenP,
            int*
                      tour)
  bool* seen = new bool[n];
  int bestind, bestlen;
  int i, node, len, start;
  for (i = 0; i < n; i++)
    seen[i] = false;
  start = 0;
  bestlen = n+1;
  bestind = -1;
  node = 0;
```

```
while (start < n) {</pre>
    for (node = 0; node < n; node++)</pre>
      if (!seen[node])
        break;
    if (node == n)
      break;
    for (len = 0; len < n; len++) \{
      tour[start+len] = node;
      seen[node] = true;
      for (i = 0; i < n; i++) {
        if (sol[node][i] > 0.5 && !seen[i]) {
          node = i;
          break;
        }
      }
      if (i == n) \{
        len++;
        if (len < bestlen) {</pre>
          bestlen = len;
          bestind = start;
        }
        start += len;
        break;
      }
    }
  }
  for (i = 0; i < bestlen; i++)
    tour[i] = tour[bestind+i];
  *tourlenP = bestlen;
  delete[] seen;
}
// Euclidean distance between points 'i' and 'j'.
double
distance(double* x,
         double* y,
         int
                  i,
         int
                  j)
  double dx = x[i]-x[j];
  double dy = y[i]-y[j];
```

```
return sqrt(dx*dx+dy*dy);
}
int
main(int argc,
     char *argv[])
  if (argc < 2) {
   cout << "Usage: tsp_c++ size" << endl;</pre>
   return 1;
 }
  int n = atoi(argv[1]);
  double* x = new double[n];
 double* y = new double[n];
 int i;
 for (i = 0; i < n; i++) {
   x[i] = ((double) rand())/RAND_MAX;
   y[i] = ((double) rand())/RAND_MAX;
 }
 GRBEnv *env = NULL;
 GRBVar **vars = NULL;
 vars = new GRBVar*[n];
 for (i = 0; i < n; i++)
   vars[i] = new GRBVar[n];
 try {
   int j;
    env = new GRBEnv();
   GRBModel model = GRBModel(*env);
   // Must set LazyConstraints parameter when using lazy constraints
   model.getEnv().set(GRB_IntParam_LazyConstraints, 1);
   // Create binary decision variables
    for (i = 0; i < n; i++) {
      for (j = 0; j \le i; j++) {
        vars[i][j] = model.addVar(0.0, 1.0, distance(x, y, i, j),
                                   GRB_BINARY, "x_"+itos(i)+"_"+itos(j));
```

```
vars[j][i] = vars[i][j];
  }
}
model.update();
// Integrate new variables
model.update();
// Degree-2 constraints
for (i = 0; i < n; i++) {
  GRBLinExpr expr = 0;
  for (j = 0; j < n; j++)
    expr += vars[i][j];
  model.addConstr(expr == 2, "deg2_"+itos(i));
}
// Forbid edge from node back to itself
for (i = 0; i < n; i++)
  vars[i][i].set(GRB_DoubleAttr_UB, 0);
// Set callback function
subtourelim cb = subtourelim(vars, n);
model.setCallback(&cb);
// Optimize model
model.optimize();
// Extract solution
if (model.get(GRB_IntAttr_SolCount) > 0) {
  double **sol = new double*[n];
  for (i = 0; i < n; i++)
    sol[i] = model.get(GRB_DoubleAttr_X, vars[i], n);
  int* tour = new int[n];
  int len;
  findsubtour(n, sol, &len, tour);
  cout << "Tour: ";</pre>
```

```
for (i = 0; i < len; i++)
        cout << tour[i] << " ";</pre>
      cout << endl;</pre>
      for (i = 0; i < n; i++)
        delete[] sol[i];
      delete[] sol;
      delete[] tour;
  } catch (GRBException e) {
    cout << "Error number: " << e.getErrorCode() << endl;</pre>
    cout << e.getMessage() << endl;</pre>
  } catch (...) {
    cout << "Error during optimization" << endl;</pre>
  for (i = 0; i < n; i++)
    delete[] vars[i];
  delete[] vars;
  delete[] x;
  delete[] y;
  delete env;
  return 0;
}
```

```
tune c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a model from a file and tunes it.
   It then writes the best parameter settings to a file
   and solves the model using these parameters. */
#include "gurobi_c++.h"
#include <cmath>
using namespace std;
int
main(int
           argc,
     char *argv[])
  if (argc < 2) {
    cout << "Usage: tune_c++ filename" << endl;</pre>
   return 1;
  }
 GRBEnv *env = 0;
 try {
    env = new GRBEnv();
   // Read model from file
    GRBModel model = GRBModel(*env, argv[1]);
   GRBEnv menv = model.getEnv();
    // Set the TuneResults parameter to 1
   menv.set(GRB_IntParam_TuneResults, 1);
    // Tune the model
   model.tune();
   // Get the number of tuning results
    int resultcount = model.get(GRB_IntAttr_TuneResultCount);
    if (resultcount > 0) {
      // Load the tuned parameters into the model's environment
```

```
model.getTuneResult(0);

// Write tuned parameters to a file

model.write("tune.prm");

// Solve the model using the tuned parameters

model.optimize();
}

catch(GRBException e) {
 cout << "Error code = " << e.getErrorCode() << endl;
 cout << e.getMessage() << endl;
} catch (...) {
 cout << "Error during tuning" << endl;
}

delete env;
return 0;
}</pre>
```

workforce1 c++.cpp /* Copyright 2013, Gurobi Optimization, Inc. */ /* Assign workers to shifts; each worker may or may not be available on a particular day. If the problem cannot be solved, use IIS to find a set of conflicting constraints. Note that there may be additional conflicts besides what is reported via IIS. */ #include "gurobi_c++.h" #include <sstream> using namespace std; main(int argc, char *argv[]) GRBEnv* env = 0;GRBConstr* c = 0;GRBVar** x = 0;int xCt = 0; try { // Sample data const int nShifts = 14; const int nWorkers = 7; // Sets of days and workers string Shifts[] = { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6", "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13", "Sun14" }; string Workers[] = { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" }; // Number of workers required for each shift double shiftRequirements[] = { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 }; // Amount each worker is paid to work one shift double pay[] = { 10, 12, 10, 8, 8, 9, 11 }; // Worker availability: 0 if the worker is unavailable for a shift double availability[][nShifts] = { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },

```
\{ 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 \},
    { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
    { 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, },
    { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
    \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
    { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
// Model
env = new GRBEnv();
GRBModel model = GRBModel(*env);
model.set(GRB_StringAttr_ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
x = new GRBVar*[nWorkers];
for (int w = 0; w < nWorkers; ++w)</pre>
 x[w] = model.addVars(nShifts);
 xCt++;
 model.update();
 for (int s = 0; s < nShifts; ++s)
    ostringstream vname;
    vname << Workers[w] << "." << Shifts[s];</pre>
    x[w][s].set(GRB_DoubleAttr_UB, availability[w][s]);
    x[w][s].set(GRB_DoubleAttr_Obj, pay[w]);
    x[w][s].set(GRB_StringAttr_VarName, vname.str());
}
// The objective is to minimize the total pay costs
model.set(GRB_IntAttr_ModelSense, 1);
// Update model to integrate new variables
model.update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (int s = 0; s < nShifts; ++s)
 GRBLinExpr lhs = 0;
  for (int w = 0; w < nWorkers; ++w)</pre>
    lhs += x[w][s];
```

```
}
    model.addConstr(lhs == shiftRequirements[s], Shifts[s]);
  }
  // Optimize
  model.optimize();
  int status = model.get(GRB_IntAttr_Status);
  if (status == GRB_UNBOUNDED)
    cout << "The model cannot be solved "</pre>
    << "because it is unbounded" << endl;
    return 1;
  }
  if (status == GRB_OPTIMAL)
    cout << "The optimal objective is " <<</pre>
    model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
    return 0;
  if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
    cout << "Optimization was stopped with status " << status << endl;</pre>
    return 1;
  // do IIS
  cout << "The model is infeasible; computing IIS" << endl;</pre>
  model.computeIIS();
  cout << "\nThe following constraint(s) "</pre>
  << "cannot be satisfied:" << endl;
  c = model.getConstrs();
  for (int i = 0; i < model.get(GRB_IntAttr_NumConstrs); ++i)</pre>
    if (c[i].get(GRB_IntAttr_IISConstr) == 1)
      cout << c[i].get(GRB_StringAttr_ConstrName) << endl;</pre>
    }
  }
catch (GRBException e)
{
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
}
```

```
catch (...)
{
   cout << "Exception during optimization" << endl;
}

delete[] c;
for (int i = 0; i < xCt; ++i) {
   delete[] x[i];
}
   delete[] x;
   delete env;
   return 0;
}</pre>
```

```
workforce2 c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, use IIS iteratively to
  find all conflicting constraints. */
#include "gurobi_c++.h"
#include <sstream>
#include <deque>
using namespace std;
int
main(int argc,
     char *argv[])
  GRBEnv* env = 0;
  GRBConstr* c = 0;
 GRBVar** x = 0;
  int xCt = 0;
 try
  {
   // Sample data
    const int nShifts = 14;
    const int nWorkers = 7;
    // Sets of days and workers
    string Shifts[] =
      { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
        "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
        "Sun14" };
    string Workers[] =
      { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
    // Number of workers required for each shift
    double shiftRequirements[] =
      { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
    // Amount each worker is paid to work one shift
    double pay[] = { 10, 12, 10, 8, 8, 9, 11 };
    // Worker availability: 0 if the worker is unavailable for a shift
    double availability[][nShifts] =
      { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
```

```
\{ 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 \},
    { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
    { 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, },
    { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
    \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
    { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
// Model
env = new GRBEnv();
GRBModel model = GRBModel(*env);
model.set(GRB_StringAttr_ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
x = new GRBVar*[nWorkers];
for (int w = 0; w < nWorkers; ++w)</pre>
 x[w] = model.addVars(nShifts);
 xCt++;
 model.update();
 for (int s = 0; s < nShifts; ++s)
    ostringstream vname;
    vname << Workers[w] << "." << Shifts[s];</pre>
    x[w][s].set(GRB_DoubleAttr_UB, availability[w][s]);
    x[w][s].set(GRB_DoubleAttr_Obj, pay[w]);
    x[w][s].set(GRB_StringAttr_VarName, vname.str());
}
// The objective is to minimize the total pay costs
model.set(GRB_IntAttr_ModelSense, 1);
// Update model to integrate new variables
model.update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (int s = 0; s < nShifts; ++s)
 GRBLinExpr lhs = 0;
  for (int w = 0; w < nWorkers; ++w)</pre>
    lhs += x[w][s];
```

```
}
 model.addConstr(lhs == shiftRequirements[s], Shifts[s]);
}
// Optimize
model.optimize();
int status = model.get(GRB_IntAttr_Status);
if (status == GRB_UNBOUNDED)
 cout << "The model cannot be solved "</pre>
  << "because it is unbounded" << endl;
 return 1;
}
if (status == GRB_OPTIMAL)
 cout << "The optimal objective is " <<</pre>
 model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
 return 0;
if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
  cout << "Optimization was stopped with status " << status << endl;</pre>
 return 1;
// do IIS
cout << "The model is infeasible; computing IIS" << endl;</pre>
deque<string> removed;
// Loop until we reduce to a model that can be solved
while (1)
 model.computeIIS();
  cout << "\nThe following constraint cannot be satisfied:" << endl;</pre>
  c = model.getConstrs();
  for (int i = 0; i < model.get(GRB_IntAttr_NumConstrs); ++i)</pre>
    if (c[i].get(GRB_IntAttr_IISConstr) == 1)
    {
      cout << c[i].get(GRB_StringAttr_ConstrName) << endl;</pre>
      // Remove a single constraint from the model
      removed.push_back(c[i].get(GRB_StringAttr_ConstrName));
      model.remove(c[i]);
      break;
    }
```

```
}
    delete[] c;
    c = 0;
    cout << endl;</pre>
    model.optimize();
    status = model.get(GRB_IntAttr_Status);
    if (status == GRB_UNBOUNDED)
      cout << "The model cannot be solved because it is unbounded" << endl;</pre>
      return 0;
    }
    if (status == GRB_OPTIMAL)
      break;
    }
    if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
      cout << "Optimization was stopped with status " << status << endl;
      return 1;
    }
  cout << "\nThe following constraints were removed "</pre>
  << "to get a feasible LP:" << endl;
  for (deque<string>::iterator r = removed.begin();
       r != removed.end();
       ++r)
    cout << *r << " ";
  cout << endl;</pre>
}
catch (GRBException e)
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
catch (...)
  cout << "Exception during optimization" << endl;</pre>
```

```
delete[] c;
  for (int i = 0; i < xCt; ++i) {
    delete[] x[i];
  }
  delete[] x;
  delete env;
  return 0;
}</pre>
```

workforce3 c++.cpp /* Copyright 2013, Gurobi Optimization, Inc. */ /* Assign workers to shifts; each worker may or may not be available on a particular day. If the problem cannot be solved, add slack variables to determine which constraints cannot be satisfied, and how much they need to be relaxed. */ #include "gurobi_c++.h" #include <sstream> #include <deque> using namespace std; int main(int argc, char *argv[]) { GRBEnv* env = 0;GRBConstr* c = 0;GRBVar** x = 0;int xCt = 0; try { // Sample data const int nShifts = 14; const int nWorkers = 7; // Sets of days and workers string Shifts[] = { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6", "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13", "Sun14" }; string Workers[] = { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" }; // Number of workers required for each shift double shiftRequirements[] = ${3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5};$ // Amount each worker is paid to work one shift double pay[] = { 10, 12, 10, 8, 8, 9, 11 }; // Worker availability: 0 if the worker is unavailable for a shift double availability[][nShifts] =

```
{ { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
   { 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 },
   { 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, },
   { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
   \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
   { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
// Model
env = new GRBEnv();
GRBModel model = GRBModel(*env);
model.set(GRB_StringAttr_ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
x = new GRBVar*[nWorkers];
for (int w = 0; w < nWorkers; ++w)</pre>
{
 x[w] = model.addVars(nShifts);
 xCt++;
 model.update();
 for (int s = 0; s < nShifts; ++s)
   ostringstream vname;
   vname << Workers[w] << "." << Shifts[s];</pre>
   x[w][s].set(GRB_DoubleAttr_UB, availability[w][s]);
   x[w][s].set(GRB_DoubleAttr_Obj, pay[w]);
   x[w][s].set(GRB_StringAttr_VarName, vname.str());
 }
}
// The objective is to minimize the total pay costs
model.set(GRB_IntAttr_ModelSense, 1);
// Update model to integrate new variables
model.update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (int s = 0; s < nShifts; ++s)
 GRBLinExpr lhs = 0;
 for (int w = 0; w < nWorkers; ++w)</pre>
  {
```

```
lhs += x[w][s];
  }
 model.addConstr(lhs == shiftRequirements[s], Shifts[s]);
}
// Optimize
model.optimize();
int status = model.get(GRB_IntAttr_Status);
if (status == GRB_UNBOUNDED)
  cout << "The model cannot be solved "</pre>
  << "because it is unbounded" << endl;</pre>
 return 1;
}
if (status == GRB_OPTIMAL)
  cout << "The optimal objective is " <<</pre>
 model.get(GRB_DoubleAttr_ObjVal) << endl;</pre>
 return 0;
if ((status != GRB_INF_OR_UNBD) && (status != GRB_INFEASIBLE))
 cout << "Optimization was stopped with status " << status << endl;</pre>
 return 1;
}
// Add slack variables to make the model feasible
cout << "The model is infeasible; adding slack variables" << endl;</pre>
// Set original objective coefficients to zero
model.setObjective(GRBLinExpr(0.0));
// Add a new slack variable to each shift constraint so that the shifts
// can be satisfied
deque<GRBVar> slacks;
c = model.getConstrs();
for (int i = 0; i < model.get(GRB_IntAttr_NumConstrs); ++i)</pre>
 GRBColumn col;
  col.addTerm(1.0, c[i]);
  GRBVar newvar =
    model.addVar(0, GRB_INFINITY, 1.0, GRB_CONTINUOUS, col,
                  c[i].get(GRB_StringAttr_ConstrName) + "Slack");
 slacks.push_back(newvar);
}
```

```
// Solve the model with slacks
  model.optimize();
  status = model.get(GRB_IntAttr_Status);
  if ((status == GRB_INF_OR_UNBD) || (status == GRB_INFEASIBLE) ||
      (status == GRB_UNBOUNDED))
    cout << "The model with slacks cannot be solved " <<</pre>
    "because it is infeasible or unbounded" << endl;
    return 1;
  if (status != GRB_OPTIMAL)
    cout << "Optimization was stopped with status " << status << endl;</pre>
    return 1;
  }
  cout << "\nSlack values:" << endl;</pre>
  for (deque<GRBVar>::iterator sv = slacks.begin();
       sv != slacks.end();
       ++sv)
    if (sv->get(GRB_DoubleAttr_X) > 1e-6)
    {
      cout << sv->get(GRB_StringAttr_VarName) << " = " <<</pre>
      sv->get(GRB_DoubleAttr_X) << endl;</pre>
    }
  }
catch (GRBException e)
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
catch (...)
  cout << "Exception during optimization" << endl;</pre>
}
delete[] c;
for (int i = 0; i < xCt; ++i) {
  delete[] x[i];
```

```
delete[] x;
delete env;
return 0;
}
```

```
workforce4 c++.cpp
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. We use Pareto optimization to solve the model:
  first, we minimize the linear sum of the slacks. Then, we constrain
  the sum of the slacks, and we minimize a quadratic objective that
  tries to balance the workload among the workers. */
#include "gurobi_c++.h"
#include <sstream>
using namespace std;
int solveAndPrint(GRBModel& model, GRBVar& totSlack,
                  int nWorkers, string* Workers,
                  GRBVar* totShifts) throw(GRBException);
int
main(int argc,
     char *argv[])
  GRBEnv* env = 0;
 GRBConstr* c = 0;
 GRBVar* v = 0;
 GRBVar** x = 0;
 GRBVar* slacks = 0;
 GRBVar* totShifts = 0;
 GRBVar* diffShifts = 0;
  int xCt = 0;
 try
  {
    // Sample data
    const int nShifts = 14;
    const int nWorkers = 7;
    // Sets of days and workers
    string Shifts[] =
      { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
        "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
        "Sun14" };
    string Workers[] =
      { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
    // Number of workers required for each shift
```

```
double shiftRequirements[] =
  { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
// Worker availability: 0 if the worker is unavailable for a shift
double availability[][nShifts] =
  { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
    { 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 },
    { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
    { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
    \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
    { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
// Model
env = new GRBEnv();
GRBModel model = GRBModel(*env);
model.set(GRB_StringAttr_ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. This is no longer a pure assignment model, so we must
// use binary variables.
x = new GRBVar*[nWorkers];
int s, w;
for (w = 0; w < nWorkers; ++w)
 x[w] = model.addVars(nShifts);
 xCt++;
 model.update();
 for (s = 0; s < nShifts; ++s)
    ostringstream vname;
    vname << Workers[w] << "." << Shifts[s];</pre>
    x[w][s].set(GRB_DoubleAttr_UB, availability[w][s]);
    x[w][s].set(GRB_CharAttr_VType, GRB_BINARY);
    x[w][s].set(GRB_StringAttr_VarName, vname.str());
}
// Slack variables for each shift constraint so that the shifts can
// be satisfied
slacks = model.addVars(nShifts);
model.update();
for (s = 0; s < nShifts; ++s)
  ostringstream vname;
```

```
vname << Shifts[s] << "Slack";</pre>
 slacks[s].set(GRB_StringAttr_VarName, vname.str());
}
// Variable to represent the total slack
GRBVar totSlack = model.addVar(0, GRB_INFINITY, 0, GRB_CONTINUOUS,
                                "totSlack");
// Variables to count the total shifts worked by each worker
totShifts = model.addVars(nWorkers);
model.update();
for (w = 0; w < nWorkers; ++w)
  ostringstream vname;
 vname << Workers[w] << "TotShifts";</pre>
 totShifts[w].set(GRB_StringAttr_VarName, vname.str());
}
// Update model to integrate new variables
model.update();
GRBLinExpr lhs;
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (s = 0; s < nShifts; ++s)
 lhs = 0;
 lhs += slacks[s];
 for (w = 0; w < nWorkers; ++w)
    lhs += x[w][s];
 model.addConstr(lhs == shiftRequirements[s], Shifts[s]);
}
// Constraint: set totSlack equal to the total slack
lhs = 0;
for (s = 0; s < nShifts; ++s)
 lhs += slacks[s];
model.addConstr(lhs == totSlack, "totSlack");
// Constraint: compute the total number of shifts for each worker
```

```
for (w = 0; w < nWorkers; ++w) {
  lhs = 0;
 for (s = 0; s < nShifts; ++s) {
    lhs += x[w][s];
  ostringstream vname;
 vname << "totShifts" << Workers[w];</pre>
 model.addConstr(lhs == totShifts[w], vname.str());
// Objective: minimize the total slack
GRBLinExpr obj = 0;
obj += totSlack;
model.setObjective(obj);
// Optimize
int status = solveAndPrint(model, totSlack, nWorkers, Workers, totShifts);
if (status != GRB_OPTIMAL)
{
 return 1;
}
// Constrain the slack by setting its upper and lower bounds
totSlack.set(GRB_DoubleAttr_UB, totSlack.get(GRB_DoubleAttr_X));
totSlack.set(GRB_DoubleAttr_LB, totSlack.get(GRB_DoubleAttr_X));
// Variable to count the average number of shifts worked
GRBVar avgShifts =
 model.addVar(0, GRB_INFINITY, 0, GRB_CONTINUOUS, "avgShifts");
// Variables to count the difference from average for each worker;
// note that these variables can take negative values.
diffShifts = model.addVars(nWorkers);
model.update();
for (w = 0; w < nWorkers; ++w) {
  ostringstream vname;
 vname << Workers[w] << "Diff";</pre>
 diffShifts[w].set(GRB_StringAttr_VarName, vname.str());
 diffShifts[w].set(GRB_DoubleAttr_LB, -GRB_INFINITY);
}
// Update model to integrate new variables
model.update();
// Constraint: compute the average number of shifts worked
```

```
lhs = 0;
  for (w = 0; w < nWorkers; ++w) {
    lhs += totShifts[w];
  model.addConstr(lhs == nWorkers * avgShifts, "avgShifts");
  // Constraint: compute the difference from the average number of shifts
  for (w = 0; w < nWorkers; ++w) {
    lhs = 0;
    lhs += totShifts[w];
    lhs -= avgShifts;
    ostringstream vname;
    vname << Workers[w] << "Diff";</pre>
    model.addConstr(lhs == diffShifts[w], vname.str());
  // Objective: minimize the sum of the square of the difference from the
  // average number of shifts worked
  GRBQuadExpr qobj;
  for (w = 0; w < nWorkers; ++w) {
    qobj += diffShifts[w] * diffShifts[w];
  model.setObjective(qobj);
  // Optimize
  status = solveAndPrint(model, totSlack, nWorkers, Workers, totShifts);
  if (status != GRB_OPTIMAL)
    return 1;
catch (GRBException e)
  cout << "Error code = " << e.getErrorCode() << endl;</pre>
  cout << e.getMessage() << endl;</pre>
}
catch (...)
  cout << "Exception during optimization" << endl;</pre>
}
delete[] c;
delete[] v;
for (int i = 0; i < xCt; ++i) {
```

```
delete[] x[i];
  }
  delete[] x;
  delete[] slacks;
  delete[] totShifts;
  delete[] diffShifts;
  delete env;
  return 0;
}
int solveAndPrint(GRBModel& model, GRBVar& totSlack,
                   int nWorkers, string* Workers,
                   GRBVar* totShifts) throw(GRBException)
{
  model.optimize();
  int status = model.get(GRB_IntAttr_Status);
  if ((status == GRB_INF_OR_UNBD) || (status == GRB_INFEASIBLE) ||
      (status == GRB_UNBOUNDED))
  {
    cout << "The model cannot be solved " <<</pre>
    "because it is infeasible or unbounded" << endl;
    return status;
  }
  if (status != GRB_OPTIMAL)
    cout << "Optimization was stopped with status " << status << endl;</pre>
    return status;
  // Print total slack and the number of shifts worked for each worker
  cout << endl << "Total slack required: " <<</pre>
    totSlack.get(GRB_DoubleAttr_X) << endl;</pre>
  for (int w = 0; w < nWorkers; ++w) {</pre>
    cout << Workers[w] << " worked " <<</pre>
    totShifts[w].get(GRB_DoubleAttr_X) << " shifts" << endl;</pre>
  }
  cout << endl;</pre>
  return status;
}
```

3.3 Java Examples

This section includes source code for all of the Gurobi Java examples. The same source code can be found in the examples/java directory of the Gurobi distribution.

Callback.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP or a MIP from a file, sets a callback
  to monitor the optimization progress and to output some progress
   information to the screen and to a log file. If it is a MIP and 10%
  gap is reached, then it aborts */
import gurobi.*;
public class Callback extends GRBCallback {
  private GRBVar[] vars;
 private double
                   lastnode;
 private double
                   lastiter;
 public Callback(GRBVar[] xvars) {
    vars = xvars;
    lastnode = lastiter = -1;
  }
 protected void callback() {
    try {
      if (where == GRB.CB_MESSAGE) {
        // Message callback
        String st = getStringInfo(GRB.CB_MSG_STRING);
        if (st != null) System.out.print(st);
      } else if (where == GRB.CB_PRESOLVE) {
        // Presolve callback
        int cdels = getIntInfo(GRB.CB_PRE_COLDEL);
        int rdels = getIntInfo(GRB.CB_PRE_ROWDEL);
        System.out.println(cdels+" columns and "+rdels+" rows are removed");
      } else if (where == GRB.CB_SIMPLEX) {
        // Simplex callback
        double itcnt = getDoubleInfo(GRB.CB_SPX_ITRCNT);
        if (itcnt - lastiter >= 100) {
          lastiter = itcnt;
          double obj = getDoubleInfo(GRB.CB_SPX_OBJVAL);
          double pinf = getDoubleInfo(GRB.CB_SPX_PRIMINF);
          double dinf = getDoubleInfo(GRB.CB_SPX_DUALINF);
          int ispert = getIntInfo(GRB.CB_SPX_ISPERT);
```

```
char ch;
        if (ispert == 0)
                              ch = ', ';
        else if (ispert == 1) ch = 'S';
                              ch = 'P';
        System.out.println(itcnt+" "+ obj + ch + " "+pinf + " " + dinf);
      }
    } else if (where == GRB.CB_MIP) {
      // General MIP callback
      double nodecnt = getDoubleInfo(GRB.CB_MIP_NODCNT);
      if (nodecnt - lastnode >= 100) {
        lastnode = nodecnt;
        double objbst = getDoubleInfo(GRB.CB_MIP_OBJBST);
        double objbnd = getDoubleInfo(GRB.CB_MIP_OBJBND);
        if (Math.abs(objbst - objbnd) < 0.1 * (1.0 + Math.abs(objbst)))</pre>
          abort();
        int actnodes = (int) getDoubleInfo(GRB.CB_MIP_NODLFT);
        int itcnt = (int) getDoubleInfo(GRB.CB_MIP_ITRCNT);
        int solcnt = getIntInfo(GRB.CB_MIP_SOLCNT);
        int cutcnt = getIntInfo(GRB.CB_MIP_CUTCNT);
        System.out.println(nodecnt + " " + actnodes + " " + itcnt + " "
          + objbst + " " + objbnd + " " + solcnt + " " + cutcnt);
    } else if (where == GRB.CB_MIPSOL) {
      // MIP solution callback
                     = getDoubleInfo(GRB.CB_MIPSOL_OBJ);
      double obj
             nodecnt = (int) getDoubleInfo(GRB.CB_MIPSOL_NODCNT);
      double[] x = getSolution(vars);
      System.out.println("**** New solution at node " + nodecnt + ", obj "
                         + obj + ", x[0] = " + x[0] + "****");
    }
  } catch (GRBException e) {
    System.out.println("Error code: " + e.getErrorCode() + ". " +
        e.getMessage());
    e.printStackTrace();
  }
}
public static void main(String[] args) {
  if (args.length < 1) {
    System.out.println("Usage: java Callback filename");
    System.exit(1);
  }
  try {
```

```
GRBEnv
                env = new GRBEnv();
      GRBModel model = new GRBModel(env, args[0]);
      model.getEnv().set(GRB.IntParam.OutputFlag, 0);
      GRBVar[] vars
                      = model.getVars();
      // Create a callback object and associate it with the model
      model.setCallback(new Callback(vars));
      model.optimize();
      double[] x
                      = model.get(GRB.DoubleAttr.X, vars);
      String[] vnames = model.get(GRB.StringAttr.VarName, vars);
      for (int j = 0; j < vars.length; j++) {
        if (x[j] != 0.0) System.out.println(vnames[j] + " " + x[j]);
      }
      \ensuremath{//} Dispose of model and environment
      model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
      e.printStackTrace();
    }
 }
}
```

Dense.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                 x + y + x^2 + x*y + y^2 + y*z + z^2
     subject to x + 2y + 3z >= 4
                 x +
                      У
                               >= 1
  The example illustrates the use of dense matrices to store A and Q
   (and dense vectors for the other relevant data). We don't recommend
  that you use dense matrices, but this example may be helpful if you
  already have your data in this format.
import gurobi.*;
public class Dense {
 protected static boolean
    dense_optimize(GRBEnv
                              env,
                   int
                              rows,
                   int
                              cols,
                   double[]
                                      // linear portion of objective function
                              С,
                   double[][] Q,
                                      // quadratic portion of objective function
                   double[][] A,
                                     // constraint matrix
                              sense, // constraint senses
                   char[]
                   double[]
                                      // RHS vector
                              rhs,
                                      // variable lower bounds
                   double[]
                              lb,
                   double[]
                              ub,
                                      // variable upper bounds
                   char[]
                              vtype, // variable types (continuous, binary, etc.)
                   double[]
                            solution) {
    boolean success = false;
    try {
      GRBModel model = new GRBModel(env);
      // Add variables to the model
     GRBVar[] vars = model.addVars(lb, ub, null, vtype, null);
     model.update();
      // Populate A matrix
```

```
for (int i = 0; i < rows; i++) {
    GRBLinExpr expr = new GRBLinExpr();
    for (int j = 0; j < cols; j++)
      if (A[i][j] != 0)
        expr.addTerm(A[i][j], vars[j]);
    model.addConstr(expr, sense[i], rhs[i], "");
  }
  // Populate objective
  GRBQuadExpr obj = new GRBQuadExpr();
  if (Q != null) {
    for (int i = 0; i < cols; i++)
      for (int j = 0; j < cols; j++)
        if (Q[i][j] != 0)
          obj.addTerm(Q[i][j], vars[i], vars[j]);
    for (int j = 0; j < cols; j++)
      if (c[j] != 0)
        obj.addTerm(c[j], vars[j]);
    model.setObjective(obj);
  }
  // Solve model
  model.optimize();
  // Extract solution
  if (model.get(GRB.IntAttr.Status) == GRB.OPTIMAL) {
    success = true;
    for (int j = 0; j < cols; j++)
      solution[j] = vars[j].get(GRB.DoubleAttr.X);
  }
  model.dispose();
} catch (GRBException e) {
  System.out.println("Error code: " + e.getErrorCode() + ". " +
      e.getMessage());
  e.printStackTrace();
}
return success;
```

}

```
public static void main(String[] args) {
    try {
      GRBEnv env = new GRBEnv();
      double c[] = new double[] \{1, 1, 0\};
      double Q[][] = new double[][] \{\{1, 1, 0\}, \{0, 1, 1\}, \{0, 0, 1\}\};
      double A[][] = new double[][] {{1, 2, 3}, {1, 1, 0}};
      char sense[] = new char[] {'>', '>'};
      double rhs[] = new double[] {4, 1};
      double lb[] = new double[] {0, 0, 0};
      boolean success;
      double sol[] = new double[3];
      success = dense_optimize(env, 2, 3, c, Q, A, sense, rhs,
                                lb, null, null, sol);
      if (success) {
        System.out.println("x: " + sol[0] + ", y: " + sol[1] + ", z: " + sol[2]);
      }
      // Dispose of environment
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
      e.printStackTrace();
    }
 }
}
```

Diet.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve the classic diet model, showing how to add constraints
  to an existing model. */
import gurobi.*;
public class Diet {
 public static void main(String[] args) {
    try {
      // Nutrition guidelines, based on
      // USDA Dietary Guidelines for Americans, 2005
      // http://www.health.gov/DietaryGuidelines/dga2005/
     String Categories[] =
          new String[] { "calories", "protein", "fat", "sodium" };
      int nCategories = Categories.length;
      double minNutrition[] = new double[] { 1800, 91, 0, 0 };
      double maxNutrition[] = new double[] { 2200, GRB.INFINITY, 65, 1779 };
      // Set of foods
      String Foods[] =
          new String[] { "hamburger", "chicken", "hot dog", "fries",
              "macaroni", "pizza", "salad", "milk", "ice cream" };
      int nFoods = Foods.length;
      double cost[] =
          new double[] { 2.49, 2.89, 1.50, 1.89, 2.09, 1.99, 2.49, 0.89,
              1.59 };
      // Nutrition values for the foods
      double nutritionValues[][] = new double[][] {
          { 410, 24, 26, 730 }, // hamburger
          { 420, 32, 10, 1190 }, // chicken
          { 560, 20, 32, 1800 }, // hot dog
          { 380, 4, 19, 270 },
                                 // fries
          { 320, 12, 10, 930 },
                                 // macaroni
          { 320, 15, 12, 820 },
                                 // pizza
          { 320, 31, 12, 1230 }, // salad
          { 100, 8, 2.5, 125 },
                                 // milk
          { 330, 8, 10, 180 }
                                 // ice cream
          };
      // Model
```

```
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.set(GRB.StringAttr.ModelName, "diet");
// Create decision variables for the nutrition information,
// which we limit via bounds
GRBVar[] nutrition = new GRBVar[nCategories];
for (int i = 0; i < nCategories; ++i) {</pre>
  nutrition[i] =
      model.addVar(minNutrition[i], maxNutrition[i], 0, GRB.CONTINUOUS,
                   Categories[i]);
}
// Create decision variables for the foods to buy
GRBVar[] buy = new GRBVar[nFoods];
for (int j = 0; j < nFoods; ++j) {
  buy[j] =
      model.addVar(0, GRB.INFINITY, cost[j], GRB.CONTINUOUS, Foods[j]);
}
// The objective is to minimize the costs
model.set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.update();
// Nutrition constraints
for (int i = 0; i < nCategories; ++i) {</pre>
  GRBLinExpr ntot = new GRBLinExpr();
  for (int j = 0; j < nFoods; ++j) {
    ntot.addTerm(nutritionValues[j][i], buy[j]);
  }
  model.addConstr(ntot, GRB.EQUAL, nutrition[i], Categories[i]);
}
// Solve
model.optimize();
printSolution(model, buy, nutrition);
System.out.println("\nAdding constraint: at most 6 servings of dairy");
GRBLinExpr lhs = new GRBLinExpr();
lhs.addTerm(1.0, buy[7]);
lhs.addTerm(1.0, buy[8]);
model.addConstr(lhs, GRB.LESS_EQUAL, 6.0, "limit_dairy");
```

```
// Solve
      model.optimize();
      printSolution(model, buy, nutrition);
      // Dispose of model and environment
      model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
    }
  }
  private static void printSolution(GRBModel model, GRBVar[] buy,
                                    GRBVar[] nutrition) throws GRBException {
    if (model.get(GRB.IntAttr.Status) == GRB.Status.OPTIMAL) {
      System.out.println("\nCost: " + model.get(GRB.DoubleAttr.ObjVal));
      System.out.println("\nBuy:");
      for (int j = 0; j < buy.length; ++j) {
        if (buy[j].get(GRB.DoubleAttr.X) > 0.0001) {
          System.out.println(buy[j].get(GRB.StringAttr.VarName) + " " +
              buy[j].get(GRB.DoubleAttr.X));
        }
      }
      System.out.println("\nNutrition:");
      for (int i = 0; i < nutrition.length; ++i) {</pre>
        System.out.println(nutrition[i].get(GRB.StringAttr.VarName) + " " +
            nutrition[i].get(GRB.DoubleAttr.X));
      }
    } else {
      System.out.println("No solution");
 }
}
```

Facility.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Facility location: a company currently ships its product from 5 plants
  to 4 warehouses. It is considering closing some plants to reduce
  costs. What plant(s) should the company close, in order to minimize
  transportation and fixed costs?
  Based on an example from Frontline Systems:
  http://www.solver.com/disfacility.htm
  Used with permission.
import gurobi.*;
public class Facility {
 public static void main(String[] args) {
   try {
      // Warehouse demand in thousands of units
      double Demand[] = new double[] { 15, 18, 14, 20 };
      // Plant capacity in thousands of units
      double Capacity[] = new double[] { 20, 22, 17, 19, 18 };
      // Fixed costs for each plant
      double FixedCosts[] =
          new double[] { 12000, 15000, 17000, 13000, 16000 };
      // Transportation costs per thousand units
      double TransCosts[][] =
          new double[][] { { 4000, 2000, 3000, 2500, 4500 },
              { 2500, 2600, 3400, 3000, 4000 },
              { 1200, 1800, 2600, 4100, 3000 },
              { 2200, 2600, 3100, 3700, 3200 } };
      // Number of plants and warehouses
      int nPlants = Capacity.length;
      int nWarehouses = Demand.length;
      // Model
      GRBEnv env = new GRBEnv();
     GRBModel model = new GRBModel(env);
     model.set(GRB.StringAttr.ModelName, "facility");
```

```
// Plant open decision variables: open[p] == 1 if plant p is open.
GRBVar[] open = new GRBVar[nPlants];
for (int p = 0; p < nPlants; ++p) {
  open[p] = model.addVar(0, 1, FixedCosts[p], GRB.BINARY, "Open" + p);
}
// Transportation decision variables: how much to transport from
// a plant p to a warehouse w
GRBVar[][] transport = new GRBVar[nWarehouses][nPlants];
for (int w = 0; w < nWarehouses; ++w) {</pre>
  for (int p = 0; p < nPlants; ++p) {
    transport[w][p] =
        model.addVar(0, GRB.INFINITY, TransCosts[w][p], GRB.CONTINUOUS,
                      "Trans" + p + "." + w);
  }
}
// The objective is to minimize the total fixed and variable costs
model.set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.update();
// Production constraints
// Note that the right-hand limit sets the production to zero if
// the plant is closed
for (int p = 0; p < nPlants; ++p) {
  GRBLinExpr ptot = new GRBLinExpr();
  for (int w = 0; w < nWarehouses; ++w) {</pre>
    ptot.addTerm(1.0, transport[w][p]);
  }
  GRBLinExpr limit = new GRBLinExpr();
  limit.addTerm(Capacity[p], open[p]);
  model.addConstr(ptot, GRB.LESS_EQUAL, limit, "Capacity" + p);
}
// Demand constraints
for (int w = 0; w < nWarehouses; ++w) {</pre>
  GRBLinExpr dtot = new GRBLinExpr();
  for (int p = 0; p < nPlants; ++p) {
    dtot.addTerm(1.0, transport[w][p]);
  }
  model.addConstr(dtot, GRB.EQUAL, Demand[w], "Demand" + w);
}
```

```
// Guess at the starting point: close the plant with the highest
// fixed costs; open all others
// First, open all plants
for (int p = 0; p < nPlants; ++p) {
  open[p].set(GRB.DoubleAttr.Start, 1.0);
// Now close the plant with the highest fixed cost
System.out.println("Initial guess:");
double maxFixed = -GRB.INFINITY;
for (int p = 0; p < nPlants; ++p) {
  if (FixedCosts[p] > maxFixed) {
    maxFixed = FixedCosts[p];
  }
}
for (int p = 0; p < nPlants; ++p) {
  if (FixedCosts[p] == maxFixed) {
    open[p].set(GRB.DoubleAttr.Start, 0.0);
    System.out.println("Closing plant " + p + "\n");
    break;
  }
}
// Use barrier to solve root relaxation
model.getEnv().set(GRB.IntParam.Method, GRB.METHOD_BARRIER);
// Solve
model.optimize();
// Print solution
System.out.println("\nTOTAL COSTS: " + model.get(GRB.DoubleAttr.ObjVal));
System.out.println("SOLUTION:");
for (int p = 0; p < nPlants; ++p) {
  if (open[p].get(GRB.DoubleAttr.X) == 1.0) {
    System.out.println("Plant " + p + " open:");
    for (int w = 0; w < nWarehouses; ++w) {
      if (transport[w][p].get(GRB.DoubleAttr.X) > 0.0001) {
        System.out.println(" Transport " +
            transport[w][p].get(GRB.DoubleAttr.X) +
            " units to warehouse " + w);
  } else {
```

Feasopt.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, adds artificial
  variables to each constraint, and then minimizes the sum of the
  artificial variables. A solution with objective zero corresponds
  to a feasible solution to the input model.
  We can also use FeasRelax feature to do it. In this example, we
  use minrelax=1, i.e. optimizing the returned model finds a solution
  that minimizes the original objective, but only from among those
  solutions that minimize the sum of the artificial variables. */
import gurobi.*;
public class Feasopt {
 public static void main(String[] args) {
    if (args.length < 1) {
     System.out.println("Usage: java Feasopt filename");
     System.exit(1);
    }
    try {
     GRBEnv env = new GRBEnv();
      GRBModel feasmodel = new GRBModel(env, args[0]);
      // Create a copy to use FeasRelax feature later */
      GRBModel feasmodel1 = new GRBModel(feasmodel);
      // Clear objective
      feasmodel.setObjective(new GRBLinExpr());
      // Add slack variables
      GRBConstr[] c = feasmodel.getConstrs();
      for (int i = 0; i < c.length; ++i) {
        char sense = c[i].get(GRB.CharAttr.Sense);
        if (sense != '>') {
          GRBConstr[] constrs = new GRBConstr[] { c[i] };
          double[] coeffs = new double[] { -1 };
          feasmodel.addVar(0.0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, constrs,
                           coeffs, "ArtN_" +
                               c[i].get(GRB.StringAttr.ConstrName));
        }
        if (sense != '<') {
          GRBConstr[] constrs = new GRBConstr[] { c[i] };
```

```
double[] coeffs = new double[] { 1 };
          feasmodel.addVar(0.0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, constrs,
                           coeffs, "ArtP_" +
                               c[i].get(GRB.StringAttr.ConstrName));
        }
      }
      feasmodel.update();
      // Optimize modified model
      feasmodel.write("feasopt.lp");
      feasmodel.optimize();
      // use FeasRelax feature */
      feasmodel1.feasRelax(GRB.FEASRELAX_LINEAR, true, false, true);
      feasmodel1.write("feasopt1.lp");
      feasmodel1.optimize();
      // Dispose of model and environment
      feasmodel1.dispose();
      feasmodel.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
    }
 }
}
```

Fixanddive.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Implement a simple MIP heuristic. Relax the model,
 sort variables based on fractionality, and fix the 25% of
 the fractional variables that are closest to integer variables.
Repeat until either the relaxation is integer feasible or
 linearly infeasible. */
import gurobi.*;
import java.util.*;
public class Fixanddive {
 public static void main(String[] args) {
    // Comparison class used to sort variable list based on relaxation
    // fractionality
    class FractionalCompare implements Comparator<GRBVar> {
      public int compare(GRBVar v1, GRBVar v2) {
        try {
          double sol1 = Math.abs(v1.get(GRB.DoubleAttr.X));
          double sol2 = Math.abs(v2.get(GRB.DoubleAttr.X));
          double frac1 = Math.abs(sol1 - Math.floor(sol1 + 0.5));
          double frac2 = Math.abs(sol2 - Math.floor(sol2 + 0.5));
          if (frac1 < frac2) {</pre>
            return -1;
          } else if (frac1 == frac2) {
            return 0;
          } else {
            return 1;
          }
        } catch (GRBException e) {
          System.out.println("Error code: " + e.getErrorCode() + ". " +
              e.getMessage());
        return 0;
      }
    }
    if (args.length < 1) {
      System.out.println("Usage: java Fixanddive filename");
      System.exit(1);
    }
```

```
try {
  // Read model
  GRBEnv env = new GRBEnv();
  GRBModel model = new GRBModel(env, args[0]);
  // Collect integer variables and relax them
  ArrayList<GRBVar> intvars = new ArrayList<GRBVar>();
  for (GRBVar v : model.getVars()) {
    if (v.get(GRB.CharAttr.VType) != GRB.CONTINUOUS) {
      intvars.add(v);
      v.set(GRB.CharAttr.VType, GRB.CONTINUOUS);
   }
  }
  model.getEnv().set(GRB.IntParam.OutputFlag, 0);
 model.optimize();
  // Perform multiple iterations. In each iteration, identify the first
  // quartile of integer variables that are closest to an integer value
  // in the relaxation, fix them to the nearest integer, and repeat.
 for (int iter = 0; iter < 1000; ++iter) {
    // create a list of fractional variables, sorted in order of
    // increasing distance from the relaxation solution to the nearest
    // integer value
    ArrayList<GRBVar> fractional = new ArrayList<GRBVar>();
    for (GRBVar v : intvars) {
      double sol = Math.abs(v.get(GRB.DoubleAttr.X));
      if (Math.abs(sol - Math.floor(sol + 0.5)) > 1e-5) {
        fractional.add(v);
    }
    System.out.println("Iteration " + iter + ", obj " +
        model.get(GRB.DoubleAttr.ObjVal) + ", fractional " +
        fractional.size());
    if (fractional.size() == 0) {
      System.out.println("Found feasible solution - objective " +
          model.get(GRB.DoubleAttr.ObjVal));
      break;
    }
```

```
// Fix the first quartile to the nearest integer value
        Collections.sort(fractional, new FractionalCompare());
        int nfix = Math.max(fractional.size() / 4, 1);
        for (int i = 0; i < nfix; ++i) {
          GRBVar v = fractional.get(i);
          double fixval = Math.floor(v.get(GRB.DoubleAttr.X) + 0.5);
          v.set(GRB.DoubleAttr.LB, fixval);
          v.set(GRB.DoubleAttr.UB, fixval);
          System.out.println(" Fix " + v.get(GRB.StringAttr.VarName) +
              " to " + fixval + " ( rel " + v.get(GRB.DoubleAttr.X) + " )");
        }
        model.optimize();
        // Check optimization result
        if (model.get(GRB.IntAttr.Status) != GRB.Status.OPTIMAL) {
          System.out.println("Relaxation is infeasible");
          break;
        }
      }
      // Dispose of model and environment
      model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
    }
  }
}
```

Lp.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
   If the model is infeasible or unbounded, the example turns off
  presolve and solves the model again. If the model is infeasible,
  the example computes an Irreducible Infeasible Subsystem (IIS),
  and writes it to a file */
import gurobi.*;
public class Lp {
 public static void main(String[] args) {
    if (args.length < 1) {
      System.out.println("Usage: java Lp filename");
     System.exit(1);
    }
    try {
      GRBEnv env = new GRBEnv();
      GRBModel model = new GRBModel(env, args[0]);
     model.optimize();
      int optimstatus = model.get(GRB.IntAttr.Status);
      if (optimstatus == GRB.Status.INF_OR_UNBD) {
        model.getEnv().set(GRB.IntParam.Presolve, 0);
        model.optimize();
        optimstatus = model.get(GRB.IntAttr.Status);
      }
      if (optimstatus == GRB.Status.OPTIMAL) {
        double objval = model.get(GRB.DoubleAttr.ObjVal);
        System.out.println("Optimal objective: " + objval);
      } else if (optimstatus == GRB.Status.INFEASIBLE) {
        System.out.println("Model is infeasible");
        // Compute and write out IIS
        model.computeIIS();
        model.write("model.ilp");
      } else if (optimstatus == GRB.Status.UNBOUNDED) {
        System.out.println("Model is unbounded");
      } else {
```

Lpmethod.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve a model with different values of the Method parameter;
   show which value gives the shortest solve time. */
import gurobi.*;
public class Lpmethod {
 public static void main(String[] args) {
    if (args.length < 1) {
      System.out.println("Usage: java Lpmethod filename");
     System.exit(1);
    try {
      // Read model
      GRBEnv env = new GRBEnv();
      GRBModel model = new GRBModel(env, args[0]);
      GRBEnv menv = model.getEnv();
      // Solve the model with different values of Method
      int bestMethod = -1;
      double bestTime = menv.get(GRB.DoubleParam.TimeLimit);
      for (int i = 0; i \le 2; ++i) {
        model.reset();
        menv.set(GRB.IntParam.Method, i);
        model.optimize();
        if (model.get(GRB.IntAttr.Status) == GRB.Status.OPTIMAL) {
          bestTime = model.get(GRB.DoubleAttr.Runtime);
          bestMethod = i;
          // Reduce the TimeLimit parameter to save time
          // with other methods
          menv.set(GRB.DoubleParam.TimeLimit, bestTime);
        }
      }
      // Report which method was fastest
      if (bestMethod == -1) {
        System.out.println("Unable to solve this model");
      } else {
        System.out.println("Solved in " + bestTime
            + " seconds with Method: " + bestMethod);
```

Lpmod.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
  If the model can be solved, then it finds the smallest positive variable,
  sets its upper bound to zero, and resolves the model two ways:
  first with an advanced start, then without an advanced start
   (i.e. 'from scratch'). */
import gurobi.*;
public class Lpmod {
 public static void main(String[] args) {
    if (args.length < 1) {
     System.out.println("Usage: java Lpmod filename");
     System.exit(1);
    }
    trv {
      // Read model and determine whether it is an LP
     GRBEnv env = new GRBEnv();
     GRBModel model = new GRBModel(env, args[0]);
      if (model.get(GRB.IntAttr.IsMIP) != 0) {
        System.out.println("The model is not a linear program");
        System.exit(1);
      }
     model.optimize();
      int status = model.get(GRB.IntAttr.Status);
      if (status == GRB.Status.INF_OR_UNBD ||
          status == GRB.Status.INFEASIBLE ||
          status == GRB.Status.UNBOUNDED
                                             ) {
        System.out.println("The model cannot be solved because it is "
            + "infeasible or unbounded");
        System.exit(1);
      }
      if (status != GRB.Status.OPTIMAL) {
        System.out.println("Optimization was stopped with status " + status);
        System.exit(0);
      }
```

```
// Find the smallest variable value
  double minVal = GRB.INFINITY;
  GRBVar minVar = null;
  for (GRBVar v : model.getVars()) {
    double sol = v.get(GRB.DoubleAttr.X);
    if ((sol > 0.0001) && (sol < minVal) &&
        (v.get(GRB.DoubleAttr.LB) == 0.0)) {
     minVal = sol;
     minVar = v;
   }
  }
  System.out.println("\n*** Setting " +
     minVar.get(GRB.StringAttr.VarName) + " from " + minVal +
      " to zero ***\n");
 minVar.set(GRB.DoubleAttr.UB, 0.0);
  // Solve from this starting point
 model.optimize();
  // Save iteration & time info
  double warmCount = model.get(GRB.DoubleAttr.IterCount);
  double warmTime = model.get(GRB.DoubleAttr.Runtime);
  // Reset the model and resolve
  System.out.println("\n*** Resetting and solving "
      + "without an advanced start ***\n");
 model.reset();
  model.optimize();
  double coldCount = model.get(GRB.DoubleAttr.IterCount);
  double coldTime = model.get(GRB.DoubleAttr.Runtime);
  System.out.println("\n*** Warm start: " + warmCount + " iterations, " +
      warmTime + " seconds");
  System.out.println("*** Cold start: " + coldCount + " iterations, " +
      coldTime + " seconds");
  // Dispose of model and environment
 model.dispose();
  env.dispose();
} catch (GRBException e) {
  System.out.println("Error code: " + e.getErrorCode() + ". " +
      e.getMessage());
```

} }

Mip1.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple MIP model:
                x +
    maximize
                       y + 2z
     subject to x + 2y + 3z \le 4
                 x + y
                               >= 1
    x, y, z binary
import gurobi.*;
public class Mip1 {
 public static void main(String[] args) {
   try {
      GRBEnv
                      = new GRBEnv("mip1.log");
     GRBModel model = new GRBModel(env);
      // Create variables
      GRBVar x = model.addVar(0.0, 1.0, 0.0, GRB.BINARY, "x");
     GRBVar y = model.addVar(0.0, 1.0, 0.0, GRB.BINARY, "y");
     GRBVar z = model.addVar(0.0, 1.0, 0.0, GRB.BINARY, "z");
     // Integrate new variables
     model.update();
     // Set objective: maximize x + y + 2z
     GRBLinExpr expr = new GRBLinExpr();
      expr.addTerm(1.0, x); expr.addTerm(1.0, y); expr.addTerm(2.0, z);
     model.setObjective(expr, GRB.MAXIMIZE);
      // Add constraint: x + 2 y + 3 z \le 4
      expr = new GRBLinExpr();
      expr.addTerm(1.0, x); expr.addTerm(2.0, y); expr.addTerm(3.0, z);
     model.addConstr(expr, GRB.LESS_EQUAL, 4.0, "c0");
      // Add constraint: x + y >= 1
      expr = new GRBLinExpr();
      expr.addTerm(1.0, x); expr.addTerm(1.0, y);
```

```
model.addConstr(expr, GRB.GREATER_EQUAL, 1.0, "c1");
      // Optimize model
      model.optimize();
      System.out.println(x.get(GRB.StringAttr.VarName)
                         + " " +x.get(GRB.DoubleAttr.X));
      System.out.println(y.get(GRB.StringAttr.VarName)
                         + " " +y.get(GRB.DoubleAttr.X));
      System.out.println(z.get(GRB.StringAttr.VarName)
                         + " " +z.get(GRB.DoubleAttr.X));
      System.out.println("Obj: " + model.get(GRB.DoubleAttr.ObjVal));
      // Dispose of model and environment
      model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
                         e.getMessage());
    }
  }
}
```

Mip2.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, solves it and
  prints the objective values from all feasible solutions
  generated while solving the MIP. Then it creates the fixed
  model and solves that model. */
import gurobi.*;
public class Mip2 {
 public static void main(String[] args) {
    if (args.length < 1) {
      System.out.println("Usage: java Mip2 filename");
      System.exit(1);
    }
    try {
      GRBEnv env = new GRBEnv();
     GRBModel model = new GRBModel(env, args[0]);
      if (model.get(GRB.IntAttr.IsMIP) == 0) {
        System.out.println("Model is not a MIP");
        System.exit(1);
      }
     model.optimize();
      int optimstatus = model.get(GRB.IntAttr.Status);
      double objval = 0;
      if (optimstatus == GRB.Status.OPTIMAL) {
        objval = model.get(GRB.DoubleAttr.ObjVal);
        System.out.println("Optimal objective: " + objval);
      } else if (optimstatus == GRB.Status.INF_OR_UNBD) {
        System.out.println("Model is infeasible or unbounded");
      } else if (optimstatus == GRB.Status.INFEASIBLE) {
        System.out.println("Model is infeasible");
      } else if (optimstatus == GRB.Status.UNBOUNDED) {
        System.out.println("Model is unbounded");
        return:
      } else {
        System.out.println("Optimization was stopped with status = "
            + optimstatus);
```

```
return;
}
/* Iterate over the solutions and compute the objectives */
GRBVar[] vars = model.getVars();
model.getEnv().set(GRB.IntParam.OutputFlag, 0);
System.out.println();
for (int k = 0; k < model.get(GRB.IntAttr.SolCount); ++k) {</pre>
  model.getEnv().set(GRB.IntParam.SolutionNumber, k);
  double objn = 0.0;
  for (int j = 0; j < vars.length; j++) {
    objn += vars[j].get(GRB.DoubleAttr.Obj)
        * vars[j].get(GRB.DoubleAttr.Xn);
  }
  System.out.println("Solution " + k + " has objective: " + objn);
}
System.out.println();
model.getEnv().set(GRB.IntParam.OutputFlag, 1);
/* Create a fixed model, turn off presolve and solve */
GRBModel fixed = model.fixedModel();
fixed.getEnv().set(GRB.IntParam.Presolve, 0);
fixed.optimize();
int foptimstatus = fixed.get(GRB.IntAttr.Status);
if (foptimstatus != GRB.Status.OPTIMAL) {
  System.err.println("Error: fixed model isn't optimal");
  return;
}
double fobjval = fixed.get(GRB.DoubleAttr.ObjVal);
if (Math.abs(fobjval - objval) > 1.0e-6 * (1.0 + Math.abs(objval))) {
  System.err.println("Error: objective values are different");
  return;
}
GRBVar[] fvars = fixed.getVars();
```

```
double[] x = fixed.get(GRB.DoubleAttr.X, fvars);
      String[] vnames = fixed.get(GRB.StringAttr.VarName, fvars);
      for (int j = 0; j < fvars.length; <math>j++) {
        if (x[j] != 0.0) {
          System.out.println(vnames[j] + " " + x[j]);
        }
      }
      // Dispose of models and environment
      fixed.dispose();
      model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". "
          + e.getMessage());
    }
 }
}
```

Params.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Use parameters that are associated with a model.
  A MIP is solved for 5 seconds with different sets of parameters.
  The one with the smallest MIP gap is selected, and the optimization
   is resumed until the optimal solution is found.
import gurobi.*;
public class Params {
  // Simple function to determine the MIP gap
 private static double gap(GRBModel model) throws GRBException {
    if ((model.get(GRB.IntAttr.SolCount) == 0) ||
        (Math.abs(model.get(GRB.DoubleAttr.ObjVal)) < 1e-6)) {
     return GRB.INFINITY;
    }
    return Math.abs(model.get(GRB.DoubleAttr.ObjBound) -
        model.get(GRB.DoubleAttr.ObjVal)) /
        Math.abs(model.get(GRB.DoubleAttr.ObjVal));
  }
 public static void main(String[] args) {
    if (args.length < 1) {
      System.out.println("Usage: java Params filename");
      System.exit(1);
    try {
      // Read model and verify that it is a MIP
     GRBEnv env = new GRBEnv();
      GRBModel base = new GRBModel(env, args[0]);
      if (base.get(GRB.IntAttr.IsMIP) == 0) {
        System.out.println("The model is not an integer program");
        System.exit(1);
      }
      // Set a 5 second time limit
      base.getEnv().set(GRB.DoubleParam.TimeLimit, 5);
      // Now solve the model with different values of MIPFocus
```

```
double bestGap = GRB.INFINITY;
      GRBModel bestModel = null;
      for (int i = 0; i <= 3; ++i) {
        GRBModel m = new GRBModel(base);
        m.getEnv().set(GRB.IntParam.MIPFocus, i);
        m.optimize();
        if (bestModel == null || bestGap > gap(m)) {
          bestModel = m;
          bestGap = gap(bestModel);
        }
      }
      // Finally, reset the time limit and continue to solve the
      // best model to optimality
      bestModel.getEnv().set(GRB.DoubleParam.TimeLimit, GRB.INFINITY);
      bestModel.optimize();
      System.out.println("Solved with MIPFocus: " +
          bestModel.getEnv().get(GRB.IntParam.MIPFocus));
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
    }
 }
}
```

Qcp.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QCP model:
     maximize
     subject to x + y + z = 1
                 x^2 + y^2 \le z^2 (second-order cone)
                                 (rotated second-order cone)
                 x^2 \le yz
*/
import gurobi.*;
public class Qcp {
 public static void main(String[] args) {
   try {
      GRBEnv
                      = new GRBEnv("qcp.log");
     GRBModel model = new GRBModel(env);
      // Create variables
      GRBVar x = model.addVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "x");
     GRBVar y = model.addVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "y");
     GRBVar z = model.addVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "z");
     // Integrate new variables
     model.update();
     // Set objective
     GRBLinExpr obj = new GRBLinExpr();
      obj.addTerm(1.0, x);
     model.setObjective(obj, GRB.MAXIMIZE);
      // Add linear constraint: x + y + z = 1
     GRBLinExpr expr = new GRBLinExpr();
      expr.addTerm(1.0, x); expr.addTerm(1.0, y); expr.addTerm(1.0, z);
     model.addConstr(expr, GRB.EQUAL, 1.0, "c0");
      // Add second-order cone: x^2 + y^2 \le z^2
     GRBQuadExpr qexpr = new GRBQuadExpr();
     qexpr.addTerm(1.0, x, x);
```

```
qexpr.addTerm(1.0, y, y);
      qexpr.addTerm(-1.0, z, z);
     model.addQConstr(qexpr, GRB.LESS_EQUAL, 0.0, "qc0");
      // Add rotated cone: x^2 <= yz
      qexpr = new GRBQuadExpr();
      qexpr.addTerm(1.0, x, x);
      qexpr.addTerm(-1.0, y, z);
     model.addQConstr(qexpr, GRB.LESS_EQUAL, 0.0, "qc1");
      // Optimize model
     model.optimize();
      System.out.println(x.get(GRB.StringAttr.VarName)
                         + " " +x.get(GRB.DoubleAttr.X));
      System.out.println(y.get(GRB.StringAttr.VarName)
                         + " " +y.get(GRB.DoubleAttr.X));
      System.out.println(z.get(GRB.StringAttr.VarName)
                         + " " +z.get(GRB.DoubleAttr.X));
      System.out.println("Obj: " + model.get(GRB.DoubleAttr.ObjVal) + " " +
                         obj.getValue());
      System.out.println();
      // Dispose of model and environment
     model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
   }
}
```

Qp.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                 x^2 + x*y + y^2 + y*z + z^2 + z
     subject to x + 2y + 3z >= 4
                 x + y
                               >= 1
  It solves it once as a continuous model, and once as an integer model.
*/
import gurobi.*;
public class Qp {
 public static void main(String[] args) {
    try {
      GRBEnv
                      = new GRBEnv("qp.log");
                env
     GRBModel model = new GRBModel(env);
      // Create variables
     GRBVar x = model.addVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "x");
      GRBVar y = model.addVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "y");
     GRBVar z = model.addVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "z");
      // Integrate new variables
     model.update();
      // Set objective
      GRBQuadExpr obj = new GRBQuadExpr();
      obj.addTerm(1.0, x, x);
      obj.addTerm(1.0, x, y);
      obj.addTerm(1.0, y, y);
      obj.addTerm(1.0, y, z);
      obj.addTerm(1.0, z, z);
      obj.addTerm(2.0, x);
     model.setObjective(obj);
      // Add constraint: x + 2 y + 3 z >= 4
     GRBLinExpr expr = new GRBLinExpr();
      expr.addTerm(1.0, x); expr.addTerm(2.0, y); expr.addTerm(3.0, z);
```

```
model.addConstr(expr, GRB.GREATER_EQUAL, 4.0, "c0");
// Add constraint: x + y >= 1
expr = new GRBLinExpr();
expr.addTerm(1.0, x); expr.addTerm(1.0, y);
model.addConstr(expr, GRB.GREATER_EQUAL, 1.0, "c1");
// Optimize model
model.optimize();
System.out.println(x.get(GRB.StringAttr.VarName)
                   + " " +x.get(GRB.DoubleAttr.X));
System.out.println(y.get(GRB.StringAttr.VarName)
                   + " " +y.get(GRB.DoubleAttr.X));
System.out.println(z.get(GRB.StringAttr.VarName)
                   + " " +z.get(GRB.DoubleAttr.X));
System.out.println("Obj: " + model.get(GRB.DoubleAttr.ObjVal) + " " +
                   obj.getValue());
System.out.println();
// Change variable types to integer
x.set(GRB.CharAttr.VType, GRB.INTEGER);
y.set(GRB.CharAttr.VType, GRB.INTEGER);
z.set(GRB.CharAttr.VType, GRB.INTEGER);
// Optimize again
model.optimize();
System.out.println(x.get(GRB.StringAttr.VarName)
                   + " " +x.get(GRB.DoubleAttr.X));
System.out.println(y.get(GRB.StringAttr.VarName)
                   + " " +y.get(GRB.DoubleAttr.X));
System.out.println(z.get(GRB.StringAttr.VarName)
                   + " " +z.get(GRB.DoubleAttr.X));
System.out.println("Obj: " + model.get(GRB.DoubleAttr.ObjVal) + " " +
                   obj.getValue());
// Dispose of model and environment
```

Sensitivity.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Simple MIP sensitivity analysis example.
For each integer variable, fix it to its lower and upper bound
and check the impact on the objective. */
import gurobi.*;
public class Sensitivity {
 public static void main(String[] args) {
    if (args.length < 1) {
      System.out.println("Usage: java Sensitivity filename");
     System.exit(1);
    }
    try {
      // Read model
     GRBEnv env = new GRBEnv();
      GRBModel a = new GRBModel(env, args[0]);
      a.optimize();
      a.getEnv().set(GRB.IntParam.OutputFlag, 0);
      // Extract variables from model
      GRBVar[] avars = a.getVars();
     for (int i = 0; i < avars.length; ++i) {</pre>
        GRBVar v = avars[i];
        if (v.get(GRB.CharAttr.VType) == GRB.BINARY) {
          // Create clone and fix variable
          GRBModel b = new GRBModel(a);
          GRBVar bv = b.getVars()[i];
          if (v.get(GRB.DoubleAttr.X) - v.get(GRB.DoubleAttr.LB) < 0.5) {
            bv.set(GRB.DoubleAttr.LB, bv.get(GRB.DoubleAttr.UB));
          } else {
            bv.set(GRB.DoubleAttr.UB, bv.get(GRB.DoubleAttr.LB));
          b.optimize();
          if (b.get(GRB.IntAttr.Status) == GRB.Status.OPTIMAL) {
            double objchg =
```

```
b.get(GRB.DoubleAttr.ObjVal) - a.get(GRB.DoubleAttr.ObjVal);
            if (objchg < 0) {
              objchg = 0;
            }
            System.out.println("Objective sensitivity for variable " +
                v.get(GRB.StringAttr.VarName) + " is " + objchg);
          } else {
            System.out.println("Objective sensitivity for variable " +
                v.get(GRB.StringAttr.VarName) + " is infinite");
          }
          // Dispose of model
          b.dispose();
        }
      }
      // Dispose of model and environment
      a.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
    }
  }
}
```

Sos.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example creates a very simple Special Ordered Set (SOS) model.
   The model consists of 3 continuous variables, no linear constraints,
   and a pair of SOS constraints of type 1. */
import gurobi.*;
public class Sos {
 public static void main(String[] args) {
      GRBEnv env = new GRBEnv();
      GRBModel model = new GRBModel(env);
      // Create variables
      double ub[]
                     = \{1, 1, 2\};
                     = \{-2, -1, -1\};
      double obj[]
      String names[] = {"x0", "x1", "x2"};
      GRBVar[] x = model.addVars(null, ub, obj, null, names);
      // Integrate new variables
      model.update();
      // Add first SOS1: x0=0 or x1=0
      GRBVar sosv1[] = \{x[0], x[1]\};
      double soswt1[] = \{1, 2\};
      model.addSOS(sosv1, soswt1, GRB.SOS_TYPE1);
      // Add second SOS1: x0=0 or x2=0
      GRBVar sosv2[] = \{x[0], x[2]\};
      double soswt2[] = \{1, 2\};
      model.addSOS(sosv2, soswt2, GRB.SOS_TYPE1);
      // Optimize model
      model.optimize();
```

Sudoku.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
  Sudoku example.
 The Sudoku board is a 9x9 grid, which is further divided into a 3x3 grid
  of 3x3 grids. Each cell in the grid must take a value from 0 to 9.
 No two grid cells in the same row, column, or 3x3 subgrid may take the
  same value.
  In the MIP formulation, binary variables x[i,j,v] indicate whether
  cell <i,j> takes value 'v'. The constraints are as follows:
    1. Each cell must take exactly one value (sum_v x[i,j,v] = 1)
    2. Each value is used exactly once per row (sum_i x[i,j,v] = 1)
    3. Each value is used exactly once per column (sum_j x[i,j,v] = 1)
    4. Each value is used exactly once per 3x3 subgrid (sum_grid x[i,j,v] = 1)
 Input datasets for this example can be found in examples/data/sudoku*.
*/
import gurobi.*;
import java.io.*;
public class Sudoku {
 public static void main(String[] args) {
    int n = 9;
    int s = 3;
    if (args.length < 1) {
     System.out.println("Usage: java Sudoku filename");
     System.exit(1);
    }
    try {
     GRBEnv env = new GRBEnv();
     GRBModel model = new GRBModel(env);
      // Create 3-D array of model variables
     GRBVar[][][] vars = new GRBVar[n][n][n];
      for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
          for (int v = 0; v < n; v++) {
            String st = "G_" + String.valueOf(i) + "_" + String.valueOf(j)
```

```
+ "_" + String.valueOf(v);
      vars[i][j][v] = model.addVar(0.0, 1.0, 0.0, GRB.BINARY, st);
    }
  }
}
// Integrate variables into model
model.update();
// Add constraints
GRBLinExpr expr;
// Each cell must take one value
for (int i = 0; i < n; i++) {
  for (int j = 0; j < n; j++) {
    expr = new GRBLinExpr();
    expr.addTerms(null, vars[i][j]);
    String st = "V_" + String.valueOf(i) + "_" + String.valueOf(j);
    model.addConstr(expr, GRB.EQUAL, 1.0, st);
  }
}
// Each value appears once per row
for (int i = 0; i < n; i++) {
  for (int v = 0; v < n; v++) {
    expr = new GRBLinExpr();
    for (int j = 0; j < n; j++)
      expr.addTerm(1.0, vars[i][j][v]);
    String st = "R_" + String.valueOf(i) + "_" + String.valueOf(v);
    model.addConstr(expr, GRB.EQUAL, 1.0, st);
  }
}
// Each value appears once per column
for (int j = 0; j < n; j++) {
  for (int v = 0; v < n; v++) {
    expr = new GRBLinExpr();
    for (int i = 0; i < n; i++)
      expr.addTerm(1.0, vars[i][j][v]);
    String st = "C_" + String.valueOf(j) + "_" + String.valueOf(v);
```

```
model.addConstr(expr, GRB.EQUAL, 1.0, st);
  }
}
// Each value appears once per sub-grid
for (int v = 0; v < n; v++) {
  for (int i0 = 0; i0 < s; i0++) {
    for (int j0 = 0; j0 < s; j0++) {
      expr = new GRBLinExpr();
      for (int i1 = 0; i1 < s; i1++) {
        for (int j1 = 0; j1 < s; j1++) {
          expr.addTerm(1.0, vars[i0*s+i1][j0*s+j1][v]);
        }
      String st = "Sub_" + String.valueOf(v) + "_" + String.valueOf(i0)
                         + "_" + String.valueOf(j0);
      model.addConstr(expr, GRB.EQUAL, 1.0, st);
    }
  }
}
// Update model
model.update();
// Fix variables associated with pre-specified cells
File file = new File(args[0]);
FileInputStream fis = new FileInputStream(file);
byte[] input = new byte[n];
for (int i = 0; i < n; i++) {
  fis.read(input);
  for (int j = 0; j < n; j++) {
    int val = (int) input[j] - 48 - 1; // 0-based
    if (val >= 0)
      vars[i][j][val].set(GRB.DoubleAttr.LB, 1.0);
  // read the endline byte
  fis.read();
}
// Optimize model
```

```
model.optimize();
      // Write model to file
      model.write("sudoku.lp");
      double[][][] x = model.get(GRB.DoubleAttr.X, vars);
      System.out.println();
      for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
          for (int v = 0; v < n; v++) {
            if (x[i][j][v] > 0.5) {
              System.out.print(v+1);
          }
        }
        System.out.println();
      }
      // Dispose of model and environment
      model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
    } catch (IOException e) {
      System.out.println("IO Error");
    }
 }
}
```

Tsp.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
// Solve a traveling salesman problem on a randomly generated set of
// points using lazy constraints.
                                    The base MIP model only includes
// 'degree-2' constraints, requiring each node to have exactly
// two incident edges. Solutions to this model may contain subtours -
// tours that don't visit every node. The lazy constraint callback
// adds new constraints to cut them off.
import gurobi.*;
public class Tsp extends GRBCallback {
 private GRBVar[][] vars;
 public Tsp(GRBVar[][] xvars) {
   vars = xvars;
  }
  // Subtour elimination callback. Whenever a feasible solution is found,
  // find the subtour that contains node 0, and add a subtour elimination
  // constraint if the tour doesn't visit every node.
 protected void callback() {
    try {
      if (where == GRB.CB_MIPSOL) {
        // Found an integer feasible solution - does it visit every node?
        int n = vars.length;
        int[] tour = findsubtour(getSolution(vars));
        if (tour.length < n) {</pre>
          // Add subtour elimination constraint
          GRBLinExpr expr = new GRBLinExpr();
          for (int i = 0; i < tour.length; i++)</pre>
            for (int j = i+1; j < tour.length; j++)</pre>
              expr.addTerm(1.0, vars[tour[i]][tour[j]]);
          addLazy(expr, GRB.LESS_EQUAL, tour.length-1);
        }
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
      e.printStackTrace();
    }
  }
```

```
// Given an integer-feasible solution 'sol', return the smallest
// sub-tour (as a list of node indices).
protected static int[] findsubtour(double[][] sol)
  int n = sol.length;
  boolean[] seen = new boolean[n];
  int[] tour = new int[n];
  int bestind, bestlen;
  int i, node, len, start;
  for (i = 0; i < n; i++)
    seen[i] = false;
  start = 0;
  bestlen = n+1;
  bestind = -1;
  node = 0;
  while (start < n) {
    for (node = 0; node < n; node++)
      if (!seen[node])
        break;
    if (node == n)
      break;
    for (len = 0; len < n; len++) \{
      tour[start+len] = node;
      seen[node] = true;
      for (i = 0; i < n; i++) {
        if (sol[node][i] > 0.5 && !seen[i]) {
          node = i;
          break;
        }
      }
      if (i == n) {
        len++;
        if (len < bestlen) {</pre>
          bestlen = len;
          bestind = start;
        start += len;
        break;
    }
  }
```

```
int result[] = new int[bestlen];
  for (i = 0; i < bestlen; i++)
    result[i] = tour[bestind+i];
  return result;
}
// Euclidean distance between points 'i' and 'j'
protected static double distance(double[] x,
                                  double[] y,
                                  int
                                           j) {
                                  int
  double dx = x[i]-x[j];
  double dy = y[i]-y[j];
  return Math.sqrt(dx*dx+dy*dy);
}
public static void main(String[] args) {
  if (args.length < 1) {
    System.out.println("Usage: java Tsp ncities");
    System.exit(1);
  int n = Integer.parseInt(args[0]);
  try {
    {\tt GRBEnv}
                   = new GRBEnv();
    GRBModel model = new GRBModel(env);
    // Must set LazyConstraints parameter when using lazy constraints
    model.getEnv().set(GRB.IntParam.LazyConstraints, 1);
    double[] x = new double[n];
    double[] y = new double[n];
    for (int i = 0; i < n; i++) {
      x[i] = Math.random();
      y[i] = Math.random();
    }
    // Create variables
```

```
GRBVar[][] vars = new GRBVar[n][n];
 for (int i = 0; i < n; i++)
    for (int j = 0; j \le i; j++) {
      vars[i][j] = model.addVar(0.0, 1.0, distance(x, y, i, j),
                                 GRB.BINARY,
                               "x"+String.valueOf(i)+"_"+String.valueOf(j));
      vars[j][i] = vars[i][j];
    }
  // Integrate variables
 model.update();
  // Degree-2 constraints
 for (int i = 0; i < n; i++) {
   GRBLinExpr expr = new GRBLinExpr();
    for (int j = 0; j < n; j++)
      expr.addTerm(1.0, vars[i][j]);
   model.addConstr(expr, GRB.EQUAL, 2.0, "deg2_"+String.valueOf(i));
  }
 // Forbid edge from node back to itself
 for (int i = 0; i < n; i++)
    vars[i][i].set(GRB.DoubleAttr.UB, 0.0);
 model.setCallback(new Tsp(vars));
 model.optimize();
  if (model.get(GRB.IntAttr.SolCount) > 0) {
    int[] tour = findsubtour(model.get(GRB.DoubleAttr.X, vars));
    System.out.print("Tour: ");
    for (int i = 0; i < tour.length; i++)</pre>
      System.out.print(String.valueOf(tour[i]) + " ");
    System.out.println();
  }
  // Dispose of model and environment
 model.dispose();
  env.dispose();
} catch (GRBException e) {
```

Tune.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a model from a file and tunes it.
  It then writes the best parameter settings to a file
  and solves the model using these parameters. */
import gurobi.*;
public class Tune {
 public static void main(String[] args) {
    if (args.length < 1) {
      System.out.println("Usage: java Tune filename");
     System.exit(1);
    try {
     GRBEnv env = new GRBEnv();
      // Read model from file
      GRBModel model = new GRBModel(env, args[0]);
      // Set the TuneResults parameter to 1
     model.getEnv().set(GRB.IntParam.TuneResults, 1);
      // Tune the model
     model.tune();
     // Get the number of tuning results
      int resultcount = model.get(GRB.IntAttr.TuneResultCount);
      if (resultcount > 0) {
        // Load the tuned parameters into the model's environment
        model.getTuneResult(0);
        // Write the tuned parameters to a file
        model.write("tune.prm");
        // Solve the model using the tuned parameters
        model.optimize();
      }
      // Dispose of model and environment
```

Workforce1.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, use IIS to find a set of
  conflicting constraints. Note that there may be additional conflicts
  besides what is reported via IIS. */
import gurobi.*;
public class Workforce1 {
 public static void main(String[] args) {
   try {
     // Sample data
     // Sets of days and workers
     String Shifts[] =
         new String[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
             "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
             "Sun14" };
     String Workers[] =
         new String[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
     int nShifts = Shifts.length;
     int nWorkers = Workers.length;
     // Number of workers required for each shift
     double shiftRequirements[] =
         new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
     // Amount each worker is paid to work one shift
     double pay[] = new double[] { 10, 12, 10, 8, 8, 9, 11 };
     // Worker availability: 0 if the worker is unavailable for a shift
     double availability[][] =
         new double[][] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
             \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\},\
             { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
             \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\},\
             { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
     // Model
```

```
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
GRBVar[][] x = new GRBVar[nWorkers][nShifts];
for (int w = 0; w < nWorkers; ++w) {
  for (int s = 0; s < nShifts; ++s) {
    x[w][s] =
        model.addVar(0, availability[w][s], pay[w], GRB.CONTINUOUS,
                     Workers[w] + "." + Shifts[s]);
  }
// The objective is to minimize the total pay costs
model.set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (int s = 0; s < nShifts; ++s) {
  GRBLinExpr lhs = new GRBLinExpr();
  for (int w = 0; w < nWorkers; ++w) {</pre>
    lhs.addTerm(1.0, x[w][s]);
  model.addConstr(lhs, GRB.EQUAL, shiftRequirements[s], Shifts[s]);
// Optimize
model.optimize();
int status = model.get(GRB.IntAttr.Status);
if (status == GRB.Status.UNBOUNDED) {
  System.out.println("The model cannot be solved "
      + "because it is unbounded");
  return;
if (status == GRB.Status.OPTIMAL) {
  System.out.println("The optimal objective is " +
      model.get(GRB.DoubleAttr.ObjVal));
  return;
}
```

```
if (status != GRB.Status.INF_OR_UNBD &&
          status != GRB.Status.INFEASIBLE
                                             ){
        System.out.println("Optimization was stopped with status " + status);
        return;
      }
      // Compute IIS
      System.out.println("The model is infeasible; computing IIS");
      model.computeIIS();
      System.out.println("\nThe following constraint(s) "
          + "cannot be satisfied:");
      for (GRBConstr c : model.getConstrs()) {
        if (c.get(GRB.IntAttr.IISConstr) == 1) {
          System.out.println(c.get(GRB.StringAttr.ConstrName));
      }
      // Dispose of model and environment
      model.dispose();
      env.dispose();
    } catch (GRBException e) {
      System.out.println("Error code: " + e.getErrorCode() + ". " +
          e.getMessage());
    }
 }
}
```

Workforce2.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, use IIS iteratively to
  find all conflicting constraints. */
import gurobi.*;
import java.util.*;
public class Workforce2 {
 public static void main(String[] args) {
   try {
     // Sample data
     // Sets of days and workers
     String Shifts[] =
         new String[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
             "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
             "Sun14" };
     String Workers[] =
         new String[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
     int nShifts = Shifts.length;
     int nWorkers = Workers.length;
     // Number of workers required for each shift
     double shiftRequirements[] =
         new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
     // Amount each worker is paid to work one shift
     double pay[] = new double[] { 10, 12, 10, 8, 8, 9, 11 };
     // Worker availability: 0 if the worker is unavailable for a shift
     double availability[][] =
         new double[][] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
             \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\},\
             { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
             \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\},\
             { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
     // Model
```

```
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
GRBVar[][] x = new GRBVar[nWorkers][nShifts];
for (int w = 0; w < nWorkers; ++w) {
  for (int s = 0; s < nShifts; ++s) {
    x[w][s] =
        model.addVar(0, availability[w][s], pay[w], GRB.CONTINUOUS,
                     Workers[w] + "." + Shifts[s]);
  }
// The objective is to minimize the total pay costs
model.set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (int s = 0; s < nShifts; ++s) {
  GRBLinExpr lhs = new GRBLinExpr();
  for (int w = 0; w < nWorkers; ++w) {</pre>
    lhs.addTerm(1.0, x[w][s]);
  model.addConstr(lhs, GRB.EQUAL, shiftRequirements[s], Shifts[s]);
// Optimize
model.optimize();
int status = model.get(GRB.IntAttr.Status);
if (status == GRB.Status.UNBOUNDED) {
  System.out.println("The model cannot be solved "
      + "because it is unbounded");
  return;
if (status == GRB.Status.OPTIMAL) {
  System.out.println("The optimal objective is " +
      model.get(GRB.DoubleAttr.ObjVal));
  return;
}
```

```
if (status != GRB.Status.INF_OR_UNBD &&
    status != GRB.Status.INFEASIBLE
                                       ) {
  System.out.println("Optimization was stopped with status " + status);
  return;
}
// Do IIS
System.out.println("The model is infeasible; computing IIS");
LinkedList<String> removed = new LinkedList<String>();
// Loop until we reduce to a model that can be solved
while (true) {
  model.computeIIS();
  System.out.println("\nThe following constraint cannot be satisfied:");
  for (GRBConstr c : model.getConstrs()) {
    if (c.get(GRB.IntAttr.IISConstr) == 1) {
      System.out.println(c.get(GRB.StringAttr.ConstrName));
      // Remove a single constraint from the model
      removed.add(c.get(GRB.StringAttr.ConstrName));
      model.remove(c);
      break;
  }
  System.out.println();
  model.optimize();
  status = model.get(GRB.IntAttr.Status);
  if (status == GRB.Status.UNBOUNDED) {
    System.out.println("The model cannot be solved "
        + "because it is unbounded");
    return;
  }
  if (status == GRB.Status.OPTIMAL) {
    break;
  }
  if (status != GRB.Status.INF_OR_UNBD &&
      status != GRB.Status.INFEASIBLE
                                          ) {
    System.out.println("Optimization was stopped with status " +
        status);
    return;
  }
}
System.out.println("\nThe following constraints were removed "
```

Workforce3.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, add slack variables
  to determine which constraints cannot be satisfied, and how much
  they need to be relaxed. */
import gurobi.*;
import java.util.*;
public class Workforce3 {
 public static void main(String[] args) {
   try {
     // Sample data
     // Sets of days and workers
     String Shifts[] =
         new String[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
             "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
             "Sun14" };
     String Workers[] =
         new String[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
      int nShifts = Shifts.length;
      int nWorkers = Workers.length;
     // Number of workers required for each shift
     double shiftRequirements[] =
         new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
     // Amount each worker is paid to work one shift
     double pay[] = new double[] { 10, 12, 10, 8, 8, 9, 11 };
      // Worker availability: 0 if the worker is unavailable for a shift
     double availability[][] =
         new double[][] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
             { 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 },
             \{ 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1 \},
             { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
             { 1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1 },
             { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
```

```
// Model
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
GRBVar[][] x = new GRBVar[nWorkers][nShifts];
for (int w = 0; w < nWorkers; ++w) {</pre>
  for (int s = 0; s < nShifts; ++s) {
    x[w][s] =
        model.addVar(0, availability[w][s], pay[w], GRB.CONTINUOUS,
                     Workers[w] + "." + Shifts[s]);
  }
}
// The objective is to minimize the total pay costs
model.set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
LinkedList<GRBConstr> reqCts = new LinkedList<GRBConstr>();
for (int s = 0; s < nShifts; ++s) {
  GRBLinExpr lhs = new GRBLinExpr();
  for (int w = 0; w < nWorkers; ++w) {
    lhs.addTerm(1.0, x[w][s]);
  GRBConstr newCt =
      model.addConstr(lhs, GRB.EQUAL, shiftRequirements[s], Shifts[s]);
  reqCts.add(newCt);
}
// Optimize
model.optimize();
int status = model.get(GRB.IntAttr.Status);
if (status == GRB.Status.UNBOUNDED) {
  System.out.println("The model cannot be solved "
      + "because it is unbounded");
  return;
}
if (status == GRB.Status.OPTIMAL) {
```

```
System.out.println("The optimal objective is " +
      model.get(GRB.DoubleAttr.ObjVal));
  return;
}
if (status != GRB.Status.INF_OR_UNBD &&
    status != GRB.Status.INFEASIBLE
                                       ) {
  System.out.println("Optimization was stopped with status " + status);
  return;
}
// Add slack variables to make the model feasible
System.out.println("The model is infeasible; adding slack variables");
// Set original objective coefficients to zero
model.setObjective(new GRBLinExpr());
// Add a new slack variable to each shift constraint so that the shifts
// can be satisfied
LinkedList<GRBVar> slacks = new LinkedList<GRBVar>();
for (GRBConstr c : reqCts) {
  GRBColumn col = new GRBColumn();
  col.addTerm(1.0, c);
  GRBVar newvar =
      model.addVar(0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, col,
                   c.get(GRB.StringAttr.ConstrName) + "Slack");
  slacks.add(newvar);
}
// Solve the model with slacks
model.optimize();
status = model.get(GRB.IntAttr.Status);
if (status == GRB.Status.INF_OR_UNBD ||
    status == GRB.Status.INFEASIBLE ||
    status == GRB.Status.UNBOUNDED
                                       ) {
  System.out.println("The model with slacks cannot be solved "
      + "because it is infeasible or unbounded");
  return;
}
if (status != GRB.Status.OPTIMAL) {
  System.out.println("Optimization was stopped with status " + status);
  return;
}
System.out.println("\nSlack values:");
for (GRBVar sv : slacks) {
```

Workforce4.java

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. We use Pareto optimization to solve the model:
  first, we minimize the linear sum of the slacks. Then, we constrain
  the sum of the slacks, and we minimize a quadratic objective that
  tries to balance the workload among the workers. */
import gurobi.*;
public class Workforce4 {
 public static void main(String[] args) {
   try {
     // Sample data
     // Sets of days and workers
     String Shifts[] =
         new String[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
             "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
             "Sun14" };
     String Workers[] =
         new String[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
     int nShifts = Shifts.length;
     int nWorkers = Workers.length;
     // Number of workers required for each shift
     double shiftRequirements[] =
         new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
     // Worker availability: 0 if the worker is unavailable for a shift
     double availability[][] =
         new double[][] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
             { 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 },
             { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
             \{1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1\}
             { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
     // Model
     GRBEnv env = new GRBEnv();
     GRBModel model = new GRBModel(env);
```

```
model.set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. This is no longer a pure assignment model, so we must
// use binary variables.
GRBVar[][] x = new GRBVar[nWorkers][nShifts];
for (int w = 0; w < nWorkers; ++w) {
  for (int s = 0; s < nShifts; ++s) {
    x[w][s] =
        model.addVar(0, availability[w][s], 0, GRB.BINARY,
                     Workers[w] + "." + Shifts[s]);
  }
}
// Slack variables for each shift constraint so that the shifts can
// be satisfied
GRBVar[] slacks = new GRBVar[nShifts];
for (int s = 0; s < nShifts; ++s) {
  slacks[s] =
      model.addVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS,
                   Shifts[s] + "Slack");
}
// Variable to represent the total slack
GRBVar totSlack = model.addVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS,
                                "totSlack");
// Variables to count the total shifts worked by each worker
GRBVar[] totShifts = new GRBVar[nWorkers];
for (int w = 0; w < nWorkers; ++w) {</pre>
  totShifts[w] = model.addVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS,
                              Workers[w] + "TotShifts");
}
// Update model to integrate new variables
model.update();
GRBLinExpr lhs;
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s, plus the slack
for (int s = 0; s < nShifts; ++s) {
  lhs = new GRBLinExpr();
  lhs.addTerm(1.0, slacks[s]);
  for (int w = 0; w < nWorkers; ++w) {</pre>
```

```
lhs.addTerm(1.0, x[w][s]);
  }
  model.addConstr(lhs, GRB.EQUAL, shiftRequirements[s], Shifts[s]);
}
// Constraint: set totSlack equal to the total slack
lhs = new GRBLinExpr();
lhs.addTerm(-1.0, totSlack);
for (int s = 0; s < nShifts; ++s) {
  lhs.addTerm(1.0, slacks[s]);
}
model.addConstr(lhs, GRB.EQUAL, 0, "totSlack");
// Constraint: compute the total number of shifts for each worker
for (int w = 0; w < nWorkers; ++w) {</pre>
  lhs = new GRBLinExpr();
  lhs.addTerm(-1.0, totShifts[w]);
  for (int s = 0; s < nShifts; ++s) {
    lhs.addTerm(1.0, x[w][s]);
  }
  model.addConstr(lhs, GRB.EQUAL, 0, "totShifts" + Workers[w]);
}
// Objective: minimize the total slack
GRBLinExpr obj = new GRBLinExpr();
obj.addTerm(1.0, totSlack);
model.setObjective(obj);
// Optimize
int status =
  solveAndPrint(model, totSlack, nWorkers, Workers, totShifts);
if (status != GRB.Status.OPTIMAL ) {
  return;
}
// Constrain the slack by setting its upper and lower bounds
totSlack.set(GRB.DoubleAttr.UB, totSlack.get(GRB.DoubleAttr.X));
totSlack.set(GRB.DoubleAttr.LB, totSlack.get(GRB.DoubleAttr.X));
// Variable to count the average number of shifts worked
GRBVar avgShifts =
  model.addVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS, "avgShifts");
// Variables to count the difference from average for each worker;
// note that these variables can take negative values.
```

```
GRBVar[] diffShifts = new GRBVar[nWorkers];
for (int w = 0; w < nWorkers; ++w) {</pre>
  diffShifts[w] = model.addVar(-GRB.INFINITY, GRB.INFINITY, 0,
                                GRB.CONTINUOUS, Workers[w] + "Diff");
}
// Update model to integrate new variables
model.update();
// Constraint: compute the average number of shifts worked
lhs = new GRBLinExpr();
lhs.addTerm(-nWorkers, avgShifts);
for (int w = 0; w < nWorkers; ++w) {</pre>
  lhs.addTerm(1.0, totShifts[w]);
model.addConstr(lhs, GRB.EQUAL, 0, "avgShifts");
// Constraint: compute the difference from the average number of shifts
for (int w = 0; w < nWorkers; ++w) {</pre>
  lhs = new GRBLinExpr();
  lhs.addTerm(-1, diffShifts[w]);
  lhs.addTerm(-1, avgShifts);
  lhs.addTerm( 1, totShifts[w]);
  model.addConstr(lhs, GRB.EQUAL, 0, Workers[w] + "Diff");
}
// Objective: minimize the sum of the square of the difference from the
// average number of shifts worked
GRBQuadExpr qobj = new GRBQuadExpr();
for (int w = 0; w < nWorkers; ++w) {</pre>
  qobj.addTerm(1.0, diffShifts[w], diffShifts[w]);
}
model.setObjective(qobj);
// Optimize
status =
  solveAndPrint(model, totSlack, nWorkers, Workers, totShifts);
if (status != GRB.Status.OPTIMAL ) {
  return;
}
// Dispose of model and environment
model.dispose();
env.dispose();
```

```
} catch (GRBException e) {
    System.out.println("Error code: " + e.getErrorCode() + ". " +
        e.getMessage());
  }
}
private static int solveAndPrint(GRBModel model, GRBVar totSlack,
                                 int nWorkers, String[] Workers,
                                 GRBVar[] totShifts) throws GRBException {
  model.optimize();
  int status = model.get(GRB.IntAttr.Status);
  if (status == GRB.Status.INF_OR_UNBD ||
      status == GRB.Status.INFEASIBLE ||
      status == GRB.Status.UNBOUNDED
                                         ) {
    System.out.println("The model cannot be solved "
        + "because it is infeasible or unbounded");
    return status;
  if (status != GRB.Status.OPTIMAL ) {
    System.out.println("Optimization was stopped with status " + status);
    return status;
  }
  // Print total slack and the number of shifts worked for each worker
  System.out.println("\nTotal slack required: " +
                     totSlack.get(GRB.DoubleAttr.X));
  for (int w = 0; w < nWorkers; ++w) {</pre>
    System.out.println(Workers[w] + " worked " +
                       totShifts[w].get(GRB.DoubleAttr.X) + " shifts");
  System.out.println("\n");
  return status;
}
```

}

3.4 C# Examples

This section includes source code for all of the Gurobi C# examples. The same source code can be found in the examples/c# directory of the Gurobi distribution.

callback cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP or a MIP from a file, sets a callback
  to monitor the optimization progress and to output some progress
   information to the screen and to a log file. If it is a MIP and 10%
  gap is reached, then it aborts. */
using System;
using Gurobi;
class callback_cs : GRBCallback
{
 private GRBVar[] vars;
 private double
                   lastnode;
 private double
                   lastiter;
 public callback_cs(GRBVar[] xvars)
  {
    vars = xvars;
    lastnode = lastiter = -1;
  }
  protected override void Callback()
    try {
      if (where == GRB.Callback.MESSAGE) {
        // Message callback
        string st = GetStringInfo(GRB.Callback.MSG_STRING);
        if (st != null) Console.Write(st);
      } else if (where == GRB.Callback.PRESOLVE) {
        // Presolve callback
        int cdels = GetIntInfo(GRB.Callback.PRE_COLDEL);
        int rdels = GetIntInfo(GRB.Callback.PRE_ROWDEL);
        Console.WriteLine(cdels+" columns and "+rdels+" rows are removed");
      } else if (where == GRB.Callback.SIMPLEX) {
        // Simplex callback
        double itcnt = GetDoubleInfo(GRB.Callback.SPX_ITRCNT);
        if (itcnt - lastiter >= 100) {
          lastiter = itcnt;
```

```
double obj = GetDoubleInfo(GRB.Callback.SPX_OBJVAL);
        double pinf = GetDoubleInfo(GRB.Callback.SPX_PRIMINF);
        double dinf = GetDoubleInfo(GRB.Callback.SPX_DUALINF);
        int ispert = GetIntInfo(GRB.Callback.SPX_ISPERT);
        char ch;
        if (ispert == 0)
                              ch = ', ';
        else if (ispert == 1) ch = 'S';
        else
                              ch = 'P';
        Console.WriteLine(itcnt+" "+ obj + ch + " "+pinf + " " + dinf);
      }
    } else if (where == GRB.Callback.MIP) {
      // General MIP callback
      double nodecnt = GetDoubleInfo(GRB.Callback.MIP_NODCNT);
      if (nodecnt - lastnode >= 100) {
        lastnode = nodecnt;
        double objbst = GetDoubleInfo(GRB.Callback.MIP_OBJBST);
        double objbnd = GetDoubleInfo(GRB.Callback.MIP_OBJBND);
        if (Math.Abs(objbst - objbnd) < 0.1 * (1.0 + Math.Abs(objbst)))</pre>
          Abort();
        int actnodes = (int) GetDoubleInfo(GRB.Callback.MIP_NODLFT);
        int itcnt = (int) GetDoubleInfo(GRB.Callback.MIP_ITRCNT);
        int solcnt = GetIntInfo(GRB.Callback.MIP_SOLCNT);
        int cutcnt = GetIntInfo(GRB.Callback.MIP_CUTCNT);
        Console.WriteLine(nodecnt + " " + actnodes + " " + itcnt + " "
          + objbst + " " + objbnd + " " + solcnt + " " + cutcnt);
    } else if (where == GRB.Callback.MIPSOL) {
      // MIP solution callback
      double obj
                     = GetDoubleInfo(GRB.Callback.MIPSOL_OBJ);
             nodecnt = (int) GetDoubleInfo(GRB.Callback.MIPSOL_NODCNT);
      double[] x = GetSolution(vars);
      Console.WriteLine("**** New solution at node " + nodecnt + ", obj "
                         + obj + ", x[0] = " + x[0] + "****");
   }
  } catch (GRBException e) {
    Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
   Console.WriteLine(e.StackTrace);
 }
}
static void Main(string[] args)
{
  if (args.Length < 1) {
   Console.Out.WriteLine("Usage: callback_cs filename");
   return;
```

```
}
   try {
     GRBEnv
                     = new GRBEnv();
                env
      GRBModel model = new GRBModel(env, args[0]);
     GRBVar[] vars
                     = model.GetVars();
     // Create a callback object and associate it with the model
     model.SetCallback(new callback_cs(vars));
     model.Optimize();
     double[] x
                      = model.Get(GRB.DoubleAttr.X, vars);
      string[] vnames = model.Get(GRB.StringAttr.VarName, vars);
     for (int j = 0; j < vars.Length; j++) {
        if (x[j] != 0.0) Console.WriteLine(vnames[j] + " " + x[j]);
      }
      // Dispose of model and env
     model.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
      Console.WriteLine(e.StackTrace);
   }
 }
}
```

```
dense cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                 x + y + x^2 + x*y + y^2 + y*z + z^2
     subject to x + 2y + 3z >= 4
                 x + y
                              >= 1
  The example illustrates the use of dense matrices to store A and Q
   (and dense vectors for the other relevant data). We don't recommend
  that you use dense matrices, but this example may be helpful if you
  already have your data in this format.
*/
using System;
using Gurobi;
class dense_cs {
 protected static bool
    dense_optimize(GRBEnv
                             env,
                   int
                             rows,
                   int
                             cols,
                   double[] c,
                                     // linear portion of objective function
                   double[,] Q,
                                    // quadratic portion of objective function
                   double[,] A,
                                    // constraint matrix
                            sense, // constraint senses
                   char[]
                   double[] rhs,
                                    // RHS vector
                   double[] lb,
                                    // variable lower bounds
                   double[] ub,
                                     // variable upper bounds
                   char[]
                             vtype, // variable types (continuous, binary, etc.)
                   double[] solution) {
    bool success = false;
    try {
     GRBModel model = new GRBModel(env);
      // Add variables to the model
     GRBVar[] vars = model.AddVars(lb, ub, null, vtype, null);
      model.Update();
     // Populate A matrix
```

```
for (int i = 0; i < rows; i++) {
    GRBLinExpr expr = new GRBLinExpr();
    for (int j = 0; j < cols; j++)
      if (A[i,j] != 0)
        expr.AddTerm(A[i,j], vars[j]); // Note: '+=' would be much slower
    model.AddConstr(expr, sense[i], rhs[i], "");
  }
  // Populate objective
  GRBQuadExpr obj = new GRBQuadExpr();
  if (Q != null) {
    for (int i = 0; i < cols; i++)
      for (int j = 0; j < cols; j++)
        if (Q[i,j] != 0)
          obj.AddTerm(Q[i,j], vars[i], vars[j]); // Note: '+=' would be much slower
    for (int j = 0; j < cols; j++)
      if (c[j] != 0)
        obj.AddTerm(c[j], vars[j]); // Note: '+=' would be much slower
    model.SetObjective(obj);
  }
  // Solve model
  model.Optimize();
  // Extract solution
  if (model.Get(GRB.IntAttr.Status) == GRB.Status.OPTIMAL) {
    success = true;
    for (int j = 0; j < cols; j++)
      solution[j] = vars[j].Get(GRB.DoubleAttr.X);
  }
  model.Dispose();
} catch (GRBException e) {
  Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
}
return success;
```

}

```
public static void Main(String[] args) {
    try {
      GRBEnv env = new GRBEnv();
      double[] c = new double[] {1, 1, 0};
      double[,] Q = new double[,] {{1, 1, 0}, {0, 1, 1}, {0, 0, 1}};
      double[,] A = new double[,] {{1, 2, 3}, {1, 1, 0}};
      char[] sense = new char[] {'>', '>'};
      double[] rhs = new double[] {4, 1};
      double[] lb = new double[] {0, 0, 0};
      bool success;
      double[] sol = new double[3];
      success = dense_optimize(env, 2, 3, c, Q, A, sense, rhs,
                               lb, null, null, sol);
      if (success) {
        Console.WriteLine("x: " + sol[0] + ", y: " + sol[1] + ", z: " + sol[2]);
      }
      // Dispose of environment
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
    }
 }
}
```

```
diet_cs.cs
```

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve the classic diet model, showing how to add constraints
  to an existing model. */
using System;
using Gurobi;
class diet_cs
 static void Main()
   try {
     // Nutrition guidelines, based on
     // USDA Dietary Guidelines for Americans, 2005
      // http://www.health.gov/DietaryGuidelines/dga2005/
      string[] Categories =
          new string[] { "calories", "protein", "fat", "sodium" };
      int nCategories = Categories.Length;
      double[] minNutrition = new double[] { 1800, 91, 0, 0 };
      double[] maxNutrition = new double[] { 2200, GRB.INFINITY, 65, 1779 };
      // Set of foods
      string[] Foods =
          new string[] { "hamburger", "chicken", "hot dog", "fries",
              "macaroni", "pizza", "salad", "milk", "ice cream" };
      int nFoods = Foods.Length;
      double[] cost =
          new double[] { 2.49, 2.89, 1.50, 1.89, 2.09, 1.99, 2.49, 0.89,
              1.59 };
      // Nutrition values for the foods
      double[,] nutritionValues = new double[,] {
          { 410, 24, 26, 730 },
                                  // hamburger
          { 420, 32, 10, 1190 }, // chicken
          { 560, 20, 32, 1800 }, // hot dog
          { 380, 4, 19, 270 },
                                  // fries
          { 320, 12, 10, 930 },
                                  // macaroni
          { 320, 15, 12, 820 },
                                  // pizza
          { 320, 31, 12, 1230 }, // salad
          { 100, 8, 2.5, 125 },
                                  // milk
          { 330, 8, 10, 180 }
                                  // ice cream
          };
```

```
// Model
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.Set(GRB.StringAttr.ModelName, "diet");
// Create decision variables for the nutrition information,
// which we limit via bounds
GRBVar[] nutrition = new GRBVar[nCategories];
for (int i = 0; i < nCategories; ++i) {</pre>
  nutrition[i] =
      model.AddVar(minNutrition[i], maxNutrition[i], 0, GRB.CONTINUOUS,
                   Categories[i]);
}
// Create decision variables for the foods to buy
GRBVar[] buy = new GRBVar[nFoods];
for (int j = 0; j < nFoods; ++j) {
  buy[j] =
      model.AddVar(0, GRB.INFINITY, cost[j], GRB.CONTINUOUS, Foods[j]);
}
// The objective is to minimize the costs
model.Set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.Update();
// Nutrition constraints
for (int i = 0; i < nCategories; ++i) {</pre>
  GRBLinExpr ntot = 0.0;
  for (int j = 0; j < nFoods; ++j)
    ntot.AddTerm(nutritionValues[j,i], buy[j]);
  model.AddConstr(ntot == nutrition[i], Categories[i]);
}
// Solve
model.Optimize();
PrintSolution(model, buy, nutrition);
Console.WriteLine("\nAdding constraint: at most 6 servings of dairy");
model.AddConstr(buy[7] + buy[8] <= 6.0, "limit_dairy");</pre>
// Solve
model.Optimize();
```

```
PrintSolution(model, buy, nutrition);
      // Dispose of model and env
      model.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " +
          e.Message);
   }
  }
 private static void PrintSolution(GRBModel model, GRBVar[] buy,
                                    GRBVar[] nutrition) {
    if (model.Get(GRB.IntAttr.Status) == GRB.Status.OPTIMAL) {
      Console.WriteLine("\nCost: " + model.Get(GRB.DoubleAttr.ObjVal));
      Console.WriteLine("\nBuy:");
      for (int j = 0; j < buy.Length; ++j) {
        if (buy[j].Get(GRB.DoubleAttr.X) > 0.0001) {
          Console.WriteLine(buy[j].Get(GRB.StringAttr.VarName) + " " +
              buy[j].Get(GRB.DoubleAttr.X));
        }
      }
      Console.WriteLine("\nNutrition:");
      for (int i = 0; i < nutrition.Length; ++i) {</pre>
        Console.WriteLine(nutrition[i].Get(GRB.StringAttr.VarName) + " " +
            nutrition[i].Get(GRB.DoubleAttr.X));
      }
    } else {
      Console.WriteLine("No solution");
   }
 }
}
```

facility cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Facility location: a company currently ships its product from 5 plants
  to 4 warehouses. It is considering closing some plants to reduce
  costs. What plant(s) should the company close, in order to minimize
  transportation and fixed costs?
  Based on an example from Frontline Systems:
  http://www.solver.com/disfacility.htm
  Used with permission.
using System;
using Gurobi;
class facility_cs
  static void Main()
   try {
      // Warehouse demand in thousands of units
      double[] Demand = new double[] { 15, 18, 14, 20 };
      // Plant capacity in thousands of units
      double[] Capacity = new double[] { 20, 22, 17, 19, 18 };
      // Fixed costs for each plant
      double[] FixedCosts =
          new double[] { 12000, 15000, 17000, 13000, 16000 };
      // Transportation costs per thousand units
      double[,] TransCosts =
          new double[,] { { 4000, 2000, 3000, 2500, 4500 },
              { 2500, 2600, 3400, 3000, 4000 },
              { 1200, 1800, 2600, 4100, 3000 },
              { 2200, 2600, 3100, 3700, 3200 } };
      // Number of plants and warehouses
      int nPlants = Capacity.Length;
      int nWarehouses = Demand.Length;
      // Model
     GRBEnv env = new GRBEnv();
```

```
GRBModel model = new GRBModel(env);
model.Set(GRB.StringAttr.ModelName, "facility");
// Plant open decision variables: open[p] == 1 if plant p is open.
GRBVar[] open = new GRBVar[nPlants];
for (int p = 0; p < nPlants; ++p) {
  open[p] = model.AddVar(0, 1, FixedCosts[p], GRB.BINARY, "Open" + p);
// Transportation decision variables: how much to transport from
// a plant p to a warehouse w
GRBVar[,] transport = new GRBVar[nWarehouses,nPlants];
for (int w = 0; w < nWarehouses; ++w) {</pre>
  for (int p = 0; p < nPlants; ++p) {
    transport[w,p] =
        model.AddVar(0, GRB.INFINITY, TransCosts[w,p], GRB.CONTINUOUS,
                     "Trans" + p + "." + w);
  }
}
// The objective is to minimize the total fixed and variable costs
model.Set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.Update();
// Production constraints
// Note that the right-hand limit sets the production to zero if
// the plant is closed
for (int p = 0; p < nPlants; ++p) {
  GRBLinExpr ptot = 0.0;
  for (int w = 0; w < nWarehouses; ++w)</pre>
    ptot.AddTerm(1.0, transport[w,p]);
  model.AddConstr(ptot <= Capacity[p] * open[p], "Capacity" + p);</pre>
}
// Demand constraints
for (int w = 0; w < nWarehouses; ++w) {
  GRBLinExpr dtot = 0.0;
  for (int p = 0; p < nPlants; ++p)
    dtot.AddTerm(1.0, transport[w,p]);
  model.AddConstr(dtot == Demand[w], "Demand" + w);
}
// Guess at the starting point: close the plant with the highest
```

```
// fixed costs; open all others
// First, open all plants
for (int p = 0; p < nPlants; ++p) {
  open[p].Set(GRB.DoubleAttr.Start, 1.0);
}
// Now close the plant with the highest fixed cost
Console.WriteLine("Initial guess:");
double maxFixed = -GRB.INFINITY;
for (int p = 0; p < nPlants; ++p) {
  if (FixedCosts[p] > maxFixed) {
    maxFixed = FixedCosts[p];
  }
}
for (int p = 0; p < nPlants; ++p) {
  if (FixedCosts[p] == maxFixed) {
    open[p].Set(GRB.DoubleAttr.Start, 0.0);
    Console.WriteLine("Closing plant " + p + "\n");
    break;
  }
}
// Use barrier to solve root relaxation
model.GetEnv().Set(GRB.IntParam.Method, GRB.METHOD_BARRIER);
// Solve
model.Optimize();
// Print solution
Console.WriteLine("\nTOTAL COSTS: " + model.Get(GRB.DoubleAttr.ObjVal));
Console.WriteLine("SOLUTION:");
for (int p = 0; p < nPlants; ++p) {</pre>
  if (open[p].Get(GRB.DoubleAttr.X) == 1.0) {
    Console.WriteLine("Plant " + p + " open:");
    for (int w = 0; w < nWarehouses; ++w) {
      if (transport[w,p].Get(GRB.DoubleAttr.X) > 0.0001) {
        Console.WriteLine(" Transport " +
            transport[w,p].Get(GRB.DoubleAttr.X) +
            " units to warehouse " + w);
      }
    }
  } else {
    Console.WriteLine("Plant " + p + " closed!");
  }
```

```
}

// Dispose of model and env
model.Dispose();
env.Dispose();

} catch (GRBException e) {
   Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
}
}
```

feasopt cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, adds artificial
  variables to each constraint, and then minimizes the sum of the
  artificial variables. A solution with objective zero corresponds
  to a feasible solution to the input model.
  We can also use FeasRelax feature to do it. In this example, we
  use minrelax=1, i.e. optimizing the returned model finds a solution
  that minimizes the original objective, but only from among those
  solutions that minimize the sum of the artificial variables. */
using Gurobi;
using System;
class feasopt_cs
  static void Main(string[] args)
    if (args.Length < 1) {
      Console.Out.WriteLine("Usage: feasopt_cs filename");
     return;
    }
    try {
      GRBEnv env = new GRBEnv();
     GRBModel feasmodel = new GRBModel(env, args[0]);
      // Create a copy to use FeasRelax feature later */
      GRBModel feasmodel1 = new GRBModel(feasmodel);
      // Clear objective
      feasmodel.SetObjective(new GRBLinExpr());
      // Add slack variables
      GRBConstr[] c = feasmodel.GetConstrs();
      for (int i = 0; i < c.Length; ++i) {
        char sense = c[i].Get(GRB.CharAttr.Sense);
        if (sense != '>') {
          GRBConstr[] constrs = new GRBConstr[] { c[i] };
          double[] coeffs = new double[] { -1 };
          feasmodel.AddVar(0.0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, constrs,
                           coeffs, "ArtN_" + c[i].Get(GRB.StringAttr.ConstrName));
        if (sense != '<') {
```

```
GRBConstr[] constrs = new GRBConstr[] { c[i] };
          double[] coeffs = new double[] { 1 };
          feasmodel.AddVar(0.0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, constrs,
                           coeffs, "ArtP_" +
                               c[i].Get(GRB.StringAttr.ConstrName));
        }
      }
      feasmodel.Update();
      // Optimize modified model
      feasmodel.Write("feasopt.lp");
      feasmodel.Optimize();
      // Use FeasRelax feature */
      feasmodel1.FeasRelax(GRB.FEASRELAX_LINEAR, true, false, true);
      feasmodel1.Write("feasopt1.lp");
      feasmodel1.Optimize();
      // Dispose of model and env
      feasmodel1.Dispose();
      feasmodel.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
    }
 }
}
```

fixanddive cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Implement a simple MIP heuristic. Relax the model,
   sort variables based on fractionality, and fix the 25% of
   the fractional variables that are closest to integer variables.
   Repeat until either the relaxation is integer feasible or
   linearly infeasible. */
using System;
using System.Collections.Generic;
using Gurobi;
class fixanddive_cs
 // Comparison class used to sort variable list based on relaxation
 // fractionality
  class FractionalCompare : IComparer<GRBVar>
   public int Compare(GRBVar v1, GRBVar v2)
      try {
        double sol1 = Math.Abs(v1.Get(GRB.DoubleAttr.X));
        double sol2 = Math.Abs(v2.Get(GRB.DoubleAttr.X));
        double frac1 = Math.Abs(sol1 - Math.Floor(sol1 + 0.5));
        double frac2 = Math.Abs(sol2 - Math.Floor(sol2 + 0.5));
        if (frac1 < frac2) {</pre>
          return -1;
        } else if (frac1 > frac2) {
          return 1;
        } else {
          return 0;
        }
      } catch (GRBException e) {
        Console.WriteLine("Error code: " + e.ErrorCode + ". " +
            e.Message);
      }
      return 0;
 }
  static void Main(string[] args)
    if (args.Length < 1) {</pre>
```

```
Console.Out.WriteLine("Usage: fixanddive_cs filename");
 return;
}
try {
  // Read model
 GRBEnv env = new GRBEnv();
 GRBModel model = new GRBModel(env, args[0]);
 // Collect integer variables and relax them
 List<GRBVar> intvars = new List<GRBVar>();
  foreach (GRBVar v in model.GetVars()) {
    if (v.Get(GRB.CharAttr.VType) != GRB.CONTINUOUS) {
      intvars.Add(v);
      v.Set(GRB.CharAttr.VType, GRB.CONTINUOUS);
    }
  }
 model.GetEnv().Set(GRB.IntParam.OutputFlag, 0);
 model.Optimize();
  // Perform multiple iterations. In each iteration, identify the first
  // quartile of integer variables that are closest to an integer value
  // in the relaxation, fix them to the nearest integer, and repeat.
 for (int iter = 0; iter < 1000; ++iter) {
    // create a list of fractional variables, sorted in order of
    // increasing distance from the relaxation solution to the nearest
    // integer value
    List<GRBVar> fractional = new List<GRBVar>();
    foreach (GRBVar v in intvars) {
      double sol = Math.Abs(v.Get(GRB.DoubleAttr.X));
      if (Math.Abs(sol - Math.Floor(sol + 0.5)) > 1e-5) {
        fractional.Add(v);
     }
    }
    Console.WriteLine("Iteration " + iter + ", obj " +
        model.Get(GRB.DoubleAttr.ObjVal) + ", fractional " +
        fractional.Count);
    if (fractional.Count == 0) {
      Console.WriteLine("Found feasible solution - objective " +
```

```
model.Get(GRB.DoubleAttr.ObjVal));
         break;
        }
        // Fix the first quartile to the nearest integer value
        fractional.Sort(new FractionalCompare());
        int nfix = Math.Max(fractional.Count / 4, 1);
        for (int i = 0; i < nfix; ++i) {
          GRBVar v = fractional[i];
          double fixval = Math.Floor(v.Get(GRB.DoubleAttr.X) + 0.5);
          v.Set(GRB.DoubleAttr.LB, fixval);
          v.Set(GRB.DoubleAttr.UB, fixval);
          Console.WriteLine(" Fix " + v.Get(GRB.StringAttr.VarName) +
              " to " + fixval + " ( rel " + v.Get(GRB.DoubleAttr.X) + " )");
        }
        model.Optimize();
        // Check optimization result
        if (model.Get(GRB.IntAttr.Status) != GRB.Status.OPTIMAL) {
          Console.WriteLine("Relaxation is infeasible");
          break;
        }
      }
      // Dispose of model and env
     model.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " +
          e.Message);
   }
}
```

```
lp cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
   If the model is infeasible or unbounded, the example turns off
  presolve and solves the model again. If the model is infeasible,
  the example computes an Irreducible Infeasible Subsystem (IIS),
  and writes it to a file. */
using System;
using Gurobi;
class lp_cs
  static void Main(string[] args)
    if (args.Length < 1) {
     Console.Out.WriteLine("Usage: lp_cs filename");
     return;
    }
    try {
      GRBEnv env = new GRBEnv();
      GRBModel model = new GRBModel(env, args[0]);
     model.Optimize();
      int optimstatus = model.Get(GRB.IntAttr.Status);
      if (optimstatus == GRB.Status.INF_OR_UNBD) {
        model.GetEnv().Set(GRB.IntParam.Presolve, 0);
        model.Optimize();
        optimstatus = model.Get(GRB.IntAttr.Status);
      }
      if (optimstatus == GRB.Status.OPTIMAL) {
        double objval = model.Get(GRB.DoubleAttr.ObjVal);
        Console.WriteLine("Optimal objective: " + objval);
      } else if (optimstatus == GRB.Status.INFEASIBLE) {
        Console.WriteLine("Model is infeasible");
        // compute and write out IIS
        model.ComputeIIS();
        model.Write("model.ilp");
```

Ipmethod _cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Solve a model with different values of the Method parameter;
   show which value gives the shortest solve time. */
using System;
using Gurobi;
class lpmethod_cs
 static void Main(string[] args)
    if (args.Length < 1) {
     Console.Out.WriteLine("Usage: lpmethod_cs filename");
     return;
    }
    try {
      // Read model
     GRBEnv env = new GRBEnv();
      GRBModel model = new GRBModel(env, args[0]);
      GRBEnv menv = model.GetEnv();
      // Solve the model with different values of Method
      int bestMethod = -1;
      double bestTime = menv.Get(GRB.DoubleParam.TimeLimit);
     for (int i = 0; i \le 2; ++i)
      {
        model.Reset();
        menv.Set(GRB.IntParam.Method, i);
        model.Optimize();
        if (model.Get(GRB.IntAttr.Status) == GRB.Status.OPTIMAL)
          bestTime = model.Get(GRB.DoubleAttr.Runtime);
          bestMethod = i;
          // Reduce the TimeLimit parameter to save time
          // with other methods
          menv.Set(GRB.DoubleParam.TimeLimit, bestTime);
      }
      // Report which method was fastest
      if (bestMethod == -1) {
        Console.WriteLine("Unable to solve this model");
```

Ipmod cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads an LP model from a file and solves it.
  If the model can be solved, then it finds the smallest positive variable,
  sets its upper bound to zero, and resolves the model two ways:
  first with an advanced start, then without an advanced start
   (i.e. 'from scratch'). */
using System;
using Gurobi;
class lpmod_cs
  static void Main(string[] args)
    if (args.Length < 1) {
     Console.Out.WriteLine("Usage: lpmod_cs filename");
     return;
    }
    try {
      // Read model and determine whether it is an LP
     GRBEnv env = new GRBEnv();
     GRBModel model = new GRBModel(env, args[0]);
      if (model.Get(GRB.IntAttr.IsMIP) != 0) {
        Console.WriteLine("The model is not a linear program");
        Environment.Exit(1);
      }
     model.Optimize();
      int status = model.Get(GRB.IntAttr.Status);
      if ((status == GRB.Status.INF_OR_UNBD) ||
          (status == GRB.Status.INFEASIBLE) ||
          (status == GRB.Status.UNBOUNDED)) {
        Console.WriteLine("The model cannot be solved because it is "
            + "infeasible or unbounded");
        Environment.Exit(1);
      }
      if (status != GRB.Status.OPTIMAL) {
        Console.WriteLine("Optimization was stopped with status " + status);
        Environment.Exit(0);
```

```
}
  // Find the smallest variable value
  double minVal = GRB.INFINITY;
  GRBVar minVar = null;
  foreach (GRBVar v in model.GetVars()) {
    double sol = v.Get(GRB.DoubleAttr.X);
    if ((sol > 0.0001) && (sol < minVal) &&
        (v.Get(GRB.DoubleAttr.LB) == 0.0)) {
     minVal = sol;
     minVar = v;
   }
  }
  Console.WriteLine("\n*** Setting " +
      minVar.Get(GRB.StringAttr.VarName) + " from " + minVal +
      " to zero ***\n");
 minVar.Set(GRB.DoubleAttr.UB, 0.0);
  // Solve from this starting point
 model.Optimize();
  // Save iteration & time info
  double warmCount = model.Get(GRB.DoubleAttr.IterCount);
  double warmTime = model.Get(GRB.DoubleAttr.Runtime);
  // Reset the model and resolve
  Console.WriteLine("\n*** Resetting and solving "
      + "without an advanced start ***\n");
 model.Reset();
 model.Optimize();
  double coldCount = model.Get(GRB.DoubleAttr.IterCount);
  double coldTime = model.Get(GRB.DoubleAttr.Runtime);
  Console.WriteLine("\n*** Warm start: " + warmCount + " iterations, " +
      warmTime + " seconds");
  Console.WriteLine("*** Cold start: " + coldCount + " iterations, " +
      coldTime + " seconds");
  // Dispose of model and env
  model.Dispose();
  env.Dispose();
} catch (GRBException e) {
```

```
mip1 cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple MIP model:
    maximize
                 x +
                      y + 2z
     subject to x + 2y + 3z \le 4
                 x + y
                               >= 1
    x, y, z binary
using System;
using Gurobi;
class mip1_cs
  static void Main()
   try {
     GRBEnv
                     = new GRBEnv("mip1.log");
                env
     GRBModel model = new GRBModel(env);
     // Create variables
     GRBVar x = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, "x");
      GRBVar y = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, "y");
     GRBVar z = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, "z");
     // Integrate new variables
     model.Update();
     // Set objective: maximize x + y + 2z
     model.SetObjective(x + y + 2 * z, GRB.MAXIMIZE);
     // Add constraint: x + 2 y + 3 z \le 4
     model.AddConstr(x + 2 * y + 3 * z \le 4.0, "c0");
      // Add constraint: x + y >= 1
     model.AddConstr(x + y >= 1.0, "c1");
     // Optimize model
```

```
model.Optimize();
      Console.WriteLine(x.Get(GRB.StringAttr.VarName)
                         + " " + x.Get(GRB.DoubleAttr.X));
      Console.WriteLine(y.Get(GRB.StringAttr.VarName)
                         + " " + y.Get(GRB.DoubleAttr.X));
      Console.WriteLine(z.Get(GRB.StringAttr.VarName)
                         + " " + z.Get(GRB.DoubleAttr.X));
      Console.WriteLine("Obj: " + model.Get(GRB.DoubleAttr.ObjVal));
      // Dispose of model and env
      model.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
    }
 }
}
```

```
mip2 cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a MIP model from a file, solves it and
  prints the objective values from all feasible solutions
  generated while solving the MIP. Then it creates the fixed
  model and solves that model. */
using System;
using Gurobi;
class mip2_cs
  static void Main(string[] args)
  {
    if (args.Length < 1) {
     Console.Out.WriteLine("Usage: mip2_cs filename");
      return;
    }
    try {
      GRBEnv
                      = new GRBEnv();
                env
     GRBModel model = new GRBModel(env, args[0]);
      if (model.Get(GRB.IntAttr.IsMIP) == 0) {
        Console.WriteLine("Model is not a MIP");
        return;
      }
     model.Optimize();
      int optimstatus = model.Get(GRB.IntAttr.Status);
      double objval = 0;
      if (optimstatus == GRB.Status.OPTIMAL) {
        objval = model.Get(GRB.DoubleAttr.ObjVal);
        Console.WriteLine("Optimal objective: " + objval);
      } else if (optimstatus == GRB.Status.INF_OR_UNBD) {
        Console.WriteLine("Model is infeasible or unbounded");
        return;
      } else if (optimstatus == GRB.Status.INFEASIBLE) {
        Console.WriteLine("Model is infeasible");
        return;
      } else if (optimstatus == GRB.Status.UNBOUNDED) {
        Console.WriteLine("Model is unbounded");
        return;
      } else {
```

```
Console.WriteLine("Optimization was stopped with status = "
                     + optimstatus);
  return;
}
/* Iterate over the solutions and compute the objectives */
GRBVar[] vars = model.GetVars();
model.GetEnv().Set(GRB.IntParam.OutputFlag, 0);
Console.WriteLine();
for (int k = 0; k < model.Get(GRB.IntAttr.SolCount); ++k) {</pre>
  model.GetEnv().Set(GRB.IntParam.SolutionNumber, k);
  double objn = 0.0;
  for (int j = 0; j < vars.Length; j++) {
    objn += vars[j].Get(GRB.DoubleAttr.Obj)
      * vars[j].Get(GRB.DoubleAttr.Xn);
  }
  Console.WriteLine("Solution " + k + " has objective: " + objn);
}
Console.WriteLine();
model.GetEnv().Set(GRB.IntParam.OutputFlag, 1);
/* Create a fixed model, turn off presolve and solve */
GRBModel fixedmodel = model.FixedModel();
fixedmodel.GetEnv().Set(GRB.IntParam.Presolve, 0);
fixedmodel.Optimize();
int foptimstatus = fixedmodel.Get(GRB.IntAttr.Status);
if (foptimstatus != GRB.Status.OPTIMAL) {
  Console.WriteLine("Error: fixed model isn't optimal");
  return;
}
double fobjval = fixedmodel.Get(GRB.DoubleAttr.ObjVal);
if (Math.Abs(fobjval - objval) > 1.0e-6 * (1.0 + Math.Abs(objval))) {
  Console.WriteLine("Error: objective values are different");
  return;
```

```
}
     GRBVar[] fvars = fixedmodel.GetVars();
     double[] x = fixedmodel.Get(GRB.DoubleAttr.X, fvars);
      string[] vnames = fixedmodel.Get(GRB.StringAttr.VarName, fvars);
     for (int j = 0; j < fvars.Length; j++) {
       if (x[j] != 0.0) Console.WriteLine(vnames[j] + " " + x[j]);
      }
     // Dispose of models and env
     fixedmodel.Dispose();
     model.Dispose();
      env.Dispose();
   } catch (GRBException e) {
     Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
   }
 }
}
```

params cs.cs /* Copyright 2013, Gurobi Optimization, Inc. */ /* Use parameters that are associated with a model. A MIP is solved for 5 seconds with different sets of parameters. The one with the smallest MIP gap is selected, and the optimization is resumed until the optimal solution is found. */ using System; using Gurobi; class params_cs // Simple function to determine the MIP gap private static double Gap(GRBModel model) { if ((model.Get(GRB.IntAttr.SolCount) == 0) || (Math.Abs(model.Get(GRB.DoubleAttr.ObjVal)) < 1e-6)) {</pre> return GRB. INFINITY; } return Math.Abs(model.Get(GRB.DoubleAttr.ObjBound) model.Get(GRB.DoubleAttr.ObjVal)) / Math.Abs(model.Get(GRB.DoubleAttr.ObjVal)); } static void Main(string[] args) if (args.Length < 1) { Console.Out.WriteLine("Usage: params_cs filename"); return; } try { // Read model and verify that it is a MIP GRBEnv env = new GRBEnv(); GRBModel basemodel = new GRBModel(env, args[0]); if (basemodel.Get(GRB.IntAttr.IsMIP) == 0) { Console.WriteLine("The model is not an integer program"); Environment.Exit(1); } // Set a 5 second time limit

basemodel.GetEnv().Set(GRB.DoubleParam.TimeLimit, 5);

```
// Now solve the model with different values of MIPFocus
      double bestGap = GRB.INFINITY;
      GRBModel bestModel = null;
      for (int i = 0; i \le 3; ++i) {
        GRBModel m = new GRBModel(basemodel);
        m.GetEnv().Set(GRB.IntParam.MIPFocus, i);
        m.Optimize();
        if (bestModel == null || bestGap > Gap(m)) {
          bestModel = m;
          bestGap = Gap(bestModel);
        }
      }
      // Finally, reset the time limit and continue to solve the
      // best model to optimality
      bestModel.GetEnv().Set(GRB.DoubleParam.TimeLimit, GRB.INFINITY);
      bestModel.Optimize();
      Console.WriteLine("Solved with MIPFocus: " +
          bestModel.GetEnv().Get(GRB.IntParam.MIPFocus));
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " +
          e.Message);
    }
  }
}
```

```
qcp cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QCP model:
     maximize
     subject to x + y + z = 1
                 x^2 + y^2 \le z^2 (second-order cone)
                 x^2 \le yz
                                 (rotated second-order cone)
*/
using System;
using Gurobi;
class qcp_cs
  static void Main()
   try {
     GRBEnv
                env = new GRBEnv("qcp.log");
     GRBModel model = new GRBModel(env);
     // Create variables
     GRBVar x = model.AddVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "x");
     GRBVar y = model.AddVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "y");
     GRBVar z = model.AddVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "z");
     // Integrate new variables
     model.Update();
      // Set objective
     GRBLinExpr obj = x;
     model.SetObjective(obj, GRB.MAXIMIZE);
      // Add linear constraint: x + y + z = 1
     model.AddConstr(x + y + z == 1.0, "c0");
      // Add second-order cone: x^2 + y^2 \le z^2
     model.AddQConstr(x*x + y*y <= z*z, "qc0");</pre>
```

```
// Add rotated cone: x^2 <= yz
      model.AddQConstr(x*x <= y*z, "qc1");</pre>
      // Optimize model
      model.Optimize();
      Console.WriteLine(x.Get(GRB.StringAttr.VarName)
                         + " " + x.Get(GRB.DoubleAttr.X));
      Console.WriteLine(y.Get(GRB.StringAttr.VarName)
                         + " " + y.Get(GRB.DoubleAttr.X));
      Console.WriteLine(z.Get(GRB.StringAttr.VarName)
                         + " " + z.Get(GRB.DoubleAttr.X));
      Console.WriteLine("Obj: " + model.Get(GRB.DoubleAttr.ObjVal) + " " +
                        obj.Value);
      // Dispose of model and env
      model.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
    }
 }
}
```

```
qp cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example formulates and solves the following simple QP model:
                 x^2 + x*y + y^2 + y*z + z^2 + z
    subject to x + 2y + 3z >= 4
                 x + y
                               >= 1
  It solves it once as a continuous model, and once as an integer model.
*/
using System;
using Gurobi;
class qp_cs
  static void Main()
  {
   try {
     GRBEnv
                      = new GRBEnv("qp.log");
                env
     GRBModel model = new GRBModel(env);
      // Create variables
     GRBVar x = model.AddVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "x");
     GRBVar y = model.AddVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "y");
     GRBVar z = model.AddVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "z");
     // Integrate new variables
     model.Update();
      // Set objective
     GRBQuadExpr obj = x*x + x*y + y*y + y*z + z*z + 2*x;
     model.SetObjective(obj);
     // Add constraint: x + 2 y + 3 z >= 4
     model.AddConstr(x + 2 * y + 3 * z >= 4.0, "c0");
      // Add constraint: x + y >= 1
     model.AddConstr(x + y >= 1.0, "c1");
```

```
// Optimize model
 model.Optimize();
  Console.WriteLine(x.Get(GRB.StringAttr.VarName)
                     + " " + x.Get(GRB.DoubleAttr.X));
  Console.WriteLine(y.Get(GRB.StringAttr.VarName)
                     + " " + y.Get(GRB.DoubleAttr.X));
  Console.WriteLine(z.Get(GRB.StringAttr.VarName)
                     + " " + z.Get(GRB.DoubleAttr.X));
  Console.WriteLine("Obj: " + model.Get(GRB.DoubleAttr.ObjVal) + " " +
                    obj.Value);
  // Change variable types to integer
 x.Set(GRB.CharAttr.VType, GRB.INTEGER);
  y.Set(GRB.CharAttr.VType, GRB.INTEGER);
 z.Set(GRB.CharAttr.VType, GRB.INTEGER);
 // Optimize model
 model.Optimize();
  Console.WriteLine(x.Get(GRB.StringAttr.VarName)
                     + " " + x.Get(GRB.DoubleAttr.X));
  Console.WriteLine(y.Get(GRB.StringAttr.VarName)
                     + " " + y.Get(GRB.DoubleAttr.X));
  Console.WriteLine(z.Get(GRB.StringAttr.VarName)
                     + " " + z.Get(GRB.DoubleAttr.X));
  Console.WriteLine("Obj: " + model.Get(GRB.DoubleAttr.ObjVal) + " " +
                    obj. Value);
  // Dispose of model and env
 model.Dispose();
  env.Dispose();
} catch (GRBException e) {
  Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
```

} }

sensitivity cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Simple MIP sensitivity analysis example.
  For each integer variable, fix it to its lower and upper bound
  and check the impact on the objective. */
using System;
using Gurobi;
class sensitivity_cs
  static void Main(string[] args)
    if (args.Length < 1) {
     Console.Out.WriteLine("Usage: sensitivity_cs filename");
     return;
    }
    try {
      // Read model
     GRBEnv env = new GRBEnv();
     GRBModel a = new GRBModel(env, args[0]);
      a.Optimize();
      a.GetEnv().Set(GRB.IntParam.OutputFlag, 0);
      // Extract variables from model
      GRBVar[] avars = a.GetVars();
     for (int i = 0; i < avars.Length; ++i) {
        GRBVar v = avars[i];
        if (v.Get(GRB.CharAttr.VType) == GRB.BINARY) {
          // Create clone and fix variable
          GRBModel b = new GRBModel(a);
          GRBVar bv = b.GetVars()[i];
          if (v.Get(GRB.DoubleAttr.X) - v.Get(GRB.DoubleAttr.LB) < 0.5) {
            bv.Set(GRB.DoubleAttr.LB, bv.Get(GRB.DoubleAttr.UB));
            bv.Set(GRB.DoubleAttr.UB, bv.Get(GRB.DoubleAttr.LB));
          }
          b.Optimize();
          if (b.Get(GRB.IntAttr.Status) == GRB.Status.OPTIMAL) {
```

```
double objchg =
                b.Get(GRB.DoubleAttr.ObjVal) - a.Get(GRB.DoubleAttr.ObjVal);
            if (objchg < 0) {
              objchg = 0;
            Console.WriteLine("Objective sensitivity for variable " +
                v.Get(GRB.StringAttr.VarName) + " is " + objchg);
          } else {
            Console.WriteLine("Objective sensitivity for variable " +
                v.Get(GRB.StringAttr.VarName) + " is infinite");
          }
          // Dispose of model
          b.Dispose();
        }
      }
      // Dispose of model and env
      a.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " +
          e.Message);
    }
 }
}
```

```
SOS CS.CS
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example creates a very simple Special Ordered Set (SOS) model.
   The model consists of 3 continuous variables, no linear constraints,
   and a pair of SOS constraints of type 1. */
using System;
using Gurobi;
class sos_cs
 static void Main()
   try {
      GRBEnv env = new GRBEnv();
      GRBModel model = new GRBModel(env);
      // Create variables
      double[] ub
                     = \{1, 1, 2\};
      double[] obj = \{-2, -1, -1\};
      string[] names = {"x0", "x1", "x2"};
      GRBVar[] x = model.AddVars(null, ub, obj, null, names);
      // Integrate new variables
      model.Update();
      // Add first SOS1: x0=0 or x1=0
      GRBVar[] sosv1 = \{x[0], x[1]\};
      double[] soswt1 = {1, 2};
      model.AddSOS(sosv1, soswt1, GRB.SOS_TYPE1);
      // Add second SOS1: x0=0 or x2=0
      GRBVar[] sosv2 = \{x[0], x[2]\};
      double[] soswt2 = {1, 2};
      model.AddSOS(sosv2, soswt2, GRB.SOS_TYPE1);
```

```
sudoku cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
  Sudoku example.
 The Sudoku board is a 9x9 grid, which is further divided into a 3x3 grid
  of 3x3 grids. Each cell in the grid must take a value from 0 to 9.
 No two grid cells in the same row, column, or 3x3 subgrid may take the
  same value.
  In the MIP formulation, binary variables x[i,j,v] indicate whether
  cell <i,j> takes value 'v'. The constraints are as follows:
    1. Each cell must take exactly one value (sum_v x[i,j,v] = 1)
    2. Each value is used exactly once per row (sum_i x[i,j,v] = 1)
    3. Each value is used exactly once per column (sum_j x[i,j,v] = 1)
    4. Each value is used exactly once per 3x3 subgrid (sum_grid x[i,j,v] = 1)
 Input datasets for this example can be found in examples/data/sudoku*.
using System;
using System. IO;
using Gurobi;
class sudoku_cs
 static void Main(string[] args)
    int n = 9;
    int s = 3;
    if (args.Length < 1) {
     Console.Out.WriteLine("Usage: sudoku_cs filename");
     return;
    }
    try {
     GRBEnv env = new GRBEnv();
     GRBModel model = new GRBModel(env);
     // Create 3-D array of model variables
     GRBVar[,,] vars = new GRBVar[n,n,n];
```

```
for (int i = 0; i < n; i++) {
  for (int j = 0; j < n; j++) {
    for (int v = 0; v < n; v++) {
      string st = "G_" + i.ToString() + "_" + j.ToString()
                       + "_" + v.ToString();
      vars[i,j,v] = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, st);
   }
  }
}
// Integrate variables into model
model.Update();
// Add constraints
GRBLinExpr expr;
// Each cell must take one value
for (int i = 0; i < n; i++) {
  for (int j = 0; j < n; j++) {
    expr = 0.0;
    for (int v = 0; v < n; v++)
      expr.AddTerm(1.0, vars[i,j,v]);
    string st = "V_" + i.ToString() + "_" + j.ToString();
    model.AddConstr(expr == 1.0, st);
  }
}
// Each value appears once per row
for (int i = 0; i < n; i++) {
  for (int v = 0; v < n; v++) {
    expr = 0.0;
    for (int j = 0; j < n; j++)
      expr.AddTerm(1.0, vars[i,j,v]);
    string st = "R_" + i.ToString() + "_" + v.ToString();
   model.AddConstr(expr == 1.0, st);
  }
}
// Each value appears once per column
for (int j = 0; j < n; j++) {
```

```
for (int v = 0; v < n; v++) {
    expr = 0.0;
    for (int i = 0; i < n; i++)
      expr.AddTerm(1.0, vars[i,j,v]);
    string st = "C_" + j.ToString() + "_" + v.ToString();
    model.AddConstr(expr == 1.0, st);
  }
}
// Each value appears once per sub-grid
for (int v = 0; v < n; v++) {
  for (int i0 = 0; i0 < s; i0++) {
    for (int j0 = 0; j0 < s; j0++) {
      expr = 0.0;
      for (int i1 = 0; i1 < s; i1++) {
        for (int j1 = 0; j1 < s; j1++) {
          expr.AddTerm(1.0, vars[i0*s+i1,j0*s+j1,v]);
        }
      }
      string st = "Sub_" + v.ToString() + "_" + i0.ToString()
                         + "_" + j0.ToString();
      model.AddConstr(expr == 1.0, st);
   }
  }
}
// Update model
model.Update();
// Fix variables associated with pre-specified cells
StreamReader sr = File.OpenText(args[0]);
for (int i = 0; i < n; i++) {
  string input = sr.ReadLine();
  for (int j = 0; j < n; j++) {
    int val = (int) input[j] - 48 - 1; // 0-based
    if (val >= 0)
      vars[i,j,val].Set(GRB.DoubleAttr.LB, 1.0);
  }
}
```

```
// Optimize model
      model.Optimize();
      // Write model to file
      model.Write("sudoku.lp");
      double[,,] x = model.Get(GRB.DoubleAttr.X, vars);
      Console.WriteLine();
      for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
          for (int v = 0; v < n; v++) {
            if (x[i,j,v] > 0.5) {
              Console.Write(v+1);
            }
          }
        }
        Console.WriteLine();
      }
      // Dispose of model and env
      model.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
    }
 }
}
```

tsp cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
// Solve a traveling salesman problem on a randomly generated set of
// points using lazy constraints.
                                    The base MIP model only includes
// 'degree-2' constraints, requiring each node to have exactly
// two incident edges. Solutions to this model may contain subtours -
// tours that don't visit every node. The lazy constraint callback
// adds new constraints to cut them off.
using System;
using Gurobi;
class tsp_cs : GRBCallback {
  private GRBVar[,] vars;
 public tsp_cs(GRBVar[,] xvars) {
    vars = xvars;
  // Subtour elimination callback. Whenever a feasible solution is found,
  // find the smallest subtour, and add a subtour elimination
 // constraint if the tour doesn't visit every node.
 protected override void Callback() {
   try {
      if (where == GRB.Callback.MIPSOL) {
        // Found an integer feasible solution - does it visit every node?
        int n = vars.GetLength(0);
        int[] tour = findsubtour(GetSolution(vars));
        if (tour.Length < n) {</pre>
          // Add subtour elimination constraint
          GRBLinExpr expr = 0;
          for (int i = 0; i < tour.Length; i++)</pre>
            for (int j = i+1; j < tour.Length; j++)</pre>
              expr.AddTerm(1.0, vars[tour[i], tour[j]]);
          AddLazy(expr <= tour.Length-1);</pre>
        }
      }
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
      Console.WriteLine(e.StackTrace);
    }
```

```
}
// Given an integer-feasible solution 'sol', return the smallest
// sub-tour (as a list of node indices).
protected static int[] findsubtour(double[,] sol)
  int n = sol.GetLength(0);
  bool[] seen = new bool[n];
  int[] tour = new int[n];
  int bestind, bestlen;
  int i, node, len, start;
  for (i = 0; i < n; i++)
    seen[i] = false;
  start = 0;
  bestlen = n+1;
  bestind = -1;
  node = 0;
  while (start < n) {
    for (node = 0; node < n; node++)</pre>
      if (!seen[node])
        break;
    if (node == n)
      break;
    for (len = 0; len < n; len++) \{
      tour[start+len] = node;
      seen[node] = true;
      for (i = 0; i < n; i++) {
        if (sol[node, i] > 0.5 && !seen[i]) {
          node = i;
          break;
        }
      }
      if (i == n) {
        len++;
        if (len < bestlen) {
          bestlen = len;
          bestind = start;
        }
        start += len;
        break;
      }
    }
```

```
}
  for (i = 0; i < bestlen; i++)
    tour[i] = tour[bestind+i];
  System.Array.Resize(ref tour, bestlen);
  return tour;
// Euclidean distance between points 'i' and 'j'
protected static double distance(double[] x,
                                 double[] y,
                                 int
                                          i,
                                 int
                                          j) {
  double dx = x[i]-x[j];
  double dy = y[i]-y[j];
  return Math.Sqrt(dx*dx+dy*dy);
}
public static void Main(String[] args) {
  if (args.Length < 1) {
    Console.WriteLine("Usage: tsp_cs nnodes");
    return;
  }
  int n = Convert.ToInt32(args[0]);
  try {
    GRBEnv
                 = new GRBEnv();
             env
    GRBModel model = new GRBModel(env);
    // Must set LazyConstraints parameter when using lazy constraints
    model.GetEnv().Set(GRB.IntParam.LazyConstraints, 1);
    double[] x = new double[n];
    double[] y = new double[n];
    Random r = new Random();
    for (int i = 0; i < n; i++) {
      x[i] = r.NextDouble();
      y[i] = r.NextDouble();
```

```
// Create variables
GRBVar[,] vars = new GRBVar[n, n];
for (int i = 0; i < n; i++) {
  for (int j = 0; j \le i; j++) {
    vars[i, j] = model.AddVar(0.0, 1.0, distance(x, y, i, j),
                              GRB.BINARY, "x"+i+"_"+j);
   vars[j, i] = vars[i, j];
  }
}
// Integrate variables
model.Update();
// Degree-2 constraints
for (int i = 0; i < n; i++) {
  GRBLinExpr expr = 0;
  for (int j = 0; j < n; j++)
    expr.AddTerm(1.0, vars[i, j]);
  model.AddConstr(expr == 2.0, "deg2_"+i);
}
// Forbid edge from node back to itself
for (int i = 0; i < n; i++)
  vars[i, i].Set(GRB.DoubleAttr.UB, 0.0);
model.SetCallback(new tsp_cs(vars));
model.Optimize();
if (model.Get(GRB.IntAttr.SolCount) > 0) {
  int[] tour = findsubtour(model.Get(GRB.DoubleAttr.X, vars));
  Console.Write("Tour: ");
  for (int i = 0; i < tour.Length; i++)</pre>
    Console.Write(tour[i] + " ");
  Console.WriteLine();
}
// Dispose of model and environment
model.Dispose();
```

```
env.Dispose();

} catch (GRBException e) {
   Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
   Console.WriteLine(e.StackTrace);
   }
}
```

```
tune cs.cs
/* Copyright 2013, Gurobi Optimization, Inc. */
/* This example reads a model from a file and tunes it.
  It then writes the best parameter settings to a file
  and solves the model using these parameters. */
using System;
using Gurobi;
class tune_cs
  static void Main(string[] args)
    if (args.Length < 1) {
     Console.Out.WriteLine("Usage: tune_cs filename");
     return;
    }
   try {
      GRBEnv env = new GRBEnv();
      // Read model from file
     GRBModel model = new GRBModel(env, args[0]);
     // Set the TuneResults parameter to 1
     model.GetEnv().Set(GRB.IntParam.TuneResults, 1);
      // Tune the model
     model.Tune();
     // Get the number of tuning results
      int resultcount = model.Get(GRB.IntAttr.TuneResultCount);
      if (resultcount > 0) {
        // Load the tuned parameters into the model's environment
        model.GetTuneResult(0);
        // Write the tuned parameters to a file
        model.Write("tune.prm");
        // Solve the model using the tuned parameters
        model.Optimize();
      }
```

```
// Dispose of model and environment
model.Dispose();
env.Dispose();

} catch (GRBException e) {
   Console.WriteLine("Error code: " + e.ErrorCode + ". " + e.Message);
}
}
```

workforce1 cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, use IIS to find a set of
  conflicting constraints. Note that there may be additional conflicts
  besides what is reported via IIS. */
using System;
using Gurobi;
class workforce1_cs
 static void Main()
   try {
     // Sample data
     // Sets of days and workers
     string[] Shifts =
         new string[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
             "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
             "Sun14" };
      string[] Workers =
         new string[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
      int nShifts = Shifts.Length;
      int nWorkers = Workers.Length;
     // Number of workers required for each shift
     double[] shiftRequirements =
         new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
      // Amount each worker is paid to work one shift
     double[] pay = new double[] { 10, 12, 10, 8, 8, 9, 11 };
     // Worker availability: 0 if the worker is unavailable for a shift
     double[,] availability =
         new double[,] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
             \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\},\
             { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
             { 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1 },
             { 1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1 },
             { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
```

```
// Model
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.Set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
GRBVar[,] x = new GRBVar[nWorkers,nShifts];
for (int w = 0; w < nWorkers; ++w) {</pre>
  for (int s = 0; s < nShifts; ++s) {
    x[w,s] =
        model.AddVar(0, availability[w,s], pay[w], GRB.CONTINUOUS,
                     Workers[w] + "." + Shifts[s]);
  }
}
// The objective is to minimize the total pay costs
model.Set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.Update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (int s = 0; s < nShifts; ++s) {
  GRBLinExpr lhs = 0.0;
  for (int w = 0; w < nWorkers; ++w)</pre>
    lhs.AddTerm(1.0, x[w, s]);
  model.AddConstr(lhs == shiftRequirements[s], Shifts[s]);
}
// Optimize
model.Optimize();
int status = model.Get(GRB.IntAttr.Status);
if (status == GRB.Status.UNBOUNDED) {
  Console.WriteLine("The model cannot be solved "
      + "because it is unbounded");
  return;
}
if (status == GRB.Status.OPTIMAL) {
  Console.WriteLine("The optimal objective is " +
      model.Get(GRB.DoubleAttr.ObjVal));
  return;
```

```
}
      if ((status != GRB.Status.INF_OR_UNBD) &&
          (status != GRB.Status.INFEASIBLE)) {
        Console.WriteLine("Optimization was stopped with status " + status);
        return;
      }
      // Do IIS
      Console.WriteLine("The model is infeasible; computing IIS");
      model.ComputeIIS();
      Console.WriteLine("\nThe following constraint(s) "
          + "cannot be satisfied:");
      foreach (GRBConstr c in model.GetConstrs()) {
        if (c.Get(GRB.IntAttr.IISConstr) == 1) {
          Console.WriteLine(c.Get(GRB.StringAttr.ConstrName));
        }
      }
      // Dispose of model and env
      model.Dispose();
      env.Dispose();
    } catch (GRBException e) {
      Console.WriteLine("Error code: " + e.ErrorCode + ". " +
          e.Message);
    }
 }
}
```

```
workforce2_cs.cs
```

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, use IIS iteratively to
  find all conflicting constraints. */
using System;
using System.Collections.Generic;
using Gurobi;
class workforce2_cs
 static void Main()
   try {
     // Sample data
     // Sets of days and workers
     string[] Shifts =
         new string[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
             "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
             "Sun14" };
      string[] Workers =
         new string[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
      int nShifts = Shifts.Length;
      int nWorkers = Workers.Length;
     // Number of workers required for each shift
     double[] shiftRequirements =
         new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
      // Amount each worker is paid to work one shift
      double[] pay = new double[] { 10, 12, 10, 8, 8, 9, 11 };
     // Worker availability: 0 if the worker is unavailable for a shift
     double[,] availability =
         new double[,] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
             \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\},\
             { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, },
             { 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1 },
             { 1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1 },
             { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
```

```
// Model
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.Set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
GRBVar[,] x = new GRBVar[nWorkers,nShifts];
for (int w = 0; w < nWorkers; ++w) {</pre>
  for (int s = 0; s < nShifts; ++s) {
    x[w,s] =
        model.AddVar(0, availability[w,s], pay[w], GRB.CONTINUOUS,
                     Workers[w] + "." + Shifts[s]);
  }
}
// The objective is to minimize the total pay costs
model.Set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.Update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
for (int s = 0; s < nShifts; ++s) {
  GRBLinExpr lhs = 0.0;
  for (int w = 0; w < nWorkers; ++w)</pre>
    lhs.AddTerm(1.0, x[w, s]);
  model.AddConstr(lhs == shiftRequirements[s], Shifts[s]);
}
// Optimize
model.Optimize();
int status = model.Get(GRB.IntAttr.Status);
if (status == GRB.Status.UNBOUNDED) {
  Console.WriteLine("The model cannot be solved "
      + "because it is unbounded");
  return;
}
if (status == GRB.Status.OPTIMAL) {
  Console.WriteLine("The optimal objective is " +
      model.Get(GRB.DoubleAttr.ObjVal));
  return;
```

```
}
if ((status != GRB.Status.INF_OR_UNBD) &&
    (status != GRB.Status.INFEASIBLE)) {
  Console.WriteLine("Optimization was stopped with status " + status);
  return;
}
// Do IIS
Console.WriteLine("The model is infeasible; computing IIS");
LinkedList<string> removed = new LinkedList<string>();
// Loop until we reduce to a model that can be solved
while (true) {
  model.ComputeIIS();
  Console.WriteLine("\nThe following constraint cannot be satisfied:");
  foreach (GRBConstr c in model.GetConstrs()) {
    if (c.Get(GRB.IntAttr.IISConstr) == 1) {
      Console.WriteLine(c.Get(GRB.StringAttr.ConstrName));
      // Remove a single constraint from the model
      removed.AddFirst(c.Get(GRB.StringAttr.ConstrName));
      model.Remove(c);
      break;
    }
  }
  Console.WriteLine();
  model.Optimize();
  status = model.Get(GRB.IntAttr.Status);
  if (status == GRB.Status.UNBOUNDED) {
    Console.WriteLine("The model cannot be solved "
        + "because it is unbounded");
    return;
  }
  if (status == GRB.Status.OPTIMAL) {
    break;
  if ((status != GRB.Status.INF_OR_UNBD) &&
      (status != GRB.Status.INFEASIBLE)) {
    Console.WriteLine("Optimization was stopped with status " +
        status);
    return;
}
```

workforce3_cs.cs

```
/* Copyright 2013, Gurobi Optimization, Inc. */
/* Assign workers to shifts; each worker may or may not be available on a
  particular day. If the problem cannot be solved, add slack variables
  to determine which constraints cannot be satisfied, and how much
  they need to be relaxed. */
using System;
using System.Collections.Generic;
using Gurobi;
class workforce3_cs
 static void Main()
   try {
     // Sample data
      // Sets of days and workers
     string[] Shifts =
         new string[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6",
             "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13",
             "Sun14" };
      string[] Workers =
         new string[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" };
      int nShifts = Shifts.Length;
      int nWorkers = Workers.Length;
     // Number of workers required for each shift
     double[] shiftRequirements =
         new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 };
      // Amount each worker is paid to work one shift
     double[] pay = new double[] { 10, 12, 10, 8, 8, 9, 11 };
      // Worker availability: 0 if the worker is unavailable for a shift
     double[,] availability =
         new double[,] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },
             \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\},\
             { 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, },
             { 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1 },
             { 1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1 },
```

```
{ 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };
// Model
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.Set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. Since an assignment model always produces integer
// solutions, we use continuous variables and solve as an LP.
GRBVar[,] x = new GRBVar[nWorkers,nShifts];
for (int w = 0; w < nWorkers; ++w) {
  for (int s = 0; s < nShifts; ++s) {
    x[w,s] =
        model.AddVar(0, availability[w,s], pay[w], GRB.CONTINUOUS,
                     Workers[w] + "." + Shifts[s]);
  }
// The objective is to minimize the total pay costs
model.Set(GRB.IntAttr.ModelSense, 1);
// Update model to integrate new variables
model.Update();
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s
LinkedList<GRBConstr> reqCts = new LinkedList<GRBConstr>();
for (int s = 0; s < nShifts; ++s) {
  GRBLinExpr lhs = 0.0;
  for (int w = 0; w < nWorkers; ++w)</pre>
    lhs.AddTerm(1.0, x[w,s]);
  GRBConstr newCt =
      model.AddConstr(lhs == shiftRequirements[s], Shifts[s]);
  reqCts.AddFirst(newCt);
}
// Optimize
model.Optimize();
int status = model.Get(GRB.IntAttr.Status);
if (status == GRB.Status.UNBOUNDED) {
  Console.WriteLine("The model cannot be solved "
      + "because it is unbounded");
  return;
}
```

```
if (status == GRB.Status.OPTIMAL) {
  Console.WriteLine("The optimal objective is " +
      model.Get(GRB.DoubleAttr.ObjVal));
  return;
}
if ((status != GRB.Status.INF_OR_UNBD) &&
    (status != GRB.Status.INFEASIBLE)) {
  Console.WriteLine("Optimization was stopped with status " + status);
  return;
}
// Add slack variables to make the model feasible
Console.WriteLine("The model is infeasible; adding slack variables");
// Set original objective coefficients to zero
model.SetObjective(new GRBLinExpr());
// Add a new slack variable to each shift constraint so that the shifts
// can be satisfied
LinkedList<GRBVar> slacks = new LinkedList<GRBVar>();
foreach (GRBConstr c in reqCts) {
  GRBColumn col = new GRBColumn();
  col.AddTerm(1.0, c);
  GRBVar newvar =
      model.AddVar(0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, col,
                   c.Get(GRB.StringAttr.ConstrName) + "Slack");
  slacks.AddFirst(newvar);
}
// Solve the model with slacks
model.Optimize();
status = model.Get(GRB.IntAttr.Status);
if ((status == GRB.Status.INF_OR_UNBD) ||
    (status == GRB.Status.INFEASIBLE) ||
    (status == GRB.Status.UNBOUNDED)) {
  Console.WriteLine("The model with slacks cannot be solved "
      + "because it is infeasible or unbounded");
  return;
}
if (status != GRB.Status.OPTIMAL) {
  Console.WriteLine("Optimization was stopped with status " + status);
  return;
}
Console.WriteLine("\nSlack values:");
```

```
foreach (GRBVar sv in slacks) {
    if (sv.Get(GRB.DoubleAttr.X) > 1e-6) {
        Console.WriteLine(sv.Get(GRB.StringAttr.VarName) + " = " +
            sv.Get(GRB.DoubleAttr.X));
    }
}

// Dispose of model and env
model.Dispose();
env.Dispose();

catch (GRBException e) {
    Console.WriteLine("Error code: " + e.ErrorCode + ". " +
            e.Message);
}
}
```

workforce4 cs.cs /* Copyright 2013, Gurobi Optimization, Inc. */ /* Assign workers to shifts; each worker may or may not be available on a particular day. We use Pareto optimization to solve the model: first, we minimize the linear sum of the slacks. Then, we constrain the sum of the slacks, and we minimize a quadratic objective that tries to balance the workload among the workers. */ using System; using Gurobi; class workforce4_cs static void Main() try { // Sample data // Sets of days and workers string[] Shifts = new string[] { "Mon1", "Tue2", "Wed3", "Thu4", "Fri5", "Sat6", "Sun7", "Mon8", "Tue9", "Wed10", "Thu11", "Fri12", "Sat13", "Sun14" }; string[] Workers = new string[] { "Amy", "Bob", "Cathy", "Dan", "Ed", "Fred", "Gu" }; int nShifts = Shifts.Length; int nWorkers = Workers.Length; // Number of workers required for each shift double[] shiftRequirements = new double[] { 3, 2, 4, 4, 5, 6, 5, 2, 2, 3, 4, 6, 7, 5 }; // Worker availability: 0 if the worker is unavailable for a shift

new double[,] { { 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1 },

{ 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0 }, { 0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1 }, { 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1 }, { 1, 1, 1, 1, 0, 0, 1, 1, 1, 0, 1, 0, 1, 1 }, { 1, 1, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1 }, { 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1 } };

// Model

double[,] availability =

```
GRBEnv env = new GRBEnv();
GRBModel model = new GRBModel(env);
model.Set(GRB.StringAttr.ModelName, "assignment");
// Assignment variables: x[w][s] == 1 if worker w is assigned
// to shift s. This is no longer a pure assignment model, so we must
// use binary variables.
GRBVar[,] x = new GRBVar[nWorkers, nShifts];
for (int w = 0; w < nWorkers; ++w) {
  for (int s = 0; s < nShifts; ++s) {
    x[w,s] =
        model.AddVar(0, availability[w,s], 0, GRB.BINARY,
                     Workers[w] + "." + Shifts[s]);
  }
// Slack variables for each shift constraint so that the shifts can
// be satisfied
GRBVar[] slacks = new GRBVar[nShifts];
for (int s = 0; s < nShifts; ++s) {
  slacks[s] =
    model.AddVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS,
                 Shifts[s] + "Slack");
}
// Variable to represent the total slack
GRBVar totSlack = model.AddVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS,
                                "totSlack");
// Variables to count the total shifts worked by each worker
GRBVar[] totShifts = new GRBVar[nWorkers];
for (int w = 0; w < nWorkers; ++w) {</pre>
  totShifts[w] = model.AddVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS,
                              Workers[w] + "TotShifts");
}
// Update model to integrate new variables
model.Update();
GRBLinExpr lhs;
// Constraint: assign exactly shiftRequirements[s] workers
// to each shift s, plus the slack
for (int s = 0; s < nShifts; ++s) {
  lhs = new GRBLinExpr();
```

```
lhs.AddTerm(1.0, slacks[s]);
  for (int w = 0; w < nWorkers; ++w) {</pre>
    lhs.AddTerm(1.0, x[w, s]);
  }
  model.AddConstr(lhs == shiftRequirements[s], Shifts[s]);
}
// Constraint: set totSlack equal to the total slack
lhs = new GRBLinExpr();
for (int s = 0; s < nShifts; ++s) {
  lhs.AddTerm(1.0, slacks[s]);
model.AddConstr(lhs == totSlack, "totSlack");
// Constraint: compute the total number of shifts for each worker
for (int w = 0; w < nWorkers; ++w) {
  lhs = new GRBLinExpr();
  for (int s = 0; s < nShifts; ++s) {
    lhs.AddTerm(1.0, x[w, s]);
  }
  model.AddConstr(lhs == totShifts[w], "totShifts" + Workers[w]);
// Objective: minimize the total slack
model.SetObjective(1.0*totSlack);
// Optimize
int status = solveAndPrint(model, totSlack, nWorkers, Workers, totShifts);
if (status != GRB.Status.OPTIMAL) {
  return;
}
// Constrain the slack by setting its upper and lower bounds
totSlack.Set(GRB.DoubleAttr.UB, totSlack.Get(GRB.DoubleAttr.X));
totSlack.Set(GRB.DoubleAttr.LB, totSlack.Get(GRB.DoubleAttr.X));
// Variable to count the average number of shifts worked
GRBVar avgShifts =
  model.AddVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS, "avgShifts");
// Variables to count the difference from average for each worker;
// note that these variables can take negative values.
GRBVar[] diffShifts = new GRBVar[nWorkers];
for (int w = 0; w < nWorkers; ++w) {
  diffShifts[w] = model.AddVar(-GRB.INFINITY, GRB.INFINITY, 0,
```

```
GRB.CONTINUOUS, Workers[w] + "Diff");
    }
    // Update model to integrate new variables
    model.Update();
    // Constraint: compute the average number of shifts worked
    lhs = new GRBLinExpr();
    for (int w = 0; w < nWorkers; ++w) {
      lhs.AddTerm(1.0, totShifts[w]);
    }
    model.AddConstr(lhs == nWorkers * avgShifts, "avgShifts");
    // Constraint: compute the difference from the average number of shifts
    for (int w = 0; w < nWorkers; ++w) {</pre>
      model.AddConstr(totShifts[w] - avgShifts == diffShifts[w],
                      Workers[w] + "Diff");
    }
    // Objective: minimize the sum of the square of the difference from the
    // average number of shifts worked
    GRBQuadExpr qobj = new GRBQuadExpr();
    for (int w = 0; w < nWorkers; ++w) {
      qobj.AddTerm(1.0, diffShifts[w], diffShifts[w]);
    }
    model.SetObjective(qobj);
    // Optimize
    status = solveAndPrint(model, totSlack, nWorkers, Workers, totShifts);
    if (status != GRB.Status.OPTIMAL) {
      return;
    }
    // Dispose of model and env
    model.Dispose();
    env.Dispose();
  } catch (GRBException e) {
    Console.WriteLine("Error code: " + e.ErrorCode + ". " +
        e.Message);
  }
}
private static int solveAndPrint(GRBModel model, GRBVar totSlack,
                                 int nWorkers, String[] Workers,
```

```
GRBVar[] totShifts)
  {
    model.Optimize();
    int status = model.Get(GRB.IntAttr.Status);
    if ((status == GRB.Status.INF_OR_UNBD) ||
        (status == GRB.Status.INFEASIBLE) ||
        (status == GRB.Status.UNBOUNDED)) {
      Console.WriteLine("The model cannot be solved "
          + "because it is infeasible or unbounded");
      return status;
    }
    if (status != GRB.Status.OPTIMAL) {
      Console.WriteLine("Optimization was stopped with status " + status);
     return status;
    }
    // Print total slack and the number of shifts worked for each worker
    Console.WriteLine("\nTotal slack required: " +
                      totSlack.Get(GRB.DoubleAttr.X));
    for (int w = 0; w < nWorkers; ++w) {
      Console.WriteLine(Workers[w] + " worked " +
                        totShifts[w].Get(GRB.DoubleAttr.X) + " shifts");
    Console.WriteLine("\n");
    return status;
 }
}
```

3.5 Visual Basic Examples

This section includes source code for all of the Gurobi Visual Basic examples. The same source code can be found in the examples/vb directory of the Gurobi distribution.

```
callback vb.vb
' Copyright 2013, Gurobi Optimization, Inc.
'This example reads an LP or a MIP from a file, sets a callback
' to monitor the optimization progress and to output some progress
' information to the screen and to a log file. If it is a MIP and 10%
' gap is reached, then it aborts.
Imports System
Imports Gurobi
Class callback_vb
    Inherits GRBCallback
    Private vars As GRBVar()
    Private lastnode As Double
    Private lastiter As Double
    Public Sub New(ByVal xvars As GRBVar())
        vars = xvars
        lastnode = lastiter = -1
    End Sub
    Protected Overloads Overrides Sub Callback()
        Try
            If where = GRB.Callback.PRESOLVE Then
                ' Presolve callback
                Dim cdels As Integer = GetIntInfo(GRB.Callback.PRE_COLDEL)
                Dim rdels As Integer = GetIntInfo(GRB.Callback.PRE_ROWDEL)
                Console.WriteLine(cdels & " columns and " & rdels & " rows are removed")
            ElseIf where = GRB.Callback.SIMPLEX Then
                ' Simplex callback
                Dim itcnt As Double = GetDoubleInfo(GRB.Callback.SPX_ITRCNT)
                If itcnt Mod - lastiter >= 100 Then
                    lastiter = itcnt
                    Dim obj As Double = GetDoubleInfo(GRB.Callback.SPX_OBJVAL)
                    Dim pinf As Double = GetDoubleInfo(GRB.Callback.SPX_PRIMINF)
                    Dim dinf As Double = GetDoubleInfo(GRB.Callback.SPX_DUALINF)
                    Dim ispert As Integer = GetIntInfo(GRB.Callback.SPX_ISPERT)
                    Dim ch As Char
                    If ispert = 0 Then
```

```
ch = " "c
                ElseIf ispert = 1 Then
                    ch = "S"c
                Else
                    ch = "P"c
                End If
                Console.WriteLine(itcnt & " " & obj & ch & " " & pinf & " " & dinf)
            End If
        ElseIf where = GRB.Callback.MIP Then
            ' General MIP callback
            Dim nodecnt As Double = GetDoubleInfo(GRB.Callback.MIP_NODCNT)
            If nodecnt - lastnode >= 100 Then
                lastnode = nodecnt
                Dim objbst As Double = GetDoubleInfo(GRB.Callback.MIP_OBJBST)
                Dim objbnd As Double = GetDoubleInfo(GRB.Callback.MIP_OBJBND)
                If Math.Abs(objbst - objbnd) < 0.1 * (1.0R + Math.Abs(objbst)) Then
                    Abort()
                End If
                Dim actnodes As Integer = CInt(GetDoubleInfo(GRB.Callback.MIP_NODLFT))
                Dim itcnt As Integer = CInt(GetDoubleInfo(GRB.Callback.MIP_ITRCNT))
                Dim solcnt As Integer = GetIntInfo(GRB.Callback.MIP_SOLCNT)
                Dim cutcnt As Integer = GetIntInfo(GRB.Callback.MIP_CUTCNT)
                Console.WriteLine(nodecnt & " " & actnodes & " " & itcnt & " " & _
                                  objbst & " " & objbnd & " " & solcnt & " " & cutcnt)
            End If
        ElseIf where = GRB.Callback.MIPSOL Then
            ' MIP solution callback
            Dim obj As Double = GetDoubleInfo(GRB.Callback.MIPSOL_OBJ)
            Dim nodecnt As Integer = CInt(GetDoubleInfo(GRB.Callback.MIPSOL_NODCNT))
            Dim x As Double() = GetSolution(vars)
            Console.WriteLine("**** New solution at node " & nodecnt & ", obj " & _
                              obj & ", x(0) = " & x(0) & "****")
        End If
    Catch e As GRBException
        Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        Console.WriteLine(e.StackTrace)
    End Try
End Sub
Shared Sub Main(ByVal args As String())
    If args.Length < 1 Then
        Console.WriteLine("Usage: callback_vb filename")
        Return
    End If
```

```
Try
            Dim env As New GRBEnv()
            Dim model As New GRBModel(env, args(0))
            Dim vars As GRBVar() = model.GetVars()
            ' Create a callback object and associate it with the model
            model.SetCallback(New callback_vb(vars))
            model.Optimize()
            Dim x As Double() = model.Get(GRB.DoubleAttr.X, vars)
            Dim vnames As String() = model.Get(GRB.StringAttr.VarName, vars)
            For j As Integer = 0 To vars.Length - 1
                If x(j) \Leftrightarrow 0.0R Then
                    Console.WriteLine(vnames(j) & " " & x(j))
                End If
            Next
            ' Dispose of model and env
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
            Console.WriteLine(e.StackTrace)
        End Try
    End Sub
End Class
```

dense vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' This example formulates and solves the following simple QP model:
                x + y + x^2 + x*y + y^2 + y*z + z^2
    subject to x + 2y + 3z >= 4
                x + y
' The example illustrates the use of dense matrices to store A and \ensuremath{\mathtt{Q}}
' (and dense vectors for the other relevant data). We don't recommend
' that you use dense matrices, but this example may be helpful if you
' already have your data in this format.
Imports Gurobi
Class dense_vb
    Protected Shared Function _
      dense_optimize(env As GRBEnv, _
                     rows As Integer, _
                     cols As Integer, _
                     c As Double(), _
                     Q As Double(,), _
                     A As Double(,), _
                     sense As Char(), _
                     rhs As Double(), _
                     lb As Double(), _
                     ub As Double(), _
                     vtype As Char(), _
                     solution As Double()) As Boolean
        Dim success As Boolean = False
        Try
            Dim model As New GRBModel(env)
            ' Add variables to the model
            Dim vars As GRBVar() = model.AddVars(lb, ub, Nothing, vtype, Nothing)
            model.Update()
            ' Populate A matrix
            For i As Integer = 0 To rows - 1
```

```
Dim expr As New GRBLinExpr()
        For j As Integer = 0 To cols - 1
            If A(i, j) \Leftrightarrow 0 Then
                 expr.AddTerm(A(i, j), vars(j))
            End If
        Next
        model.AddConstr(expr, sense(i), rhs(i), "")
    Next
    ' Populate objective
    Dim obj As New GRBQuadExpr()
    If Q IsNot Nothing Then
        For i As Integer = 0 To cols - 1
            For j As Integer = 0 To cols - 1
                 If Q(i, j) \Leftrightarrow 0 Then
                     obj.AddTerm(Q(i, j), vars(i), vars(j))
                 End If
            Next
        Next
        For j As Integer = 0 To cols - 1
            If c(j) \iff 0 Then
                 obj.AddTerm(c(j), vars(j))
            End If
        Next
        model.SetObjective(obj)
    End If
    ' Solve model
    model.Optimize()
    ' Extract solution
    If model.Get(GRB.IntAttr.Status) = GRB.Status.OPTIMAL Then
        success = True
        For j As Integer = 0 To cols - 1
            solution(j) = vars(j).Get(GRB.DoubleAttr.X)
        Next.
    End If
    model.Dispose()
Catch e As GRBException
```

```
Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
        Return success
    End Function
    Public Shared Sub Main(args As String())
        Try
            Dim env As New GRBEnv()
            Dim c As Double() = New Double() {1, 1, 0}
            Dim Q As Double(,) = New Double(,) {{1, 1, 0}, {0, 1, 1}, {0, 0, 1}}
            Dim A As Double(,) = New Double(,) \{\{1, 2, 3\}, \{1, 1, 0\}\}
            Dim sense As Char() = New Char() {">"C, ">"C}
            Dim rhs As Double() = New Double() {4, 1}
            Dim lb As Double() = New Double() {0, 0, 0}
            Dim success As Boolean
            Dim sol As Double() = New Double(2) {}
            success = dense_optimize(env, 2, 3, c, Q, A, sense, rhs, lb, Nothing, _
                                     Nothing, sol)
            If success Then
                Console.WriteLine("x: " & sol(0) & ", y: " & sol(1) & ", z: " & sol(2))
            End If
            ' Dispose of environment
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
   End Sub
End Class
```

diet vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Solve the classic diet model, showing how to add constraints
' to an existing model.
Imports System
Imports Gurobi
Class diet_vb
    Shared Sub Main()
        Try
            ' Nutrition guidelines, based on
            ' USDA Dietary Guidelines for Americans, 2005
            ' http://www.health.gov/DietaryGuidelines/dga2005/
            Dim Categories As String() = New String() {"calories", "protein", "fat", _
                                                        "sodium"}
            Dim nCategories As Integer = Categories.Length
            Dim minNutrition As Double() = New Double() {1800, 91, 0, 0}
            Dim maxNutrition As Double() = New Double() {2200, GRB.INFINITY, 65, 1779}
            ' Set of foods
            Dim Foods As String() = New String() {"hamburger", "chicken", "hot dog", _
                                                   "fries", "macaroni", "pizza", _
                                                   "salad", "milk", "ice cream"}
            Dim nFoods As Integer = Foods.Length
            Dim cost As Double() = New Double() {2.49, 2.89, 1.5R, 1.89, 2.09, 1.99, _
                                                  2.49, 0.89, 1.59}
            ' Nutrition values for the foods
            , hamburger
            ' chicken
            , hot dog
            ' fries
            ' macaroni
            , pizza
            ' salad
            ' milk
            ' ice cream
            Dim nutritionValues As Double(,) = New Double(,) {{410, 24, 26, 730}, _
                                                               {420, 32, 10, 1190}, _
                                                               {560, 20, 32, 1800}, _
                                                               {380, 4, 19, 270}, _
                                                               {320, 12, 10, 930}, _
```

```
{100, 8, 2.5, 125}, _
                                                   {330, 8, 10, 180}}
, Model
Dim env As New GRBEnv()
Dim model As New GRBModel(env)
model.Set(GRB.StringAttr.ModelName, "diet")
' Create decision variables for the nutrition information,
' which we limit via bounds
Dim nutrition As GRBVar() = New GRBVar(nCategories - 1) {}
For i As Integer = 0 To nCategories - 1
    nutrition(i) = model.AddVar(minNutrition(i), maxNutrition(i), 0, _
                                GRB.CONTINUOUS, Categories(i))
Next
' Create decision variables for the foods to buy
Dim buy As GRBVar() = New GRBVar(nFoods - 1) {}
For j As Integer = 0 To nFoods - 1
    buy(j) = model.AddVar(0, GRB.INFINITY, cost(j), GRB.CONTINUOUS, _
                          Foods(j))
Next
' The objective is to minimize the costs
model.Set(GRB.IntAttr.ModelSense, 1)
' Update model to integrate new variables
model.Update()
' Nutrition constraints
For i As Integer = 0 To nCategories - 1
    Dim ntot As GRBLinExpr = 0
    For j As Integer = 0 To nFoods - 1
        ntot.AddTerm(nutritionValues(j, i), buy(j))
    model.AddConstr(ntot = nutrition(i), Categories(i))
Next
, Solve
model.Optimize()
PrintSolution(model, buy, nutrition)
Console.WriteLine(vbLf & "Adding constraint: at most 6 servings of dairy")
```

{320, 15, 12, 820}, _ {320, 31, 12, 1230}, _

```
model.AddConstr(buy(7) + buy(8) <= 6, "limit_dairy")</pre>
            , Solve
            model.Optimize()
            PrintSolution(model, buy, nutrition)
            ' Dispose of model and env
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
    End Sub
    Private Shared Sub PrintSolution(ByVal model As GRBModel, ByVal buy As GRBVar(), _
                                     ByVal nutrition As GRBVar())
        If model.Get(GRB.IntAttr.Status) = GRB.Status.OPTIMAL Then
            Console.WriteLine(vbLf & "Cost: " & model.Get(GRB.DoubleAttr.ObjVal))
            Console.WriteLine(vbLf & "Buy:")
            For j As Integer = 0 To buy.Length - 1
                If buy(j).Get(GRB.DoubleAttr.X) > 0.0001 Then
                    Console.WriteLine(buy(j).Get(GRB.StringAttr.VarName) & " " & _
                                      buy(j).Get(GRB.DoubleAttr.X))
                End If
            Next
            Console.WriteLine(vbLf & "Nutrition:")
            For i As Integer = 0 To nutrition.Length - 1
                Console.WriteLine(nutrition(i).Get(GRB.StringAttr.VarName) & " " & _
                                  nutrition(i).Get(GRB.DoubleAttr.X))
            Next
        Else
            Console.WriteLine("No solution")
        End If
    End Sub
End Class
```

facility vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Facility location: a company currently ships its product from 5 plants
' to 4 warehouses. It is considering closing some plants to reduce
' costs. What plant(s) should the company close, in order to minimize
' transportation and fixed costs?
' Based on an example from Frontline Systems:
' http://www.solver.com/disfacility.htm
' Used with permission.
Imports System
Imports Gurobi
Class facility_vb
    Shared Sub Main()
        Try
            ' Warehouse demand in thousands of units
            Dim Demand As Double() = New Double() {15, 18, 14, 20}
            ' Plant capacity in thousands of units
            Dim Capacity As Double() = New Double() {20, 22, 17, 19, 18}
            ' Fixed costs for each plant
            Dim FixedCosts As Double() = New Double() {12000, 15000, 17000, 13000, _
                                                        16000}
            ' Transportation costs per thousand units
            Dim TransCosts As Double(,) = New Double(,) {{4000, 2000, 3000, 2500, 4500}, _
                                                         {2500, 2600, 3400, 3000, 4000}, _
                                                         {1200, 1800, 2600, 4100, 3000}, _
                                                          {2200, 2600, 3100, 3700, 3200}}
            ' Number of plants and warehouses
            Dim nPlants As Integer = Capacity.Length
            Dim nWarehouses As Integer = Demand.Length
            , Model
            Dim env As New GRBEnv()
            Dim model As New GRBModel(env)
            model.Set(GRB.StringAttr.ModelName, "facility")
            'Plant open decision variables: open(p) == 1 if plant p is open.
```

```
Dim open As GRBVar() = New GRBVar(nPlants - 1) {}
For p As Integer = 0 To nPlants - 1
    open(p) = model.AddVar(0, 1, FixedCosts(p), GRB.BINARY, "Open" & p)
Next
' Transportation decision variables: how much to transport from
' a plant p to a warehouse w
Dim transport As GRBVar(,) = New GRBVar(nWarehouses - 1, nPlants - 1) {}
For w As Integer = 0 To nWarehouses - 1
    For p As Integer = 0 To nPlants - 1
        transport(w, p) = model.AddVar(0, GRB.INFINITY, _
                                       TransCosts(w, p), GRB.CONTINUOUS, _
                                        "Trans" & p & "." & w)
    Next
Next
' The objective is to minimize the total fixed and variable costs
model.Set(GRB.IntAttr.ModelSense, 1)
' Update model to integrate new variables
model.Update()
' Production constraints
' Note that the right-hand limit sets the production to zero if
' the plant is closed
For p As Integer = 0 To nPlants - 1
    Dim ptot As GRBLinExpr = 0
    For w As Integer = 0 To nWarehouses - 1
        ptot.AddTerm(1.0, transport(w, p))
    Next
    model.AddConstr(ptot <= Capacity(p) * open(p), "Capacity" & p)</pre>
Next
' Demand constraints
For w As Integer = 0 To nWarehouses - 1
    Dim dtot As GRBLinExpr = 0
    For p As Integer = 0 To nPlants - 1
        dtot.AddTerm(1.0, transport(w, p))
    Next
    model.AddConstr(dtot = Demand(w), "Demand" & w)
Next
' Guess at the starting point: close the plant with the highest
' fixed costs; open all others
```

```
' First, open all plants
For p As Integer = 0 To nPlants - 1
    open(p).Set(GRB.DoubleAttr.Start, 1.0)
Next
' Now close the plant with the highest fixed cost
Console.WriteLine("Initial guess:")
Dim maxFixed As Double = -GRB.INFINITY
For p As Integer = 0 To nPlants - 1
    If FixedCosts(p) > maxFixed Then
        maxFixed = FixedCosts(p)
    End If
Next
For p As Integer = 0 To nPlants - 1
    If FixedCosts(p) = maxFixed Then
        open(p).Set(GRB.DoubleAttr.Start, 0.0)
        Console.WriteLine("Closing plant " & p & vbLf)
        Exit For
    End If
Next
' Use barrier to solve root relaxation
model.GetEnv().Set(GRB.IntParam.Method, GRB.METHOD_BARRIER)
' Solve
model.Optimize()
' Print solution
Console.WriteLine(vbLf & "TOTAL COSTS: " & model.Get(GRB.DoubleAttr.ObjVal))
Console.WriteLine("SOLUTION:")
For p As Integer = 0 To nPlants - 1
    If open(p).Get(GRB.DoubleAttr.X) = 1.0 Then
        Console.WriteLine("Plant " & p & " open:")
        For w As Integer = 0 To nWarehouses - 1
            If transport(w, p).Get(GRB.DoubleAttr.X) > 0.0001 Then
                Console.WriteLine(" Transport " & _
                                  transport(w, p).Get(GRB.DoubleAttr.X) & _
                                  " units to warehouse " & w)
            End If
        Next
    Else
        Console.WriteLine("Plant " & p & " closed!")
    End If
Next
```

```
' Dispose of model and env
model.Dispose()
env.Dispose()

Catch e As GRBException
Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
End Try
End Sub
End Class
```

feasopt vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' This example reads a MIP model from a file, adds artificial
' variables to each constraint, and then minimizes the sum of the
' artificial variables. A solution with objective zero corresponds
' to a feasible solution to the input model.
' We can also use FeasRelax feature to do it. In this example, we
' use minrelax=1, i.e. optimizing the returned model finds a solution
' that minimizes the original objective, but only from among those
' solutions that minimize the sum of the artificial variables.
Imports Gurobi
Imports System
Class feasopt_vb
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: feasopt_vb filename")
            Return
        End If
        Try
            Dim env As New GRBEnv()
            Dim feasmodel As New GRBModel(env, args(0))
            'Create a copy to use FeasRelax feature later
            Dim feasmodel1 As New GRBModel(feasmodel)
            ' Clear objective
            feasmodel.SetObjective(New GRBLinExpr())
            ' Add slack variables
            Dim c As GRBConstr() = feasmodel.GetConstrs()
            For i As Integer = 0 To c.Length - 1
                Dim sense As Char = c(i).Get(GRB.CharAttr.Sense)
                If sense <> ">"c Then
                    Dim constrs As GRBConstr() = New GRBConstr() {c(i)}
                    Dim coeffs As Double() = New Double() {-1}
                    feasmodel.AddVar(0.0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, _
                                     constrs, coeffs, _
                                     "ArtN_" & c(i).Get(GRB.StringAttr.ConstrName))
                End If
                If sense <> "<"c Then
```

```
Dim constrs As GRBConstr() = New GRBConstr() {c(i)}
                    Dim coeffs As Double() = New Double() {1}
                    feasmodel.AddVar(0.0, GRB.INFINITY, 1.0, GRB.CONTINUOUS, _
                                     constrs, coeffs, _
                                     "ArtP_" & c(i).Get(GRB.StringAttr.ConstrName))
                End If
            Next
            feasmodel.Update()
            ' Optimize modified model
            feasmodel.Write("feasopt.lp")
            feasmodel.Optimize()
            ' Use FeasRelax feature */
            feasmodel1.FeasRelax(GRB.FEASRELAX_LINEAR, true, false, true)
            feasmodel1.Write("feasopt1.lp")
            feasmodel1.Optimize()
            ' Dispose of model and env
            feasmodel1.Dispose()
            feasmodel.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
    End Sub
End Class
```

fixanddive_vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Implement a simple MIP heuristic. Relax the model,
's ort variables based on fractionality, and fix the 25% of
' the fractional variables that are closest to integer variables.
' Repeat until either the relaxation is integer feasible or
' linearly infeasible.
Imports System
Imports System.Collections.Generic
Imports Gurobi
Class fixanddive_vb
    ' Comparison class used to sort variable list based on relaxation
    ' fractionality
    Private Class FractionalCompare: Implements IComparer(Of GRBVar)
        Public Function Compare(ByVal v1 As GRBVar, ByVal v2 As GRBVar) As Integer _
                             Implements IComparer(Of Gurobi.GRBVar).Compare
            Try
                Dim sol1 As Double = Math.Abs(v1.Get(GRB.DoubleAttr.X))
                Dim sol2 As Double = Math.Abs(v2.Get(GRB.DoubleAttr.X))
                Dim frac1 As Double = Math.Abs(sol1 - Math.Floor(sol1 + 0.5))
                Dim frac2 As Double = Math.Abs(sol2 - Math.Floor(sol2 + 0.5))
                If frac1 < frac2 Then
                    Return -1
                ElseIf frac1 > frac2 Then
                    Return 1
                Else
                    Return 0
                End If
            Catch e As GRBException
                Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
            End Try
            Return 0
        End Function
    End Class
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: fixanddive_vb filename")
            Return
        End If
```

```
Try
    ' Read model
    Dim env As New GRBEnv()
    Dim model As New GRBModel(env, args(0))
    ' Collect integer variables and relax them
    Dim intvars As New List(Of GRBVar)()
    For Each v As GRBVar In model.GetVars()
        If v.Get(GRB.CharAttr.VType) <> GRB.CONTINUOUS Then
            intvars.Add(v)
            v.Set(GRB.CharAttr.VType, GRB.CONTINUOUS)
        End If
    Next
    model.GetEnv().Set(GRB.IntParam.OutputFlag, 0)
    model.Optimize()
    ' Perform multiple iterations. In each iteration, identify the first
    ' quartile of integer variables that are closest to an integer value
    ' in the relaxation, fix them to the nearest integer, and repeat.
    For iter As Integer = 0 To 999
        ' create a list of fractional variables, sorted in order of
        ' increasing distance from the relaxation solution to the nearest
        ' integer value
        Dim fractional As New List(Of GRBVar)()
        For Each v As GRBVar In intvars
            Dim sol As Double = Math.Abs(v.Get(GRB.DoubleAttr.X))
            If Math.Abs(sol - Math.Floor(sol + 0.5)) > 0.00001 Then
                fractional.Add(v)
            End If
        Next
        Console.WriteLine("Iteration " & iter & ", obj " & _
                          model.Get(GRB.DoubleAttr.ObjVal) & _
                          ", fractional " & fractional.Count)
        If fractional.Count = 0 Then
            Console.WriteLine("Found feasible solution - objective " & \_
                              model.Get(GRB.DoubleAttr.ObjVal))
            Exit For
        End If
```

```
' Fix the first quartile to the nearest integer value
                fractional.Sort(New FractionalCompare())
                Dim nfix As Integer = Math.Max(fractional.Count / 4, 1)
                For i As Integer = 0 To nfix - 1
                    Dim v As GRBVar = fractional(i)
                    Dim fixval As Double = Math.Floor(v.Get(GRB.DoubleAttr.X) + 0.5)
                    v.Set(GRB.DoubleAttr.LB, fixval)
                    v.Set(GRB.DoubleAttr.UB, fixval)
                    Console.WriteLine(" Fix " & v.Get(GRB.StringAttr.VarName) & _
                                      " to " & fixval & _
                                      " ( rel " & v.Get(GRB.DoubleAttr.X) & " )")
                Next
                model.Optimize()
                ' Check optimization result
                If model.Get(GRB.IntAttr.Status) <> GRB.Status.OPTIMAL Then
                    Console.WriteLine("Relaxation is infeasible")
                    Exit For
                End If
            Next
            ' Dispose of model and env
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " + e.Message)
        End Try
    End Sub
End Class
```

lp_vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' This example reads an LP model from a file and solves it.
' If the model is infeasible or unbounded, the example turns off
' presolve and solves the model again. If the model is infeasible,
' the example computes an Irreducible Infeasible Subsystem (IIS),
' and writes it to a file.
Imports System
Imports Gurobi
Class lp_vb
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: lp_vb filename")
            Return
        End If
        Try
            Dim env As GRBEnv = New GRBEnv("lp1.log")
            Dim model As GRBModel = New GRBModel(env, args(0))
            model.Optimize()
            Dim optimstatus As Integer = model.Get(GRB.IntAttr.Status)
            If optimstatus = GRB.Status.INF_OR_UNBD Then
                model.GetEnv().Set(GRB.IntParam.Presolve, 0)
                model.Optimize()
                optimstatus = model.Get(GRB.IntAttr.Status)
            End If
            If optimstatus = GRB.Status.OPTIMAL Then
                Dim objval As Double = model.Get(GRB.DoubleAttr.ObjVal)
                Console.WriteLine("Optimal objective: " & objval)
            ElseIf optimstatus = GRB.Status.INFEASIBLE Then
                Console.WriteLine("Model is infeasible")
                model.ComputeIIS()
                model.Write("model.ilp")
            ElseIf optimstatus = GRB.Status.UNBOUNDED Then
                Console.WriteLine("Model is unbounded")
                Console.WriteLine("Optimization was stopped with status = " & \_
```

optimstatus)

End If

```
'Dispose of model and env
model.Dispose()
env.Dispose()

Catch e As GRBException
Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
End Try
End Sub
End Class
```

Ipmethod vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Solve a model with different values of the Method parameter;
' show which value gives the shortest solve time.
Imports System
Imports Gurobi
Class lpmethod_vb
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: lpmethod_vb filename")
            Return
        End If
        Try
            ' Read model and verify that it is a MIP
            Dim env As New GRBEnv()
            Dim model As New GRBModel(env, args(0))
            Dim menv As GRBEnv = model.GetEnv()
            ' Solve the model with different values of Method
            Dim bestMethod As Integer = -1
            Dim bestTime As Double = menv.get(GRB.DoubleParam.TimeLimit)
            For i As Integer = 0 To 2
                model.Reset()
                menv.Set(GRB.IntParam.Method, i)
                model.Optimize()
                If model.Get(GRB.IntAttr.Status) = GRB.Status.OPTIMAL Then
                    bestTime = model.Get(GRB.DoubleAttr.Runtime)
                    bestMethod = i
                    ' Reduce the TimeLimit parameter to save time
                    ' with other methods
                    menv.Set(GRB.DoubleParam.TimeLimit, bestTime)
                End If
            Next
            ' Report which method was fastest
            If bestMethod = -1 Then
                Console.WriteLine("Unable to solve this model")
                Console.WriteLine("Solved in " & bestTime & _
```

lpmod vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' This example reads an LP model from a file and solves it.
' If the model can be solved, then it finds the smallest positive variable,
' sets its upper bound to zero, and resolves the model two ways:
' first with an advanced start, then without an advanced start
' (i.e. from scratch).
Imports System
Imports Gurobi
Class lpmod_vb
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: lpmod_vb filename")
            Return
        End If
        Try
            ' Read model and determine whether it is an LP
            Dim env As New GRBEnv()
            Dim model As New GRBModel(env, args(0))
            If model.Get(GRB.IntAttr.IsMIP) <> 0 Then
                Console.WriteLine("The model is not a linear program")
                Environment.Exit(1)
            End If
            model.Optimize()
            Dim status As Integer = model.Get(GRB.IntAttr.Status)
            If (status = GRB.Status.INF_OR_UNBD) OrElse _
               (status = GRB.Status.INFEASIBLE) OrElse _
               (status = GRB.Status.UNBOUNDED) Then
                Console.WriteLine("The model cannot be solved because it is " & _
                                  "infeasible or unbounded")
                Environment.Exit(1)
            End If
            If status <> GRB.Status.OPTIMAL Then
                Console.WriteLine("Optimization was stopped with status " & status)
                Environment.Exit(0)
            End If
```

```
' Find the smallest variable value
Dim minVal As Double = GRB.INFINITY
Dim minVar As GRBVar = Nothing
For Each v As GRBVar In model.GetVars()
    Dim sol As Double = v.Get(GRB.DoubleAttr.X)
    If (sol > 0.0001) AndAlso _
       (sol < minVal) AndAlso _</pre>
       (v.Get(GRB.DoubleAttr.LB) = 0.0) Then
        minVal = sol
        minVar = v
    End If
Next
Console.WriteLine(vbLf & "*** Setting " & _
                  minVar.Get(GRB.StringAttr.VarName) & _
                  " from " & minVal & " to zero ***" & vbLf)
minVar.Set(GRB.DoubleAttr.UB, 0)
' Solve from this starting point
model.Optimize()
' Save iteration & time info
Dim warmCount As Double = model.Get(GRB.DoubleAttr.IterCount)
Dim warmTime As Double = model.Get(GRB.DoubleAttr.Runtime)
' Reset the model and resolve
Console.WriteLine(vbLf & "*** Resetting and solving " & _
                  "without an advanced start ***" & vbLf)
model.Reset()
model.Optimize()
Dim coldCount As Double = model.Get(GRB.DoubleAttr.IterCount)
Dim coldTime As Double = model.Get(GRB.DoubleAttr.Runtime)
Console.WriteLine(vbLf & "*** Warm start: " & warmCount & _
                  " iterations, " & warmTime & " seconds")
Console.WriteLine("*** Cold start: " & coldCount & " iterations, " & _
                  coldTime & " seconds")
' Dispose of model and env
model.Dispose()
env.Dispose()
```

```
Catch e As GRBException

Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)

End Try

End Sub

End Class
```

```
mip1 vb.vb
```

```
' Copyright 2013, Gurobi Optimization, Inc.
' This example formulates and solves the following simple MIP model:
    maximize
                 x +
                      y + 2z
    subject to x + 2y + 3z \le 4
                 x + y
                              >= 1
    x, y, z binary
Imports System
Imports Gurobi
Class mip1_vb
    Shared Sub Main()
        Try
            Dim env As GRBEnv = New GRBEnv("mip1.log")
            Dim model As GRBModel = New GRBModel(env)
            ' Create variables
            Dim x As GRBVar = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, "x")
            Dim y As GRBVar = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, "y")
            Dim z As GRBVar = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, "z")
            ' Integrate new variables
            model.Update()
            'Set objective: maximize x + y + 2z
            model.SetObjective(x + y + 2 * z, GRB.MAXIMIZE)
            ' Add constraint: x + 2 y + 3 z \le 4
            model.AddConstr(x + 2 * y + 3 * z \le 4.0, "c0")
            ' Add constraint: x + y >= 1
            model.AddConstr(x + 2 * y + 3 * z \le 4.0, "c1")
            ' Optimize model
            model.Optimize()
```

```
mip2 vb.vb
' Copyright 2013, Gurobi Optimization, Inc.
' This example reads a MIP model from a file, solves it and
' prints the objective values from all feasible solutions
' generated while solving the MIP. Then it creates the fixed
' model and solves that model.
Imports System
Imports Gurobi
Class mip2_vb
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: mip2_vb filename")
            Return
        End If
        Try
            Dim env As GRBEnv = New GRBEnv("lp1.log")
            Dim model As GRBModel = New GRBModel(env, args(0))
            If model.Get(GRB.IntAttr.IsMIP) = 0 Then
                Console.WriteLine("Model is not a MIP")
                Return
            End If
            model.Optimize()
            Dim optimstatus As Integer = model.Get(GRB.IntAttr.Status)
            If optimstatus = GRB.Status.INF_OR_UNBD Then
                model.GetEnv().Set(GRB.IntParam.Presolve, 0)
                model.Optimize()
                optimstatus = model.Get(GRB.IntAttr.Status)
            End If
            Dim objval As Double
            If optimstatus = GRB.Status.OPTIMAL Then
                objval = model.Get(GRB.DoubleAttr.ObjVal)
                Console.WriteLine("Optimal objective: " & objval)
            ElseIf optimstatus = GRB.Status.INFEASIBLE Then
```

```
Console.WriteLine("Model is infeasible")
    model.ComputeIIS()
    model.Write("model.ilp")
    Return
ElseIf optimstatus = GRB.Status.UNBOUNDED Then
    Console.WriteLine("Model is unbounded")
Else
    Console.WriteLine("Optimization was stopped with status = " & _
                      optimstatus)
    Return
End If
' Iterate over the solutions and compute the objectives
Dim vars() As GRBVar = model.GetVars()
model.GetEnv().Set(GRB.IntParam.OutputFlag, 0)
Console.WriteLine()
For k As Integer = 0 To model.Get(GRB.IntAttr.SolCount) - 1
    model.GetEnv().Set(GRB.IntParam.SolutionNumber, k)
    Dim objn As Double = 0.0
    For j As Integer = 0 To vars.Length - 1
        objn += vars(j).Get(GRB.DoubleAttr.Obj) * _
            vars(j).Get(GRB.DoubleAttr.Xn)
    Next
    Console.WriteLine("Solution " & k & " has objective: " & objn)
Next
Console.WriteLine()
model.GetEnv().Set(GRB.IntParam.OutputFlag, 1)
' Solve fixed model
Dim fixedmodel As GRBModel = model.FixedModel()
fixedmodel.GetEnv().Set(GRB.IntParam.Presolve, 0)
fixedmodel.Optimize()
Dim foptimstatus As Integer = fixedmodel.Get(GRB.IntAttr.Status)
If foptimstatus <> GRB.Status.OPTIMAL Then
    Console.WriteLine("Error: fixed model isn't optimal")
    Return
End If
Dim fobjval As Double = fixedmodel.Get(GRB.DoubleAttr.ObjVal)
```

```
If Math.Abs(fobjval - objval) > 0.000001 * (1.0 + Math.Abs(objval)) Then
            End If
            Dim fvars() As GRBVar = fixedmodel.GetVars()
            Dim x() As Double = fixedmodel.Get(GRB.DoubleAttr.X, fvars)
            Dim vnames() As String = fixedmodel.Get(GRB.StringAttr.VarName, fvars)
            For j As Integer = 0 To fvars.Length - 1
                If x(j) \iff 0 Then
                    Console.WriteLine(vnames(j) & " " & x(j))
                End If
            Next
            ' Dispose of models and env
            fixedmodel.Dispose()
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
    End Sub
End Class
```

params vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Use parameters that are associated with a model.
' A MIP is solved for 5 seconds with different sets of parameters.
' The one with the smallest MIP gap is selected, and the optimization
' is resumed until the optimal solution is found.
Imports System
Imports Gurobi
Class params_vb
    ' Simple function to determine the MIP gap
    Private Shared Function Gap(ByVal model As GRBModel) As Double
        If (model.Get(GRB.IntAttr.SolCount) = 0) OrElse _
           (Math.Abs(model.Get(GRB.DoubleAttr.ObjVal)) < 0.000001) Then
            Return GRB.INFINITY
        End If
        Return Math.Abs(model.Get(GRB.DoubleAttr.ObjBound) - _
                        model.Get(GRB.DoubleAttr.ObjVal)) / _
                   Math.Abs(model.Get(GRB.DoubleAttr.ObjVal))
    End Function
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: params_vb filename")
            Return
        End If
        Try
            ' Read model and verify that it is a MIP
            Dim env As New GRBEnv()
            Dim basemodel As New GRBModel(env, args(0))
            If basemodel.Get(GRB.IntAttr.IsMIP) = 0 Then
                Console.WriteLine("The model is not an integer program")
                Environment.Exit(1)
            End If
            ' Set a 5 second time limit
            basemodel.GetEnv().Set(GRB.DoubleParam.TimeLimit, 5)
            ' Now solve the model with different values of MIPFocus
            Dim bestGap As Double = GRB.INFINITY
```

```
Dim bestModel As GRBModel = Nothing
            For i As Integer = 0 To 3
                Dim m As New GRBModel(basemodel)
                m.GetEnv().Set(GRB.IntParam.MIPFocus, i)
                m.Optimize()
                If bestModel Is Nothing OrElse bestGap > Gap(m) Then
                   bestModel = m
                    bestGap = Gap(bestModel)
                End If
            Next
            ' Finally, reset the time limit and continue to solve the
            ' best model to optimality
            bestModel.GetEnv().Set(GRB.DoubleParam.TimeLimit, GRB.INFINITY)
            bestModel.Optimize()
            Console.WriteLine("Solved with MIPFocus: " & _
                              bestModel.GetEnv().Get(GRB.IntParam.MIPFocus))
       Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
       End Try
   End Sub
End Class
```

qcp vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' This example formulates and solves the following simple QCP model:
     maximize
      subject to x + y + z = 1
                  x^2 + y^2 \le z^2 (second-order cone)
                  x^2 \ll yz
                              (rotated second-order cone)
Imports Gurobi
Class qcp_cs
    Shared Sub Main()
        Try
            Dim env As New GRBEnv("qcp.log")
            Dim model As New GRBModel(env)
            ' Create variables
            Dim x As GRBVar = model.AddVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "x")
            Dim y As GRBVar = model.AddVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "y")
            Dim z As GRBVar = model.AddVar(0.0, GRB.INFINITY, 0.0, GRB.CONTINUOUS, "z")
            ' Integrate new variables
            model.Update()
            ' Set objective
            Dim obj As GRBLinExpr = x
            model.SetObjective(obj, GRB.MAXIMIZE)
            ' Add linear constraint: x + y + z = 1
            model.AddConstr(x + y + z = 1.0, "c0")
            ' Add second-order cone: x^2 + y^2 \le z^2
            model.AddQConstr(x * x + y * y \le z * z, "qc0")
            ' Add rotated cone: x^2 <= yz
            model.AddQConstr(x * x \le y * z, "qc1")
```

```
' Optimize model
            model.Optimize()
            Console.WriteLine(x.Get(GRB.StringAttr.VarName) & " " & _
                              x.Get(GRB.DoubleAttr.X))
            Console.WriteLine(y.Get(GRB.StringAttr.VarName) & " " & _
                              y.Get(GRB.DoubleAttr.X))
            Console.WriteLine(z.Get(GRB.StringAttr.VarName) & " " & _
                              z.Get(GRB.DoubleAttr.X))
            Console.WriteLine("Obj: " & model.Get(GRB.DoubleAttr.ObjVal) & " " & _
                              obj.Value)
            ' Dispose of model and env
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
    End Sub
End Class
```

qp vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' This example formulates and solves the following simple QP model:
     minimize
                 x^2 + x*y + y^2 + y*z + z^2 + z
      subject to x + 2y + 3z >= 4
                  x +
                                >= 1
                      У
    It solves it once as a continuous model, and once as an integer model.
Imports Gurobi
Class qp_vb
   Shared Sub Main()
        Try
            Dim env As New GRBEnv("qp.log")
            Dim model As New GRBModel(env)
            ' Create variables
            Dim x As GRBVar = model.AddVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "x")
            Dim y As GRBVar = model.AddVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "y")
            Dim z As GRBVar = model.AddVar(0.0, 1.0, 0.0, GRB.CONTINUOUS, "z")
            ' Integrate new variables
            model.Update()
            ' Set objective
            Dim obj As New GRBQuadExpr()
            obj = x*x + x*y + y*y + y*z + z*z + 2*x
            model.SetObjective(obj)
            ' Add constraint: x + 2 y + 3 z >= 4
            model.AddConstr(x + 2 * y + 3 * z >= 4.0, "c0")
            , Add constraint: x + y >= 1
            model.AddConstr(x + y >= 1.0, "c1")
            ' Optimize model
```

```
model.Optimize()
            Console.WriteLine(x.Get(GRB.StringAttr.VarName) & " " & _
                              x.Get(GRB.DoubleAttr.X))
            Console.WriteLine(y.Get(GRB.StringAttr.VarName) & " " & _
                              y.Get(GRB.DoubleAttr.X))
            Console.WriteLine(z.Get(GRB.StringAttr.VarName) & " " & _
                              z.Get(GRB.DoubleAttr.X))
            Console.WriteLine("Obj: " & model.Get(GRB.DoubleAttr.ObjVal) & _
                              " " & obj. Value)
            ' Change variable types to integer
            x.Set(GRB.CharAttr.VType, GRB.INTEGER)
            y.Set(GRB.CharAttr.VType, GRB.INTEGER)
            z.Set(GRB.CharAttr.VType, GRB.INTEGER)
            ' Optimize model
            model.Optimize()
            Console.WriteLine(x.Get(GRB.StringAttr.VarName) & " " & _
                              x.Get(GRB.DoubleAttr.X))
            Console.WriteLine(y.Get(GRB.StringAttr.VarName) & " " & _
                              y.Get(GRB.DoubleAttr.X))
            Console.WriteLine(z.Get(GRB.StringAttr.VarName) & " " & _
                              z.Get(GRB.DoubleAttr.X))
            Console.WriteLine("Obj: " & model.Get(GRB.DoubleAttr.ObjVal) & _
                               " " & obj. Value)
            ' Dispose of model and env
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
    End Sub
End Class
```

sensitivity vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Simple MIP sensitivity analysis example.
' For each integer variable, fix it to its lower and upper bound
' and check the impact on the objective.
Imports System
Imports Gurobi
Class sensitivity_vb
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.WriteLine("Usage: sensitivity_vb filename")
            Return
        End If
        Try
            ' Read model
            Dim env As New GRBEnv()
            Dim a As New GRBModel(env, args(0))
            a.Optimize()
            a.GetEnv().Set(GRB.IntParam.OutputFlag, 0)
            ' Extract variables from model
            Dim avars As GRBVar() = a.GetVars()
            For i As Integer = 0 To avars.Length - 1
                Dim v As GRBVar = avars(i)
                If v.Get(GRB.CharAttr.VType) = GRB.BINARY Then
                    ' Create clone and fix variable
                    Dim b As New GRBModel(a)
                    Dim bv As GRBVar = b.GetVars()(i)
                    If v.Get(GRB.DoubleAttr.X) - v.Get(GRB.DoubleAttr.LB) < 0.5 Then
                        bv.Set(GRB.DoubleAttr.LB, bv.Get(GRB.DoubleAttr.UB))
                    Else
                        bv.Set(GRB.DoubleAttr.UB, bv.Get(GRB.DoubleAttr.LB))
                    End If
                    b.Optimize()
                    If b.Get(GRB.IntAttr.Status) = GRB.Status.OPTIMAL Then
                        Dim objchg As Double = b.Get(GRB.DoubleAttr.ObjVal) - _
```

```
a.Get(GRB.DoubleAttr.ObjVal)
                        If objchg < 0 Then
                            objchg = 0
                        End If
                        Console.WriteLine("Objective sensitivity for variable " & _
                                           v.Get(GRB.StringAttr.VarName) & _
                                           " is " & objchg)
                    Else
                        Console.WriteLine("Objective sensitivity for variable " & _
                                           v.Get(GRB.StringAttr.VarName) & _
                                           " is infinite")
                    End If
                    ' Dispose of model
                    b.Dispose()
                End If
            Next
            ' Dispose of model and env
            a.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " + e.Message)
        End Try
    End Sub
End Class
```

```
sos vb.vb
' Copyright 2013, Gurobi Optimization, Inc.
'This example creates a very simple Special Ordered Set (SOS) model.
'The model consists of 3 continuous variables, no linear constraints,
' and a pair of SOS constraints of type 1.
Imports System
Imports Gurobi
Class sos_vb
    Shared Sub Main()
        Try
            Dim env As New GRBEnv()
            Dim model As New GRBModel(env)
            ' Create variables
            Dim ub As Double() = \{1, 1, 2\}
            Dim obj As Double() = \{-2, -1, -1\}
            Dim names As String() = {"x0", "x1", "x2"}
            Dim x As GRBVar() = model.AddVars(Nothing, ub, obj, Nothing, names)
            ' Integrate new variables
            model.Update()
            ' Add first SOS1: x0=0 or x1=0
            Dim sosv1 As GRBVar() = \{x(0), x(1)\}
            Dim soswt1 As Double() = {1, 2}
            model.AddSOS(sosv1, soswt1, GRB.SOS_TYPE1)
            ' Add second SOS1: x0=0 or x2=0
            Dim sosv2 As GRBVar() = \{x(0), x(2)\}
            Dim soswt2 As Double() = {1, 2}
            model.AddSOS(sosv2, soswt2, GRB.SOS_TYPE1)
            ' Optimize model
            model.Optimize()
```

sudoku vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Sudoku example.
' The Sudoku board is a 9x9 grid, which is further divided into a 3x3 grid
' of 3x3 grids. Each cell in the grid must take a value from 0 to 9.
' No two grid cells in the same row, column, or 3x3 subgrid may take the
' same value.
' In the MIP formulation, binary variables x(i,j,v) indicate whether
' cell <i,j> takes value 'v'. The constraints are as follows:
   1. Each cell must take exactly one value (sum_v x(i,j,v) = 1)
   2. Each value is used exactly once per row (sum_i x(i,j,v) = 1)
   3. Each value is used exactly once per column (sum_j x(i,j,v) = 1)
   4. Each value is used exactly once per 3x3 subgrid (sum_grid x(i,j,v) = 1)
' Input datasets for this example can be found in examples/data/sudoku*.
Imports System
Imports System. IO
Imports Gurobi
Class sudoku_vb
    Shared Sub Main(ByVal args as String())
        Dim n As Integer = 9
        Dim s As Integer = 3
        If args.Length < 1 Then
            Console.WriteLine("Usage: sudoku_vb filename")
            Return
        End If
        Try
            Dim env As New GRBEnv()
            Dim model As New GRBModel(env)
            ' Create 3-D array of model variables
            Dim vars As GRBVar(,,) = New GRBVar(n - 1, n - 1, n - 1) {}
            For i As Integer = 0 To n - 1
                For j As Integer = 0 To n - 1
                    For v As Integer = 0 To n - 1
                        Dim st As String = "G_" & i & "_" & j & "_" & v
```

```
vars(i, j, v) = model.AddVar(0.0, 1.0, 0.0, GRB.BINARY, st)
        Next
    Next
Next
' Integrate variables into model
model.Update()
' Add constraints
Dim expr As GRBLinExpr
' Each cell must take one value
For i As Integer = 0 To n - 1
    For j As Integer = 0 To n - 1
        expr = 0
        For v As Integer = 0 To n - 1
            expr.AddTerm(1.0, vars(i, j, v))
        Dim st As String = "V_" & i & "_" & j
        model.AddConstr(expr = 1, st)
   Next
Next
' Each value appears once per row
For i As Integer = 0 To n - 1
    For v As Integer = 0 To n - 1
        expr = 0
        For j As Integer = 0 To n - 1
            expr.AddTerm(1.0, vars(i, j, v))
        Next
        Dim st As String = "R_" & i & "_" & v
        model.AddConstr(expr = 1, st)
    Next
Next
' Each value appears once per column
For j As Integer = 0 To n - 1
    For v As Integer = 0 To n - 1
        expr = 0
        For i As Integer = 0 To n - 1
```

```
expr.AddTerm(1.0, vars(i, j, v))
        Next
        Dim st As String = "C_" & j & "_" & v
        model.AddConstr(expr = 1, st)
    Next
Next
' Each value appears once per sub-grid
For v As Integer = 0 To n - 1
    For iO As Integer = 0 To s - 1
        For j0 As Integer = 0 To s - 1
            expr = 0
            For i1 As Integer = 0 To s - 1
                For j1 As Integer = 0 To s - 1
                    expr.AddTerm(1.0, vars(i0 * s + i1, j0 * s + j1, v))
                Next
            Next
            Dim st As String = "Sub_" & v & "_" & i0 & "_" & j0
            model.AddConstr(expr = 1, st)
        Next
    Next
Next
' Update model
model.Update()
' Fix variables associated with pre-specified cells
Dim sr As StreamReader = File.OpenText(args(0))
For i As Integer = 0 To n - 1
    Dim input As String = sr.ReadLine()
    For j As Integer = 0 To n - 1
        Dim val As Integer = Microsoft.VisualBasic.Asc(input(j)) - 48 - 1
        , 0-based
        If val >= 0 Then
            vars(i, j, val).Set(GRB.DoubleAttr.LB, 1.0)
        End If
   Next
Next
' Optimize model
```

```
model.Optimize()
            ' Write model to file
            model.Write("sudoku.lp")
            Dim x As Double(,,) = model.Get(GRB.DoubleAttr.X, vars)
            Console.WriteLine()
            For i As Integer = 0 To n - 1
                For j As Integer = 0 To n - 1
                    For v As Integer = 0 To n - 1
                        If x(i, j, v) > 0.5 Then
                            Console.Write(v + 1)
                        End If
                    Next
                Next
                Console.WriteLine()
            Next
            ' Dispose of model and env
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
    End Sub
End Class
```

```
tsp vb.vb
' Copyright 2013, Gurobi Optimization, Inc.
' Solve a traveling salesman problem on a randomly generated set of
' points using lazy constraints.
                                   The base MIP model only includes
' 'degree-2' constraints, requiring each node to have exactly
' two incident edges. Solutions to this model may contain subtours -
' tours that don't visit every node. The lazy constraint callback
' adds new constraints to cut them off.
Imports Gurobi
Class tsp_vb
    Inherits GRBCallback
    Private vars As GRBVar(,)
    Public Sub New(xvars As GRBVar(,))
        vars = xvars
    End Sub
    ' Subtour elimination callback.
                                       Whenever a feasible solution is found,
    ' find the smallest subtour, and add a subtour elimination constraint
    ' if the tour doesn't visit every node.
    Protected Overrides Sub Callback()
        Try
            If where = GRB.Callback.MIPSOL Then
                ' Found an integer feasible solution - does it visit every node?
                Dim n As Integer = vars.GetLength(0)
                Dim tour As Integer() = findsubtour(GetSolution(vars))
                If tour.Length < n Then
                    ' Add subtour elimination constraint
                    Dim expr As GRBLinExpr = 0
                    For i As Integer = 0 To tour.Length - 1
                        For j As Integer = 0 To tour.Length - 1
                            expr.AddTerm(1.0, vars(tour(i), tour(j)))
                        Next
                    Next
                    AddLazy(expr <= tour.Length - 1)
                End If
```

Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)

End If

Catch e As GRBException

```
Console.WriteLine(e.StackTrace)
    End Try
End Sub
'Given an integer-feasible solution 'sol', returns the smallest
' sub-tour (as a list of node indices).
Protected Shared Function findsubtour(sol As Double(,)) As Integer()
   Dim n As Integer = sol.GetLength(0)
   Dim seen As Boolean() = New Boolean(n - 1) {}
    Dim tour As Integer() = New Integer(n - 1) {}
    Dim bestind As Integer, bestlen As Integer
    Dim i As Integer, node As Integer, len As Integer, start As Integer
    For i = 0 To n - 1
        seen(i) = False
    Next
    start = 0
    bestlen = n+1
    bestind = -1
    node = 0
    While start < n
        For node = 0 To n - 1
            if Not seen(node)
                Exit For
            End if
        Next
        if node = n
            Exit While
        End if
        For len = 0 To n - 1
            tour(start+len) = node
            seen(node) = true
            For i = 0 To n - 1
                if sol(node, i) > 0.5 AndAlso Not seen(i)
                    node = i
                    Exit For
                End If
            Next
            If i = n
                len = len + 1
                If len < bestlen
                    bestlen = len
                    bestind = start
```

```
End If
                start = start + len
                Exit For
            End If
        Next
    End While
    For i = 0 To bestlen - 1
      tour(i) = tour(bestind+i)
    System.Array.Resize(tour, bestlen)
    Return tour
End Function
' Euclidean distance between points 'i' and 'j'
Protected Shared Function distance(x As Double(), y As Double(), _
                                    i As Integer, j As Integer) As Double
    Dim dx As Double = x(i) - x(j)
    Dim dy As Double = y(i) - y(j)
   Return Math.Sqrt(dx * dx + dy * dy)
End Function
Public Shared Sub Main(args As String())
    If args.Length < 1 Then
        Console.WriteLine("Usage: tsp_vb nnodes")
        Return
    End If
    Dim n As Integer = Convert.ToInt32(args(0))
    Try
        Dim env As New GRBEnv()
        Dim model As New GRBModel(env)
        ' Must set LazyConstraints parameter when using lazy constraints
        model.GetEnv().Set(GRB.IntParam.LazyConstraints, 1)
        Dim \times As Double() = New Double(n - 1) {}
        Dim y As Double() = New Double(n - 1) {}
        Dim r As New Random()
```

```
For i As Integer = 0 To n - 1
   x(i) = r.NextDouble()
    y(i) = r.NextDouble()
Next
' Create variables
Dim vars As GRBVar(,) = New GRBVar(n - 1, n - 1) {}
For i As Integer = 0 To n - 1
    For j As Integer = 0 To i
        vars(i, j) = model.AddVar(0.0, 1.0, distance(x, y, i, j), _
                                  GRB.BINARY, "x" & i & "_" & j)
        vars(j, i) = vars(i, j)
    Next
Next
' Integrate variables
model.Update()
' Degree-2 constraints
For i As Integer = 0 To n - 1
    Dim expr As GRBLinExpr = 0
    For j As Integer = 0 To n - 1
        expr.AddTerm(1.0, vars(i, j))
    model.AddConstr(expr = 2.0, "deg2_" & i)
Next
' Forbid edge from node back to itself
For i As Integer = 0 To n - 1
    vars(i, i).Set(GRB.DoubleAttr.UB, 0.0)
Next
model.SetCallback(New tsp_vb(vars))
model.Optimize()
If model.Get(GRB.IntAttr.SolCount) > 0 Then
    Dim tour As Integer() = findsubtour(model.Get(GRB.DoubleAttr.X, vars))
    Console.Write("Tour: ")
    For i As Integer = 0 To tour.Length - 1
```

```
Console.Write(tour(i) & " ")

Next
Console.WriteLine()

End If

'Dispose of model and environment
model.Dispose()

env.Dispose()

Catch e As GRBException
Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
Console.WriteLine(e.StackTrace)
End Try
End Sub
End Class
```

```
tune vb.vb
' Copyright 2013, Gurobi Optimization, Inc. */
' This example reads a model from a file and tunes it.
' It then writes the best parameter settings to a file
' and solves the model using these parameters.
Imports System
Imports Gurobi
Class tune_vb
    Shared Sub Main(ByVal args As String())
        If args.Length < 1 Then
            Console.Out.WriteLine("Usage: tune_vb filename")
            Return
        End If
        Try
            Dim env As New GRBEnv()
            ' Read model from file
            Dim model As New GRBModel(env, args(0))
            ' Set the TuneResults parameter to 1
            model.GetEnv().Set(GRB.IntParam.TuneResults, 1)
            ' Tune the model
            model.Tune()
            ' Get the number of tuning results
            Dim resultcount As Integer = model.Get(GRB.IntAttr.TuneResultCount)
            If resultcount > 0 Then
                ' Load the tuned parameters into the model's environment
                model.GetTuneResult(0)
                ' Write the tuned parameters to a file
                model.Write("tune.prm")
                ' Solve the model using the tuned parameters
                model.Optimize()
            End If
```

workforce1 vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Assign workers to shifts; each worker may or may not be available on a
' particular day. If the problem cannot be solved, use IIS to find a set of
' conflicting constraints. Note that there may be additional conflicts
' besides what is reported via IIS.
Imports System
Imports Gurobi
Class workforce1_vb
    Shared Sub Main()
        Try
            ' Sample data
            ' Sets of days and workers
            Dim Shifts As String() = New String() {"Mon1", "Tue2", "Wed3", "Thu4", _
                                                    "Fri5", "Sat6", "Sun7", "Mon8", _
                                                    "Tue9", "Wed10", "Thu11", _
                                                    "Fri12", "Sat13", "Sun14"}
            Dim Workers As String() = New String() {"Amy", "Bob", "Cathy", "Dan", _
                                                     "Ed", "Fred", "Gu"}
            Dim nShifts As Integer = Shifts.Length
            Dim nWorkers As Integer = Workers.Length
            ' Number of workers required for each shift
            Dim shiftRequirements As Double() = New Double() {3, 2, 4, 4, 5, 6, _
                                                               5, 2, 2, 3, 4, 6, _
                                                               7, 5}
            ' Amount each worker is paid to work one shift
            Dim pay As Double() = New Double() {10, 12, 10, 8, 8, 9, 11}
            ' Worker availability: O if the worker is unavailable for a shift
            Dim availability As Double(,) = New Double(,) { _
                       \{0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1\}, \_
                       \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\}, \_
                       \{0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1\}, \bot
                       \{0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1\}, \_
                       \{1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1\}, \_
                       {1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1}, _
                       \{1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1\}
```

```
' Model
Dim env As New GRBEnv()
Dim model As New GRBModel(env)
model.Set(GRB.StringAttr.ModelName, "assignment")
'Assignment variables: x(w)(s) == 1 if worker w is assigned
' to shift s. Since an assignment model always produces integer
' solutions, we use continuous variables and solve as an LP.
Dim x As GRBVar(,) = New GRBVar(nWorkers - 1, nShifts - 1) {}
For w As Integer = 0 To nWorkers - 1
    For s As Integer = 0 To nShifts - 1
        x(w, s) = model.AddVar(0, availability(w, s), pay(w), _
                               GRB.CONTINUOUS, _
                               Workers(w) & "." & Shifts(s))
    Next
Next
' The objective is to minimize the total pay costs
model.Set(GRB.IntAttr.ModelSense, 1)
' Update model to integrate new variables
model.Update()
' Constraint: assign exactly shiftRequirements(s) workers
' to each shift s
For s As Integer = 0 To nShifts - 1
    Dim lhs As GRBLinExpr = 0
    For w As Integer = 0 To nWorkers - 1
        lhs.AddTerm(1.0, x(w, s))
    Next
    model.AddConstr(lhs = shiftRequirements(s), Shifts(s))
Next
' Optimize
model.Optimize()
Dim status As Integer = model.Get(GRB.IntAttr.Status)
If status = GRB.Status.UNBOUNDED Then
    Console.WriteLine("The model cannot be solved " & _
                      "because it is unbounded")
    Exit Sub
End If
If status = GRB.Status.OPTIMAL Then
    Console.WriteLine("The optimal objective is " & _
                      model.Get(GRB.DoubleAttr.ObjVal))
    Exit Sub
```

```
End If
            If (status <> GRB.Status.INF_OR_UNBD) AndAlso _
               (status <> GRB.Status.INFEASIBLE) Then
                Console.WriteLine("Optimization was stopped with status " & status)
                Exit Sub
            End If
            , Do IIS
            Console.WriteLine("The model is infeasible; computing IIS")
            model.ComputeIIS()
            Console.WriteLine(vbLf & "The following constraint(s) " & _
                              "cannot be satisfied:")
            For Each c As GRBConstr In model.GetConstrs()
                If c.Get(GRB.IntAttr.IISConstr) = 1 Then
                    Console.WriteLine(c.Get(GRB.StringAttr.ConstrName))
                End If
            Next
            ' Dispose of model and env
            model.Dispose()
            env.Dispose()
        Catch e As GRBException
            Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
        End Try
    End Sub
End Class
```

workforce2 vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Assign workers to shifts; each worker may or may not be available on a
' particular day. If the problem cannot be solved, use IIS iteratively to
' find all conflicting constraints.
Imports System
Imports System.Collections.Generic
Imports Gurobi
Class workforce2_vb
    Shared Sub Main()
        Try
            ' Sample data
            ' Sets of days and workers
            Dim Shifts As String() = New String() {"Mon1", "Tue2", "Wed3", "Thu4", _
                                                    "Fri5", "Sat6", "Sun7", "Mon8", _
                                                    "Tue9", "Wed10", "Thu11", _
                                                    "Fri12", "Sat13", "Sun14"}
            Dim Workers As String() = New String() {"Amy", "Bob", "Cathy", "Dan", _
                                                     "Ed", "Fred", "Gu"}
            Dim nShifts As Integer = Shifts.Length
            Dim nWorkers As Integer = Workers.Length
            ' Number of workers required for each shift
            Dim shiftRequirements As Double() = New Double() {3, 2, 4, 4, 5, 6, _
                                                               5, 2, 2, 3, 4, 6, _
                                                               7, 5}
            ' Amount each worker is paid to work one shift
            Dim pay As Double() = New Double() {10, 12, 10, 8, 8, 9, 11}
            ' Worker availability: O if the worker is unavailable for a shift
            Dim availability As Double(,) = New Double(,) { _
                       \{0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1\}, \_
                       \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\}, \_
                       \{0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1\}, \bot
                       \{0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1\}, 
                       \{1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1\}, \_
                       {1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1}, _
                       {1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1}}
```

```
' Model
Dim env As New GRBEnv()
Dim model As New GRBModel(env)
model.Set(GRB.StringAttr.ModelName, "assignment")
'Assignment variables: x(w)(s) == 1 if worker w is assigned
' to shift s. Since an assignment model always produces integer
' solutions, we use continuous variables and solve as an LP.
Dim x As GRBVar(,) = New GRBVar(nWorkers - 1, nShifts - 1) {}
For w As Integer = 0 To nWorkers - 1
    For s As Integer = 0 To nShifts - 1
        x(w, s) = model.AddVar(0, availability(w, s), pay(w), _
                               GRB.CONTINUOUS, _
                               Workers(w) & "." & Shifts(s))
    Next
Next
' The objective is to minimize the total pay costs
model.Set(GRB.IntAttr.ModelSense, 1)
' Update model to integrate new variables
model.Update()
' Constraint: assign exactly shiftRequirements(s) workers
' to each shift s
For s As Integer = 0 To nShifts - 1
    Dim lhs As GRBLinExpr = 0
    For w As Integer = 0 To nWorkers - 1
        lhs.AddTerm(1.0, x(w, s))
    Next
    model.AddConstr(lhs = shiftRequirements(s), Shifts(s))
Next
' Optimize
model.Optimize()
Dim status As Integer = model.Get(GRB.IntAttr.Status)
If status = GRB.Status.UNBOUNDED Then
    Console.WriteLine("The model cannot be solved " & _
                      "because it is unbounded")
    Exit Sub
End If
If status = GRB.Status.OPTIMAL Then
    Console.WriteLine("The optimal objective is " & _
                      model.Get(GRB.DoubleAttr.ObjVal))
    Exit Sub
```

```
End If
If (status <> GRB.Status.INF_OR_UNBD) AndAlso _
   (status <> GRB.Status.INFEASIBLE) Then
    Console.WriteLine("Optimization was stopped with status " & status)
    Exit Sub
End If
, Do IIS
Console.WriteLine("The model is infeasible; computing IIS")
Dim removed As LinkedList(Of String) = New LinkedList(Of String)()
' Loop until we reduce to a model that can be solved
While True
    model.ComputeIIS()
    Console.WriteLine(vbLf & "The following constraint cannot be satisfied:")
    For Each c As GRBConstr In model.GetConstrs()
        If c.Get(GRB.IntAttr.IISConstr) = 1 Then
            Console.WriteLine(c.Get(GRB.StringAttr.ConstrName))
            ' Remove a single constraint from the model
            removed.AddFirst(c.Get(GRB.StringAttr.ConstrName))
            model.Remove(c)
            Exit For
        End If
    Next
    Console.WriteLine()
    model.Optimize()
    status = model.Get(GRB.IntAttr.Status)
    If status = GRB.Status.UNBOUNDED Then
        Console.WriteLine("The model cannot be solved " & _
                          "because it is unbounded")
        Exit Sub
    End If
    If status = GRB.Status.OPTIMAL Then
        Exit While
    If (status <> GRB.Status.INF_OR_UNBD) AndAlso _
       (status <> GRB.Status.INFEASIBLE) Then
        Console.WriteLine("Optimization was stopped with status " & _
                          status)
        Exit Sub
    End If
End While
```

workforce3 vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Assign workers to shifts; each worker may or may not be available on a
' particular day. If the problem cannot be solved, add slack variables
' to determine which constraints cannot be satisfied, and how much
' they need to be relaxed.
Imports System
Imports System.Collections.Generic
Imports Gurobi
Class workforce3_vb
    Shared Sub Main()
        Try
            ' Sample data
            ' Sets of days and workers
            Dim Shifts As String() = New String() {"Mon1", "Tue2", "Wed3", "Thu4", _
                                                    "Fri5", "Sat6", "Sun7", "Mon8", _
                                                    "Tue9", "Wed10", "Thu11", _
                                                    "Fri12", "Sat13", "Sun14"}
            Dim Workers As String() = New String() {"Amy", "Bob", "Cathy", "Dan", _
                                                     "Ed", "Fred", "Gu"}
            Dim nShifts As Integer = Shifts.Length
            Dim nWorkers As Integer = Workers.Length
            ' Number of workers required for each shift
            Dim shiftRequirements As Double() = New Double() {3, 2, 4, 4, 5, 6, _
                                                               5, 2, 2, 3, 4, 6, _
                                                               7, 5}
            ' Amount each worker is paid to work one shift
            Dim pay As Double() = New Double() {10, 12, 10, 8, 8, 9, 11}
            ' Worker availability: O if the worker is unavailable for a shift
            Dim availability As Double(,) = New Double(,) { _
                       \{0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1\}, \bot
                       \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\}, \_
                       \{0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1\}, \bot
                       \{0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1\}, 
                       {1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1}, _
                       {1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1}, _
                       {1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1}}
```

```
, Model
Dim env As New GRBEnv()
Dim model As New GRBModel(env)
model.Set(GRB.StringAttr.ModelName, "assignment")
'Assignment variables: x(w)(s) == 1 if worker w is assigned
' to shift s. Since an assignment model always produces integer
' solutions, we use continuous variables and solve as an LP.
Dim x As GRBVar(,) = New GRBVar(nWorkers - 1, nShifts - 1) {}
For w As Integer = 0 To nWorkers - 1
    For s As Integer = 0 To nShifts - 1
        x(w, s) = model.AddVar(0, availability(w, s), pay(w), _
                               GRB.CONTINUOUS, _
                               Workers(w) & "." & Shifts(s))
    Next
Next
' The objective is to minimize the total pay costs
model.Set(GRB.IntAttr.ModelSense, 1)
' Update model to integrate new variables
model.Update()
' Constraint: assign exactly shiftRequirements(s) workers
' to each shift s
Dim reqCts As New LinkedList(Of GRBConstr)()
For s As Integer = 0 To nShifts - 1
    Dim lhs As GRBLinExpr = 0
    For w As Integer = 0 To nWorkers - 1
        lhs.AddTerm(1.0, x(w, s))
    Next
    Dim newCt As GRBConstr = model.AddConstr(lhs = shiftRequirements(s), _
                                             Shifts(s))
    reqCts.AddFirst(newCt)
Next
' Optimize
model.Optimize()
Dim status As Integer = model.Get(GRB.IntAttr.Status)
If status = GRB.Status.UNBOUNDED Then
    Console.WriteLine("The model cannot be solved " & _
                      "because it is unbounded")
    Exit Sub
End If
```

```
If status = GRB.Status.OPTIMAL Then
    Console.WriteLine("The optimal objective is " & _
                      model.Get(GRB.DoubleAttr.ObjVal))
    Exit Sub
End If
If (status <> GRB.Status.INF_OR_UNBD) AndAlso _
   (status <> GRB.Status.INFEASIBLE) Then
    Console.WriteLine("Optimization was stopped with status " & status)
   Exit Sub
End If
' Add slack variables to make the model feasible
Console.WriteLine("The model is infeasible; adding slack variables")
' Set original objective coefficients to zero
model.SetObjective(New GRBLinExpr())
' Add a new slack variable to each shift constraint so that the shifts
' can be satisfied
Dim slacks As New LinkedList(Of GRBVar)()
For Each c As GRBConstr In reqCts
    Dim col As New GRBColumn()
    col.AddTerm(1.0, c)
    Dim newvar As GRBVar = model.AddVar(0, GRB.INFINITY, 1.0, _
                                         GRB.CONTINUOUS, col, _
                                         c.Get(GRB.StringAttr.ConstrName) & _
                                         "Slack")
    slacks.AddFirst(newvar)
Next
' Solve the model with slacks
model.Optimize()
status = model.Get(GRB.IntAttr.Status)
If (status = GRB.Status.INF_OR_UNBD) OrElse _
   (status = GRB.Status.INFEASIBLE) OrElse _
   (status = GRB.Status.UNBOUNDED) Then
    Console.WriteLine("The model with slacks cannot be solved " & _
                      "because it is infeasible or unbounded")
   Exit Sub
End If
If status <> GRB.Status.OPTIMAL Then
    Console.WriteLine("Optimization was stopped with status " & status)
    Exit Sub
End If
```

```
Console.WriteLine(vbLf & "Slack values:")

For Each sv As GRBVar In slacks

If sv.Get(GRB.DoubleAttr.X) > 0.000001 Then

Console.WriteLine(sv.Get(GRB.StringAttr.VarName) & " = " & _

sv.Get(GRB.DoubleAttr.X))

End If

Next

' Dispose of model and env

model.Dispose()

env.Dispose()

Catch e As GRBException

Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)

End Try

End Sub

End Class
```

workforce4 vb.vb

```
' Copyright 2013, Gurobi Optimization, Inc.
' Assign workers to shifts; each worker may or may not be available on a
' particular day. We use Pareto optimization to solve the model:
' first, we minimize the linear sum of the slacks. Then, we constrain
' the sum of the slacks, and we minimize a quadratic objective that
' tries to balance the workload among the workers.
Imports System
Imports Gurobi
Class workforce4_vb
    Shared Sub Main()
        Try
            ' Sample data
            ' Sets of days and workers
            Dim Shifts As String() = New String() {"Mon1", "Tue2", "Wed3", "Thu4", _
                                                    "Fri5", "Sat6", "Sun7", "Mon8", _
                                                    "Tue9", "Wed10", "Thu11", _
                                                    "Fri12", "Sat13", "Sun14"}
            Dim Workers As String() = New String() {"Amy", "Bob", "Cathy", "Dan", _
                                                     "Ed", "Fred", "Gu"}
            Dim nShifts As Integer = Shifts.Length
            Dim nWorkers As Integer = Workers.Length
            ' Number of workers required for each shift
            Dim shiftRequirements As Double() = New Double() {3, 2, 4, 4, 5, 6, _
                                                               5, 2, 2, 3, 4, 6, _
                                                               7, 5}
            ' Worker availability: O if the worker is unavailable for a shift
            Dim availability As Double(,) = New Double(,) { _
                       \{0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1\}, \_
                       \{1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0\}, \_
                       \{0, 0, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1\}, \_
                       \{0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1\}, 
                       \{1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1\}, \_
                       {1, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1}, _
                       \{1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1\}
            ' Model
            Dim env As New GRBEnv()
```

```
Dim model As New GRBModel(env)
model.Set(GRB.StringAttr.ModelName, "assignment")
'Assignment variables: x(w)(s) == 1 if worker w is assigned
' to shift s. This is no longer a pure assignment model, so we
' must use binary variables.
Dim x As GRBVar(,) = New GRBVar(nWorkers - 1, nShifts - 1) {}
For w As Integer = 0 To nWorkers - 1
    For s As Integer = 0 To nShifts - 1
        x(w, s) = model.AddVar(0, availability(w, s), 0, _
                               GRB.BINARY, _
                               Workers(w) & "." & Shifts(s))
    Next
Next
' Add a new slack variable to each shift constraint so that the
' shifts can be satisfied
Dim slacks As GRBVar() = New GRBVar(nShifts - 1) {}
For s As Integer = 0 To nShifts - 1
    slacks(s) = _{-}
        model.AddVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS, _
                     Shifts(s) & "Slack")
Next
' Variable to represent the total slack
Dim totSlack As GRBVar = model.AddVar(0, GRB.INFINITY, 0, _
                                      GRB.CONTINUOUS, "totSlack")
' Variables to count the total shifts worked by each worker
Dim totShifts As GRBVar() = New GRBVar(nWorkers - 1) {}
For w As Integer = 0 To nWorkers - 1
    totShifts(w) = _{-}
        model.AddVar(0, GRB.INFINITY, 0, GRB.CONTINUOUS, _
                     Workers(w) & "TotShifts")
Next
' Update model to integrate new variables
model.Update()
Dim lhs As GRBLinExpr
' Constraint: assign exactly shiftRequirements(s) workers
' to each shift s, plus the slack
For s As Integer = 0 To nShifts - 1
    lhs = 0
```

```
lhs.AddTerm(1.0, slacks(s))
    For w As Integer = 0 To nWorkers - 1
        lhs.AddTerm(1.0, x(w, s))
    Next
    model.AddConstr(lhs = shiftRequirements(s), Shifts(s))
Next
' Constraint: set totSlack equal to the total slack
For s As Integer = 0 To nShifts - 1
    lhs.AddTerm(1.0, slacks(s))
Next.
model.AddConstr(lhs = totSlack, "totSlack")
' Constraint: compute the total number of shifts for each worker
For w As Integer = 0 To nWorkers - 1
    For s As Integer = 0 To nShifts - 1
        lhs.AddTerm(1.0, x(w, s))
    Next
    model.AddConstr(lhs = totShifts(w), "totShifts" & Workers(w))
Next
' Objective: minimize the total slack
model.SetObjective(1.0*totSlack)
' Optimize
Dim status As Integer = _
    solveAndPrint(model, totSlack, nWorkers, Workers, totShifts)
If status <> GRB.Status.OPTIMAL Then
    Exit Sub
End If
' Constrain the slack by setting its upper and lower bounds
totSlack.Set(GRB.DoubleAttr.UB, totSlack.Get(GRB.DoubleAttr.X))
totSlack.Set(GRB.DoubleAttr.LB, totSlack.Get(GRB.DoubleAttr.X))
' Variable to count the average number of shifts worked
Dim avgShifts As GRBVar = model.AddVar(0, GRB.INFINITY, 0, _
                                      GRB.CONTINUOUS, "avgShifts")
' Variables to count the difference from average for each worker;
' note that these variables can take negative values.
Dim diffShifts As GRBVar() = New GRBVar(nWorkers - 1) {}
For w As Integer = 0 To nWorkers - 1
```

```
diffShifts(w) = _{-}
                model.AddVar(-GRB.INFINITY, GRB.INFINITY, 0, _
                             GRB.CONTINUOUS, Workers(w) & "Diff")
        Next
        ' Update model to integrate new variables
        model.Update()
        ' Constraint: compute the average number of shifts worked
        For w As Integer = 0 To nWorkers - 1
            lhs.AddTerm(1.0, totShifts(w))
        Next
        model.AddConstr(lhs = nWorkers * avgShifts, "avgShifts")
        ' Constraint: compute the difference from the average number of shifts
        For w As Integer = 0 To nWorkers - 1
            model.AddConstr(totShifts(w) - avgShifts = diffShifts(w), _
                            Workers(w) & "Diff")
        Next
        ' Objective: minimize the sum of the square of the difference
        ' from the average number of shifts worked
        Dim qobj As GRBQuadExpr = New GRBQuadExpr
        For w As Integer = 0 To nWorkers - 1
            qobj.AddTerm(1.0, diffShifts(w), diffShifts(w))
        Next
        model.SetObjective(qobj)
        ' Optimize
        status = solveAndPrint(model, totSlack, nWorkers, Workers, totShifts)
        If status <> GRB.Status.OPTIMAL Then
            Exit Sub
        End If
        ' Dispose of model and env
        model.Dispose()
        env.Dispose()
    Catch e As GRBException
        Console.WriteLine("Error code: " & e.ErrorCode & ". " & e.Message)
    End Try
Private Shared Function solveAndPrint(ByVal model As GRBModel, _
```

End Sub

```
ByVal totSlack As GRBVar, _
                                          ByVal nWorkers As Integer, _
                                          ByVal Workers As String(), _
                                          ByVal totShifts As GRBVar()) As Integer
        model.Optimize()
        Dim status As Integer = model.Get(GRB.IntAttr.Status)
        solveAndPrint = status
        If (status = GRB.Status.INF_OR_UNBD) OrElse _
           (status = GRB.Status.INFEASIBLE) OrElse _
           (status = GRB.Status.UNBOUNDED) Then
            Console.WriteLine("The model cannot be solved because " & _
                              "it is infeasible or unbounded")
            Exit Function
        End If
        If status <> GRB.Status.OPTIMAL Then
            Console.WriteLine("Optimization was stopped with status " _
                              & status)
            Exit Function
        End If
        ' Print total slack and the number of shifts worked for each worker
        Console.WriteLine(vbLf & "Total slack required: " & _
                          totSlack.Get(GRB.DoubleAttr.X))
        For w As Integer = 0 To nWorkers - 1
            Console.WriteLine(Workers(w) & " worked " & _
                              totShifts(w).Get(GRB.DoubleAttr.X) & _
                              " shifts")
        Next
        Console.WriteLine(vbLf)
    End Function
End Class
```

3.6 Python Examples

This section includes source code for all of the Gurobi Python examples. The same source code can be found in the examples/python directory of the Gurobi distribution.

callback.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example reads an LP or a MIP from a file, sets a callback
# to monitor the optimization progress, and outputs progress
# information to the screen and to the log file. If the input model
# is a MIP, the callback aborts the optimization after 10000 nodes have
# been explored.
import sys
from gurobipy import *
# Define callback function
def mycallback(model, where):
    if where == GRB.callback.PRESOLVE:
        # Presolve callback
        print('Removed %d columns and %d rows' % \
              (model.cbGet(GRB.callback.PRE_COLDEL), \
               model.cbGet(GRB.callback.PRE_ROWDEL)))
    elif where == GRB.callback.SIMPLEX:
        # Simplex callback
        itcnt = model.cbGet(GRB.callback.SPX_ITRCNT)
        if itcnt - model._lastiter >= 100:
            model._lastiter = itcnt
            obj = model.cbGet(GRB.callback.SPX_OBJVAL)
            pinf = model.cbGet(GRB.callback.SPX_PRIMINF)
            dinf = model.cbGet(GRB.callback.SPX_DUALINF)
            pert = model.cbGet(GRB.callback.SPX_ISPERT)
            if pert == 0:
                ch = '
            elif pert == 1:
                ch = 'S'
            else:
                ch = 'P'
            print('%d %g %s %g %g' % (int(itcnt), obj, ch, pinf, dinf))
```

```
elif where == GRB.callback.MIP:
        # General MIP callback
        nodecnt = model.cbGet(GRB.callback.MIP_NODCNT)
        if nodecnt - model._lastnode >= 100:
            model._lastnode = nodecnt
            objbst = model.cbGet(GRB.callback.MIP_OBJBST)
            objbnd = model.cbGet(GRB.callback.MIP_OBJBND)
            print('%d %g %g' % (int(nodecnt), objbst, objbnd))
        if nodecnt > model._mynodelimit:
            model.terminate()
    elif where == GRB.callback.MIPSOL:
        # MIP solution callback
                = model.cbGet(GRB.callback.MIPSOL_OBJ)
        obj
        nodecnt = int(model.cbGet(GRB.callback.MIPSOL_NODCNT))
        print('*** New solution at node %g objective %g' % (nodecnt, obj))
        print(model.cbGetSolution(model.getVars()))
    elif where == GRB.callback.MIPNODE:
        # MIP node callback
        print('*** New node')
        if model.cbGet(GRB.callback.MIPNODE_STATUS) == GRB.status.OPTIMAL:
            x = model.cbGetNodeRel(model.getVars())
            model.cbSetSolution(model.getVars(), x)
if len(sys.argv) < 2:
    print('Usage: callback.py filename')
    quit()
# Read and solve model
model = read(sys.argv[1])
# Pass data into my callback function
model._mynodelimit = 10000
model.\_lastnode = -1
model._lastiter = -1
model.params.heuristics = 0
model.optimize(mycallback)
```

custom.py

```
# Copyright 2013, Gurobi Optimization, Inc.
# Interactive shell customization example
# Define a set of customizations for the Gurobi shell.
# Type 'from custom import *' to import them into your shell.
from gurobipy import *
# custom read command --- change directory as appropriate
def myread(name):
    return read('/home/jones/models/' + name)
# simple termination callback
def mycallback(model, where):
    if where == GRB.callback.MIP:
        time = model.cbGet(GRB.callback.RUNTIME)
        best = model.cbGet(GRB.callback.MIP_OBJBST)
        if time > 10 and best < GRB.INFINITY:
            model.terminate()
# custom optimize() function that uses callback
def myopt(model):
   model.optimize(mycallback)
```

dense.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple QP model:
#
#
                 x + y + x^2 + x*y + y^2 + y*z + z^2
     minimize
#
     subject to x + 2y + 3z >= 4
                 x + y
#
                               >= 1
\# The example illustrates the use of dense matrices to store A and Q
# (and dense vectors for the other relevant data). We don't recommend
# that you use dense matrices, but this example may be helpful if you
# already have your data in this format.
import sys
from gurobipy import *
def dense_optimize(rows, cols, c, Q, A, sense, rhs, lb, ub, vtype,
                   solution):
 model = Model()
 # Add variables to model
 for j in range(cols):
    model.addVar(lb=lb[j], ub=ub[j], vtype=vtype[j])
 model.update()
 vars = model.getVars()
  # Populate A matrix
  for i in range(rows):
    expr = LinExpr()
    for j in range(cols):
      if A[i][j] != 0:
        expr += A[i][j]*vars[j]
   model.addConstr(expr, sense[i], rhs[i])
  # Populate objective
  obj = QuadExpr()
  for i in range(cols):
    for j in range(cols):
      if Q[i][j] != 0:
        obj += Q[i][j]*vars[i]*vars[j]
  for j in range(cols):
```

```
if c[j] != 0:
      obj += c[j]*vars[j]
 model.setObjective(obj)
 # Write model to a file
 model.update()
 model.write('dense.lp')
 # Solve
 model.optimize()
  if model.status == GRB.OPTIMAL:
   x = model.getAttr('x', vars)
   for i in range(cols):
      solution[i] = x[i]
   return True
  else:
   return False
# Put model data into dense matrices
c = [1, 1, 0]
Q = [[1, 1, 0], [0, 1, 1], [0, 0, 1]]
A = [[1, 2, 3], [1, 1, 0]]
sense = [GRB.GREATER_EQUAL, GRB.GREATER_EQUAL]
rhs = [4, 1]
1b = [0, 0, 0]
ub = [GRB.INFINITY, GRB.INFINITY, GRB.INFINITY]
vtype = [GRB.CONTINUOUS, GRB.CONTINUOUS, GRB.CONTINUOUS]
sol = [0]*3
# Optimize
success = dense_optimize(2, 3, c, Q, A, sense, rhs, lb, ub, vtype, sol)
if success:
 print('x: %g, y: %g, z: %g' % (sol[0], sol[1], sol[2]))
```

diet.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Solve the classic diet model, showing how to add constraints
# to an existing model.
from gurobipy import *
# Nutrition guidelines, based on
# USDA Dietary Guidelines for Americans, 2005
# http://www.health.gov/DietaryGuidelines/dga2005/
categories, minNutrition, maxNutrition = multidict({
  'calories': [1800, 2200],
  'protein': [91, GRB.INFINITY],
              [0, 65],
  'fat':
  'sodium':
              [0, 1779] })
foods, cost = multidict({
  'hamburger': 2.49,
  'chicken':
               2.89,
  'hot dog':
               1.50,
  'fries':
               1.89,
  'macaroni': 2.09,
  'pizza':
               1.99,
  'salad':
               2.49,
  'milk':
               0.89,
  'ice cream': 1.59 })
# Nutrition values for the foods
nutritionValues = {
  ('hamburger', 'calories'): 410,
  ('hamburger', 'protein'):
  ('hamburger', 'fat'):
                              26,
  ('hamburger', 'sodium'):
                             730,
  ('chicken',
                'calories'): 420,
  ('chicken',
                'protein'):
                             32,
                'fat'):
  ('chicken',
                              10,
  ('chicken',
                'sodium'):
                             1190,
  ('hot dog',
                'calories'): 560,
  ('hot dog',
                'protein'):
                             20,
  ('hot dog',
                'fat'):
                              32,
  ('hot dog',
                'sodium'):
                             1800,
```

```
('fries',
                'calories'): 380,
  ('fries',
                'protein'):
                             4,
  ('fries',
                'fat'):
                             19,
  ('fries',
                'sodium'):
                             270,
  ('macaroni',
                'calories'): 320,
  ('macaroni',
                'protein'):
  ('macaroni',
                'fat'):
  ('macaroni',
                'sodium'):
                             930,
                'calories'): 320,
  ('pizza',
  ('pizza',
                'protein'):
                             15,
                'fat'):
  ('pizza',
                             12,
                'sodium'):
  ('pizza',
                             820,
  ('salad',
                'calories'): 320,
  ('salad',
                'protein'):
                             31,
  ('salad',
                'fat'):
                             12,
  ('salad',
                'sodium'):
                             1230,
  ('milk',
                'calories'): 100,
  ('milk',
                'protein'): 8,
  ('milk',
                'fat'):
                             2.5,
  ('milk',
                'sodium'):
                             125,
  ('ice cream', 'calories'): 330,
  ('ice cream', 'protein'):
  ('ice cream', 'fat'):
                             10,
  ('ice cream', 'sodium'):
                             180 }
# Model
m = Model("diet")
# Create decision variables for the nutrition information,
# which we limit via bounds
nutrition = {}
for c in categories:
    nutrition[c] = m.addVar(lb=minNutrition[c], ub=maxNutrition[c], name=c)
# Create decision variables for the foods to buy
buy = \{\}
for f in foods:
    buy[f] = m.addVar(obj=cost[f], name=f)
# The objective is to minimize the costs
m.modelSense = GRB.MINIMIZE
# Update model to integrate new variables
m.update()
```

```
# Nutrition constraints
for c in categories:
    m.addConstr(
      quicksum(nutritionValues[f,c] * buy[f] for f in foods) == nutrition[c],
def printSolution():
    if m.status == GRB.status.OPTIMAL:
        print('\nCost: %g' % m.objVal)
        print('\nBuy:')
        buyx = m.getAttr('x', buy)
        nutritionx = m.getAttr('x', nutrition)
        for f in foods:
            if buy[f].x > 0.0001:
                print('%s %g' % (f, buyx[f]))
        print('\nNutrition:')
        for c in categories:
            print('%s %g' % (c, nutritionx[c]))
    else:
        print('No solution')
# Solve
m.optimize()
printSolution()
print('\nAdding constraint: at most 6 servings of dairy')
m.addConstr(buy['milk'] + buy['ice cream'] <= 6, "limit_dairy")</pre>
# Solve
m.optimize()
printSolution()
```

diet2.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Separate the model (dietmodel.py) from the data file (diet2.py), so
# that the model can be solved with different data files.
# Nutrition guidelines, based on
# USDA Dietary Guidelines for Americans, 2005
# http://www.health.gov/DietaryGuidelines/dga2005/
from gurobipy import *
categories, minNutrition, maxNutrition = multidict({
  'calories': [1800, 2200],
  'protein': [91, GRB.INFINITY],
              [0, 65],
  'fat':
              [0, 1779] })
  'sodium':
foods, cost = multidict({
  'hamburger': 2.49,
  'chicken':
               2.89,
  'hot dog':
               1.50,
  'fries':
               1.89,
  'macaroni': 2.09,
  'pizza':
               1.99,
  'salad':
               2.49,
  'milk':
               0.89,
  'ice cream': 1.59 })
# Nutrition values for the foods
nutritionValues = {
  ('hamburger', 'calories'): 410,
  ('hamburger', 'protein'):
  ('hamburger', 'fat'):
                             26,
  ('hamburger', 'sodium'):
                             730,
  ('chicken',
                'calories'): 420,
  ('chicken',
                'protein'):
                             32,
                'fat'):
  ('chicken',
                             10,
  ('chicken',
                'sodium'):
                             1190,
  ('hot dog',
                'calories'): 560,
  ('hot dog',
                'protein'):
  ('hot dog',
                'fat'):
                             32,
  ('hot dog',
                'sodium'):
                             1800,
```

```
('fries',
                'calories'): 380,
  ('fries',
                'protein'):
                              4,
                'fat'):
  ('fries',
                              19,
  ('fries',
                'sodium'):
                              270,
  ('macaroni',
                'calories'): 320,
  ('macaroni',
                'protein'):
  ('macaroni',
                'fat'):
                              10,
  ('macaroni',
                'sodium'):
                              930,
  ('pizza',
                'calories'): 320,
                'protein'):
  ('pizza',
                              15,
  ('pizza',
                'fat'):
                              12,
  ('pizza',
                'sodium'):
                              820,
                'calories'): 320,
  ('salad',
  ('salad',
                'protein'):
                              31,
                'fat'):
  ('salad',
                              12,
  ('salad',
                'sodium'):
                              1230,
  ('milk',
                'calories'): 100,
  ('milk',
                'protein'): 8,
  ('milk',
                'fat'):
                              2.5,
  ('milk',
                'sodium'):
                              125,
  ('ice cream', 'calories'): 330,
  ('ice cream', 'protein'):
  ('ice cream', 'fat'):
                              10,
  ('ice cream', 'sodium'):
                              180 }
import dietmodel
dietmodel.solve(categories, minNutrition, maxNutrition,
                foods, cost, nutritionValues)
```

diet3.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Use a SQLite database with the diet model (dietmodel.py). The database
# (diet.db) can be recreated using the included SQL script (diet.sql).
# Note that this example reads an external data file (..\data\diet.db).
# As a result, it must be run from the Gurobi examples/python directory.
import os
import sqlite3
from gurobipy import *
con = sqlite3.connect(os.path.join('...', 'data', 'diet.db'))
cur = con.cursor()
cur.execute('select category,minnutrition,maxnutrition from categories')
result = cur.fetchall()
categories, minNutrition, maxNutrition = multidict(
    (cat,[minv,maxv]) for cat,minv,maxv in result)
cur.execute('select food,cost from foods')
result = cur.fetchall()
foods, cost = multidict(result)
cur.execute('select food, category, value from nutrition')
result = cur.fetchall()
nutritionValues = dict(((f,c),v) for f,c,v in result)
con.close()
import dietmodel
dietmodel.solve(categories, minNutrition, maxNutrition,
                foods, cost, nutritionValues)
```

diet4.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Read diet model data from an Excel spreadsheet (diet.xls).
# Pass the imported data into the diet model (dietmodel.py).
# Note that this example reads an external data file (..\data\diet.xls).
# As a result, it must be run from the Gurobi examples/python directory.
# This example requires Python package 'xlrd', which isn't included
# in most Python distributions. You can obtain it from
# http://pypi.python.org/pypi/xlrd.
import os
import xlrd
book = xlrd.open_workbook(os.path.join("..", "data", "diet.xls"))
sh = book.sheet_by_name("Categories")
categories = []
minNutrition = {}
maxNutrition = {}
i = 1
while True:
    try:
        c = sh.cell_value(i, 0)
        categories.append(c)
        minNutrition[c] = sh.cell_value(i,1)
        maxNutrition[c] = sh.cell_value(i,2)
        i = i + 1
    except IndexError:
        break
sh = book.sheet_by_name("Foods")
foods = []
cost = \{\}
i = 1
while True:
    try:
        f = sh.cell_value(i, 0)
        foods.append(f)
        cost[f] = sh.cell_value(i,1)
        i = i + 1
```

dietmodel.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Solve the classic diet model. This file implements
# a function that formulates and solves the model,
# but it contains no model data. The data is
# passed in by the calling program. Run example 'diet2.py',
# 'diet3.py', or 'diet4.py' to invoke this function.
from gurobipy import *
def solve(categories, minNutrition, maxNutrition, foods, cost,
         nutritionValues):
    # Model
   m = Model("diet")
   # Create decision variables for the nutrition information,
    # which we limit via bounds
    nutrition = {}
    for c in categories:
        nutrition[c] = m.addVar(lb=minNutrition[c], ub=maxNutrition[c], name=c)
    # Create decision variables for the foods to buy
    buy = \{\}
    for f in foods:
        buy[f] = m.addVar(obj=cost[f], name=f)
    # The objective is to minimize the costs
    m.modelSense = GRB.MINIMIZE
    # Update model to integrate new variables
    m.update()
    # Nutrition constraints
    for c in categories:
        m.addConstr(
          quicksum(nutritionValues[f,c] * buy[f] for f in foods) ==
                    nutrition[c], c)
    def printSolution():
        if m.status == GRB.status.OPTIMAL:
            print('\nCost: %g' % m.objVal)
```

```
print('\nBuy:')
        for f in foods:
            if buy[f].x > 0.0001:
                print('%s %g' % (f, buy[f].x))
        print('\nNutrition:')
        for c in categories:
            print('%s %g' % (c, nutrition[c].x))
    else:
        print('No solution')
# Solve
m.optimize()
printSolution()
print('\nAdding constraint: at most 6 servings of dairy')
m.addConstr(buy['milk'] + buy['ice cream'] <= 6, "limit_dairy")</pre>
# Solve
m.optimize()
printSolution()
```

facility.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Facility location: a company currently ships its product from 5 plants
# to 4 warehouses. It is considering closing some plants to reduce
# costs. What plant(s) should the company close, in order to minimize
# transportation and fixed costs?
# Note that this example uses lists instead of dictionaries.
# it does not work with sparse data, lists are a reasonable option.
# Based on an example from Frontline Systems:
   http://www.solver.com/disfacility.htm
# Used with permission.
from gurobipy import *
# Warehouse demand in thousands of units
demand = [15, 18, 14, 20]
# Plant capacity in thousands of units
capacity = [20, 22, 17, 19, 18]
# Fixed costs for each plant
fixedCosts = [12000, 15000, 17000, 13000, 16000]
# Transportation costs per thousand units
transCosts = [[4000, 2000, 3000, 2500, 4500],
              [2500, 2600, 3400, 3000, 4000],
              [1200, 1800, 2600, 4100, 3000],
              [2200, 2600, 3100, 3700, 3200]]
# Range of plants and warehouses
plants = range(len(capacity))
warehouses = range(len(demand))
# Model
m = Model("facility")
# Plant open decision variables: open[p] == 1 if plant p is open.
open = []
for p in plants:
    open.append(m.addVar(vtype=GRB.BINARY, name="Open%d" % p))
```

```
# Transportation decision variables: how much to transport from
# a plant p to a warehouse w
transport = []
for w in warehouses:
    transport.append([])
    for p in plants:
        transport[w].append(m.addVar(obj=transCosts[w][p],
                                     name="Trans%d.%d" % (p, w)))
# The objective is to minimize the total fixed and variable costs
m.modelSense = GRB.MINIMIZE
# Update model to integrate new variables
m.update()
# Set optimization objective - minimize sum of fixed costs
m.setObjective(quicksum([fixedCosts[p]*open[p] for p in plants]))
# Production constraints
# Note that the right-hand limit sets the production to zero if the plant
# is closed
for p in plants:
   m.addConstr(
        quicksum(transport[w][p] for w in warehouses) <= capacity[p] * open[p],
        "Capacity%d" % p)
# Demand constraints
for w in warehouses:
    m.addConstr(quicksum(transport[w][p] for p in plants) == demand[w],
                "Demand%d" % w)
# Guess at the starting point: close the plant with the highest fixed costs;
# open all others
# First, open all plants
for p in plants:
    open[p].start = 1.0
# Now close the plant with the highest fixed cost
print('Initial guess:')
maxFixed = max(fixedCosts)
for p in plants:
    if fixedCosts[p] == maxFixed:
        open[p].start = 0.0
```

```
print('Closing plant %s' % p)
        break
print('')
# Use barrier to solve root relaxation
m.params.method = 2
# Solve
m.optimize()
# Print solution
print('\nTOTAL COSTS: %g' % m.objVal)
print('SOLUTION:')
for p in plants:
    if open[p].x == 1.0:
        print('Plant %s open' % p)
        for w in warehouses:
            if transport[w][p].x > 0:
                print(' Transport %g units to warehouse %s' % \
                      (transport[w][p].x, w))
    else:
        print('Plant %s closed!' % p)
```

feasopt.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example reads a MIP model from a file, adds artificial
# variables to each constraint, and then minimizes the sum of the
# artificial variables. A solution with objective zero corresponds
# to a feasible solution to the input model.
# We can also use FeasRelax feature to do it. In this example, we
# use minrelax=1, i.e. optimizing the returned model finds a solution
# that minimizes the original objective, but only from among those
# solutions that minimize the sum of the artificial variables.
import sys
from gurobipy import *
if len(sys.argv) < 2:
    print('Usage: feasopt.py filename')
    quit()
feasmodel = gurobi.read(sys.argv[1])
#create a copy to use FeasRelax feature later
feasmodel1 = feasmodel.copy()
# clear objective
feasmodel.setObjective(0.0)
# add slack variables
for c in feasmodel.getConstrs():
    sense = c.sense
    if sense != '>':
        feasmodel.addVar(obj=1.0, name="ArtN_" + c.constrName,
                         column=Column([-1], [c]))
    if sense != '<':
        feasmodel.addVar(obj=1.0, name="ArtP_" + c.constrName,
                         column=Column([1], [c]))
feasmodel.update()
```

```
# optimize modified model
feasmodel.write('feasopt.lp')
feasmodel.optimize()
# use FeasRelax feature
feasmodel1.feasRelaxS(0, True, False, True);
feasmodel1.write("feasopt1.lp");
feasmodel1.optimize();
```

fixanddive.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Implement a simple MIP heuristic. Relax the model,
# sort variables based on fractionality, and fix the 25% of
# the fractional variables that are closest to integer variables.
# Repeat until either the relaxation is integer feasible or
# linearly infeasible.
import sys
from gurobipy import *
# Key function used to sort variables based on relaxation fractionality
def sortkey(v1):
    sol = v1.x
    return abs(sol-int(sol+0.5))
if len(sys.argv) < 2:
    print('Usage: fixanddive.py filename')
    quit()
# Read model
model = gurobi.read(sys.argv[1])
# Collect integer variables and relax them
intvars = []
for v in model.getVars():
    if v.vType != GRB.CONTINUOUS:
        intvars += [v]
        v.vType = GRB.CONTINUOUS
model.params.outputFlag = 0
model.optimize()
# Perform multiple iterations. In each iteration, identify the first
# quartile of integer variables that are closest to an integer value in the
# relaxation, fix them to the nearest integer, and repeat.
```

```
for iter in range(1000):
# create a list of fractional variables, sorted in order of increasing
# distance from the relaxation solution to the nearest integer value
    fractional = []
    for v in intvars:
        sol = v.x
        if abs(sol - int(sol+0.5)) > 1e-5:
            fractional += [v]
    fractional.sort(key=sortkey)
    print('Iteration %d, obj %g, fractional %d' % \
          (iter, model.objVal, len(fractional)))
    if len(fractional) == 0:
        print('Found feasible solution - objective %g' % model.objVal)
        break
# Fix the first quartile to the nearest integer value
   nfix = max(int(len(fractional)/4), 1)
    for i in range(nfix):
        v = fractional[i]
        fixval = int(v.x+0.5)
        v.lb = fixval
        v.ub = fixval
        print(' Fix %s to %g (rel %g)' % (v.varName, fixval, v.x))
   model.optimize()
# Check optimization result
    if model.status != GRB.status.OPTIMAL:
        print('Relaxation is infeasible')
        break
```

lp.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example reads an LP model from a file and solves it.
# If the model is infeasible or unbounded, the example turns off
# presolve and solves the model again. If the model is infeasible,
# the example computes an Irreducible Infeasible Subsystem (IIS),
# and writes it to a file
import sys
from gurobipy import *
if len(sys.argv) < 2:
    print('Usage: lp.py filename')
    quit()
# Read and solve model
model = read(sys.argv[1])
model.optimize()
if model.status == GRB.status.INF_OR_UNBD:
    # Turn presolve off to determine whether model is infeasible
    # or unbounded
    model.setParam(GRB.param.presolve, 0)
    model.optimize()
if model.status == GRB.status.OPTIMAL:
    print('Optimal objective: %g' % model.objVal)
    model.write('model.sol')
    exit(0)
elif model.status != GRB.status.INFEASIBLE:
    print('Optimization was stopped with status %d' % model.status)
    exit(0)
# Model is infeasible - compute an Irreducible Infeasible Subsystem (IIS)
print('')
print('Model is infeasible')
model.computeIIS()
model.write("model.ilp")
print("IIS written to file 'model.ilp'")
```

Ipmethod.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Solve a model with different values of the Method parameter;
# show which value gives the shortest solve time.
import sys
from gurobipy import *
if len(sys.argv) < 2:
    print('Usage: lpmethod.py filename')
    quit()
# Read model
m = read(sys.argv[1])
# Solve the model with different values of Method
bestTime = m.params.timeLimit
bestMethod = -1
for i in range(3):
    m.reset()
    m.params.method = i
    m.optimize()
    if m.status == GRB.status.OPTIMAL:
        bestTime = m.Runtime
        bestMethod = i
        # Reduce the TimeLimit parameter to save time with other methods
        m.params.timeLimit = bestTime
# Report which method was fastest
if bestMethod == -1:
    print('Unable to solve this model')
else:
    print('Solved in %g seconds with Method %d' % (bestTime, bestMethod))
```

Ipmod.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example reads an LP model from a file and solves it.
# If the model can be solved, then it finds the smallest positive variable,
# sets its upper bound to zero, and resolves the model two ways:
# first with an advanced start, then without an advanced start
# (i.e. 'from scratch').
import sys
from gurobipy import *
if len(sys.argv) < 2:
    print('Usage: lpmod.py filename')
    quit()
# Read model and determine whether it is an LP
model = read(sys.argv[1])
if model.isMIP == 1:
    print('The model is not a linear program')
    exit(1)
model.optimize()
status = model.status
if status == GRB.status.INF_OR_UNBD or status == GRB.status.INFEASIBLE \
   or status == GRB.status.UNBOUNDED:
    print('The model cannot be solved because it is infeasible or unbounded')
    exit(1)
if status != GRB.status.OPTIMAL:
    print('Optimization was stopped with status %d' % status)
    exit(0)
# Find the smallest variable value
minVal = GRB.INFINITY
for v in model.getVars():
    if v.x > 0.0001 and v.x < minVal and v.lb == 0.0:
        minVal = v.x
        minVar = v
```

```
print('\n*** Setting %s from %g to zero ***\n' % (minVar.varName, minVal))
minVar.ub = 0.0
# Solve from this starting point
model.optimize()
# Save iteration & time info
warmCount = model.IterCount
warmTime = model.Runtime
# Reset the model and resolve
print('\n*** Resetting and solving without an advanced start ***\n')
model.reset()
model.optimize()
coldCount = model.IterCount
coldTime = model.Runtime
print('')
print('*** Warm start: %g iterations, %g seconds' % (warmCount, warmTime))
print('*** Cold start: %g iterations, %g seconds' % (coldCount, coldTime))
```

mip1.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple MIP model:
  maximize
#
#
        x +
               y + 2z
 subject to
#
        x + 2 y + 3 z <= 4
#
                   >= 1
        x + y
# x, y, z binary
from gurobipy import *
try:
    # Create a new model
    m = Model("mip1")
    # Create variables
    x = m.addVar(vtype=GRB.BINARY, name="x")
    y = m.addVar(vtype=GRB.BINARY, name="y")
    z = m.addVar(vtype=GRB.BINARY, name="z")
    # Integrate new variables
    m.update()
    # Set objective
    m.setObjective(x + y + 2 * z, GRB.MAXIMIZE)
    # Add constraint: x + 2 y + 3 z \le 4
    m.addConstr(x + 2 * y + 3 * z \le 4, "c0")
    # Add constraint: x + y >= 1
    m.addConstr(x + y >= 1, "c1")
    m.optimize()
    for v in m.getVars():
        print('%s %g' % (v.varName, v.x))
    print('Obj: %g' % m.objVal)
```

except GurobiError:
 print('Error reported')

mip2.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example reads a MIP model from a file, solves it and prints
# the objective values from all feasible solutions generated while
# solving the MIP. Then it creates the associated fixed model and
# solves that model.
import sys
from gurobipy import *
if len(sys.argv) < 2:
    print('Usage: mip2.py filename')
    quit()
# Read and solve model
model = read(sys.argv[1])
if model.isMIP == 0:
   print('Model is not a MIP')
    exit(0)
model.optimize()
if model.status == GRB.status.OPTIMAL:
    print('Optimal objective: %g' % model.objVal)
elif model.status == GRB.status.INF_OR_UNBD:
    print('Model is infeasible or unbounded')
    exit(0)
elif model.status == GRB.status.INFEASIBLE:
    print('Model is infeasible')
    exit(0)
elif model.status == GRB.status.UNBOUNDED:
    print('Model is unbounded')
    exit(0)
else:
    print('Optimization ended with status %d' % model.status)
    exit(0)
# Iterate over the solutions and compute the objectives
model.params.outputFlag = 0
print('')
```

```
for k in range(model.solCount):
    model.params.solutionNumber = k
    objn = 0
    for v in model.getVars():
        objn += v.obj * v.xn
    print('Solution %d has objective %g' % (k, objn))
model.params.outputFlag = 1
fixed = model.fixed()
fixed.params.presolve = 0
fixed.optimize()
if fixed.status != GRB.status.OPTIMAL:
    print("Error: fixed model isn't optimal")
    exit(1)
diff = model.objVal - fixed.objVal
if abs(diff) > 1e-6 * (1.0 + abs(model.objVal)):
    print('Error: objective values are different')
    exit(1)
# Print values of nonzero variables
for v in fixed.getVars():
    if v.x != 0:
        print('%s %g' % (v.varName, v.x))
```

netflow.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Solve a multi-commodity flow problem. Two products ('Pencils' and 'Pens')
# are produced in 2 cities ('Detroit' and 'Denver') and must be sent to
# warehouses in 3 cities ('Boston', 'New York', and 'Seattle') to
# satisfy demand ('inflow[h,i]').
# Flows on the transportation network must respect arc capacity constraints
# ('capacity[i,j]'). The objective is to minimize the sum of the arc
# transportation costs ('cost[i,j]').
from gurobipy import *
# Model data
commodities = ['Pencils', 'Pens']
nodes = ['Detroit', 'Denver', 'Boston', 'New York', 'Seattle']
arcs, capacity = multidict({
  ('Detroit', 'Boston'):
  ('Detroit', 'New York'): 80,
  ('Detroit', 'Seattle'): 120,
  ('Denver', 'Boston'):
                           120,
  ('Denver', 'New York'): 120,
  ('Denver', 'Seattle'): 120 })
arcs = tuplelist(arcs)
cost = {
  ('Pencils', 'Detroit', 'Boston'):
                                      10,
  ('Pencils', 'Detroit', 'New York'): 20,
  ('Pencils', 'Detroit', 'Seattle'):
  ('Pencils', 'Denver', 'Boston'):
  ('Pencils', 'Denver',
                        'New York'): 40,
  ('Pencils', 'Denver', 'Seattle'): 30,
              'Detroit', 'Boston'):
  ('Pens',
                                      20,
              'Detroit', 'New York'): 20,
  ('Pens',
              'Detroit', 'Seattle'): 80,
  ('Pens',
              'Denver', 'Boston'):
  ('Pens',
              'Denver',
  ('Pens',
                        'New York'): 70,
  ('Pens',
              'Denver',
                        'Seattle'): 30 }
inflow = {
```

```
('Pencils', 'Detroit'):
                            50,
  ('Pencils', 'Denver'):
                            60,
  ('Pencils', 'Boston'):
                           -50,
  ('Pencils', 'New York'): -50,
  ('Pencils', 'Seattle'): -10,
  ('Pens',
             'Detroit'):
                            60,
  ('Pens',
             'Denver'):
                            40,
             'Boston'):
  ('Pens',
                           -40,
             'New York'): -30,
  ('Pens',
             'Seattle'): -30 }
  ('Pens',
# Create optimization model
m = Model('netflow')
# Create variables
flow = {}
for h in commodities:
    for i, j in arcs:
        flow[h,i,j] = m.addVar(ub=capacity[i,j], obj=cost[h,i,j],
                               name='flow_%s_%s_%s' % (h, i, j))
m.update()
# Arc capacity constraints
for i,j in arcs:
    m.addConstr(quicksum(flow[h,i,j] for h in commodities) <= capacity[i,j],</pre>
                'cap_%s_%s' % (i, j))
# Flow conservation constraints
for h in commodities:
    for j in nodes:
        m.addConstr(
          quicksum(flow[h,i,j] for i,j in arcs.select('*',j)) +
              inflow[h,j] ==
          quicksum(flow[h,j,k] for j,k in arcs.select(j,'*')),
                   'node_%s_%s' % (h, j))
# Compute optimal solution
m.optimize()
# Print solution
if m.status == GRB.status.OPTIMAL:
    solution = m.getAttr('x', flow)
    for h in commodities:
        print('\nOptimal flows for %s:' % h)
        for i,j in arcs:
```

```
if solution[h,i,j] > 0:
    print('%s -> %s: %g' % (i, j, solution[h,i,j]))
```

params.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Use parameters that are associated with a model.
# A MIP is solved for 5 seconds with different sets of parameters.
# The one with the smallest MIP gap is selected, and the optimization
# is resumed until the optimal solution is found.
import sys
from gurobipy import *
if len(sys.argv) < 2:
    print('Usage: params.py filename')
    quit()
# Simple function to determine the MIP gap
def gap(model):
    if model.solCount == 0 or abs(model.objVal) < 1e-6:
        return GRB.INFINITY
    return abs(model.objBound - model.objVal)/abs(model.objVal)
# Read model and verify that it is a MIP
base = read(sys.argv[1])
if base.isMIP == 0:
    print('The model is not an integer program')
    exit(1)
# Set a 5 second time limit
base.params.timeLimit = 5
# Now solve the model with different values of MIPFocus
bestGap = GRB.INFINITY
bestModel = None
for i in range(4):
   m = base.copy()
   m.params.MIPFocus = i
    m.optimize()
    if bestModel == None or bestGap > gap(m):
        bestModel = m
        bestGap = gap(bestModel)
```

```
# Finally, reset the time limit and continue to solve the
# best model to optimality
bestModel.params.timeLimit = "default"
bestModel.optimize()
print('Solved with MIPFocus: %d' % bestModel.params.MIPFocus)
```

qcp.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple QCP model:
      maximize
#
      subject to x + y + z = 1
                  x^2 + y^2 \le z^2 (second-order cone)
                  x^2 \le yz
                                    (rotated second-order cone)
from gurobipy import *
# Create a new model
m = Model("qcp")
# Create variables
x = m.addVar(name="x")
y = m.addVar(name="y")
z = m.addVar(name="z")
# Integrate new variables
m.update()
# Set objective: x
obj = 1.0*x
m.setObjective(obj, GRB.MAXIMIZE)
# Add constraint: x + y + z = 1
m.addConstr(x + y + z == 1, "c0")
# Add second-order cone: x^2 + y^2 \le z^2
m.addQConstr(x*x + y*y \le z*z, "qc0")
# Add rotated cone: x^2 <= yz
m.addQConstr(x*x <= y*z, "qc1")</pre>
m.optimize()
for v in m.getVars():
    print('%s %g' % (v.varName, v.x))
print('Obj: %g' % obj.getValue())
```

qp.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple QP model:
# minimize
       x^2 + x*y + y^2 + y*z + z^2 + z
#
  subject to
      x + 2 y + 3 z >= 4
#
#
       x + y >= 1
# It solves it once as a continuous model, and once as an integer model.
from gurobipy import *
# Create a new model
m = Model("qp")
# Create variables
x = m.addVar(ub=1.0, name="x")
y = m.addVar(ub=1.0, name="y")
z = m.addVar(ub=1.0, name="z")
# Integrate new variables
m.update()
# Set objective: x^2 + x*y + y^2 + y*z + z^2 + z
obj = x*x + x*y + y*y + y*z + z*z + 2*x
m.setObjective(obj)
# Add constraint: x + 2 y + 3 z \le 4
m.addConstr(x + 2 * y + 3 * z >= 4, "c0")
# Add constraint: x + y >= 1
m.addConstr(x + y >= 1, "c1")
m.optimize()
for v in m.getVars():
    print('%s %g' % (v.varName, v.x))
print('Obj: %g' % obj.getValue())
x.vType = GRB.INTEGER
```

```
y.vType = GRB.INTEGER
z.vType = GRB.INTEGER
m.optimize()
for v in m.getVars():
    print('%s %g' % (v.varName, v.x))
print('Obj: %g' % obj.getValue())
```

sensitivity.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Simple MIP sensitivity analysis example.
# For each integer variable, fix it to its lower and upper bound
# and check the impact on the objective.
import sys
from gurobipy import *
if len(sys.argv) < 2:</pre>
    print('Usage: sensitivity.py filename')
    quit()
a = gurobi.read(sys.argv[1])
a.optimize()
a.params.outputFlag = 0
# Extract variables from model
avars = a.getVars()
# Iterate through binary variables in model
for i in range(len(avars)):
    v = avars[i]
    if v.vType == GRB.BINARY:
# Create clone and fix variable
        b = a.copy()
        bv = b.getVars()[i]
        if v.x - v.1b < 0.5:
            bv.lb = bv.ub
        else:
            bv.ub = bv.lb
        b.optimize()
        if b.status == GRB.status.OPTIMAL:
            objchg = b.objVal - a.objVal
            if objchg < 0:
```

sos.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example creates a very simple Special Ordered Set (SOS) model.
# The model consists of 3 continuous variables, no linear constraints,
# and a pair of SOS constraints of type 1.
from gurobipy import *
try:
    # Create a new model
   model = Model("sos")
   # Create variables
   x0 = model.addVar(ub=1.0, name="x0")
    x1 = model.addVar(ub=1.0, name="x1")
   x2 = model.addVar(ub=2.0, name="x2")
    # Integrate new variables
   model.update()
    # Set objective
    model.setObjective(2 * x0 + x1 + x2, GRB.MAXIMIZE)
    # Add first SOS: x0 = 0 or x1 = 0
    model.addSOS(GRB.SOS_TYPE1, [x0, x1], [1, 2])
    # Add second SOS: x0 = 0 or x2 = 0
    model.addSOS(GRB.SOS_TYPE1, [x0, x2], [1, 2])
   model.optimize()
    for v in model.getVars():
        print('%s %g' % (v.varName, v.x))
    print('Obj: %g' % model.objVal)
except GurobiError:
```

print('Encountered an error')

sudoku.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Sudoku example.
# The Sudoku board is a 9x9 grid, which is further divided into a 3x3 grid
# of 3x3 grids. Each cell in the grid must take a value from 0 to 9.
# No two grid cells in the same row, column, or 3x3 subgrid may take the
# same value.
# In the MIP formulation, binary variables x[i,j,v] indicate whether
# cell <i,j> takes value 'v'. The constraints are as follows:
   1. Each cell must take exactly one value (sum_v x[i,j,v] = 1)
   2. Each value is used exactly once per row (sum_i x[i,j,v] = 1)
   3. Each value is used exactly once per column (sum_j x[i,j,v] = 1)
   4. Each value is used exactly once per 3x3 subgrid (sum_grid x[i,j,v] = 1)
# Input datasets for this example can be found in examples/data/sudoku*.
import sys
import math
from gurobipy import *
if len(sys.argv) < 2:
    print('Usage: sudoku.py filename')
    quit()
f = open(sys.argv[1])
grid = f.read().split()
n = len(grid[0])
s = int(math.sqrt(n))
# 3-D array of variables will be indexed by (i,j,v) tuples
vars = \{\}
# Create our 3-D array of model variables
model = Model('sudoku')
```

```
for i in range(n):
    for j in range(n):
        for v in range(n):
            vars[i,j,v] = model.addVar(vtype=GRB.BINARY,
                                       name='G_'+ str(i)+'_'+str(j)+'_'+str(v))
# Update model to integrate new variables
model.update()
# Fix variables associated with cells whose values are pre-specified
for i in range(n):
    for j in range(n):
        if grid[i][j] != '.':
            v = int(grid[i][j]) - 1
            model.addConstr(vars[i,j,v] == 1, 'Fix_' + str(i) + '_' + str(j))
# Each cell must take one value
for i in range(n):
    for j in range(n):
        model.addConstr(quicksum([vars[i,j,v] for v in range(n)]) == 1,
                        'V_' + str(i) + '_' + str(j))
# Each value appears once per row
for i in range(n):
    for v in range(n):
        model.addConstr(quicksum([vars[i,j,v] for j in range(n)]) == 1,
                        'R_' + str(i) + '_' + str(v))
# Each value appears once per column
for j in range(n):
    for v in range(n):
        model.addConstr(quicksum([vars[i,j,v] for i in range(n)]) == 1,
                        'C_' + str(j) + '_' + str(v))
# Each value appears once per subgrid
for v in range(n):
    for i0 in range(s):
```

```
for j0 in range(s):
            subgrid = [vars[i,j,v] for i in range(i0*s, (i0+1)*s)
                                     for j in range(j0*s, (j0+1)*s)]
            model.addConstr(quicksum(subgrid) == 1,
                            'Sub_' + str(i0) + '_' + str(j0) + '_' + str(v))
model.optimize()
model.write('sudoku.lp')
print('')
print('Solution:')
print('')
# Retrieve optimization result
solution = model.getAttr('X', vars)
for i in range(n):
    sol = ''
    for j in range(n):
        for v in range(n):
            if solution[i,j,v] > 0.5:
                sol += str(v+1)
    print(sol)
```

tsp.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Solve a traveling salesman problem on a randomly generated set of
# points using lazy constraints.
                                   The base MIP model only includes
# 'degree-2' constraints, requiring each node to have exactly
# two incident edges. Solutions to this model may contain subtours -
# tours that don't visit every city. The lazy constraint callback
# adds new constraints to cut them off.
import sys
import math
import random
from gurobipy import *
# Callback - use lazy constraints to eliminate sub-tours
def subtourelim(model, where):
    if where == GRB.callback.MIPSOL:
        selected = []
        # make a list of edges selected in the solution
        for i in range(n):
            sol = model.cbGetSolution([model._vars[i,j] for j in range(n)])
            selected += [(i,j) \text{ for } j \text{ in range(n) if sol[j]} > 0.5]
        # find the shortest cycle in the selected edge list
        tour = subtour(selected)
        if len(tour) < n:
            # add a subtour elimination constraint
            expr = 0
            for i in range(len(tour)):
                for j in range(i+1, len(tour)):
                    expr += model._vars[tour[i], tour[j]]
            model.cbLazy(expr <= len(tour)-1)</pre>
# Euclidean distance between two points
def distance(points, i, j):
    dx = points[i][0] - points[j][0]
    dy = points[i][1] - points[j][1]
    return math.sqrt(dx*dx + dy*dy)
```

```
# Given a list of edges, finds the shortest subtour
def subtour(edges):
    visited = [False]*n
    cycles = []
    lengths = []
    selected = [[] for i in range(n)]
    for x,y in edges:
        selected[x].append(y)
    while True:
        current = visited.index(False)
        thiscycle = [current]
        while True:
            visited[current] = True
            neighbors = [x for x in selected[current] if not visited[x]]
            if len(neighbors) == 0:
                break
            current = neighbors[0]
            thiscycle.append(current)
        cycles.append(thiscycle)
        lengths.append(len(thiscycle))
        if sum(lengths) == n:
            break
    return cycles[lengths.index(min(lengths))]
# Parse argument
if len(sys.argv) < 2:</pre>
    print('Usage: tsp.py npoints')
    exit(1)
n = int(sys.argv[1])
# Create n random points
random.seed(1)
points = []
for i in range(n):
    points.append((random.randint(0,100),random.randint(0,100)))
m = Model()
# Create variables
```

```
vars = {}
for i in range(n):
    for j in range(i+1):
        vars[i,j] = m.addVar(obj=distance(points, i, j), vtype=GRB.BINARY,
                             name='e'+str(i)+'_'+str(j))
        vars[j,i] = vars[i,j]
m.update()
# Add degree-2 constraint, and forbid loops
for i in range(n):
    m.addConstr(quicksum(vars[i,j] for j in range(n)) == 2)
    vars[i,i].ub = 0
m.update()
# Optimize model
m._vars = vars
m.params.LazyConstraints = 1
m.optimize(subtourelim)
solution = m.getAttr('x', vars)
selected = [(i,j) for i in range(n) for j in range(n) if solution[i,j] > 0.5]
assert len(subtour(selected)) == n
print('')
print('Optimal tour: %s' % str(subtour(selected)))
print('Optimal cost: %g' % m.objVal)
print('')
```

tune.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# This example reads a model from a file and tunes it.
# It then writes the best parameter settings to a file
# and solves the model using these parameters.
import sys
from gurobipy import *
if len(sys.argv) < 2:</pre>
    print('Usage: tune.py filename')
    quit()
# Read the model
model = read(sys.argv[1])
# Set the TuneResults parameter to 1
model.params.tuneResults = 1
# Tune the model
model.tune()
if model.tuneResultCount > 0:
    # Load the best tuned parameters into the model
    model.getTuneResult(0)
    # Write tuned parameters to a file
    model.write('tune.prm')
    # Solve the model using the tuned parameters
    model.optimize()
```

workforce1.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Assign workers to shifts; each worker may or may not be available on a
# particular day. If the problem cannot be solved, use IIS to find a set of
# conflicting constraints. Note that there may be additional conflicts besides
# what is reported via IIS.
from gurobipy import *
# Number of workers required for each shift
shifts, shiftRequirements = multidict({
  "Mon1": 3,
  "Tue2":
          2,
  "Wed3":
  "Thu4":
  "Fri5":
  "Sat6":
  "Sun7": 5,
  "Mon8":
  "Tue9":
  "Wed10": 3,
  "Thu11": 4,
  "Fri12": 6,
  "Sat13": 7,
  "Sun14": 5 })
# Amount each worker is paid to work one shift
workers, pay = multidict({
  "Amy":
           10,
  "Bob":
           12,
  "Cathy": 10,
  "Dan":
           8,
  "Ed":
           8,
  "Fred":
          9,
  "Gu":
           11 })
# Worker availability
availability = tuplelist([
('Amy', 'Tue2'), ('Amy', 'Wed3'), ('Amy', 'Fri5'), ('Amy', 'Sun7'),
('Amy', 'Tue9'), ('Amy', 'Wed10'), ('Amy', 'Thu11'), ('Amy', 'Fri12'),
('Amy', 'Sat13'), ('Amy', 'Sun14'), ('Bob', 'Mon1'), ('Bob', 'Tue2'),
('Bob', 'Fri5'), ('Bob', 'Sat6'), ('Bob', 'Mon8'), ('Bob', 'Thu11'),
```

```
('Bob', 'Sat13'), ('Cathy', 'Wed3'), ('Cathy', 'Thu4'), ('Cathy', 'Fri5'),
('Cathy', 'Sun7'), ('Cathy', 'Mon8'), ('Cathy', 'Tue9'), ('Cathy', 'Wed10'),
('Cathy', 'Thu11'), ('Cathy', 'Fri12'), ('Cathy', 'Sat13'),
('Cathy', 'Sun14'), ('Dan', 'Tue2'), ('Dan', 'Wed3'), ('Dan', 'Fri5'),
('Dan', 'Sat6'), ('Dan', 'Mon8'), ('Dan', 'Tue9'), ('Dan', 'Wed10'),
('Dan', 'Thu11'), ('Dan', 'Fri12'), ('Dan', 'Sat13'), ('Dan', 'Sun14'),
('Ed', 'Mon1'), ('Ed', 'Tue2'), ('Ed', 'Wed3'), ('Ed', 'Thu4'),
('Ed', 'Fri5'), ('Ed', 'Sun7'), ('Ed', 'Mon8'), ('Ed', 'Tue9'),
('Ed', 'Thu11'), ('Ed', 'Sat13'), ('Ed', 'Sun14'), ('Fred', 'Mon1'),
('Fred', 'Tue2'), ('Fred', 'Wed3'), ('Fred', 'Sat6'), ('Fred', 'Mon8'),
('Fred', 'Tue9'), ('Fred', 'Fri12'), ('Fred', 'Sat13'), ('Fred', 'Sun14'),
('Gu', 'Mon1'), ('Gu', 'Tue2'), ('Gu', 'Wed3'), ('Gu', 'Fri5'),
('Gu', 'Sat6'), ('Gu', 'Sun7'), ('Gu', 'Mon8'), ('Gu', 'Tue9'),
('Gu', 'Wed10'), ('Gu', 'Thu11'), ('Gu', 'Fri12'), ('Gu', 'Sat13'),
('Gu', 'Sun14')
1)
# Model
m = Model("assignment")
# Assignment variables: x[w,s] == 1 if worker w is assigned to shift s.
# Since an assignment model always produces integer solutions, we use
# continuous variables and solve as an LP.
x = \{\}
for w,s in availability:
    x[w,s] = m.addVar(ub=1, obj=pay[w], name=w+"."+s)
# The objective is to minimize the total pay costs
m.modelSense = GRB.MINIMIZE
# Update model to integrate new variables
m.update()
# Constraint: assign exactly shiftRequirements[s] workers to each shift s
reqCts = {}
for s in shifts:
    regCts[s] = m.addConstr(
      quicksum(x[w,s] for w,s in availability.select('*', s)) ==
        shiftRequirements[s], s)
# Optimize
m.optimize()
status = m.status
if status == GRB.status.UNBOUNDED:
    print('The model cannot be solved because it is unbounded')
```

```
exit(0)
if status == GRB.status.OPTIMAL:
    print('The optimal objective is %g' % m.objVal)
    exit(0)
if status != GRB.status.INF_OR_UNBD and status != GRB.status.INFEASIBLE:
    print('Optimization was stopped with status %d' % status)
    exit(0)

# do IIS
print('The model is infeasible; computing IIS')
m.computeIIS()
print('\nThe following constraint(s) cannot be satisfied:')
for c in m.getConstrs():
    if c.IIsConstr:
        print('%s' % c.constrName)
```

workforce2.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Assign workers to shifts; each worker may or may not be available on a
# particular day. If the problem cannot be solved, use IIS iteratively to
# find all conflicting constraints.
from gurobipy import *
# Number of workers required for each shift
shifts, shiftRequirements = multidict({
  "Mon1": 3,
  "Tue2": 2,
  "Wed3": 4,
  "Thu4": 4,
  "Fri5": 5,
  "Sat6":
  "Sun7": 5,
  "Mon8": 2,
  "Tue9": 2,
  "Wed10": 3,
  "Thu11": 4,
  "Fri12": 6,
  "Sat13": 7,
  "Sun14": 5 })
# Amount each worker is paid to work one shift
workers, pay = multidict({
  "Amy":
           10,
  "Bob":
           12,
  "Cathy": 10,
  "Dan":
           8,
  "Ed":
           8,
  "Fred": 9,
  "Gu":
          11 })
# Worker availability
availability = tuplelist([
('Amy', 'Tue2'), ('Amy', 'Wed3'), ('Amy', 'Fri5'), ('Amy', 'Sun7'),
('Amy', 'Tue9'), ('Amy', 'Wed10'), ('Amy', 'Thu11'), ('Amy', 'Fri12'),
('Amy', 'Sat13'), ('Amy', 'Sun14'), ('Bob', 'Mon1'), ('Bob', 'Tue2'),
('Bob', 'Fri5'), ('Bob', 'Sat6'), ('Bob', 'Mon8'), ('Bob', 'Thu11'),
('Bob', 'Sat13'), ('Cathy', 'Wed3'), ('Cathy', 'Thu4'), ('Cathy', 'Fri5'),
```

```
('Cathy', 'Sun7'), ('Cathy', 'Mon8'), ('Cathy', 'Tue9'), ('Cathy', 'Wed10'),
('Cathy', 'Thu11'), ('Cathy', 'Fri12'), ('Cathy', 'Sat13'),
('Cathy', 'Sun14'), ('Dan', 'Tue2'), ('Dan', 'Wed3'), ('Dan', 'Fri5'),
('Dan', 'Sat6'), ('Dan', 'Mon8'), ('Dan', 'Tue9'), ('Dan', 'Wed10'),
('Dan', 'Thu11'), ('Dan', 'Fri12'), ('Dan', 'Sat13'), ('Dan', 'Sun14'),
('Ed', 'Mon1'), ('Ed', 'Tue2'), ('Ed', 'Wed3'), ('Ed', 'Thu4'),
('Ed', 'Fri5'), ('Ed', 'Sun7'), ('Ed', 'Mon8'), ('Ed', 'Tue9'),
('Ed', 'Thu11'), ('Ed', 'Sat13'), ('Ed', 'Sun14'), ('Fred', 'Mon1'),
('Fred', 'Tue2'), ('Fred', 'Wed3'), ('Fred', 'Sat6'), ('Fred', 'Mon8'),
('Fred', 'Tue9'), ('Fred', 'Fri12'), ('Fred', 'Sat13'), ('Fred', 'Sun14'),
('Gu', 'Mon1'), ('Gu', 'Tue2'), ('Gu', 'Wed3'), ('Gu', 'Fri5'),
('Gu', 'Sat6'), ('Gu', 'Sun7'), ('Gu', 'Mon8'), ('Gu', 'Tue9'),
('Gu', 'Wed10'), ('Gu', 'Thu11'), ('Gu', 'Fri12'), ('Gu', 'Sat13'),
('Gu', 'Sun14')
])
# Model
m = Model("assignment")
# Assignment variables: x[w,s] == 1 if worker w is assigned to shift s.
# Since an assignment model always produces integer solutions, we use
# continuous variables and solve as an LP.
x = \{\}
for w,s in availability:
    x[w,s] = m.addVar(ub=1, obj=pay[w], name=w+"."+s)
# The objective is to minimize the total pay costs
m.modelSense = GRB.MINIMIZE
# Update model to integrate new variables
m.update()
# Constraint: assign exactly shiftRequirements[s] workers to each shift s
reqCts = {}
for s in shifts:
    regCts[s] = m.addConstr(
      quicksum(x[w,s] for w,s in availability.select('*', s)) ==
        shiftRequirements[s], s)
# Optimize
m.optimize()
status = m.status
if status == GRB.status.UNBOUNDED:
    print('The model cannot be solved because it is unbounded')
    exit(0)
```

```
if status == GRB.status.OPTIMAL:
    print('The optimal objective is %g' % m.objVal)
    exit(0)
if status != GRB.status.INF_OR_UNBD and status != GRB.status.INFEASIBLE:
    print('Optimization was stopped with status %d' % status)
    exit(0)
# do IIS
print('The model is infeasible; computing IIS')
removed = []
# Loop until we reduce to a model that can be solved
while True:
   m.computeIIS()
    print('\nThe following constraint cannot be satisfied:')
    for c in m.getConstrs():
        if c.IISConstr:
            print('%s' % c.constrName)
            # Remove a single constraint from the model
            removed.append(str(c.constrName))
            m.remove(c)
            break
    print('')
    m.optimize()
    status = m.status
    if status == GRB.status.UNBOUNDED:
        print('The model cannot be solved because it is unbounded')
        exit(0)
    if status == GRB.status.OPTIMAL:
        break
    if status != GRB.status.INF_OR_UNBD and status != GRB.status.INFEASIBLE:
        print('Optimization was stopped with status %d' % status)
        exit(0)
print('\nThe following constraints were removed to get a feasible LP:')
print(removed)
```

workforce3.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Assign workers to shifts; each worker may or may not be available on a
# particular day. If the problem cannot be solved, add slack variables
# to determine which constraints cannot be satisfied, and how much
# they need to be relaxed.
from gurobipy import *
# Number of workers required for each shift
shifts, shiftRequirements = multidict({
  "Mon1": 3,
  "Tue2":
           2,
  "Wed3":
  "Thu4":
  "Fri5":
  "Sat6":
  "Sun7": 5,
  "Mon8":
  "Tue9":
  "Wed10": 3,
  "Thu11": 4,
  "Fri12": 6,
  "Sat13": 7,
  "Sun14": 5 })
# Amount each worker is paid to work one shift
workers, pay = multidict({
  "Amy":
           10,
  "Bob":
           12,
  "Cathy": 10,
  "Dan":
           8,
  "Ed":
           8,
  "Fred":
           9,
  "Gu":
           11 })
# Worker availability
availability = tuplelist([
('Amy', 'Tue2'), ('Amy', 'Wed3'), ('Amy', 'Fri5'), ('Amy', 'Sun7'),
('Amy', 'Tue9'), ('Amy', 'Wed10'), ('Amy', 'Thu11'), ('Amy', 'Fri12'),
('Amy', 'Sat13'), ('Amy', 'Sun14'), ('Bob', 'Mon1'), ('Bob', 'Tue2'),
('Bob', 'Fri5'), ('Bob', 'Sat6'), ('Bob', 'Mon8'), ('Bob', 'Thu11'),
```

```
('Bob', 'Sat13'), ('Cathy', 'Wed3'), ('Cathy', 'Thu4'), ('Cathy', 'Fri5'),
('Cathy', 'Sun7'), ('Cathy', 'Mon8'), ('Cathy', 'Tue9'), ('Cathy', 'Wed10'),
('Cathy', 'Thu11'), ('Cathy', 'Fri12'), ('Cathy', 'Sat13'),
('Cathy', 'Sun14'), ('Dan', 'Tue2'), ('Dan', 'Wed3'), ('Dan', 'Fri5'),
('Dan', 'Sat6'), ('Dan', 'Mon8'), ('Dan', 'Tue9'), ('Dan', 'Wed10'),
('Dan', 'Thu11'), ('Dan', 'Fri12'), ('Dan', 'Sat13'), ('Dan', 'Sun14'),
('Ed', 'Mon1'), ('Ed', 'Tue2'), ('Ed', 'Wed3'), ('Ed', 'Thu4'),
('Ed', 'Fri5'), ('Ed', 'Sun7'), ('Ed', 'Mon8'), ('Ed', 'Tue9'),
('Ed', 'Thu11'), ('Ed', 'Sat13'), ('Ed', 'Sun14'), ('Fred', 'Mon1'),
('Fred', 'Tue2'), ('Fred', 'Wed3'), ('Fred', 'Sat6'), ('Fred', 'Mon8'),
('Fred', 'Tue9'), ('Fred', 'Fri12'), ('Fred', 'Sat13'), ('Fred', 'Sun14'),
('Gu', 'Mon1'), ('Gu', 'Tue2'), ('Gu', 'Wed3'), ('Gu', 'Fri5'),
('Gu', 'Sat6'), ('Gu', 'Sun7'), ('Gu', 'Mon8'), ('Gu', 'Tue9'),
('Gu', 'Wed10'), ('Gu', 'Thu11'), ('Gu', 'Fri12'), ('Gu', 'Sat13'),
('Gu', 'Sun14')
1)
# Model
m = Model("assignment")
# Assignment variables: x[w,s] == 1 if worker w is assigned to shift s.
# Since an assignment model always produces integer solutions, we use
# continuous variables and solve as an LP.
x = \{\}
for w,s in availability:
    x[w,s] = m.addVar(ub=1, obj=pay[w], name=w+"."+s)
# The objective is to minimize the total pay costs
m.modelSense = GRB.MINIMIZE
# Update model to integrate new variables
m.update()
# Constraint: assign exactly shiftRequirements[s] workers to each shift s
reqCts = {}
for s in shifts:
    regCts[s] = m.addConstr(
      quicksum(x[w,s] for w,s in availability.select('*', s)) ==
        shiftRequirements[s], s)
# Optimize
m.optimize()
status = m.status
if status == GRB.status.UNBOUNDED:
    print('The model cannot be solved because it is unbounded')
```

```
exit(0)
if status == GRB.status.OPTIMAL:
    print('The optimal objective is %g' % m.objVal)
if status != GRB.status.INF_OR_UNBD and status != GRB.status.INFEASIBLE:
    print('Optimization was stopped with status %d' % status)
# Add slack variables to make the model feasible
print('The model is infeasible; adding slack variables')
# Set original objective coefficients to zero
m.setObjective(0.0)
# Add a new slack variable to each shift constraint so that the shifts can
# be satisfied
slacks = {}
for s,c in reqCts.items():
    slacks[s] = m.addVar(obj=1.0, name=s+"Slack", column=Column([1], [c]))
# Solve the model with slacks
m.optimize()
status = m.status
if status == GRB.status.INF_OR_UNBD or status == GRB.status.INFEASIBLE \
   or status == GRB.status.UNBOUNDED:
    print('The model with slacks cannot be solved \
           because it is infeasible or unbounded')
    exit(1)
if status != GRB.status.OPTIMAL:
    print('Optimization was stopped with status %d' % status)
    exit(1)
print('\nSlack values:')
for sv in slacks.values():
    if sv.x > 1e-6:
        print(%s = %g% (sv.varName, sv.x))
```

workforce4.py

```
#!/usr/bin/python
# Copyright 2013, Gurobi Optimization, Inc.
# Assign workers to shifts; each worker may or may not be available on a
# particular day. We use lexicographic optimization to solve the model:
# first, we minimize the linear sum of the slacks. Then, we constrain
# the sum of the slacks, and we minimize a quadratic objective that
# tries to balance the workload among the workers.
from gurobipy import *
# Number of workers required for each shift
shifts, shiftRequirements = multidict({
  "Mon1": 3,
  "Tue2":
  "Wed3": 4,
  "Thu4": 4,
  "Fri5": 5,
  "Sat6": 6,
  "Sun7": 5,
  "Mon8": 2,
  "Tue9": 2,
  "Wed10": 3,
  "Thu11": 4,
  "Fri12": 6,
  "Sat13": 7,
  "Sun14": 5 })
# Amount each worker is paid to work one shift
workers, pay = multidict({
  "Amy":
           10,
  "Bob":
           12,
  "Cathy": 10,
  "Dan":
           8,
  "Ed":
           8,
  "Fred": 9,
  "Gu":
          11 })
# Worker availability
availability = tuplelist([
('Amy', 'Tue2'), ('Amy', 'Wed3'), ('Amy', 'Fri5'), ('Amy', 'Sun7'),
('Amy', 'Tue9'), ('Amy', 'Wed10'), ('Amy', 'Thu11'), ('Amy', 'Fri12'),
('Amy', 'Sat13'), ('Amy', 'Sun14'), ('Bob', 'Mon1'), ('Bob', 'Tue2'),
```

```
('Bob', 'Fri5'), ('Bob', 'Sat6'), ('Bob', 'Mon8'), ('Bob', 'Thu11'),
('Bob', 'Sat13'), ('Cathy', 'Wed3'), ('Cathy', 'Thu4'), ('Cathy', 'Fri5'),
('Cathy', 'Sun7'), ('Cathy', 'Mon8'), ('Cathy', 'Tue9'), ('Cathy', 'Wed10'),
('Cathy', 'Thu11'), ('Cathy', 'Fri12'), ('Cathy', 'Sat13'),
('Cathy', 'Sun14'), ('Dan', 'Tue2'), ('Dan', 'Wed3'), ('Dan', 'Fri5'),
('Dan', 'Sat6'), ('Dan', 'Mon8'), ('Dan', 'Tue9'), ('Dan', 'Wed10'),
('Dan', 'Thu11'), ('Dan', 'Fri12'), ('Dan', 'Sat13'), ('Dan', 'Sun14'),
('Ed', 'Mon1'), ('Ed', 'Tue2'), ('Ed', 'Wed3'), ('Ed', 'Thu4'),
('Ed', 'Fri5'), ('Ed', 'Sun7'), ('Ed', 'Mon8'), ('Ed', 'Tue9'),
('Ed', 'Thu11'), ('Ed', 'Sat13'), ('Ed', 'Sun14'), ('Fred', 'Mon1'),
('Fred', 'Tue2'), ('Fred', 'Wed3'), ('Fred', 'Sat6'), ('Fred', 'Mon8'),
('Fred', 'Tue9'), ('Fred', 'Fri12'), ('Fred', 'Sat13'), ('Fred', 'Sun14'),
('Gu', 'Mon1'), ('Gu', 'Tue2'), ('Gu', 'Wed3'), ('Gu', 'Fri5'),
('Gu', 'Sat6'), ('Gu', 'Sun7'), ('Gu', 'Mon8'), ('Gu', 'Tue9'),
('Gu', 'Wed10'), ('Gu', 'Thu11'), ('Gu', 'Fri12'), ('Gu', 'Sat13'),
('Gu', 'Sun14')
])
# Model
m = Model("assignment")
# Assignment variables: x[w,s] == 1 if worker w is assigned to shift s.
# This is no longer a pure assignment model, so we must use binary variables.
x = \{\}
for w,s in availability:
    x[w,s] = m.addVar(vtype=GRB.BINARY, obj=pay[w], name=w+"."+s)
# Slack variables for each shift constraint so that the shifts can
# be satisfied
slacks = {}
for s in shifts:
    slacks[s] = m.addVar(name=s+"Slack")
# Variable to represent the total slack
totSlack = m.addVar(name="totSlack")
# Variables to count the total shifts worked by each worker
totShifts = {}
for w in workers:
    totShifts[w] = m.addVar(name=w+"TotShifts")
# Update model to integrate new variables
m.update()
# Constraint: assign exactly shiftRequirements[s] workers to each shift s,
```

```
# plus the slack
for s in shifts:
   m.addConstr(slacks[s] +
      quicksum(x[w,s] for w,s in availability.select('*', s)) ==
        shiftRequirements[s], s)
# Constraint: set totSlack equal to the total slack
m.addConstr(totSlack == quicksum(slacks[s] for s in shifts), "totSlack")
# Constraint: compute the total number of shifts for each worker
for w in workers:
    m.addConstr(totShifts[w] ==
      quicksum(x[w,s] for w,s in availability.select(w, '*')),
      "totShifts" + w)
# Objective: minimize the total slack
# Note that this replaces the previous 'pay' objective coefficients
m.setObjective(totSlack)
# Optimize
def solveAndPrint():
   m.optimize()
    status = m.status
    if status == GRB.status.INF_OR_UNBD or status == GRB.status.INFEASIBLE \
      or status == GRB.status.UNBOUNDED:
        print('The model cannot be solved because it is infeasible or \
               unbounded')
        exit(1)
    if status != GRB.status.OPTIMAL:
        print('Optimization was stopped with status %d' % status)
        exit(0)
    # Print total slack and the number of shifts worked for each worker
    print('')
    print('Total slack required: %g' % totSlack.x)
    for w in workers:
        print('%s worked %g shifts' % (w, totShifts[w].x))
    print('')
solveAndPrint()
# Constrain the slack by setting its upper and lower bounds
totSlack.ub = totSlack.x
```

```
totSlack.lb = totSlack.x
# Variable to count the average number of shifts worked
avgShifts = m.addVar(name="avgShifts")
# Variables to count the difference from average for each worker;
# note that these variables can take negative values.
diffShifts = {}
for w in workers:
    diffShifts[w] = \
     m.addVar(lb=-GRB.INFINITY, ub=GRB.INFINITY, name=w+"Diff")
# Update model to integrate new variables
m.update()
# Constraint: compute the average number of shifts worked
m.addConstr(len(workers) * avgShifts ==
              quicksum(totShifts[w] for w in workers),
            "avgShifts")
# Constraint: compute the difference from the average number of shifts
for w in workers:
    m.addConstr(diffShifts[w] == totShifts[w] - avgShifts, w + "Diff")
# Objective: minimize the sum of the square of the difference from the
# average number of shifts worked
m.setObjective(quicksum(diffShifts[w]*diffShifts[w] for w in workers))
# Optimize
solveAndPrint()
```

3.7 MATLAB Examples

This section includes source code for all of the Gurobi MATLAB examples. The same source code can be found in the examples/matlab directory of the Gurobi distribution.

diet.m

```
function diet()
% diet Solve the classic diet model
% Copyright 2013, Gurobi Optimization, Inc
% Nutrition guidelines, based on
% USDA Dietary Guidelines for Americans, 2005
% http://www.health.gov/DietaryGuidelines/dga2005/
ncategories = 4;
categories = {'calories'; 'protein'; 'fat'; 'sodium'};
              minNutrition maxNutrition
categorynutrition = [ 1800 2200;
                                   % calories
                           inf;
                                   % protein
                           65;
                                   % fat
                           1779]; % sodium
nfoods = 9;
foods = {'hamburger';
         'chicken';
         'hot dog';
         'fries';
         'macaroni';
         'pizza';
         'salad';
         'milk';
         'ice cream'};
foodcost = [2.49;
                   % hamburger
            2.89; % chicken
            1.50; % hot dog
                   % fries
            1.89;
            2.09; % macaroni
            1.99; % pizza
            2.49; % salad
            0.89; % milk
            1.59]; % ice cream
```

```
% calories protein fat sodium
nutritionValues = [ 410
                                     26 730;
                             24
                                                % hamburger
                    420
                             32
                                     10 1190; % chicken
                    560
                             20
                                     32 1800;
                                                % hot dog
                                                % fries
                    380
                             4
                                     19 270;
                    320
                                     10 930;
                                                % macaroni
                             12
                    320
                             15
                                     12 820;
                                                % pizza
                    320
                             31
                                     12 1230;
                                                % salad
                    100
                             8
                                     2.5 125;
                                                % milk
                                     10 180]; % ice cream
                    330
                             8
nutritionValues = sparse(nutritionValues);
model.modelName = 'diet';
% The variables are layed out as [buy; nutrition]
model.obj
            = [ foodcost;
                                  zeros(ncategories, 1)];
model.lb
            = [ zeros(nfoods, 1); categorynutrition(:, 1)];
model.ub
            = [ inf(nfoods, 1); categorynutrition(:, 2)];
            = [ nutritionValues' -speye(ncategories)];
model.A
model.rhs
          = zeros(ncategories, 1);
model.sense = repmat('=', ncategories, 1);
function printSolution(result)
    if strcmp(result.status, 'OPTIMAL')
                  = result.x(1:nfoods);
        buy
        nutrition = result.x(nfoods+1:nfoods+ncategories);
        fprintf('\nCost: %f\n', result.objval);
        fprintf('\nBuy:\n')
        for f=1:nfoods
            if buy(f) > 0.0001
                fprintf('%10s %g\n', foods{f}, buy(f));
            end
        end
        fprintf('\nNutrition:\n')
        for c=1:ncategories
            fprintf('%10s %g\n', categories{c}, nutrition(c));
        end
    else
        fprintf('No solution\n');
    end
end
% Solve
results = gurobi(model);
printSolution(results);
```

linprog.m

```
function [x, fval, exitflag] = linprog(f, A, b, Aeq, beq, lb, ub)
%LINPROG A linear programming example using the Gurobi MATLAB interface
%
    This example is based on the linprog interface defined in the
    MATLAB Optimization Toolbox. The Optimization Toolbox
%
%
    is a registered trademark of The MathWorks, Inc.
%
%
    x = LINPROG(f,A,b) solves the linear programming problem:
%
%
    minimize
                 f'*x
%
    subject to
                 A*x <= b
%
%
%
    x = LINPROG(f,A,b,Aeq,beq) solves the problem:
%
%
    minimize
                 f'*x
%
                   A*x <= b,
    subject to
%
                 Aeq*x == beq.
%
%
    x = LINPROG(f,A,b,Aeq,beq,lb,ub) solves the problem:
%
%
    minimize
                 f'*x
%
    subject to
                   A*x \le b,
%
                 Aeq*x == beq,
%
                     x \le ub.
           lb <=
%
%
    You can set lb(j) = -inf, if x(j) has no lower bound,
%
    and ub(j) = inf, if x(j) has no upper bound.
%
%
    [x, fval] = LINPROG(f, A, b) returns the objective value
%
    at the solution. That is, fval = f'*x.
%
%
    [x, fval, exitflag] = LINPROG(f, A, b) returns an exitflag
%
    containing the status of the optimization. The values for
%
    exitflag and corresponding status codes are:
%
       1 - OPTIMAL,
%
       O - ITERATION_LIMIT,
%
      -2 - INFEASIBLE,
%
      -3 - UNBOUNDED.
%
if nargin < 3
    error('linprog(f, A, b)')
end
```

```
if nargin > 7
    error('linprog(f, A, b, Aeq, beq, lb, ub)');
end
n = size(A, 2);
model.obj = f;
if nargin < 4
    model.A = A;
    model.rhs = b;
    model.sense = '<';</pre>
else
    model.A = [A; Aeq];
    model.rhs = [b; beq];
    model.sense = [repmat('<', size(A,1), 1); repmat('=', size(Aeq,1), 1)];</pre>
end
if nargin < 6
    model.lb = -inf(n,1);
else
    model.lb = lb;
end
if nargin == 7
   model.ub = ub;
end
params.outputflag = 0;
result = gurobi(model, params);
if strcmp(result.status, 'OPTIMAL')
    exitflag = 1;
elseif strcmp(result.status, 'ITERATION_LIMIT')
    exitflag = 0;
elseif strcmp(result.status, 'INF_OR_UNBD')
    params.dualreductions = 0;
    result = gurobi(model, params);
    if strcmp(result.status, 'INFEASIBLE')
        exitflag = -2;
    elseif strcmp(result.status, 'UNBOUNDED')
        exitflag = -3;
    else
```

```
exitflag = nan;
end

else
    exitflag = nan;
end

if isfield(result, 'x')
    x = result.x;
else
    x = nan(n,1);
end

if isfield(result, 'objval')
    fval = result.objval;
else
    fval = nan;
end
```

lp.m

```
% Copyright 2013, Gurobi Optimization, Inc.
% This example formulates and solves the following simple LP model:
% maximize
%
        x + 2 y + 3 z
% subject to
        x +
                    <= 1
              У
%
              y + z \ll 1
%
clear model;
model.A = sparse([1 1 0; 0 1 1]);
model.obj = [1 2 3];
model.modelsense = 'Max';
model.rhs = [1 1];
model.sense = [ '<' '<'];
result = gurobi(model)
disp(result.objval);
disp(result.x);
\mbox{\ensuremath{\%}} Alterantive representation of A - as sparse triplet matrix
i = [1; 1; 2; 2];
j = [1; 2; 2; 3];
x = [1; 1; 1; 1];
model.A = sparse(i, j, x, 2, 3);
clear params;
params.method = 2;
params.timelimit = 100;
result = gurobi(model, params);
disp(result.objval);
disp(result.x)
```

lp2.m

```
% Copyright 2013, Gurobi Optimization, Inc.
%
% Formulate a simple linear program, solve it, and then solve it
% again using the optimal basis.

clear model;
model.A = sparse([1 3 4; 8 2 3]);
model.obj = [1 2 3];
model.rhs = [4 7];
model.sense = ['>' '>'];

% First solve requires a few simplex iterations
result = gurobi(model)

model.vbasis = result.vbasis;
model.cbasis = result.cbasis;
% Second solve - start from an optimal basis, so no iterations
result = gurobi(model)
```

mip1.m

```
% Copyright 2013, Gurobi Optimization, Inc.
% This example formulates and solves the following simple MIP model:
% maximize
%
         x +
             y + 2z
% subject to
%
        x + 2 y + 3 z <= 4
%
                      >= 1
         x +
               У
% x, y, z binary
names = {'x'; 'y'; 'z'};
try
    clear model;
    model.A = sparse([1 2 3; 1 1 0]);
    model.obj = [1 1 2];
    model.rhs = [4; 1];
    model.sense = '<>';
    model.vtype = 'B';
    model.modelsense = 'max';
    model.varnames = names;
    gurobi_write(model, 'mip1.lp');
    clear params;
    params.outputflag = 0;
    result = gurobi(model, params);
    disp(result)
    for v=1:length(names)
        fprintf('%s %d\n', names\{v\}, result.x(v));
    end
    fprintf('Obj: %e\n', result.objval);
catch gurobiError
    fprintf('Error reported\n');
end
```

qcp.m

```
% Copyright 2013, Gurobi Optimization, Inc.
% This example formulates and solves the following simple QCP model:
% maximize
%
       x
% subject to
       x + y + z = 1
%
%
       x^2 + y^2 \le z^2 (second-order cone)
%
       x^2 \le yz
                        (rotated second-order cone)
clear model
names = {'x', 'y', 'z'};
model.varnames = names;
% Set objective: x
model.obj = [ 1 0 0 ];
model.modelsense = 'max';
% Add constraint: x + y + z = 1
model.A
          = sparse([1 1 1]);
model.rhs = 1;
model.sense = '=';
% Add second-order cone: x^2 + y^2 \le z^2
model.quadcon(1).Qc = sparse([ 1 0 0;
                                0 1 0;
                                0 0 -1]);
model.quadcon(1).q = zeros(3,1);
model.quadcon(1).rhs = 0.0;
% Add rotated cone: x^2 \le yz
model.quadcon(2).Qc = sparse([ 1 0 0;
                                0 \ 0 \ -1;
                                0 0 0]);
model.quadcon(2).q = zeros(3,1);
model.quadcon(2).rhs = 0;
gurobi_write(model, 'qcp.lp');
result = gurobi(model);
for j=1:3
    fprintf('%s %e\n', names{j}, result.x(j))
end
```

fprintf('Obj: %e\n', result.objval);

qp.m

```
% Copyright 2013, Gurobi Optimization, Inc.
% This example formulates and solves the following simple QP model:
% minimize
%
       x^2 + x*y + y^2 + y*z + z^2 + z
% subject to
       x + 2 y + 3 z >= 4
%
%
       x + y
                   >= 1
% It solves it once as a continuous model, and once as an integer
% model.
clear model;
names = {'x', 'y', 'z'};
model.varnames = names;
model.Q = sparse([1 0.5 0; 0.5 1 0.5; 0 0.5 1]);
model.A = sparse([1 2 3; 1 1 0]);
model.obj = [2 0 0];
model.rhs = [4 1];
model.sense = '>';
gurobi_write(model, 'qp.lp');
results = gurobi(model);
for v=1:length(names)
    fprintf('%s %e\n', names{v}, results.x(v));
end
fprintf('Obj: %e\n', results.objval);
model.vtype = 'B';
results = gurobi(model);
for v=1:length(names)
    fprintf('%s %e\n', names{v}, results.x(v));
end
fprintf('Obj: %e\n', results.objval);
```

sos.m

```
% Copyright 2013, Gurobi Optimization, Inc.
% This example creates a very simple Special Ordered Set (SOS)
% model. The model consists of 3 continuous variables, no linear
\% constraints, and a pair of SOS constraints of type 1.
try
    clear model;
    model.ub = [1 1 2];
    model.obj = [2 1 1];
    model.modelsense = 'Max';
    model.A = sparse(1,3);
    model.rhs = 0;
    model.sense = '=';
    % Add first SOS: x1 = 0 or x2 = 0
    model.sos(1).type
    model.sos(1).index = [1 2];
    model.sos(1).weight = [1 2];
    % Add second SOS: x1 = 0 or x3 = 0
    model.sos(2).type
    model.sos(2).index = [1 3];
    model.sos(2).weight = [1 2];
    % Write model to file
    gurobi_write(model, 'sos.lp');
    result = gurobi(model);
    for i=1:3
        fprintf('x%d %e\n', i, result.x(i))
    end
    fprintf('Obj: %e\n', result.objval);
catch gurobiError
    fprintf('Encountered an error\n')
end
```

3.8 R Examples

This section includes source code for all of the Gurobi R examples. The same source code can be found in the examples/R directory of the Gurobi distribution.

lp.R

```
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple LP model:
   maximize
         x + 2 y + 3 z
  subject to
#
         x +
                        <= 1
               У
               y +
                      z \le 1
library("Matrix")
library("gurobi")
model <- list()
                  <- matrix(c(1,1,0,0,1,1), nrow=2, byrow=T)
model$A
model$obj
                  <-c(1,1,2)
model$modelsense <- "max"</pre>
model$rhs
                  <-c(1,1)
                  <- c('<=', '<=')
model$sense
result <- gurobi(model)
print(result$objval)
print(result$x)
# Second option for A - as a sparseMatrix (using the Matrix package)...
model\$A \leftarrow spMatrix(2, 3, c(1, 1, 2, 2), c(1, 2, 2, 3), c(1, 1, 1, 1))
params <- list(Method=2, TimeLimit=100)</pre>
result <- gurobi(model, params)
print(result$objval)
print(result$x)
# Third option for A - as a sparse triplet matrix (using the slam package)...
model$A \leftarrow simple_triplet_matrix(c(1, 1, 2, 2), c(1, 2, 2, 3), c(1, 1, 1, 1))
```

```
params <- list(Method=2, TimeLimit=100)

result <- gurobi(model, params)

print(result$objval)
print(result$x)</pre>
```

lp2.R

```
# Copyright 2013, Gurobi Optimization, Inc.
# Formulate a simple linear program, solve it, and then solve it
# again using the optimal basis.
library("gurobi")
model <- list()</pre>
            <- matrix(c(1,3,4,8,2,3), nrow=2, byrow=T)
model$A
model sobj <- c(1,2,3)
model$rhs <- c(4,7)
model$sense <- c('>=', '>=')
# First solve - requires a few simplex iterations
result <- gurobi(model)</pre>
model$vbasis <- result$vbasis</pre>
model$cbasis <- result$cbasis</pre>
# Second solve - start from optimal basis, so no iterations
result <- gurobi(model)</pre>
```

mip.R

```
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple MIP model:
# maximize
#
             y + 2z
        x +
# subject to
        x + 2 y + 3 z <= 4
#
        x + y >= 1
        x, y, z binary
library("gurobi")
model <- list()</pre>
                <- matrix(c(1,2,3,1,1,0), nrow=2, ncol=3, byrow=T)
model$A
model$obj
                 <-c(1,1,2)
model$modelsense <- "max"</pre>
model$rhs
                <-c(4,1)
                <- c('<=', '>=')
model$sense
                <- 'B'
model$vtype
params <- list(OutputFlag=0)</pre>
result <- gurobi(model, params)</pre>
print('Solution:')
print(result$objval)
print(result$x)
```

qcp.R

```
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple QCP model:
# minimize
#
         x^2 + x*y + y^2 + y*z + z^2
#
 subject to
         x + 2 y + 3z >= 4
#
#
                        >= 1
         x + y
                       t = 0.7071
         [x^2 + y^2 - t^2] < 0 (a second-order cone constraint)
#
library("gurobi")
model <- list()</pre>
model$A
             \leftarrow matrix(c(1,2,3,0,1,1,0,0,0,0,0,1), nrow=3, byrow=T)
             \leftarrow matrix(c(2,1,0,0,1,2,1,0,0,1,2,0,0,0,0,0), nrow=4, byrow=T)
model$Q
model$cones <- list(list(4,1,2))</pre>
            <-c(1,2,3,0)
model$obj
model$rhs
             <- c(4,1,0.717067811)
model$sense <- c('>=', '>=', '=')
result <- gurobi(model)</pre>
print(result$objval)
print(result$x)
```

qp.R

```
# Copyright 2013, Gurobi Optimization, Inc.
# This example formulates and solves the following simple QP model:
# minimize
#
         x^2 + x*y + y^2 + y*z + z^2 + z
# subject to
        x + 2 y + 3z >= 4
#
        x + y >= 1
library("gurobi")
model <- list()</pre>
            <- matrix(c(1,2,3,1,1,0), nrow=2, byrow=T)
model$A
            <- matrix(c(2,1,0,1,2,1,0,1,2), nrow=3, byrow=T)
model$Q
model\$obj <- c(2,0,0)
model$rhs
            <-c(4,1)
model$sense <- c('>=', '>=')
result <- gurobi(model)</pre>
print(result$objval)
print(result$x)
```