

utdallas.edu/~kjp

↳ Teaching

Grading Policy:

Exam I: → 30%

Exam II: → 30%

Exam III: → 30%

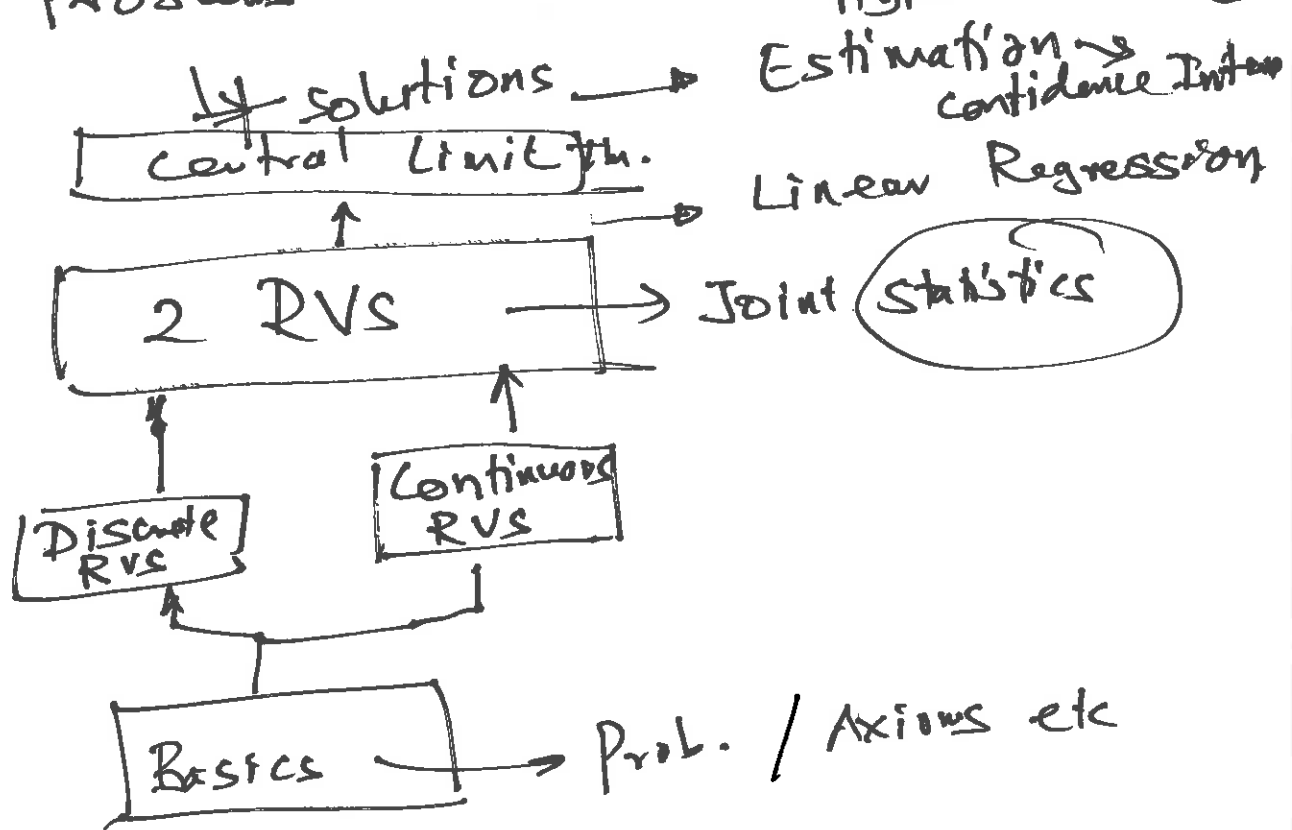
Quizzes → 10% →

80 → A-

65 → B-

50 → C-

HW Problems will be posted. Hypothesis Testing



Set Theory

Elements, ✓ Sets ✓



Universal Set U → Set Space → S

Set of all elements in the problem

↓ varies from problem to problem

Null Set → ϕ → no elements in it

Empty Set → N

A, B, C → Sets

↓
By → students major in EE
" in the 1st row.

Subset

B is a subset of A

(3)

All elements of B are also elements of A

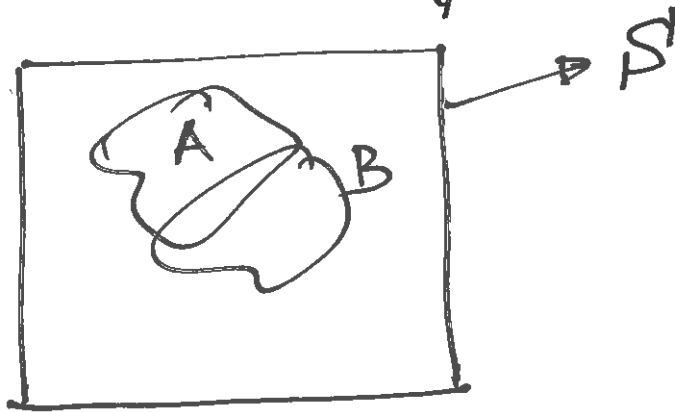
Notⁿ: $B \subset A$

$A \subset S$

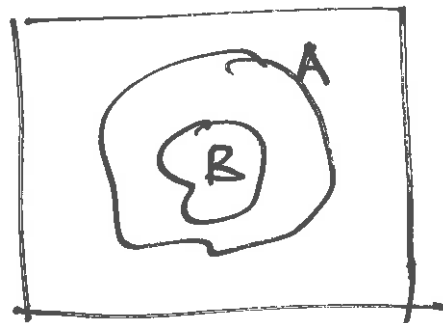
$\phi \subset A$

Graphical Representation

Venn Diagram

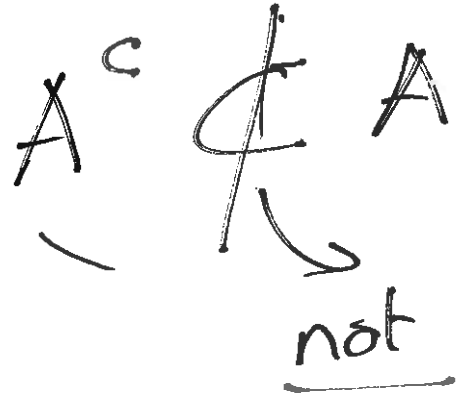
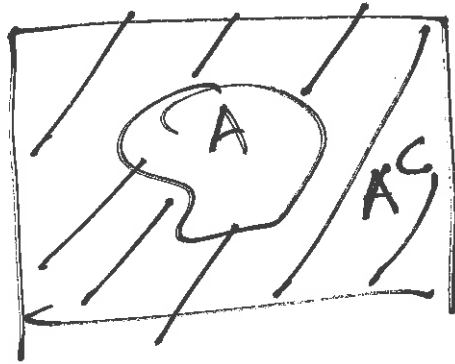


If $B \subset A$



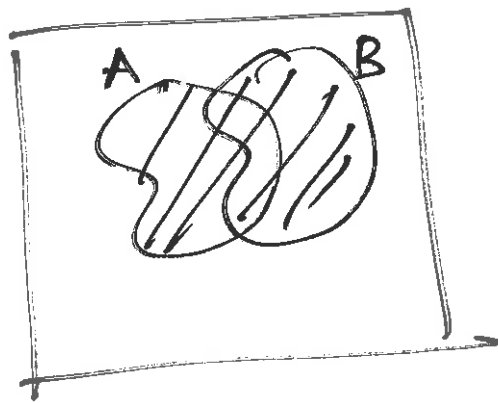
Complement of $A \rightarrow A^c$ (\bar{A}) ④

↳ Set of all elements excluding those of A



Union of $A \cup B$

Set of all elements of A , ^{and} elements of B including those common to $A \cup B$.

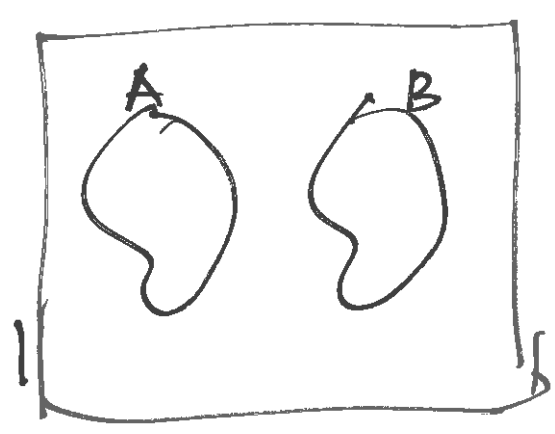
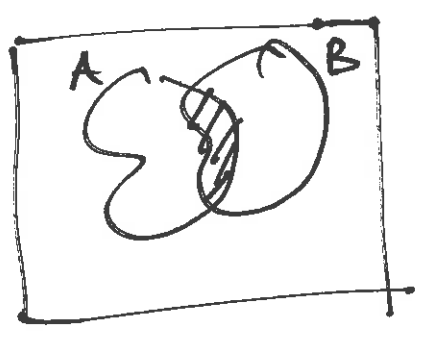


Notⁿ: $A \cup B$
 \downarrow
 $[A + B]$

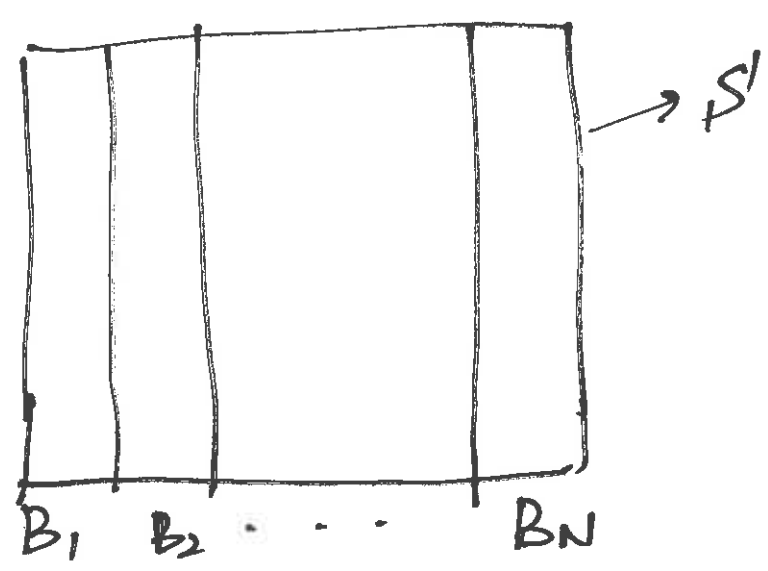
Intersection of A & B
Set of elements

common to both
A & B

$A \cap B$
or
 AB



$AB = \emptyset$
A & B are
Disjoint



$B_i \cap B_j = \emptyset$
 B_i s are disjoint

$$B_1 + B_2 + \dots + B_N = S$$
$$\bigcup_{i=1}^N B_i = S$$

eg:- $A = \{1, 3, 5, 6, 8, 10\}$ ⑥

$$B = \{2, 3, 7, 8, 12, 14\}$$

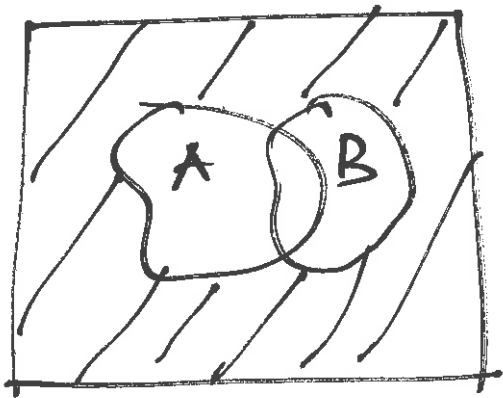
$$(A+B) = \{1, 2, 3, 5, 6, 7, 8, 10, 12, 14\}$$

$$AB = \{3, 8\}$$

$$A^C = \text{Not enough information.}$$

De Morgan's Thm

1. $(A+B)^C = A^C B^C \rightarrow$ Complement of a union is equal to the intersection of the complements



2. $(AB)^C = A^C + B^C \rightarrow$ Complement of the intersection is the union of the complements.

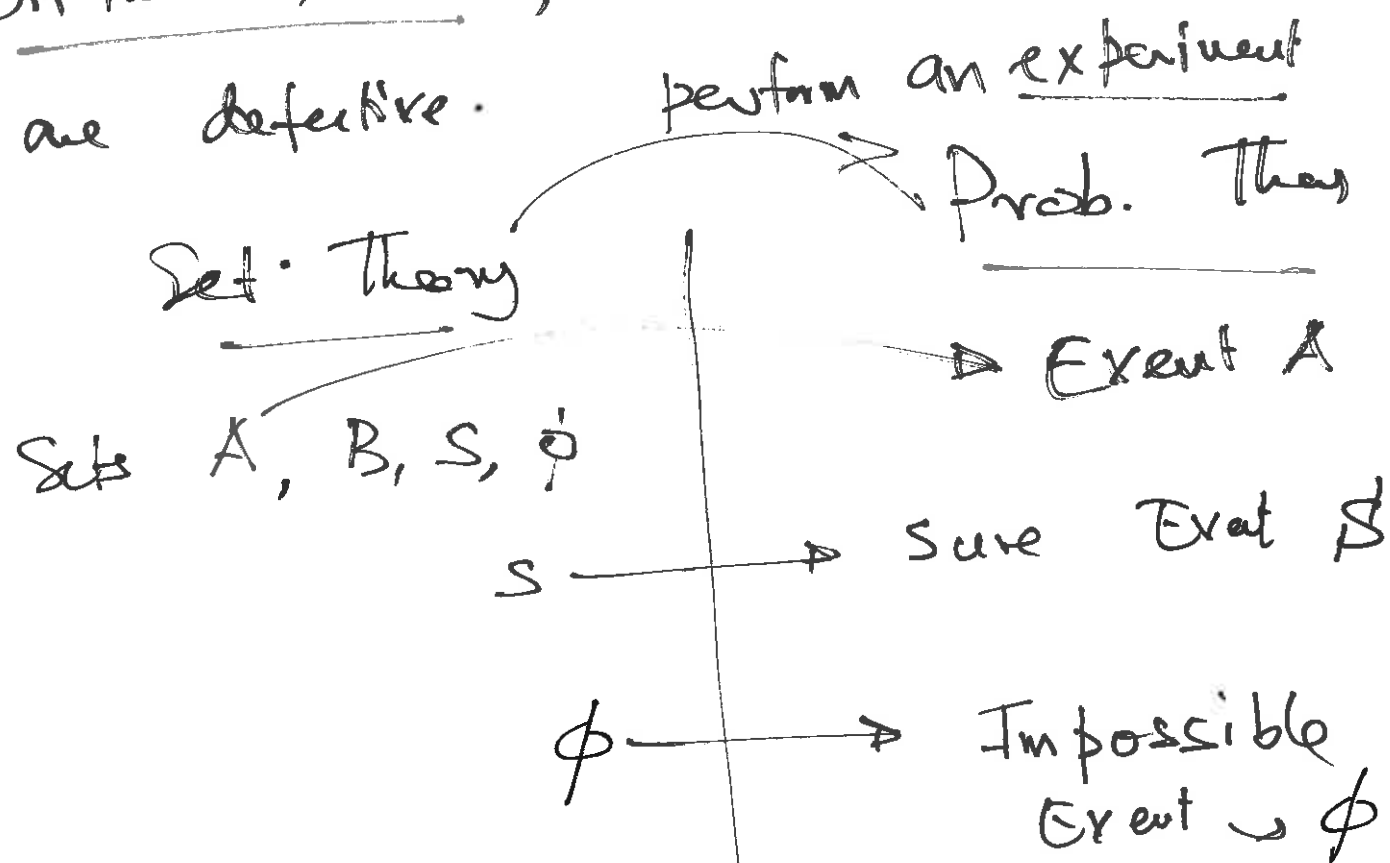
Prob. Theory

⑦

Prob. \rightarrow chance of occurrence.

eg: 2% of products are defective.

On the average, 2 out of 100 are defective.



Experiment \rightarrow Can be selecting a student from the class
" a product from a store.

Sets + Experiment

→ chance a set occurs.

randomly select a student

→ every one has the same chance.

eg:- 40 students in the class

$P[\text{Any particular student gets selected}] = \frac{1}{40}$

$P[A] =$ chance that A occurs when the experiment is performed.

All set operations are valid with events too.

✓
Can use the Venn Diagram.

Axioms of Prob.

⑨

1. $P[A] \geq 0$

2. $P[S] = 1 \Rightarrow$ chance that the space occurs

3. If A & B cannot occur simultaneously by

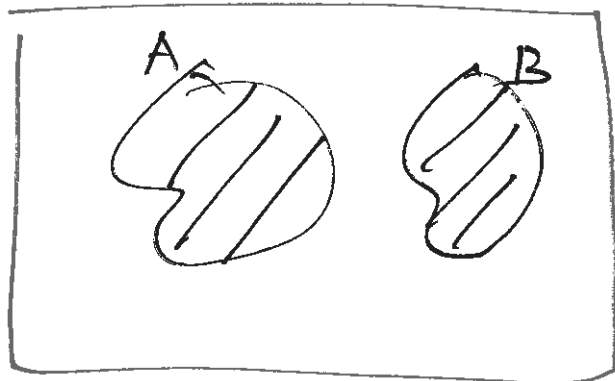
$$P[A+B] = P[A] + P[B]$$



A & B are called Mutually Exclusive



come from disjoint sets

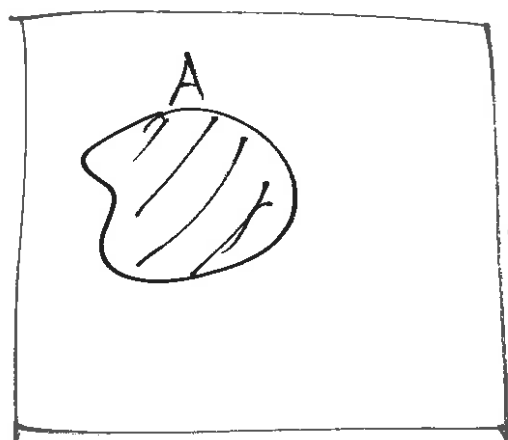


2

Prob. Mass

10

unit less $\checkmark P[A] =$ Mass of A on the Venn Diagram.

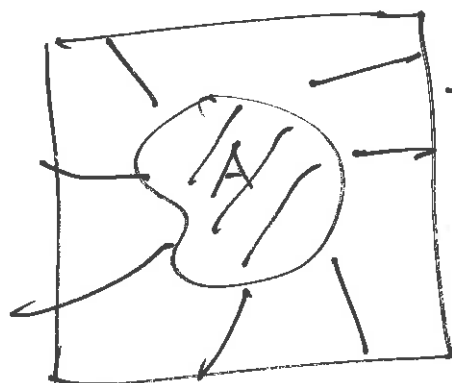


$$\hookrightarrow \frac{\text{Mass of } A}{\text{Mass of } S}$$

\checkmark Mass of $S = 1$

$$P[A] = \text{Mass of } A$$

$\S P[A^c] =$



\rightarrow Mass = 1

$$P[A^c] = \text{Mass of } A^c \\ = 1 - P[A]$$

Proof of $P[A^c] = 1 - P[A]$ (11)

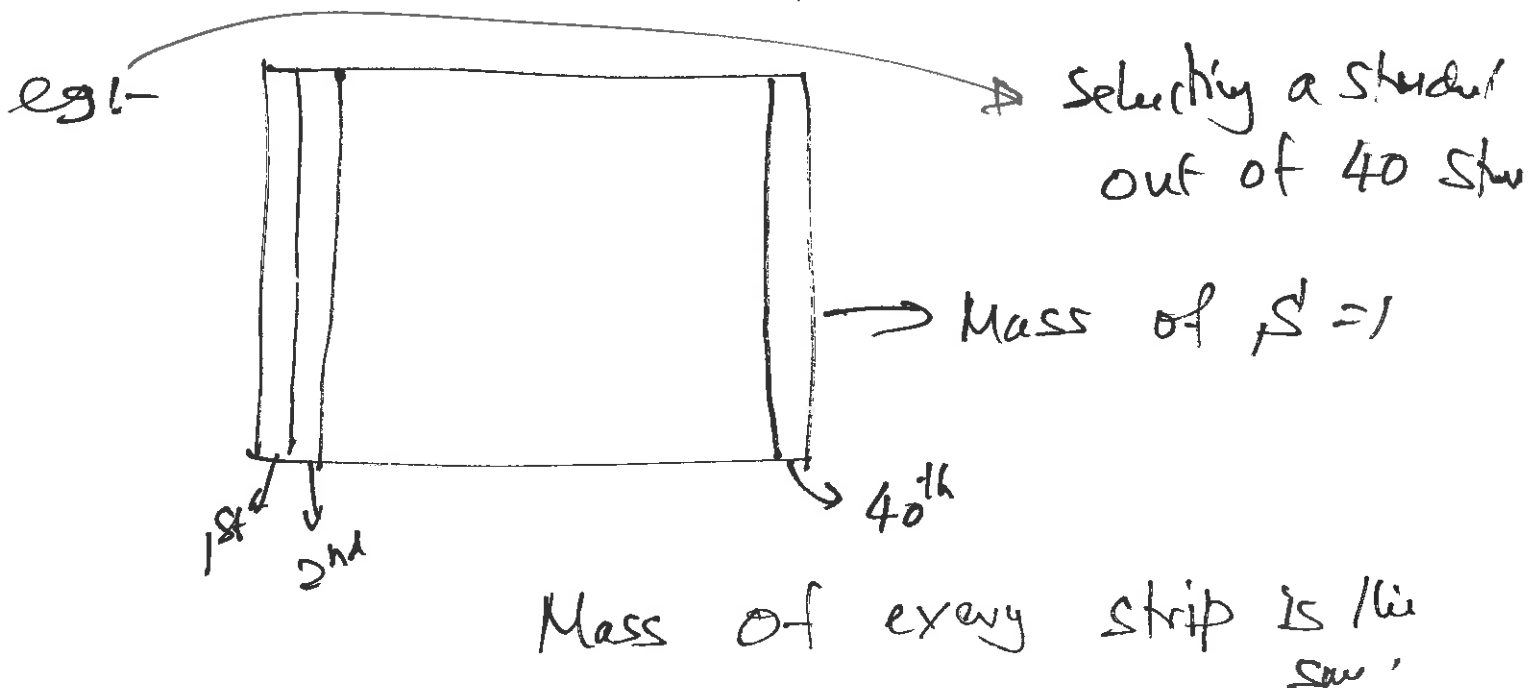
A & A^c are Mutually Exclusive

$$\therefore \underbrace{P[A + A^c]}_{S} = P[A] + P[A^c] \quad \begin{matrix} \searrow \\ 3^{\text{rd}} \text{ Axiom} \end{matrix}$$

$$\underbrace{P[S]}_{\parallel} = P[A] + P[A^c]$$

2nd Axiom $\leftarrow 1$

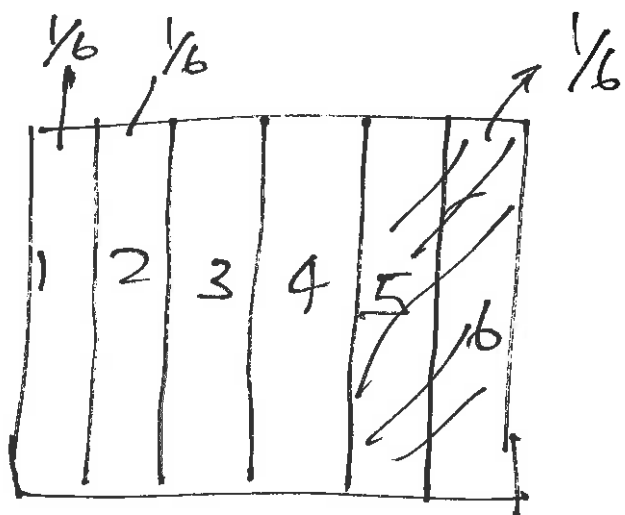
$$\therefore P[A^c] = 1 - P[A]$$



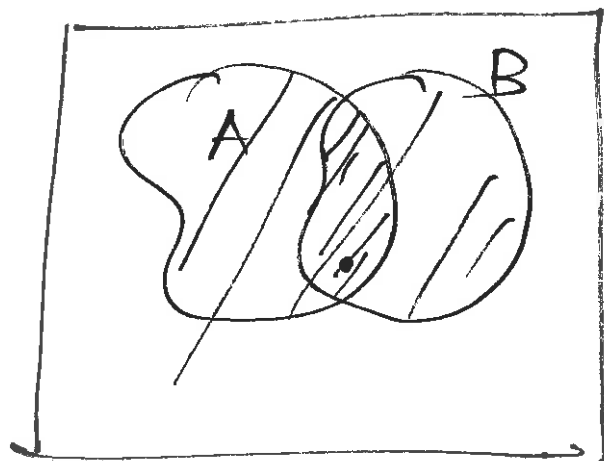
Mass of an individual strip = $\frac{1}{40}$ ⑫

eg: Roll a fair dice

Find the prob. of getting a number above 4



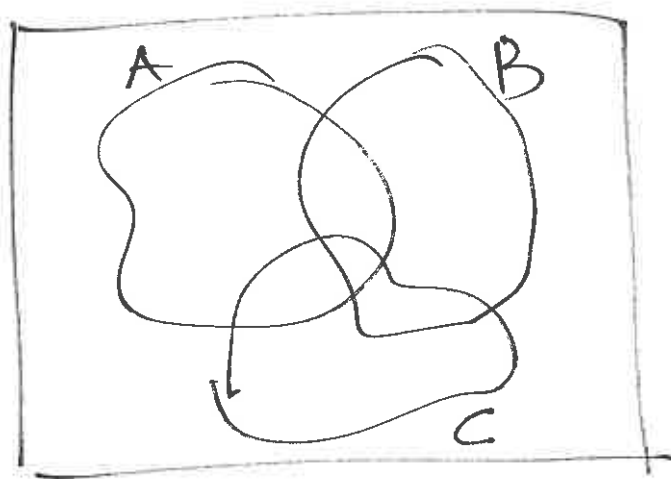
$$P[\text{Above } 4] = \text{Mass of } [5 \text{ \& } 6] \\ = \frac{1}{3}$$



$$P[A+B] = P[A] + P[B] - P[AB]$$

HW

⑬



Find $P[A+B+C]$

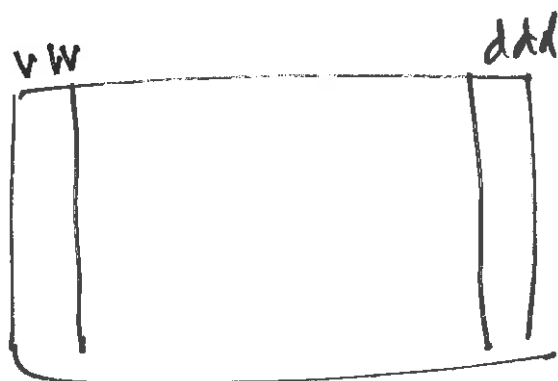
eg:- Monitor 3 calls

Each call is classified as Voice (V)
or Data (D)

$$S = \{VVV, VVd, VdV, Vdd, dVV, dVd, ddV, ddd\}$$

2^3 possible outcomes.

"
8



Disjoint

(14)

	$\underbrace{\quad\quad}_{0.6 \text{ L}} \quad \underbrace{\quad\quad}_{0.4 \text{ B}}$	
$\underbrace{\quad}_{0.7 \text{ V}}$	0.35	0.35
$\underbrace{\quad}_{0.3 \text{ D}}$	0.25	0.05

$$P[V] = 0.7$$

$$P[L] = 0.6$$

$$P[VL] = 0.35$$

Prob. that the call is voice and long

$$P[D] = 0.3$$

$$P[B] = 0.4$$

$$P[DL] = 0.25$$

$$P[D \cup L] = 1 - 0.35$$

$$P[LB] = 0$$

Conditional Prob.

15

A & B are 2 events.

$P[A]$, $P[B]$, $P[AB]$, $P[A+B]$

Told B has occurred

or Given.

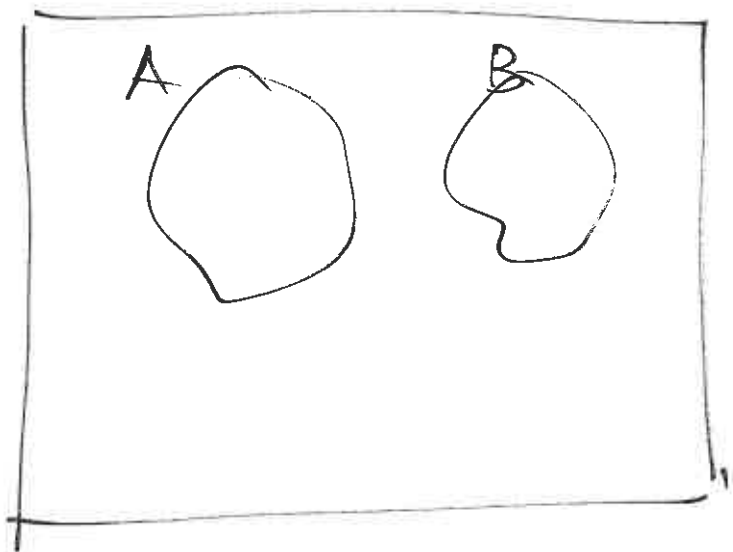
~~$P[B]$~~ chance that A occurs when
it is known that
B has occurred.

different from the $P[A]$
is called a conditional Prob.

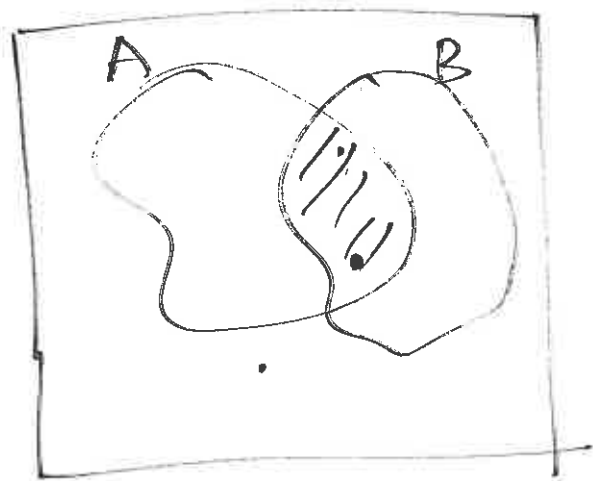
Notⁿ: $P[A|B] = ?$

eg:-

16



$$P[A/B] = 0$$



$$P[A/B] = \frac{\text{Mass of } AB}{\text{Mass of } B}$$

↳ Shrinks down to B

$$P[A/B] = \frac{P[AB]}{P[B]}$$

$$P[B|A] = \frac{P[AB]}{P[A]}$$

(17)

$$P[A|B] P[B] = P[B|A] P[A] = P[AB]$$

→ Bayes' th