

1. 要将函数 $f(x_1, x_2) = 6x_1^2 - 6x_1x_2 + 2x_2^2 - x_1 - 2x_2$ 转换为 $f = B^T X + \frac{1}{2} X^T A X$ 的形式
其中其中 $X = [x_1 x_2]^T$ 且 A 要对角化。还要画出 A 的等高线图像, 在这个基础上还有 SQP 考察
2. 泰勒展开, P17 这个是一元是, 最好把二元的也学习一下

FIGURE 1.12

Concept of derivative.

In most optimization problems, which are generally nonlinear, $f'(x)$ has to be evaluated numerically. We can use *forward difference*, *backward difference*, and *central difference* methods to find the derivative of a function at a point. If the value of a function $f(x)$ is known at a point x , then the value of the function at its neighboring point $x + \Delta x$ can be computed using *Taylor's series* as

$$f(x + \Delta x) = f(x) + \Delta x f'(x) + \frac{\Delta x^2}{2!} f''(x) + \frac{\Delta x^3}{3!} f'''(x) + \dots \quad (1.36)$$

Rearranging Equation 1.36 gives

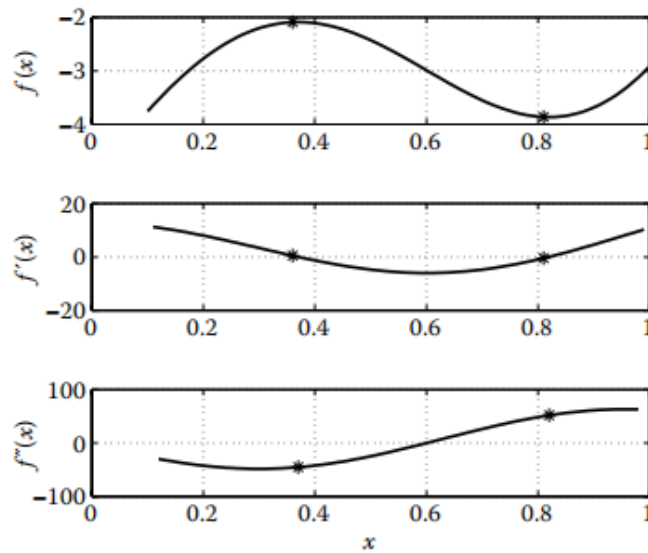
$$\frac{f(x + \Delta x) - f(x)}{\Delta x} = f'(x) + \frac{\Delta x}{2!} f''(x) + \frac{\Delta x^2}{3!} f'''(x) + \dots \quad (1.37)$$

The *forward difference* formula for evaluating the derivative of a function can be written as

$$f'(x) = \frac{f(x + \Delta x) - f(x)}{\Delta x} + O(\Delta x) \quad (1.38)$$

The quantity $O(\Delta x)$ represents that this formula is first-order accurate. In a similar fashion, the *backward difference* formula can be written as

$$f'(x) = \frac{f(x) - f(x - \Delta x)}{\Delta x} + O(\Delta x) \quad (1.39)$$



4.HESSION矩阵, 雅可比矩阵P19-21 P22的例子 P24,25

20. Find the directional derivative of the function

$$f(x) = x_1^2 x_2 + x_2^2 x_3 - x_1 x_2 x_3^2$$

5.

at $(1, 1, -1)$ in the direction $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$.

5.bisection P39

6.牛顿法P42 考P65

7.Cubic P44 2.3.4

8. 遗传算法和PSOP159

9. 加权和法Algorithms-for-optimization第12章内容, 加权最小-最大法

10. 高斯分布Algorithms-for-optimization 第15章内容15.1 15.3