

Create a project named Set that illustrates the use of generic classes and generic methods.

Implementing a Generic Set Class

DEFINITION 1. **Generics** is a way of defining classes, interfaces and methods by using type parameters to represent types. A more technical term for generics is **parametric polymorphism**. A generic method, interface or class is fully specified at run time. In Java, a generic type can only be specialized using an object type. Every primitive type in Java has an associated object type (a wrapper class).

DEFINITION 2. A **set** is a finite or infinite collection of objects in which order has no significance, and multiplicity is generally also ignored. Members of a set are often referred to as elements and the notation $x \in A$ is used to denote that x is an element of a set A . A set is usually denoted as a list of elements. For example, $\{2, 3, 4, 5, 6\}$ is a set that contains five elements.

In today's lab, you will implement a generic class, the **Set<T>** class. The class will be generic but its methods will not be generic. Some methods will use the formal type parameter of the class. In this lab, we introduce a basic software engineering concept called *composition* - one object is composed of another. A set is composed of a list. We will use the Java API `ArrayList<T>`, also a generic class, to implement the `Set<T>` class.

Basic Set Operations

DEFINITION 3. The **cardinality** of a set is the number of elements that the set contains. For example, the cardinality of $A = \{2, 3, 4, 5, 6\}$, denoted $|A|$ is 5.

DEFINITION 4. The **intersection** of two sets A and B is the set of elements common to A and B . This is written $A \cap B$, and is pronounced "intersection" or "cap."

DEFINITION 5. The **union** of two sets A and B is the set obtained by combining the members of each without allowing multiplicity. This is written $A \cup B$, and is pronounced "union" or "cup."

DEFINITION 6. The **difference** of sets A and B , denoted $A - B$, is the set of elements belonging to set A but not B .

DEFINITION 7. Sets A and B are **equal**, denoted $A = B$, when both sets have the same elements. The way in which the elements are ordered does not matter.

DEFINITION 8. A set A is a **subset** of set B , denoted $A \subseteq B$, if every element of set A is also an element of set B .

DEFINITION 9. A set A is a **proper subset** of set B , denoted $A \subset B$ or $A \subsetneq B$, if every element of set A is also an element of set B but both sets A and B are not equal.

Some Useful Java ArrayList API Methods

1. `ArrayList<ObjectType> listName = new ArrayList();` creates an empty array list, *listName*, that can store objects of the specified type.
2. `listName.add(item);` appends the specified *item* to the (back of) the list.
3. `listName.get(index);` returns the item in the array list with the specified index. Array lists use zero-based indexing.
4. `listName.size();` returns the current length, number of items, in the specified array list.
5. `listName.isEmpty();` returns true if the length of *listName* is 0 and, false, otherwise.
6. `listName.contains(item);` returns true if the array list contains the specified *item* and, false, otherwise.

This project will have the following two classes:

```
public class Set<T>
```

Complete the implementation of the `Set<T>` class provided in the starter code by implementing the methods `union`, `diff`, `equals`, `subset`, and `properSubset`.

```
public class SetDemo
```

Complete the implementation of the `SetDemo` class provided in the starter code by implementing the generic methods `setOperationsDemo` and `getMax`. Implement the method `setOperationsDemo` so that it produces exactly the output shown below. In the output, `u` means union, `n` means intersection, and the minus sign means difference. The method `getMax` finds and returns the maximum element in the set.

Output

$s1 = \{4, 2, 5, 1, 3\}$
 $s2 = \{7, 3, 2, 9, 5\}$
 $s3 = \{5, 8, 3, 2, 4\}$
 $(s1 - s2) \cup (s2 - s1) = \{4, 1, 7, 9\}$ ✓
 $(s1 \cup s2) - (s1 \cap s2) = \{4, 1, 7, 9\}$ ✓
Is $(s1 - s2) \cap (s2 - s1)$ empty? true
Are $s1 \cap (s2 \cup s3)$ and $(s1 \cap s2) \cup (s1 \cap s3)$ equal? true ✓
Are $(s1 \cap s2) \cup (s2 \cap s3)$ and $(s1 \cup s3)$ equal? false ✓
Is $(s1 - s2)$ a subset of $s2$? false
Is $(s1 - s2) \cup (s2 \cap s3)$ a subset of $s1$? true
Is $(s1 - s2) \cup (s2 \cap s3)$ a proper subset of $s1$? false
Max element in $s1 = 5$
Max element in $s2 = 9$
Max element in $s3 = 8$

$s1 = \{D, B, A, E, C\}$
 $s2 = \{G, I, C, B, E\}$
 $s3 = \{F, C, H, B, D\}$
 $(s1 - s2) \cup (s2 - s1) = \{D, A, G, I\}$
 $(s1 \cup s2) - (s1 \cap s2) = \{D, A, G, I\}$
Is $(s1 - s2) \cap (s2 - s1)$ empty? true
Are $s1 \cap (s2 \cup s3)$ and $(s1 \cap s2) \cup (s1 \cap s3)$ equal? true
Are $(s1 \cap s2) \cup (s2 \cap s3)$ and $(s1 \cup s3)$ equal? false
Is $(s1 - s2)$ a subset of $s2$? false
Is $(s1 - s2) \cup (s2 \cap s3)$ a subset of $s1$? true
Is $(s1 - s2) \cup (s2 \cap s3)$ a proper subset of $s1$? true
Max element in $s1 = E$
Max element in $s2 = I$
Max element in $s3 = H$

$s1 = \{Gina, Bob, Jim, Anna, Mary\}$
 $s2 = \{Tom, Hal, Mary, Bob, Anna\}$
 $s3 = \{Hal, Mary, Bob, Sara, Gina\}$
 $(s1 - s2) \cup (s2 - s1) = \{Gina, Jim, Tom, Hal\}$
 $(s1 \cup s2) - (s1 \cap s2) = \{Gina, Jim, Tom, Hal\}$
Is $(s1 - s2) \cap (s2 - s1)$ empty? true
Are $s1 \cap (s2 \cup s3)$ and $(s1 \cap s2) \cup (s1 \cap s3)$ equal? true
Are $(s1 \cap s2) \cup (s2 \cap s3)$ and $(s1 \cup s3)$ equal? false
Is $(s1 - s2)$ a subset of $s2$? false
Is $(s1 - s2) \cup (s2 \cap s3)$ a subset of $s1$? false
Is $(s1 - s2) \cup (s2 \cap s3)$ a proper subset of $s1$? false
Max element in $s1 = Mary$
Max element in $s2 = Tom$
Max element in $s3 = Sara$