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RSA Algorithm

Generate the keys-code1

Step 1: Generate the RSA modulus (N)

We need to two generate numbers, then we need to create the prime numbers for this process. They are method of creating prime numbers:

- Miller-Rabin code (Library)
- Fermat code (Library)

The initial procedure begins with selection of two prime numbers namely p and q , and then calculating their product N :

$$N = p * q$$

Step 2: Derived Number (e)

Consider number e as a derived number which should be greater than 1 and less than multiplication of $(p-1)$ and $(q-1)$.

$$1 < e < (p-1) * (q-1)$$

Step 3: Public Key (e)

Choose "e" and e must be prime. We can try to use prime numbers test again.

Step 4: Private Key (d)

Private Key d is calculated from the numbers p , q and e . The mathematical relationship between the numbers is as follows:

$$d * e = 1 \bmod (n)$$

- Extended Euclidean Algorithm (Library)

Encryption-code2

We need to plaint text and we create the new plain text by using ASCII.

- ASCII code (Library)

Every letter in original text converted by using ASCII and we define the "P". By the way, P means that plain text and C means that cipher text.

$$C = P^e \text{mod}((p-1) * (q-1))$$

Decryption-code3

Considering receiver C has the private key d, the result modulus will be calculated as:

$$P = C^d \bmod ((p-1) * (q-1))$$

Basic RSA attacks-code4 and code 5

- If chooses the small "e"

$$P < N^{1/e}$$

We can just take the e-th root and reach the plain text.

- If secret messages send to many receivers by using same e and different d. These encrypted by Chinese Remainder Thm.(Library)