

Estimating the Intended Color from the Terms that make up it's Name

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2018-07-10

Abstract


Color names are often made up of multiple words, as a task in natural language understanding we investigate in depth the capacity of neural networks based on sums of word embeddings (SOWE), recurrence (RNN) and convolution (CNN), on their ability to make estimates of colors from sequences of terms. We contrast their performance to direct non-term based methods which form a rough upper-bound by directly using the training data. Surprisingly, the sum of word embeddings generally performs the best, coming close to this upper bound on almost all evaluations. It is trailed slightly by the CNN, and most substantially by the RNN.

To further evaluated the models, and there capacity in this natural language understanding task we consider both the creation of point estimates of color as well as distribution estimates of color. We argue the latter has particular value as there is no clear agreement between people as to what a particular color describes – different people have a different idea of what it means to be “very dark orange”. We find consistent results across the point estimation and distribution estimation tasks.

We investigate 3 different slices of the data, to assess if different properties hold. We define the full task to assess overall performance, full training and testset. We define the ordered task to assess performance when word order may matter, using a subset of the testset with only color descriptions that occur with the same words in different orders. We define the unseen combinations task to assess the ability of the models to make predictions for color names made up of words that have never been seen in that combination during training; restricting the training set to not contain certain combinations and the test-set to only contain those combinations. We find our results to be consistent

across all subtasks. This is particularly interesting as the unordered sum of word embeddings performs best on the ordered evaluation task.

1 Introduction

Color understanding is an important subtask in natural language understanding. It is a challenging domain, due to ambiguity, multiple roles taken by the same words, the many modifiers, and shades of meaning. In many ways it is a grounded microcosm of natural language understanding. Due to its difficulty, texts containing color descriptions such as **the flower has petals that are bright pinkish purple with white stigma** are used as demonstrations for state of the art image generation systems [Reed et al., 2016, Mansimov et al., 2015]. The core focus of the work we present here is addressing these linguistic phenomena around the short-phrase descriptions of the color, in a single patch, as represented in a color-space such as HSV [Smith, 1978]. Issues of illumination and perceived color based on context are considered out of the scope. We evaluated a variety of neural-network based systems, for their capacity to be used for this natural language understanding task. We believe our results are suggestive to the capacity of these systems for other similar tasks involving short token sequences. 

Consider that the word **tan** may mean one of many colors for different people in different circumstances: ranging from the bronze of a tanned sunbather, to the brown of tanned leather; **green** may mean anything from aquamarine to forest green; and even **forest green** may mean the rich shades of a rain-forest, or the near grey of the Australian bush. Thus the color intended cannot be uniquely inferred from the color name. Without further context, it does nevertheless remain possible to estimate likelihoods of which colors are intended based on the population’s use of the words. The primary aim of this work is to map a sequence of color description words to a probability distribution over a color-space. This is required for a proper understanding of color language. We also consider the more basic point estimation of colors, though we question its value.

Proper understanding requires considering *the color intended* as a random variable. In other words, a color name should map to a distribution, not just a single point or region. For a given color name, any number of points in the color-space could be intended, with some being more or less likely than others. Or equivalently, up to interpretation, it may intend a region but the likelihood of what points are covered is variable and uncertain. This distribution is often multimodal and has high and asymmetrical variance, which further renders regression to a single point unsuitable. We do produce results point estimate results for interest, however we argue for any form of precise work the use of such systems is limited. A single point estimate, does not capture the nature of the problem adequately. The mean

of a multimodal distribution (one with two peaks) will lie in the valley between the – a less likely color. Similarly it will be off to the side of the mode, in an asymmetrical distribution. The other problem is that is that a point estimate does not capture the sensitivity. In an asymmetrical distribution, having point slight off-centre in one direction may result in very different probability, this more generally holds for a narrow variance distribution. Conversely for a very wide variance distribution (for example one approaching the uniform distribution) the point estimate value may matter very little with all points providing similar probabilities. Color distributions are always one or more of multimodal or asymmetrical, and feature widely different variances for different names. While by definition the mean color point minimizes the squared error, it may not meaningful actually be a reasonable point estimate. As such, we feel producing a point estimate has limited value. However we do consider the task, as it remains an interesting challenge for assessing the systems under evaluation.

When we estimate a probability distribution over the color-space. To qualify our estimate of the distribution we discretize the space to produce into a histogram. This allows us to take advantage of the well-known softmax based methods for estimating a probability mass distribution using a neural network.

An interesting consideration when considering this discretization is the smoothness of the estimate. The true space is continuous, even if we are discretizing it at resolution as high as the original color displays used to collect the data. Being continuous means that a small change in point the color-space should correspond to a small change in how likely that point is. Or more informally: histograms should look smooth, and not spiky. We investigated using a KDE based method for smoothing the training data, and further we conclude that the neural network based models are learning this smoothness with or without the smoothing of the training data (Results for this are in Appendix B). It is however essential when directly estimating from the training data.

Estimating color probabilities has a clear use as a subsystem in many systems. For example, in a human-interfacing system, when asked to select the **dark bluish green** object, each object can be ranked based on how likely its color is according to the distribution. This way if extra information eliminates the most-likely object, the second most likely object can immediately be determined. Further, if the probability of the color of the object being described by the user input is known, a threshold can be set to report that no object is found, or to ask for additional information. More generally, the distribution based on the color name alone can be used as a prior probability and combined with additional context information to yield better predictions.

1.1 Contributions

Our contributions in this work are (in order of significance)

- Investigation of term-based neural network color estimation models based on:
 - processing inputs per term using Sum of Word Embeddings (SOWE), Convolutional Neural Networks (CNN) and Recurrent Neural Networks (RNN).
 - producing outputs as distributions models using softmax based histograms, and as point estimates using a novel HSV neural network output layer.
 - we conclude that while all these models learn useful outputs, the SOWE and the CNN far out perform the RNN.
- Investigation into the effect of smoothing the distribution training histograms, using a kernel density based (KDE) method; featuring wrapped around effects on the hue channel. We find the interesting conclusion that while smoothing is essential for direct methods of estimation, it has little effect on the machine learning based methods that we investigate.

The investigations include investigating the estimation capacity of the models:

- generally on all color names (full task)
- for color names when the order of the words matters (order task)
- for color names which never occur in the training data exactly, but for which all terms occur in the training data (unseen combinations task)
- for color names with terms that do not occur in the training data at all, but for which we know word embeddings for (embedding only task).

The last investigation is not carried out in depth, but is presented merely as a point of interest. We believe that due to the nature of color understanding as a microcosm of natural language understanding, the results of our investigations have some implications for the capacity of the models for their general use in short phrase understanding.

2 Related Work

The understanding of color names has long been a concern of psycholinguistics and anthropology [Berlin and Kay, 1969, Heider, 1972, Heider and

Olivier, 1972, Mylonas et al., 2015]. It is thus no surprise that there should be a corresponds field of research in natural language processing.

The earliest works revolve around explicit color dictionaries. This includes the ISCC-NBS color system [Kelly et al., 1955] of 26 words, including modifiers, that are composed according to a context free grammar such that phrases are mapped to single points in the color-space; and the simpler, non-compositional, 11 basic colors of Berlin and Kay [1969]. Works including Berk et al. [1982], Conway [1992], ele Lammens [1994], Mojsilovic [2005], Menegaz et al. [2007], Van De Weijer et al. [2009] which propose methods for the automatic mapping of colors to and from these small manually defined sets of colors. We note that Menegaz et al. [2007], Van De Weijer et al. [2009] both propose systems that discretize the color-space, though to a much courser level than we consider in this work.

More recent works, including the work presented here, function with much larger number of colors, larger vocabularies, and larger pools of respondents. In particular making uses of the large Munroe dataset Munroe [2010], as we do here. This allows a data driven approach towards the modelling.

McMahan and Stone [2015] and Meo et al. [2014] present color naming methods, mapping from colors to to their names, the reverse of our task. These works are based on defining fuzzy rectangular distributions in the color-space to cover the distribution estimated from the data, which are used in a Bayesian system to non-compositionally determine the color name. Monroe et al. [2016] maps a point in the color-space, to a sequence of probability estimates over color terms. They extends beyond, all prior color naming systems to produce a compositional color namer based on the Munroe dataset. Their method uses a recurrent neural network (RNN), which takes as input a color-space point, and the previous output word, and gives a probability of the next word to be output – this is a conditional language model. In this work we tackle the inverse problem to the creation of a conditional language model. Our distribution estimation models map from a sequence of terms, to distribution in color space. Similarly, our point estimation models map from sequence of terms to single point in color-space.

Kawakami et al. [2016] propose another compositional color naming model. They use a per-character RNN and a variational autoencoder approach. It is in principle very similar to Monroe et al. [2016], but functioning on a character, rather than a word level. The work by Kawakami et al. also includes a method for generating colors. However they only consider the generation of point estimated, rather than distributions. The primary focus of our work is on generating distributions. The datasets used by Kawakami et al. contain only very small numbers of observations for each color name (often just one). These datasets are thus not suitable for modelling the distribution in color space as interpreted by the population. Further, given the very small number of examples they are not well suited for use with word-

based modelling: the character based modelling employed by Kawakami et al. is much more suitable. As such we do not attempt comparison to their work.

Monroe et al. [2017] presents a neural network solution to a communication game, where a speaker is presented with three colors and asked to describe one of them, and the listener is to work out which is being described. Speaker and listener models are trained, using LSTM-based decoders and encoders respectively. The final time-step of their model produces a 100 dimensional representation of the description provided. From this, a Gaussian distributed score function is calculated, over a high dimensional color-space from Monroe et al. [2016], which is then used to score each of the three options. While this method does work with a probability distribution, as a step in its goal, this distribution is always both symmetric and unimodal – albeit in a high-dimensional color-space.

The generation of color from text has not received a significant amount of attention in prior work. In particular the generation of probability distributions in color space, to our knowledge has not been considered at all. Conversely, there has been several works on the reverse problem: the generation of a textual name for a color from color space point. The work presented here closed that gap.

3 Method

3.1 HSV color-space

We use the HSV color-space [Smith, 1978] through-out this work. We use the format which the data is originally provided in. In this format: hue, saturation and value all range between zero and one. Note that hue is measured in *turns*, rather than the more traditional degrees, or radians. Having hue be measured between zero and one, like the other channels, makes the modelling task more consistent. Were the hue to range between 0 and 2π (radians) or between 0 and 360 (degrees) it would be over-weighted compared to the other channels. This regular space means that errors on all channels can be considered equally. Unlike many other colors spaces (CIELab, Luv etc.) the gamut is square and all values of all channels corresponds to realizable colors.

When working with the hue, all measures need to take into account the wrap-around effect. When ever we refer to mean squared error, mean or mode on the HSV space in this paper, we are referring to the angularly corrected forms given in Section 3.2.

Unlike the RGB color space, the HSV channels do correspond to how humans perceive colors. However, it is not designed to be a perceptually uniform color space across hue (unlike CIELab), which does suggest using squared error for the point estimates is not necessarily finding the perceptual

average of the color color. However, given the other issues outlined above with point estimates that averaging at all is not ideal given the asymmetrical and multimodal nature, such that even a more perceptual average would not solve this. We thus do not judge this a major concern, and focus on it as a modelling task. Point estimates have only limited utility, and we include them as a secondary task for the assessment of the models capacities. There are no such issues for our distribution estimations.

An important advantage of HSV over other color spaces is that it best meets the assumption that for a given color name each channel is statistically independent (see Section 4.1).

3.2 Angularly Correct Calculations on HSV

When performing calculations with the HSV color space it is important to take into account that hue is an angle. As we are working with the color space regularized to range between zero and one for all channels, this means a hue of one and a hue of zero are equivalent (as we measure in turns, in radian's this would be 0 and 2π).

The square error of two hue values is thus calculated as:

$$SE(h_1, h_2) = \min \left((h_1 - h_2)^2, (h_1 - h_2 - 1)^2 \right) \quad (1)$$

This takes into account the error could be calculated clockwise or counter-clockwise. (Note that the -1 term related to using units of turns, were we using radians it would be -2π)

The mean of a set of hues ($\{h_1, \dots, h_N\}$) is calculated as:

$$\bar{h} = \text{atan2} \left(\frac{1}{N} \sum_{i=1}^{i=N} \sin(h_i), \frac{1}{N} \sum_{i=1}^{i=N} \cos(h_i) \right) \quad (2)$$

This gives the mean angle. (Note again: as we measure angle in turns we use the turn trigonometric functions in implementation, though this mean is the same expression or any units).

4 Distribution Estimation

4.1 Conditional Independence Assumption

We make the assumption that given the name of the color, the distribution of the H, S and V channels are independent. That is to say, it is assumed if the color name is known, then knowing the value of one channel would not provide any additional information as to the value of the other two channels. The same assumption is made, though not remarked upon, in Meo et al. [2014] and McMahan and Stone [2015]. This assumption of conditional independence allows considerable saving in computational resources.

Approximating the 3D joint distribution as the product of three 1D distributions decreases the space complexity from $O(n^3)$ to $O(n)$ in the discretized step that follows.

Superficial checks were carried out on the accuracy of this assumption. Spearman’s correlation on the training data suggests that for over three quarters of all color names, there is only weak correlation between the channels for most colors ($Q3 = 0.187$). However, this measure underestimates correlation for values that have circular relative value, such as hue. Of the 16 color-spaces evaluated, HSV had the lowest correlation by a large margin. Full details, including the table of correlations, are available in supplementary materials (Appendix A). These results are suggestive, rather than solidly indicative, on the degree of correctness of the conditional independence assumption. We consider the assumption sufficient for this investigation.

4.2 Discretization

For distribution estimation, our models are trained to output histograms. This is a discretized representation of the continuous distribution. Following standard practice interpolation-based methods can be used to handle it as a continuous distribution. By making use of the conditional independence assumption (see Section 4.1), we output one 256-bin histogram per channel. We note that 24-bit color (as was used in the survey that collected the dataset) can have all information captured by a 256 bin discretization per channel. 24 bit color allows for a total of 2^{24} colors to be represented, and even one-hot encoding for each of the 256 bin discretization channels allows for the same. As such there is no meaningful loss of information when using histograms over a truly continuous estimation method, such as a Gaussian mixture model. Although such models may have other advantages (such as the a priori information added by specifying the distribution), we do not investigate them here, instead considering the simplest non-parametric estimation model (the histogram), which has the simple implementation in a neural network using a softmax output layer.

Discretizing the data in this way is a useful solution used in several other machine learning systems. Oord et al. [2016], van den Oord et al. [2016] apply a similar discretization step and found their method to outperforming the more complex continuous distribution outputs.

For training purposes we thus convert all the observations into histograms. One set of histograms is produced per color description present in the dataset. We perform a uniform weight attribution of points to bins as described by Jones and Lotwick [1984]. In-short, this method of tabulation is to define the bins by their midpoints, and for each point a point then probability mass is allocated the bins with midpoints to each side of the observation in proportion to the distance.

4.3 Perplexity in Color-Space (Evaluation Metric for Distributions)

Perplexity is a measure of how well the distribution, estimated by the model, matches reality according to the observations in the test set. Perplexity is commonly used for evaluating language models. However here it is being used to evaluate the discretized distribution estimate. It can loosely be thought of as to how well the model’s distribution does in terms of the size of an equivalent uniform distribution. Note that this metrics does not assume conditional independence of the color channels.

Here τ is the test-set made up of pairs consisting of a color name t , and color-space point \tilde{x} ; and $p(\tilde{x} | t)$ the output of the evaluated model. Perplexity is defined:

$$PP(\tau) = \exp_2 \left(\frac{-1}{|\tau|} \sum_{\forall (t, (\tilde{x})) \in \tau} \log_2 p(\tilde{x} | t) \right) \quad (3)$$

As the perplexity for a high-resolution discretized model will inherently be very large and difficult to read, we define the standardized perplexity: $\frac{PP(\tau)}{n_{res}}$, where n_{res} is the total number of bins in the discretization scheme. For all the results we present here $n_{res} = 256^3$. This standardized perplexity gives the easily interpretable values *usually* between zero and one. It is equivalent to comparing the relative performance of the model to that of a uniform distribution of the same total resolution. $\frac{PP(\tau)}{n_{res}} = 1$ means the result is equal what we would have to if we had distributed the probability mass uniformly into all bins in a 3D histogram. $\frac{PP(\tau)}{n_{res}} = 0.5$ means the result twice as good as if we were to simply use an uniform distribution: it is equivalent to saying that the correct bin is selected as often as it would be had an uniform distribution with half as many bins (ie larger bins with twice the area) were used. The standardised perplexity is also invariant under different output resolutions. Though for brevity we only present results with 256 bins per channel, our preliminary results for using other resolutions are similar under standardized perplexity.

5 Experimental Setup

5.1 Implementation

The implementation of the all models was in the Julia programming language [Bezanson et al., 2014]. The full implementation is included in the supplementary materials. can be downloaded from the GitHub repository.¹

¹Implementation source is at <https://github.com/oxinabox/ColoringNames.jl>

The machine learning components make heavy use of the `MLDataUtils.jl`² and `TensorFlow.jl`,³ packages. The latter of which we enhanced significantly to allow for this work to be carried out. The discretization and blurring process is done using `KernalDensityEstimation.jl`.⁴

5.2 Evaluations

5.2.1 Full Task

We make use of the Munroe dataset as prepared by McMahan and Stone [2015] from the results of the XKCD color survey. The XKCD color survey [Munroe, 2010], collected over 3.4 million observations from over 222,500 respondents. McMahan and Stone take a subset from Munroe’s full survey, by restricting it to the responses from native English speakers, and removing very rare color names with less than 100 uses. This gives a total of 2,176,417 observations and 829 color names. They also define a standard test, development and train split.

5.2.2 Unseen Combinations Task

A primary interest in using the term based models is to be able to make predictions for never before seen descriptions of colors. For example, based on the learned understanding of `salmon` and of `bright`, from examples like `bright green` and `bright red`, we wish for the systems to make predictions about `bright salmon`, even though that description never occurs in the training data. The ability to make predictions like this shows term-based natural language understanding. It can’t be done with the Operation Upper Bound model, which by-passes the term processing step. To evaluate this generalisation capacity, we define new sub-datasets for both testing and training. We select the rarest 100 color descriptions from the full dataset, with the restriction that every token in a selected description must still have at least 8 uses in other descriptions in the training set. The selected examples include multi-token descriptions such as: `bright yellow green` and also single tokens that occur more commonly as modifiers than as stand-alone descriptions such as `pale`.

The unseen combinations testing set has only observations from the full test set that do use those rare descriptions. We define a corresponding restricted training set made up of the data from the full training set, excluding those corresponding to the rare descriptions. Similar is done for a restricted development set, so as no direct knowledge of the combined terms can leak during early-stopping.

²`MLDataUtils.jl` is available from <https://github.com/JuliaML/MLDataUtils.jl>

³`TensorFlow.jl` is available from <https://github.com/malmaud/TensorFlow.jl>

⁴`KernalDensityEstimation.jl` is available from <https://github.com/JuliaStats/KernelDensity.jl>

By training on the restricted training set and testing on the unseen combinations, we can assess the capacity of the models to make predictions for color descriptions not seen in training. A similar approach was used in Atzmon et al. [2016]. We contrast this to the same models when trained on the full training set to see how much accuracy was lost.

5.2.3 Order Task

It is believed that the order of words in a color description matters, at least to some extent. For example, **greenish brown** and **brownish green** are distinct, if similar, colors. To assess the models on their ability to make predictions when order matters we construct the order testset. This is a subset of the full test set containing only descriptions with terms that occur in multiple different orders. There are 76 such descriptions in the full dataset. Each of which has exactly one alternate ordering. This is unsurprising as while color descriptions may have more than 2 terms, normally one or more of the terms is a joining token such as **ish** or **-**. We only constructed an order testing set, and not a corresponding training set, as this is an evaluation using the model trained on the full training data.

5.3 Common Network Features

Drop-out [Srivastava et al., 2014] is used on all layers, other than the embedding layer, with threshold of 0.5 during training. The network is optimized using Adam [Kingma and Ba, 2014], using a learning rate of 0.001. Early stopping is checked every 10 epochs using the development dataset. Distribution estimation methods are trained using full batch (where each observation is a distribution) for every epoch. Point Estimation trains using randomized mini-batches of size 2^{16} observations (which are each color-space triples). All hidden-layers, except as otherwise precluded (in side the convolution, and in the penultimate layer of the point estimation networks) have the same width 300, as does the embedding layer.

5.3.1 Embeddings

All our neural network based solutions incorporate an embedding layer. This embedding layer maps from tokenized words to vectors. We make use of 300d pretrained FastText embeddings [Bojanowski et al., 2017]⁵.

The embeddings are not trained during the task, but are kept fixed. As per the universal approximation theorem [Leshno et al., 1993, Sonoda and Murata, 2017] the layers above allow for arbitrary non-linear continuous transformation. By fixing the embeddings, and learning this transformation,

⁵Available from <https://fasttext.cc/docs/en/english-vectors.html>

we can produce estimates of colors from their embedding alone, without any training data at all, as shown in Section 6.4.

5.3.2 Tokenization

For all the term based methods, we perform tokenization. During tokenization a color name is split into terms, with consistent spelling. For example, **bluish kahki** would become the sequence of 3 tokens: **[blue, ish, khaki]**. Other than spelling, the tokenization results in the splitting of affixes and combine tokens. Combining tokens and related affixes affect how multiple colors can be combined. The full list of tokenization rules can be found in the accompanying source code. Some further examples showing how combining tokens and affixes are used and tokenized:

- **blue purple** \mapsto **[blue, purple]**.
- **blue-purple** \mapsto **[blue, -, purple]**.
- **bluish purple** \mapsto **[blue, ish, purple]**
- **bluy purple** \mapsto **[blue, y, purple]**
- **blurple** \mapsto **[blue-purple]**

The final example of **blurple** is a special-case. It is the only portmanteau in the dataset, and we do not have a clear way to tokenize it into a series of terms which occur in our pretrained embedding’s vocabulary (see Section 5.3.1). The portmanteau **blurple** is not in common use in any training set used for creating word embeddings, so no pretrained embedding is available. As such we handle it by treating it as the single token **blue-purple** for purposes of finding an embedding. There are many similar hyphenated tokens in the pretrained embeddings vocabulary, however (with that exception) we do not use them as it reduced the sequential modelling task to the point of being uninteresting.

5.4 Input Modules

For each of the models we investigate we define an input module. This is a portion of the over-all network which when is combined with an appropriate output module (see Section 5.5) to perform either point estimation, or distribution estimation.

5.4.1 Recurrent Neural Network(RNN)

A Recurrent Neural Network is a common choice for this kind of task, due to the variable length of the input. The general structure of this network, shown in Figure 1 is similar to Monroe et al. [2016], or indeed to most other

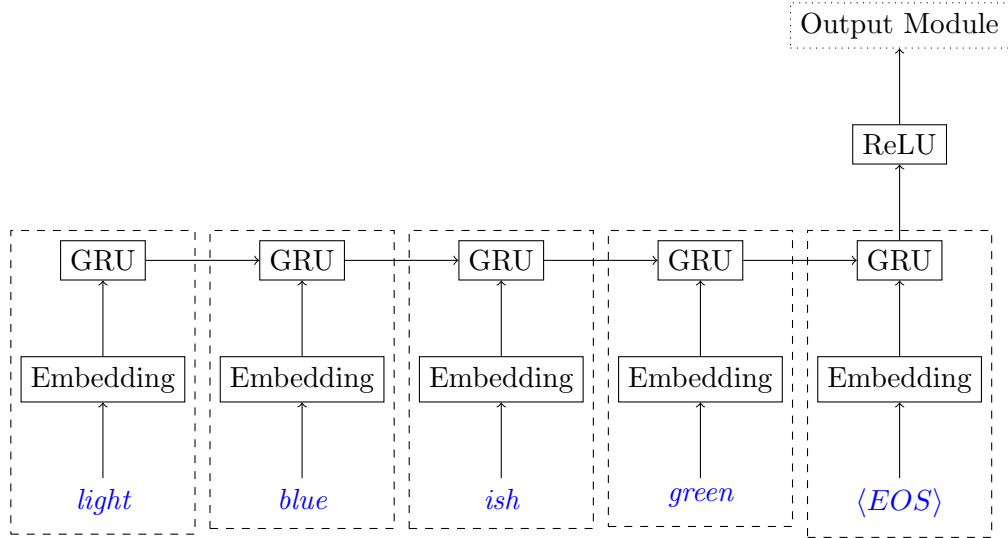


Figure 1: The RNN Input module for the example input **light greenish blue**. Each dashed box represents 1 time-step.

word sequence learning models. Each word is first transformed to an embedding representation. This representation is trained with the rest of the network allowing per word information to be efficiently learned. The embedding is used as the input for a Gated Recurrent Unit (GRU). The stream was terminated with an End of Stream ($\langle \text{EOS} \rangle$) pseudo-token, represented using a zero-vector. The output of the last time-step is fed to a Rectified Linear Unit (ReLU).

We make use of a GRU [Cho et al., 2014], which we found to marginally out-perform the basic RNN in preliminary testing. The small improvement is unsurprising, as the color names have at most 5 terms, so longer short term memory is not required.

5.4.2 Sum of Word Embeddings (SOWE)

Using a simple sum of word embeddings as a layer in a neural network is less typical than an RNN structure. Though it is well established as a useful representation, and has been used as an input to other classifiers such as support vector machines [White et al., 2015, 2018]. Any number of word embeddings can be added to the sum, thus allowing it to handle sequences of any length. However, it has no representation of the order. The structure we used is shown in Figure 2.

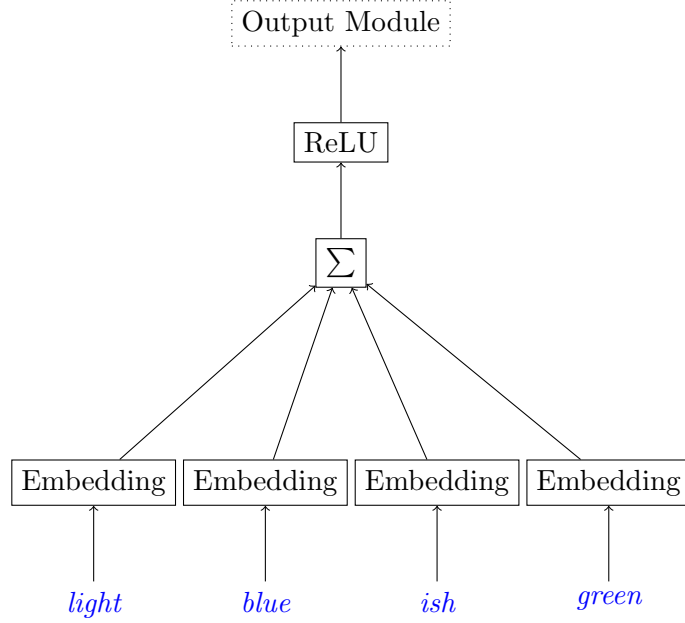


Figure 2: The SOWE input module for the example input `light bluish green`

5.4.3 Convolutional Neural Network(CNN)

A convolutional neural network can be applied to the task by applying 2D convolution over the stacked word embeddings. Figure 3 We use 64 filters of size between one and the length of the longest padded embedding (5).

5.5 Output Modules

On top of the input module we define an output module to suit the neural network for the task for either distribution estimation or point estimation. The input module defines how the terms are composed into the network. The output module defines how the network takes its hidden representation and produces an output.

5.5.1 Distribution Estimation

The distributions are trained to produce the discretized representation as discussed in Section 4.2. Making use of the conditional independence assumption (see Section 4.1), we output the three discretized distributions. This is done using the softmax output layers, as shown in Figure 4 the three output layers. They share a common input, but have separate weights and biases. The loss function is given the sum of the cross-entropy for each of the three softmax outputs.

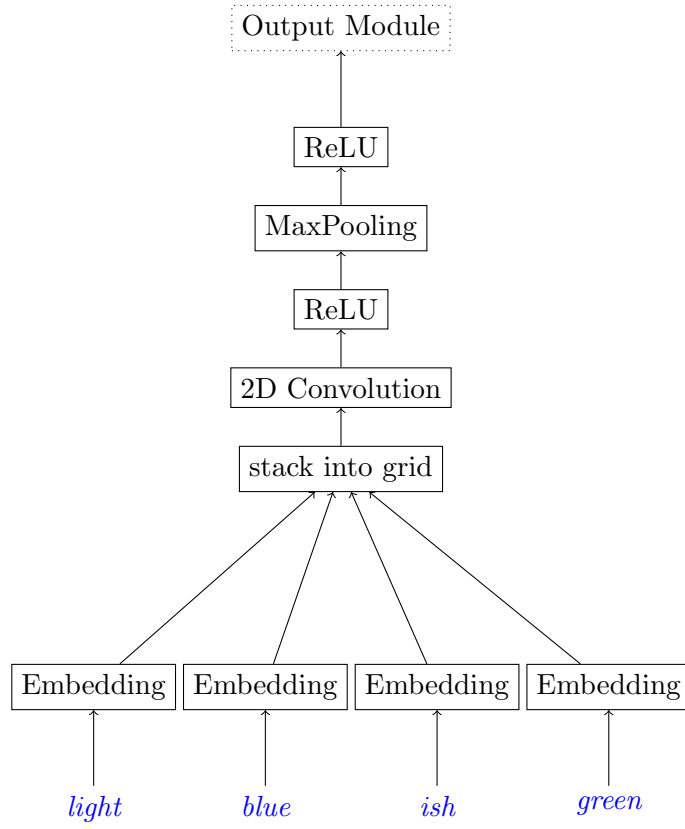


Figure 3: The CNN input module for the example input **light greenish blue**

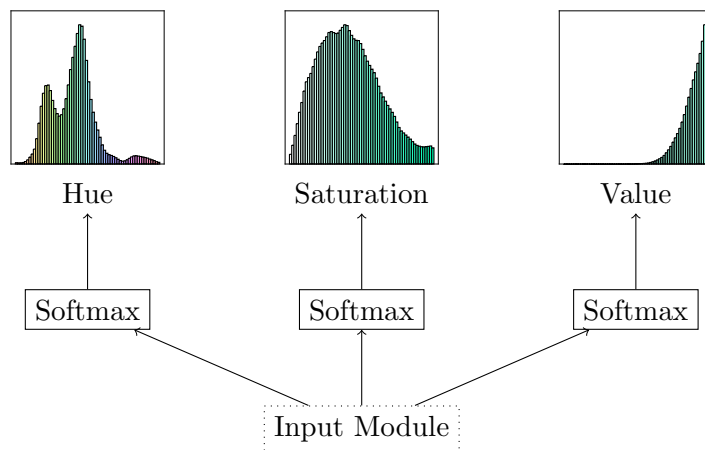


Figure 4: The Distribution Output Module

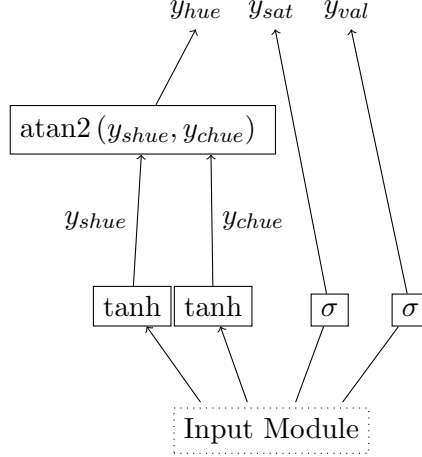


Figure 5: The Point Estimate Output Module. Here atan2 is the quadrant preserving arctangent, outputting as a regularized angle (as per in all evaluations).

5.5.2 Point Estimation

Our point estimation output module is shown in Figure 5. The hidden-layer from the top of the input module is feed to an four single output neurons.⁶ Two of these use the sigmoid activation function (range 0:1) to produce the outputs for the saturation and value channels. The other two use the tanh activation function (range -1:1), they produce the intermediate output that we call y_{shue} and y_{chue} for the sine and cosine of the hue channel respectively. The hue can be found as $y_{hue} = \text{atan2}(y_{shue}, y_{chue})$. We use the intermediate values when calculated the loss function. During training we use the following loss function for each observation y^* , and each corresponding prediction y .

$$\begin{aligned}
 loss = & \frac{1}{2} (\sin(y_{hue}^*) - y_{shue})^2 \\
 & + \frac{1}{2} (\cos(y_{hue}^*) - y_{chue})^2 \\
 & + (y_{sat}^* - y_{sat})^2 \\
 & + (y_{val}^* - y_{val})^2
 \end{aligned} \tag{4}$$

This mean of this loss is taken over all observations in each mini-batch during training. This loss function is continuous and correctly handles the wrap-around nature of the hue channel [White, 2016].

⁶Equivalently these four single neurons can be expressed as a layer with four outputs and two different activation functions.

5.6 Operational Upper-bounds

To establish an rough upper-limit on the modelling results we evaluate a direct method which bypasses the language understanding component of the task. These direct methods do not process term-by-term, they do not work with the language at all. They simply map from the exact input text (no tokenization) to the pre-calculated distribution or mean of the training data for the exact color name. This operational upper bounds bypass the compositional language understanding part of the process. It is as if the input module (as discussed in Section 5.4) perfectly resolved the sequence of terms into a single item.

They represent an approximate upper bound, as they fully exploit all information in the training data for each input. There is no attempting to determine how each term affects the result. We say approximate upper-bound, as it is not strictly impossible that the term-based methods may happen to model the test data better than can be directly determined by training data as processed per exact color name. This would require learning how the terms in the color name combine in a way that exceeds the information directly present in the training data per class. It is this capacity of learning how the terms combine that allow for the models to predict the outputs for combinations of terms that never occur in the training data (Section 5.2.2). Doing this in a way that generalizes to get better results than the direct exploitation of the training data, would require very well calibrated control of (over/under)-fitting.

5.6.1 Operational Upper-bound for Distribution Estimation: KDE

To determine an operational upper-bound for the distribution estimation tasks, we use kernel-density estimation (KDE) in a formulation for non-parametric estimation [Silverman, 1986]. The KDE effectively produces a smoothed histogram. It caused adjacent bins to have most similar probabilities, thus matching to the mathematical notion of a continuous random variable. This is applied on-top of the histogram used for the training data. We use the Fast Fourier Transform (FFT) based KDE method of the Silverman [1982]. We use a Gaussian kernel, and select the bandwidth per color description based on leave-one-out cross validation on the training data. A known issue with the FFT-based KDE method is that it has a wrap-around effect near the boundaries where mass that would be assigned outside the boundaries is instead assigned to the bin on the other side. For the value and saturation channels we follow the standard solution of initially defining additional bins outside the true boundaries, then discard those bins and rescale the probability to one. For the hue channel this wrap-around effect is exactly as desired.

In our evaluations using KDE rather than just the training histograms

directly proved much more successful on all distribution estimation tasks. This is because it avoids empty bins, and effectually interpolates probabilities between observations. Thus improving the results We found in preliminary investigations that using KDE based method to be much better than add-one smoothing.

We also investigated applying the KDE to the training data, before training our term-based neural network based distribution models. Results for this can be found in Appendix B. In brief, we found that smoothing the training data does not significantly effect the result of the neural network based models. As discussed in Section 6.2, this is because the neural networks are able to learn the smoothness relationship of adjacent bins.

Our KDE based operational upper bound for distribution estimation bypassed the natural language understanding part of the task, and directly uses the standard non-parametric probability estimation method to focus solely on modelling the distributions. Matching its performance indicates that a model is effectively succeeding well at both the natural language understanding component and the distribution estimation component.

5.6.2 Operational Upper-bound for Point estimation: Mean-point

In a similar approach, we also a method that directly produces a point estimate from a color name. We define this by taking the mean of all the training observations for a given exact color name. The mean is taken in the angularly correct way (as discussed in Section 3.2). Taking the mean of all the observations give the theoretically optimal solution to minimizing the squared error on the training data set. As with our direct distribution estimation method, this bypasses the term based language understanding, and directly exploits the training data. It thus represents an approximate upper bound on the point estimation performance of the term based models. Though as discussed in Section 1, the notion of mean and of minimizing the square error is not necessarily the correct way to characterize selecting the optimal point estimate for colors. It is however a consistent way to do so, and so we use it for our evaluations.

6 Results

6.1 Qualitative Results

To get an understanding of the problem and how the models are performing on it, we consider some of the outputs of the model for particular cases. For models trained on the full dataset Figure 6 shows examples of distribution estimates, and Figure 7 shows similar examples for point estimates. It can be seen the the model’s outputs using term based estimations are generally similar to the the non-term-based Operational Upper-Bound, as is intended.

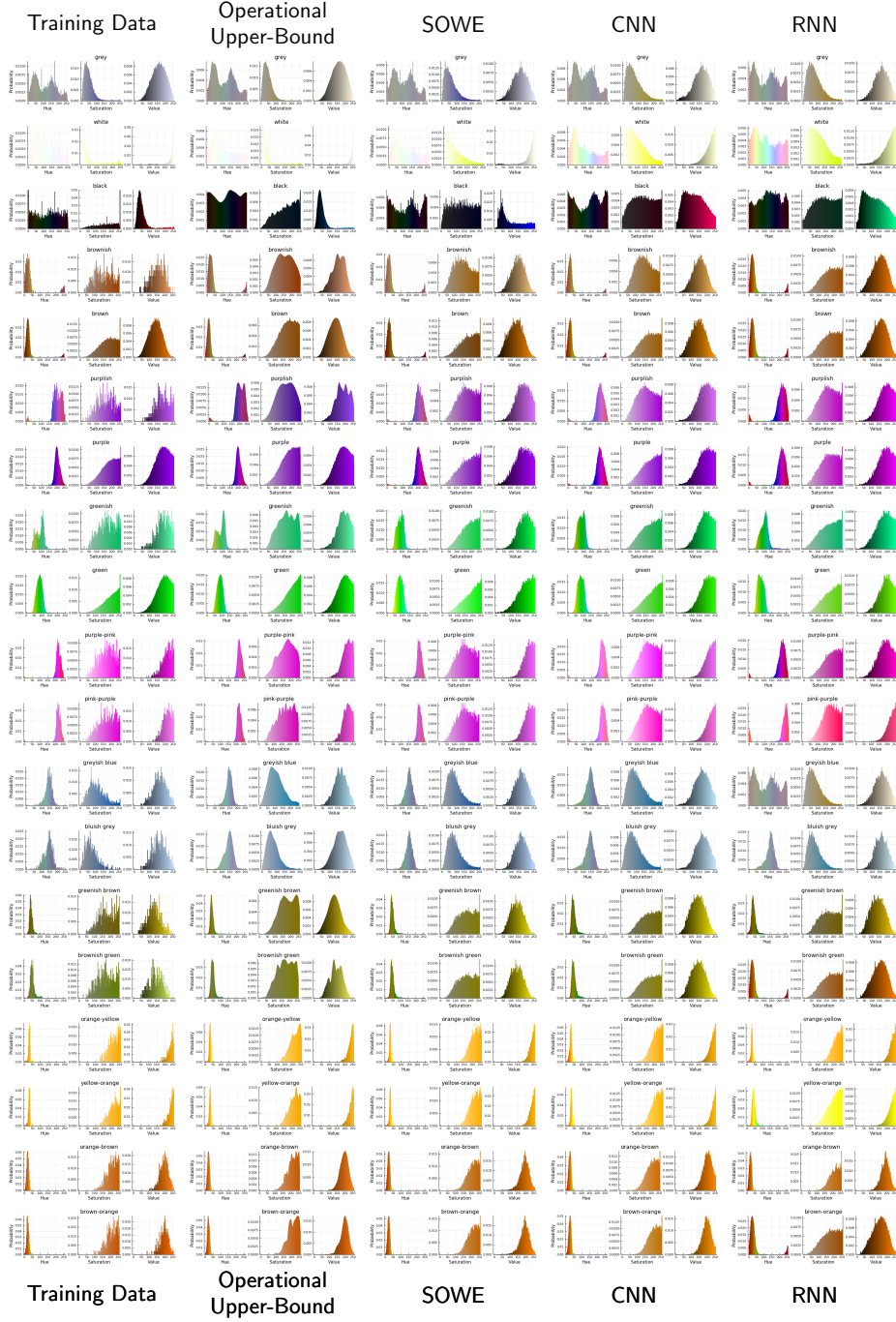


Figure 6: Some examples of the output distribution estimations from the models trained on the full dataset



Figure 7: Some examples of the output point estimates from the models trained on the full dataset

This shows models are correctly fitting to estimate the colors. This aligns with the strong results found in that quantitative evaluations discussed in Section 6.2.

6.1.1 Qualitative results on word-order

The different input modules have different capacity to leverage word-order. This is reflected in in Figure 6 and Figure 7, when considering the pairs of outputs that differ only in word order, such as **purple-pink** and **pink-purple**. The figures presented for the training data and for the Operational Upper-Bound that such color name pairs are subtly different but similar. The SOWE models is unable to take into account word order at all, and so produces identical output all orders. The CNN models produce very similar outputs but not strictly identical – spotting the different requires very close observation. This is in-line with the different filter sizes allowing it to use n-gram features, and it finding the unigram features most useful. The RNN produces the most strikingly different results. It seems the first term dominates the final output: **purple-pink** is more purple, and **pink-purple** is more pink. We can see that the first time is not solely responsible for the final output however, as **purple-pink**, **purple** and **purplish** (tokenized as **purple**, **ish**) are all different. It is surprising that the RNN is dominated by the first term and not the latter terms⁷ this shows the GRU is functioning to remember the earlier inputs. This is happening too strongly however as is causing incorrect outputs.

6.1.2 On smoothness in learned distribution estimates

In Figure 6 can be seen that the term-based distribution estimation models are much smoother than corresponding histograms taken from the the training data. They are not as smooth as the Operational Upper-Bound which explicitly uses KDE. However, they are much smoother than would be expected were the output being being treated independently. Thus it is clear that the models are learning that adjacent bins should have similar output values. This is a common feature of all the training data no matter the color. This learned effect is in line with the fact that color is continuous, and is only being represented here as discrete. We note in relation to this learned smoothness: that while the models capture the highly asymmetrical shapes of most distributions well, they do not do well at capturing small dips. Larger multi-modes as seen in the achromatic colors like **white**, **grey**, **black**, **white**, are captured; but smaller dips such as the hue of **greenish** being most likely to be either side of the green spectrum are largely filled in. In general, it seems clear that additional smoothing of the training data

⁷So much so that we double checked out implementation to be sure it wasn't processing the inputs backwards.

is not required for the neural network based models. This aligned with the results presented in Appendix B.

6.2 Quantitative Results

Overall, we see that our models are able to learn to estimate colors based on sequences of terms. From the consideration of all results Table 4, Table 1, Table 2, Table 5, Table 6, and Table 3. The CNN and SOWE models perform almost as well as the Operational Upper-Bound. With the SOWE having a marginal lead for distribution estimation, and the CNN and SOWE being nearly exactly equal for most point estimation tasks. We believe the reason for this is the SOWE is an easier to learn model from a gradient descent perspective: is very shallow model with only one true hidden layer. The RNN did not perform as well at these tasks. While it is only marginally behind the SOWE and CNN on the full point estimation task (Table 4), on all other tasks for both point estimation and distribution estimation is significantly worse. This may indicate that it is hard to capture the significant relationship between terms in the sequence. However, as will be shown in the examples in the next section it did learn generally acceptable colors.

6.2.1 Ordered Task

The performance of SOWE on the order tasks (Table 2 and Table 5) is surprising. For distribution estimation it outperforms the CNN, and for point estimation ties with the CNN. The CNN (and RNN) can take into account word order, but the SOWE model can not. Its good results suggest that the word-order is not very significant for color names. While word order matters, different colors with the same terms in different order are similar enough that it still performs very well. In theory the models capable of using word order have the capacity to ignore it, and thus could achieve a similar result. An RNN can learn to perform a sum of its inputs (the word embeddings), and the CNN can learn to weight all non-unigram filters to zero. In practice we see that for the RNN in particular this clearly did not occur. This can be attributed to the more complex networks being more challenging to train via gradient descent. It seems color-naming is not a task where word order substantially matters, and thus the simpler SOWE model excels.

6.3 Unseen Combinations of Terms

The SOWE and CNN models are able to generalize well to making estimates for combinations of color terms not seen in training. Table 3 and Table 6 show the results of the model on the testset made up of rare combinations of color names (as described in Section 5.2.2) for the restricted training set

(which does not contain those terms). These results are costed with the same models on this test set when trained on the full training set. The Operation Upper Bound models are unable to produce estimated from the restricted training set as they do not process the color names term-wise. The RNN models continue to perform badly on the unseen combination of terms task for both point and distribution estimation.

For distribution estimation (Table 3) the SOWE results are only marginally worse for the restricted training set as they are for the full training set. The CNN results are worse again, but still are better than the results on the full test-set. The distributions estimated are good on absolute terms getting low perplexity

In the point estimation (Table 6) task the order is flipped with the CNN outperforming the SOWE model. In-fact the CNN actually perform better with the restricted test-set. This may be due to the CNN not fitting to the training data as well as the SOWE, as on the full training set (For this test set) we see the SOWE out performs the CNN. This suggests that the CNN point estimation model may be better capturing the shared information about term usages, at the expense of fitting to the final point. Unlike for distribution estimates the unseen color point estimates are worse than the over all results from the full task (Table 4), though they are still small errors on an absolute scale.

6.3.1 Extracting the mean from the distribution estimates

In the point estimation results discussed so far have been from models trained specifically for point estimation (As described by Section 5.5.2). However, it is also possible to derive the mean from the distribution estimation models. Those results are also presented in Table 4, Table 5 and Table 6. In general these results perform marginally worse (using the MSE metric) than their corresponding modules using the point estimation output module. We note that for the Operational Upper Bounds, the distributions mean is almost identical to the true mean of points, as is expected.

Beyond the output module there are a few key differences between the point estimation modules and the distribution estimate modules. When training distribution estimates all examples of a particular color name is grouped into a single high information training observation using the histogram as the output. Where as point estimates process each example individually, while using minibatches. This means that distribution estimating models fits to all color names with equal priority. Where as for point estimates, more frequently used color names have more examples, and so more frequent color names are fit with priority over rarer ones. Another consequence of using training per example, rather than aggregating is that training via random minibatch is more resistant to local minima. One of the upsides of the aggregated training used in distribution estimation is that it

Method	$\frac{PP}{256^3}$
Operational Upper Bound	0.071
SOWE	0.075
CNN	0.078
RNN	0.089

Table 1: The results for the **full distribution estimation task**. Lower perplexity (PP) is better.

Method	$\frac{PP}{256^3}$
Operational Upper Bound	0.053
SOWE	0.055
CNN	0.057
RNN	0.124

Table 2: The results for the **order distribution estimation task**. Lower perplexity (PP) is better. This is a subset of the full test set containing only tests where the order of the words matters.

trains much faster as only a small number of high-information training examples much be processed, rather than a much larger number of individual observations. It may be interesting in future work to consider training the distribution estimates per example using one-hot output representations; thus making the process similar to that used in the point estimate training. We suspect that such a method may have trouble learning the smoothness of the output space (as discussed in Section 6.1.2).

Method	Full Training Set $\frac{PP}{256^3}$	Restricted Training Set $\frac{PP}{256^3}$
Operational Upper Bound	0.050	—
SOWE	0.050	0.055
CNN	0.052	0.065
RNN	0.117	0.182

Table 3: The results for the **unseen combinations distribution estimation task**. Lower perplexity (PP) is better. This uses the extrapolation subset of the full test set. In the extrapolating results certain rare word combinations were removed from the training and development sets. In the non-extrapolating results the full training and development set was used.

Method	<i>MSE</i>
Operational Upper Bound	0.066
SOWE	0.067
CNN	0.067
RNN	0.071
Distribution Mean Operational Upper Bound	0.066
Distribution Mean SOWE	0.068
Distribution Mean CNN	0.069
Distribution Mean RNN	0.077

Table 4: The results for the **full point estimation task**. Lower mean squared error (MSE) is better.

Method	<i>MSE</i>
Operational Upper Bound	0.065
SOWE	0.066
CNN	0.066
RNN	0.096
Distribution Mean Operational Upper Bound	0.065
Distribution Mean SOWE	0.066
Distribution Mean CNN	0.066
Distribution Mean RNN	0.095

Table 5: The results for the **order point estimation task**. Lower mean squared error (MSE) is better. This is a subset of the full test set containing only tests where the order of the words matters.

Method	Full Training Set <i>MSE</i>	Restricted Training Set <i>MSE</i>
Operational Upper Bound	0.062	–
SOWE	0.065	0.079
CNN	0.072	0.070
RNN	0.138	0.142
Distribution Mean Operational Upper Bound	0.062	–
Distribution Mean SOWE	0.073	0.076
Distribution Mean CNN	0.073	0.084
Distribution Mean RNN	0.105	0.152

Table 6: The results for the **unseen combinations point estimation task**. Lower mean squared error (MSE) is better. This uses the extrapolation subset of the full test set. In the extrapolating results certain rare word combinations were removed from the training and development sets. In the non-extrapolating results the full training and development set was used.

6.4 Completely Unseen Color Estimation From Embedding Only

As an interesting demonstration of how the models function by learning the transformation from the embedding space to the output we briefly consider the outputs for color-names that do not occur in the training data (or testing) at all. This is even more extreme than the unseen combinations task considered in Table 3 and Table 6 where the terms appeared in training, but not the combination of terms. In the examples shown in Figure 8 and Figure 9, the terms never occurred in the training data at all, but our models exploit the fact that they work by transforming the word-embedding space to predict the colors. There is no equivalent for this in the direct models. While **Grey** and **gray** never occur in the training data; **grey** does, and it is near-by in word-embedding space. Similar is true for the other colors that vary by capitalization. We only present a few examples of single term colors here, and no quantitative investigation, as this is merely a matter of interest.

It is particularly interesting to note that all the models make similar estimations for each color. This occurs both for point estimation and for distribution estimation. They do well on the same colors and make similar mistakes on the colors they do poorly at. The saturation of **Gray** is estimated too high, making it appear too blue/purple, this is also true of **grey** though to a much lesser extent. **Purple** and **Green** produce generally reasonable estimates. The hue for **Brown** is estimated as having too much variance, allowing the color to swing into the red or yellowish-green parts of the spectrum. This suggests that in general all models are learning a more generally similar transformation of the space. In general the overall quality of each model seems to be in line with that found in the results for the full tests.

7 Conclusion

We have presented three input modules (SOWE, CNN, RNN), and two output modules (distribution estimate, and point estimate) suitable for using machine learning to make estimates about color based on the terms making up its name. We contrasted these to a practical Operational Upper Bound model for each task which bypassed the term-wise natural language understanding component of the problem. We found the results for SOWE, and CNN were very strong, approaching this upper bound.

A key take away from our results is that using a SOWE should be preferred over an RNN for short phrase natural language understanding tasks when order is not a very significant factor. The RNN is the standard type of model for this task. However, we find its performance to be significantly exceeded by the SOWE and CNN. The SOWE is an unordered model correspondent to a bag of words. The CNN over word embeddings is corre-

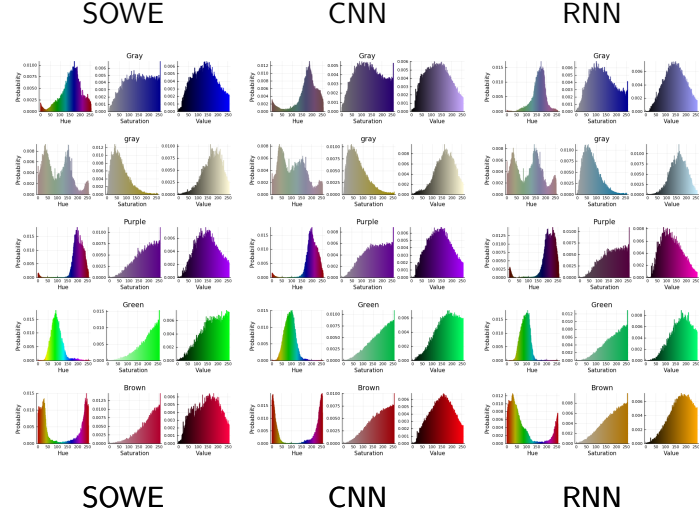


Figure 8: Some example distribution estimations for colors names which are completely outside the training data. The terms: **Brown**, **gray**, **Gray**, **Green**, and **Purple**, do not occur in any of the color data; however **brown**, **grey** **green**, and **purple** do occur.

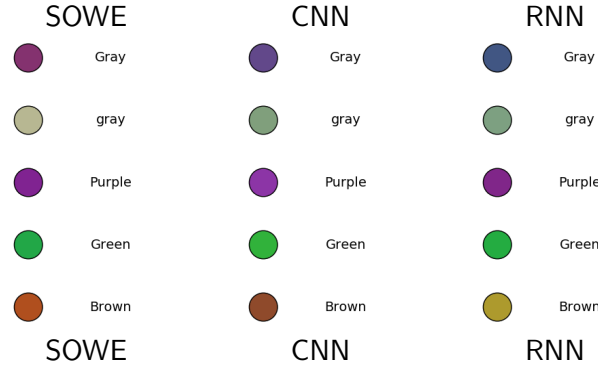


Figure 9: Some example point estimates for colors names which are completely outside the training data. The terms: **Brown**, **gray**, **Gray**, **Green**, and **Purple**, do not occur in any of the color data; however **brown**, **grey** **green**, and **purple** do occur.

spondent to a bag of ngrams, in our case as bag of all 1,2,3,4 and 5-grams. This means the CNN can readily take advantage of both fully ordered information, using the filters of length 5, down to unordered information using the filters of length one. The RNN however must fully process the ordered nature of its inputs, as its output comes only from the final node. It would be interesting to further contrast a bidirectional RNN.

A further interesting avenue for investigation would condition the model not only on the words used but also on the speaker. The original source of the data Munroe [2010], includes some demographic information which is not exploited by any known methods. It is expected that color-term usage may vary with subcultures.

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A On the Conditional Independence of Color Channels given a Color Name

As discussed in the main text, we conducted a superficial investigation into the truth of our assumption that given a color name, the distributions of the hue, value and saturation are statistically independent.

We note that this investigation is, by no means, conclusive though it is suggestive. The investigation focusses around the use of Spearman’s rank correlation. This correlation measures the monotonicity of the relationship between the random variables. A key limitation is that the relationship may exist but be non-monotonic. This is almost certainly true for any relationship involving channels, such as hue, which wrap around. In the case of such relationships Spearman’s correlation will underestimate the true strength of the relationship. Thus, this test is of limited use in proving the conditional independence. However, it is a quick test to perform and does suggest that the conditional independence assumption may not be so incorrect as one might assume.

For the Monroe Color Dataset training data given by $V \subset \mathbb{R}^3 \times T$, where \mathbb{R}^3 is the value in the color-space under consideration, and T is the natural language space. The subset of the training data for the description $t \in T$ is given by $V_t = \{(\tilde{v}_i, t_i) \in V \mid t_i = t\}$. Further let $T_V = \{t_i \mid (\tilde{v}, t_i) \in V\}$ be the set of color names used in the training set. Let $V_{\alpha|t}$ be the α channel component of V_t , i.e. $V_{\alpha|t} = \{v_\alpha \mid ((v_1, v_2, v_3), t) \in V_t\}$.

The set of absolute Spearman’s rank correlations between channels a and b for each color name is given by $S_{ab} = \{|\rho(V_{a|t}, V_{b|t})| \mid t \in T_V\}$.

Color-Space	$Q3(S_{12})$	$Q3(S_{13})$	$Q3(S_{23})$	max
HSV	0.1861	0.1867	0.1628	0.1867
HSL	0.1655	0.2147	0.3113	0.3113
YCbCr	0.4005	0.4393	0.3377	0.4393
YIQ	0.4088	0.4975	0.4064	0.4975
LCHab	0.5258	0.411	0.3688	0.5258
DIN99d	0.5442	0.4426	0.4803	0.5442
DIN99	0.5449	0.4931	0.5235	0.5449
DIN99o	0.5608	0.4082	0.5211	0.5608
RGB	0.603	0.4472	0.5656	0.603
Luv	0.5598	0.6112	0.4379	0.6112
LCHuv	0.6124	0.4072	0.3416	0.6124
HSI	0.2446	0.2391	0.6302	0.6302
CIELab	0.573	0.4597	0.639	0.639
xyY	0.723	0.5024	0.4165	0.723
LMS	0.968	0.7458	0.779	0.968
XYZ	0.9726	0.8167	0.7844	0.9726

Table 7: The third quartile for the pairwise Spearman’s correlation of the color channels given the color name.

We consider the third quartile of that correlation as the indicative statistic in Table 7. That is to say for 75% of all color names, for the given color-space, the correlation is less than this value.

Of the 16 color-spaces considered, it can be seen that the HSV exhibits the strongest signs of conditional independence – under this (mildly flawed) metric. More properly put, it exhibits the weakest signs of non-independence. This includes being significantly less correlated than other spaces featuring circular channels such as HSL and HSI.

Our overall work makes the conditional independence assumption, much like n-gram language models making Markov assumption. The success of the main work indicates that the assumption does not cause substantial issues.

B KDE based smoothing of Training Data

It can be seen that smoothing has very little effect on the performance of any of the neural network based distribution estimation models. All 3 term based models (SOWE, CNN, RNN) all perform very similarly whether or not the training data is smoothed. This is seen consistently in all the distribution estimation tasks (Table 1, Table 2, Table 3). Conversely, the direct method which bypasses learning the functioning of terms is very substantially effected by the smoothing. This is because without smoothing it results in estimating the probability based on bins unfilled by any observation (Which

is zero due to the cap on the minimum value. See Section 5.6.1). This is particularly notable in the case of the direct, (unsmoothed) non-extrapolating result reported in Table 3. As these were some of the rarest terms in the training set, they were thus more likely to not coincide with any terms from the testing set. Conversely, on this dataset the term models do quite well, with or without smoothing. The SOWE model out out even performs the the Direct method. As the network can effectively learn the smoothness, not just from the observations of one color but from all of the observations. It learns that increasing the value of one bin should increase adjacent ones. As such it does not need the smoothing applied to the training data.