Quantitative Management Modeling

Assignment #1

Linear Programming Model

Question 1:

Decision Variables

- A = Collegiate backpacks
- B = Mini backpacks

Objective Function - The objective is to maximize the profit.

Mathematical Formulation:

$$X = 32A + 24B$$

Nylon Constraint - $3A + 2B \le 5000$ Sales Constraint - $A \le 1000$, $B \le 1200$

Labor Constraint - $45A + 40B \le 35*40*60$

Question 2:

Decision Variables

- A^1 , A^m , and A^s = number of large, medium, and small units for plant 1
- B^{l} , B^{m} , and B^{s} = number of large, medium, and small units for plant 2
- C^{l} , C^{m} , and C^{s} = number of large, medium, and small units for plant 3

Objective - The objective is to maximize the profit

Mathematical Formulation:

(Max)
$$X = 420(A^1 + B^1 + C^1) + 360(A^m + B^m + C^m) + 300(A^s + B^s + C^s)$$

Constraint 1: Production

$$P1 - A^1 + A^m + A^s \le 750$$

$$P2 - B^1 + B^m + B^s \le 900$$

$$P3$$
 - $C^l + C^m + C^s \leq 450$

Constraint 2: Storage

$$P1 - 20A^1 + 15A^m + 12A^s \le 13000$$

$$P2 - 20B^1 + 15B^m + 12B^s \le 12000$$

$$P3 - 20C^1 + 15C^m + 12C^s \le 5000$$

Constraint 3: Sales

$$\begin{aligned} &Large - A^l + B^l + C^l \leq 900 \\ &Medium - A^m + B^m + C^m \leq 1200 \\ &Small - A^s + B^s + C^s \leq 750 \end{aligned}$$

Constraint 4: Same ratio

$$A^{1} + A^{m} + A^{s} / 750 = B^{1} + B^{m} + B^{s} / 900 = C^{1} + C^{m} + C^{s} / 450$$