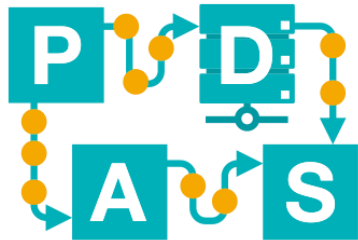


# Model Quality, Alpha Miner & Process Exploration

Benedikt Knopp

**BPI-Instruction 4**



Chair of Process  
and Data Science

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# Today's Agenda

**Model Quality Assessment**

**Alpha Miner: Step-by-Step Example**

**Alpha Miner: Many Examples**

**Process Exploration (ProM, Celonis)**

# Recap: Model Quality Assessment

## **Fitness (Recall):**

To what extend can the behavior recorded in the log be replayed by the model?

## **Precision:**

To what extend is the model behavior present in the log?

## **Generalization:**

How likely is it that an unseen trace can be replayed by the model?



**Hard / Ambiguous answers.**  
Requires knowledge or assumptions about the process apart from what is seen in the log.

## **Simplicity:**

How simple and readable is the model?



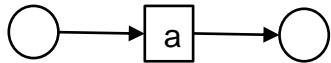
**E.g. number of nodes, no label duplications...**  
**Let's keep the discussion informal here**

# Recap: Model Quality Assessment

## Generalization:

How likely is it that an unseen trace can be replayed by the model?

**Log-based assessment:** Gain confidence from observing log frequencies.



$$L_1 = [\langle a \rangle^1]$$

$$L_2 = [\langle a \rangle^{100}]$$

*For this model, generalization w.r.t  $L_2$  is higher than w.r.t  $L_1$  because we have more evidence that future traces look the same.*

**Non-Log based assessment:** Make assumptions about the process apart from what is seen in the log.

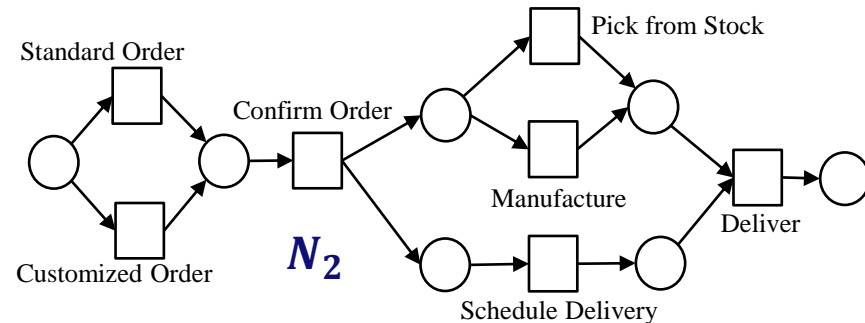
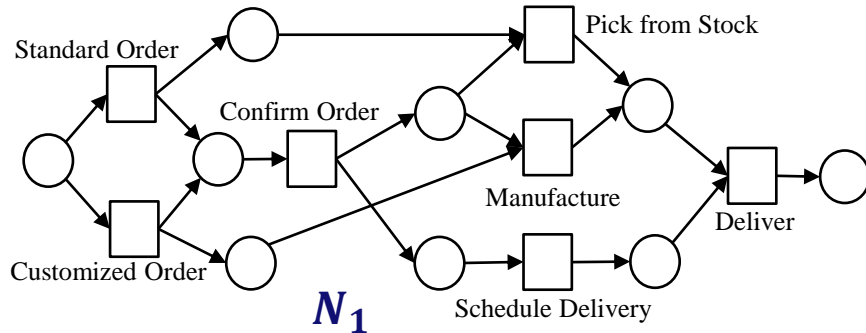
*See next slides...*

# Exercise 1a: Model Quality Assessment

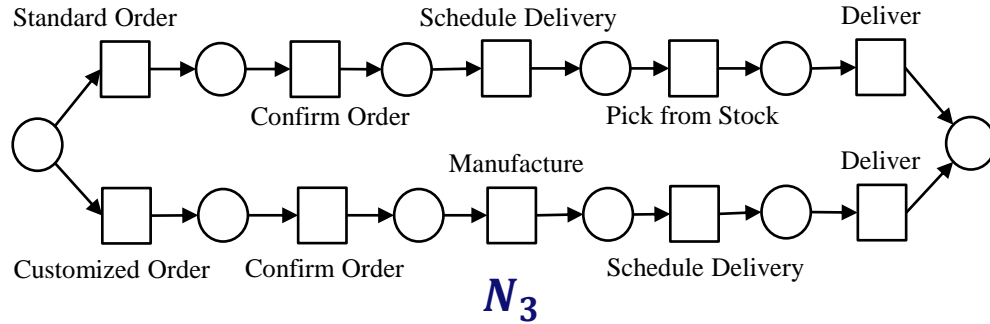
Recall the „carpenter“ process from last instruction (Exercise 6). Given the following event log  $L$  describing observed behavior:

$L = [\langle \text{Standard}, \text{Confirm}, \text{Schedule}, \text{Pick}, \text{Deliver} \rangle,$   
 $\langle \text{Customized}, \text{Confirm}, \text{Manufacture}, \text{Schedule}, \text{Deliver} \rangle]$

argue which of the following two Petri nets  $N_1$ ,  $N_2$  is better with respect to **precision**, **fitness**, **generalization** and **simplicity**.

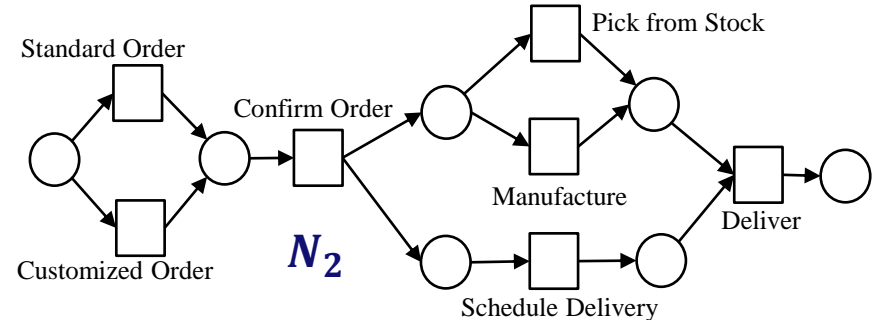


# Exercise 1b: Model Quality Assessment



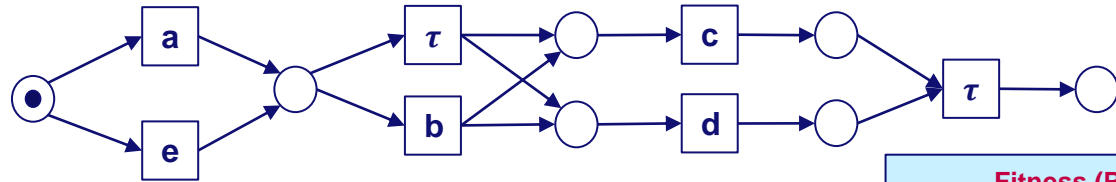
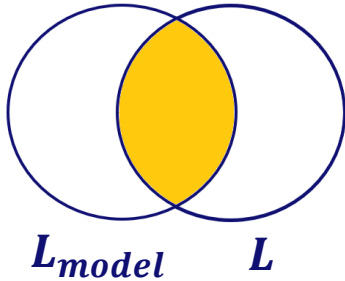
VS.

...argue which of the following two Petri nets  $N_3$ ,  $N_2$  is better with respect to **precision**, **fitness**, **generalization** and **simplicity**.



# Exercise 2a: Model Quality Metrics

Consider the following model and the following event log. Argue about fitness and precision of the model **using the complete model and log traces as model/log behavior.**



$$L = [\langle a, c \rangle^2, \langle e, d, c \rangle^5, \langle e, b, c, d \rangle^5]$$

**Fitness:**  $\frac{|L_{model} \cap L|}{|L|}$

With respect to trace frequencies

**Precision:**  $\frac{|L_{model} \cap L|}{|L_{model}|}$

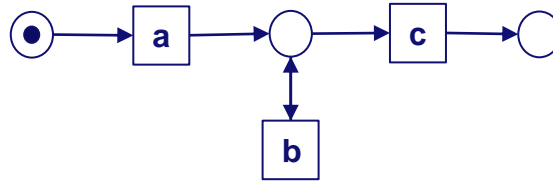
Without respect to trace frequencies

**Fitness (Recall):**  
To what extent can the behavior recorded in the log be replayed by the model?

**Precision:**  
To what extent is the model behavior present in the log?

# Exercise 2b: Model Quality Metrics

Consider the following model and the following event log. When reasoning about model quality as before, what is the problem here?



$$L = [\langle a, c \rangle^5, \langle a, b, c \rangle^3, \langle a, b, b, c \rangle^3]$$



# Recap – Alpha Miner

Let  $L$  be an event log over  $T$ .  $\alpha(L)$  is defined as follows.

1.  $T_L = \{ t \in T \mid \exists_{\sigma \in L} t \in \sigma \},$
2.  $T_I = \{ t \in T \mid \exists_{\sigma \in L} t = \text{first}(\sigma) \},$
3.  $T_O = \{ t \in T \mid \exists_{\sigma \in L} t = \text{last}(\sigma) \},$
4.  $X_L = \{ (A,B) \mid A \subseteq T_L \wedge A \neq \emptyset \wedge B \subseteq T_L \wedge B \neq \emptyset \wedge \forall_{a \in A} \forall_{b \in B} a \rightarrow_L b \wedge \forall_{a_1, a_2 \in A} a_1 \#_L a_2 \wedge \forall_{b_1, b_2 \in B} b_1 \#_L b_2 \},$
5.  $Y_L = \{ (A,B) \in X_L \mid \forall_{(A',B') \in X_L} A \subseteq A' \wedge B \subseteq B' \Rightarrow (A,B) = (A',B') \},$
6.  $P_L = \{ p_{(A,B)} \mid (A,B) \in Y_L \} \cup \{ i_L, o_L \},$
7.  $F_L = \{ (a, p_{(A,B)}) \mid (A,B) \in Y_L \wedge a \in A \} \cup \{ (p_{(A,B)}, b) \mid (A,B) \in Y_L \wedge b \in B \} \cup \{ (i_L, t) \mid t \in T_I \} \cup \{ (t, o_L) \mid t \in T_O \},$  and
8.  $\alpha(L) = (P_L, T_L, F_L).$

# Recap – Alpha Miner

Let  $L$  be an event log over  $T$ .  $\alpha(L)$  is defined as follows.

1.  $T_L = \{ t \in T \mid \exists_{\sigma \in L} t \in \sigma \}$ , Identifying activities
2.  $T_I = \{ t \in T \mid \exists_{\sigma \in L} t = \text{first}(\sigma) \}$ ,
3.  $T_O = \{ t \in T \mid \exists_{\sigma \in L} t = \text{last}(\sigma) \}$ ,
4.  $X_L = \{ (A, B) \mid A \subseteq T_L \wedge A \neq \emptyset \wedge B \subseteq T_L \wedge B \neq \emptyset \wedge \forall_{a \in A} \forall_{b \in B} a \rightarrow_L b \wedge \forall_{a_1, a_2 \in A} a_1 \#_L a_2 \wedge \forall_{b_1, b_2 \in B} b_1 \#_L b_2 \}$ ,
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2.  $T_I = \{ t \in T \mid \exists_{\sigma \in L} t = \text{first}(\sigma) \},$  ← Set of start activities
3.  $T_O = \{ t \in T \mid \exists_{\sigma \in L} t = \text{last}(\sigma) \},$
4.  $X_L = \{ (A,B) \mid A \subseteq T_L \wedge A \neq \emptyset \wedge B \subseteq T_L \wedge B \neq \emptyset \wedge \forall_{a \in A} \forall_{b \in B} a \rightarrow_L b \wedge \forall_{a_1, a_2 \in A} a_1 \#_L a_2 \wedge \forall_{b_1, b_2 \in B} b_1 \#_L b_2 \},$
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3.  $T_O = \{ t \in T \mid \exists_{\sigma \in L} t = \text{last}(\sigma) \}$ ,  **Set of end activities**
4.  $X_L = \{ (A, B) \mid A \subseteq T_L \wedge A \neq \emptyset \wedge B \subseteq T_L \wedge B \neq \emptyset \wedge \forall_{a \in A} \forall_{b \in B} a \rightarrow_L b \wedge \forall_{a_1, a_2 \in A} a_1 \#_L a_2 \wedge \forall_{b_1, b_2 \in B} b_1 \#_L b_2 \}$ ,
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8.  $\alpha(L) = (P_L, T_L, F_L).$

(A, B) pairs



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Deleting non maximal pairs




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5.  $Y_L = \{ (A,B) \in X_L \mid \forall_{(A',B') \in X_L} A \subseteq A' \wedge B \subseteq B' \Rightarrow (A,B) = (A',B') \}$ ,
6.  $P_L = \{ p_{(A,B)} \mid (A,B) \in Y_L \} \cup \{ i_L, o_L \}$ , ← **Places from pairs**
7.  $F_L = \{ (a, p_{(A,B)}) \mid (A,B) \in Y_L \wedge a \in A \} \cup \{ (p_{(A,B)}, b) \mid (A,B) \in Y_L \wedge b \in B \} \cup \{ (i_L, t) \mid t \in T_I \} \cup \{ (t, o_L) \mid t \in T_O \}$ , and
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8.  $\alpha(L) = (P_L, T_L, F_L).$

**Add arcs**



# Alpha Miner - Example

Consider the following event log  $L$ :

$$L = [\langle a, b, c \rangle, \langle a, c \rangle]$$

1. Give the directly-follows matrix and the footprint matrix of  $L$ .
2. Derive the set of pairs of transition sets  $X$  and identify the maximal pairs  $Y$ .
3. Write down the resulting Petri net  $\alpha(L)$ .
4. Is the discovered model a sound workflow net?
5. Does the discovered process model represent both traces in the event log? If not, explain why.

# Alpha Miner - Example

Give the directly-follows matrix and the footprint matrix of  $L$ .

$$L = [\langle a, b, c \rangle, \langle a, c \rangle]$$

Directly-follows relations

	a	b	c
a		>	>
b			>
c			

Footprint Matrix

	a	b	c
a	#	→	→
b	←	#	→
c	←	←	#

Causality:  $x \rightarrow y$  iff  $x > y$  and not  $y > x$ .

Parallelism:  $x \parallel y$  iff  $x > y$  and  $y > x$

Independence:  $x \# y$  iff not  $x > y$  and not  $y > x$ .

# Alpha Miner - Example

Derive the set of pairs of maximal transition sets  $Y$ .

We look at all pairs of non-empty activity sets

$$X_L = \{ (A, B) \mid A \subseteq T_L \wedge A \neq \emptyset \wedge B \subseteq T_L \wedge B \neq \emptyset \wedge \forall a \in A \forall b \in B a \rightarrow_L b \wedge \forall a_1, a_2 \in A a_1 \#_L a_2 \wedge \forall b_1, b_2 \in B b_1 \#_L b_2 \}$$

Each activity in A should be causal  $\rightarrow_L$  to each in B

All activities in each A and B should be independent

Then  $Y$  is the maximal pairs in  $X$ . **Suggestion:...**

# Alpha Miner - Example

Derive the set of pairs of maximal transition sets  $Y$ .

Suggestion: Write down pairs of sets  $A, B$ . Start with what you find in the footprint matrix. **Mind that here already**,  $a\#a$ ,  $b\#b$ ,  $c\#c$  needs to hold.

$A$	$B$
$\{a\}$	$\{b\}$
$\{a\}$	$\{c\}$
$\{b\}$	$\{c\}$

# Alpha Miner - Example

Derive the set of pairs of maximal transition sets  $Y$ .

Iteratively, combine rows by joining  $A$  with  $A$  and  $B$  with  $B$ , **if applicable**.

Footprint Matrix

	a	b	c
a	#	→	→
b	←	#	→
c	←	←	#

	<i>A</i>	<i>B</i>
<b>1</b>	$\{a\}$	$\{b\}$
<b>2</b>	$\{a\}$	$\{c\}$
<b>3</b>	$\{b\}$	$\{c\}$
<b>1+2</b>	<del><math>\{a\}</math></del>	<del><math>\{b, c\}</math></del>
<b>2+3</b>	<del><math>\{a, b\}</math></del>	<del><math>\{c\}</math></del>
<b>1+3</b>	<del><math>\{a, b\}</math></del>	<del><math>\{b, c\}</math></del>

Cannot do that:  $b\#c$  does not hold.

Cannot do that:  $a\#b$  does not hold.

Cannot do that:  $a\#b$  and  $b\#c$  and  $b \rightarrow b$  do not hold.

# Alpha Miner - Example

Derive the set of pairs of maximal transition sets  $Y$ .

We are done: This is  $X$ .

$A$	$B$
$\{a\}$	$\{b\}$
$\{a\}$	$\{c\}$
$\{b\}$	$\{c\}$

All pairs  $A, B$  are maximal. Therefore,  $Y = X$  in this case.

# Alpha Miner - Example

$L = [<a, b, c>, <a, c>]$

1.  $T_L = \{ a, b, c \},$

2.  $T_I = \{ a \},$

3.  $T_O = \{ c \},$

Footprint

	a	b	c
a	#	→	→
b	←	#	→
c	←	←	#

a

b

c

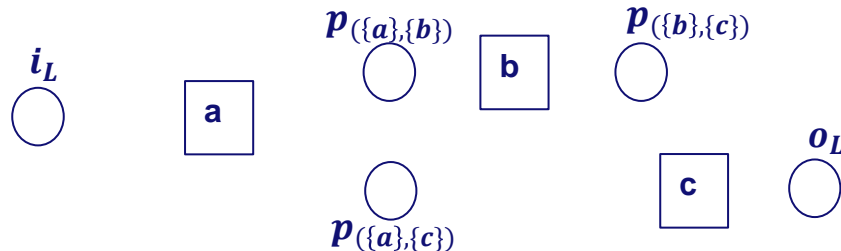
# Alpha Miner - Example

**$L = [\langle a, b, c \rangle, \langle a, c \rangle]$**

1.  $T_L = \{ a, b, c \},$
2.  $T_I = \{ a \},$
3.  $T_O = \{ c \},$
4.  $X_L = \{ (\{a\}, \{b\}), (\{b\}, \{c\}), (\{a\}, \{c\}) \}$
5.  $Y_L = \{ (\{a\}, \{b\}), (\{b\}, \{c\}), (\{a\}, \{c\}) \}$
6.  $P_L = \{ p_{(A,B)} \mid (A,B) \in Y_L \} \cup \{i_L, o_L\},$

Footprint

	a	b	c
a	#	→	→
b	←	#	→
c	←	←	#





# Alpha Miner - Example

$L = [\langle a, b, c \rangle, \langle a, c \rangle]$

1.  $T_L = \{ a, b, c \},$

2.  $T_I = \{ a \},$

3.  $T_O = \{ c \},$

4.  $X_L = \{ (\{a\}, \{b\}), (\{b\}, \{c\}), (\{a\}, \{c\}) \}$

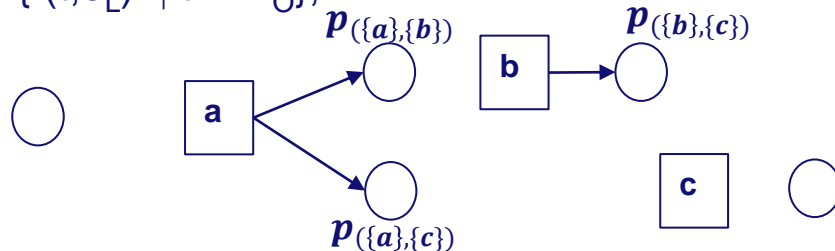
5.  $Y_L = \{ (\{a\}, \{b\}), (\{b\}, \{c\}), (\{a\}, \{c\}) \}$

6.  $P_L = \{ p_{(A,B)} \mid (A,B) \in Y_L \} \cup \{ i_L, o_L \},$

7.  $F_L = \boxed{\{ (a, p_{(A,B)}) \mid (A,B) \in Y_L \wedge a \in A \}} \cup \{ (p_{(A,B)}, b) \mid (A,B) \in Y_L \wedge b \in B \} \cup \{ (i_L, t) \mid t \in T_I \} \cup \{ (t, o_L) \mid t \in T_O \},$

Footprint

	a	b	c
a	#	→	→
b	←	#	→
c	←	←	#



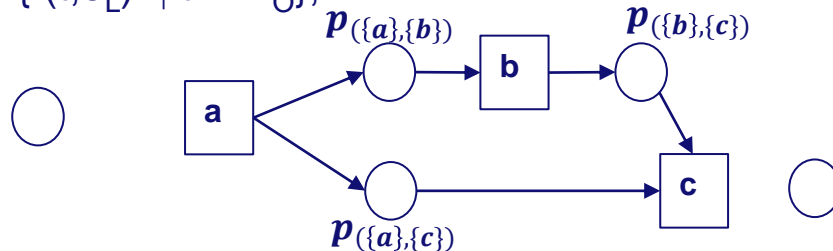
# Alpha Miner - Example

$L = [<a, b, c>, <a, c>]$

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5.  $Y_L = \{ (\{a\}, \{b\}), (\{b\}, \{c\}), (\{a\}, \{c\}) \}$
6.  $P_L = \{ p_{(A,B)} \mid (A,B) \in Y_L \} \cup \{ i_L, o_L \},$
7.  $F_L = \{ (a, p_{(A,B)}) \mid (A,B) \in Y_L \wedge a \in A \} \cup \{ (p_{(A,B)}, b) \mid (A,B) \in Y_L \wedge b \in B \} \cup \{ (i_L, t) \mid t \in T_I \} \cup \{ (t, o_L) \mid t \in T_O \},$

Footprint

	a	b	c
a	#	→	→
b	←	#	→
c	←	←	#



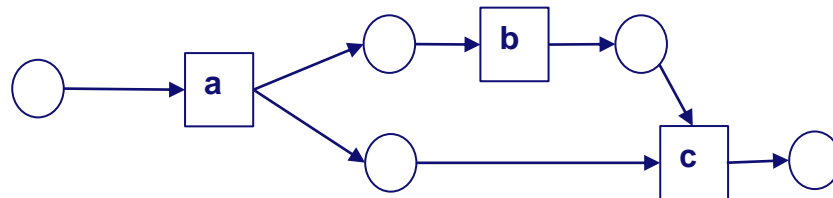
# Alpha Miner - Example

$L = [\langle a, b, c \rangle, \langle a, c \rangle]$

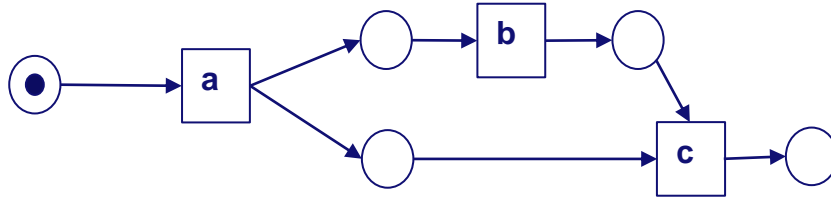
1.  $T_L = \{ a, b, c \},$
2.  $T_I = \{ a \},$
3.  $T_O = \{ c \},$
4.  $X_L = \{ (\{a\}, \{b\}), (\{b\}, \{c\}), (\{a\}, \{c\}) \}$
5.  $Y_L = \{ (\{a\}, \{b\}), (\{b\}, \{c\}), (\{a\}, \{c\}) \}$
6.  $P_L = \{ p_{(A,B)} \mid (A,B) \in Y_L \} \cup \{ i_L, o_L \},$
7.  $F_L = \{ (a, p_{(A,B)}) \mid (A,B) \in Y_L \wedge a \in A \} \cup \{ (p_{(A,B)}, b) \mid (A,B) \in Y_L \wedge b \in B \} \cup \{ (i_L, t) \mid t \in T_I \} \cup \{ (t, o_L) \mid t \in T_O \},$

Footprint

	a	b	c
a	#	→	→
b	←	#	→
c	←	←	#



# Exercise 3: Alpha Miner Example



$L = [\langle a, b, c \rangle, \langle a, c \rangle]$

1. Is the discovered model a sound workflow net?
2. Does the discovered process model represent both traces in the event log? If not, explain why.

# Exercise 4: Alpha Miner – Practice, Practice

Consider the event logs given below. For each event log, think about what a Petri net might look like that describes the behavior suitably. Apply the Alpha algorithm, validate your result with ProM, and compare the result with your conceived net. If the net is a sound workflow net, argue about precision and fitness (and generalization).

- a)  $L_1 = [\langle \text{order, pay} \rangle, \langle \text{order, reminder, pay} \rangle, \langle \text{order, reminder, reminder, pay} \rangle]$
- b)  $L_2 = [\langle \text{a,b,c,d,e,f,b,d,c,e,g} \rangle, \langle \text{a,b,d,c,e,g} \rangle, \langle \text{a,b,c,d,e,f,b,c,d,e,f,b,d,c,e,g} \rangle]$
- c)  $L_3 = [\langle \text{awake, eat, study, sleep} \rangle, \langle \text{awake, study, eat, sleep} \rangle]$
- d)  $L_4 = [\langle \text{awake, eat, study, eat, study, sleep} \rangle]$

Let  $L_5 = [\langle \text{awake, eat, study, eat, study, sleep} \rangle, \langle \text{awake, study, eat, study, eat, sleep} \rangle]$ . What Petri net would describe this process well? Compare the directly-follows matrices of  $L_3, L_4$  and  $L_5$ . What is  $\alpha(L_5)$ ?

# Exercise 4: Alpha Miner – Practice, Practice

Consider the event logs given below. For each event log, think about what a Petri net might look like that describes the behavior suitably. Apply the Alpha algorithm, validate your result with ProM, and compare the result with your conceived net. If the net is a sound workflow net, argue about precision and fitness (and generalization).

a)  $L_1 = [\langle \text{order, pay} \rangle, \langle \text{order, reminder, pay} \rangle, \langle \text{order, reminder, reminder, pay} \rangle]$

b)  $L_2 = [\langle \text{a,b,c,d,e,f,b,d,c,e,a} \rangle, \langle \text{a,b,c,d,e,f,b,c,d,e,f,b,c,d,e,a} \rangle]$

c)  $L_3 = [\langle \text{awake, eat, study} \rangle]$

d)  $L_4 = [\langle \text{awake, eat, study} \rangle]$

Let  $L_5 = [\langle \text{awake, eat, study} \rangle]$

What Petri net would describe

matrices of  $L_3, L_4$  and  $L_5$ . What is  $\alpha(L_5)$ .

Use the `alpha_L[xxx]` files. If you want to practice with more logs, you can just modify any of these files (with a standard Texteditor) so that it features the log you want.

Take care to have a **correct sorting** (timestamps) and that each trace has a **unique case id**!



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# Exercise 4: Alpha Miner – Practice, Practice

Consider the event logs given below. For each event log, think about what a Petri net might look like that describes the behavior suitably. Apply the Alpha algorithm, validate your result with ProM, and compare the result with your conceived net. If the net is a sound workflow net, argue about precision and fitness (and generalization).

Be careful here!

a)  $L_1 = [\langle \text{order, pay} \rangle, \langle \text{order, reminder, pay} \rangle, \langle \text{order, reminder, reminder, pay} \rangle]$

b)  $L_2 = [\langle \text{a,b,c,d,e,f,b,d,c,e,g} \rangle, \langle \text{a,b,d,c,e,g} \rangle, \langle \text{a,b,c,d,e,f,b,c,d,e,f,b,d,c,e,g} \rangle]$

c)  $L_3 = [\langle \text{awake, eat, study, sleep} \rangle, \langle \text{awake, study, eat, sleep} \rangle]$

d)  $L_4 = [\langle \text{awake, eat, study, eat, study, sleep} \rangle]$

Hint: c and d are concurrent

Let  $L_5 = [\langle \text{awake, eat, study, eat, study, sleep} \rangle, \langle \text{awake, study, eat, study, eat, sleep} \rangle]$ . What Petri net would describe this process well? Compare the directly-follows matrices of  $L_3, L_4$  and  $L_5$ . What is  $\alpha(L_5)$ ?

# Exercise 4: Alpha Miner – Practice, Practice

Consider the event logs given below. For each event log, think about what a Petri net might look like that describes the behavior suitably. Apply the Alpha algorithm, validate your result with ProM, and compare the result with your conceived net. If the net is a sound workflow net, argue about precision and fitness (and generalization).

- a)  $L_1 = [\langle \text{order, pay} \rangle, \langle \text{order, reminder, pay} \rangle, \langle \text{order, reminder, reminder, pay} \rangle]$
  - b)  $L_2 = [\langle \text{a,b,c,d,e,f,b,d,c,e,g} \rangle, \langle \text{a,b,d,c,e,g} \rangle, \langle \text{a,b,c,d,e,f,b,c,d,e,f,b,d,c,e,g} \rangle]$
  - c)  $L_3 = [\langle \text{awake, eat, study, sleep} \rangle, \langle \text{awake, study, eat, sleep} \rangle]$
  - d)  $L_4 = [\langle \text{awake, eat, study, eat, study, sleep} \rangle]$
- Note:**
- Loop of length 1
  - Loop of length 2
  - Loop of length 3

Let  $L_5 = [\langle \text{awake, eat, study, eat, study, sleep} \rangle, \langle \text{awake, study, eat, study, eat, sleep} \rangle]$ . What Petri net would describe this process well? Compare the directly-follows matrices of  $L_3, L_4$  and  $L_5$ . What is  $\alpha(L_5)$ ?



# Exercise 5 – Process Exploration

## Hands On ProM and Celonis

Load the provided *delivery\_management* event log into both ProM and Celonis to:

1. Give an overview of what days are busy (ProM) and the average throughput times of cases (Celonis).
2. Show the two most frequent variants and their DFGs (both tools).
3. Discover a model. *Advanced*: Discover a model only for cases that **do not** contain “failed delivery” (both tools).

### Suggestions / Hints

#### ProM Plugins

Dotted Chart

(Explore Event Log), Inductive Visual Miner

(any) Miner, Filter Event Log (next slide)

#### Celonis Sheets

Process Overview, (New Sheet with Line Chart)

New Sheet with Variant Explorer

Conformance

# ProM: Advanced Filtering

## Example

