

# Chapter 5

## Dams and Spillways

A dam is an impervious barrier built across a water course to:

- ☀ store water
- ☀ create a head
- ☀ form a lake



Atatürk Dam

## Classification of dams on type and material

- ④ Gravity Dams
- ④ Arch Dams
- ④ Buttress Dams
- ④ Embankment (Fill) Dams

## Classification of dams on size

- ④ Large Dams
- ④ High Dams
- ④ Small Dams

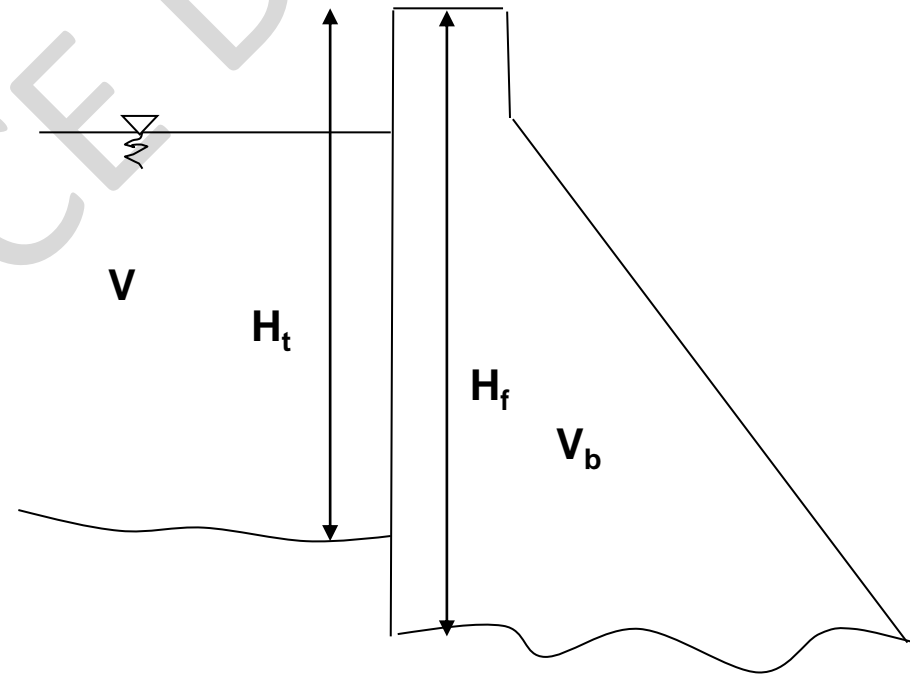
## Additional classification by ICOLD (International Commission on Large Dams)

④ Large Dam: ( $H_f > 15$  m)

or 
$$\begin{cases} 10 \text{ m} \leq H_f \leq 15 \text{ m} \\ V > 10^6 \text{ m}^3 \\ L > 500 \text{ m} \end{cases}$$

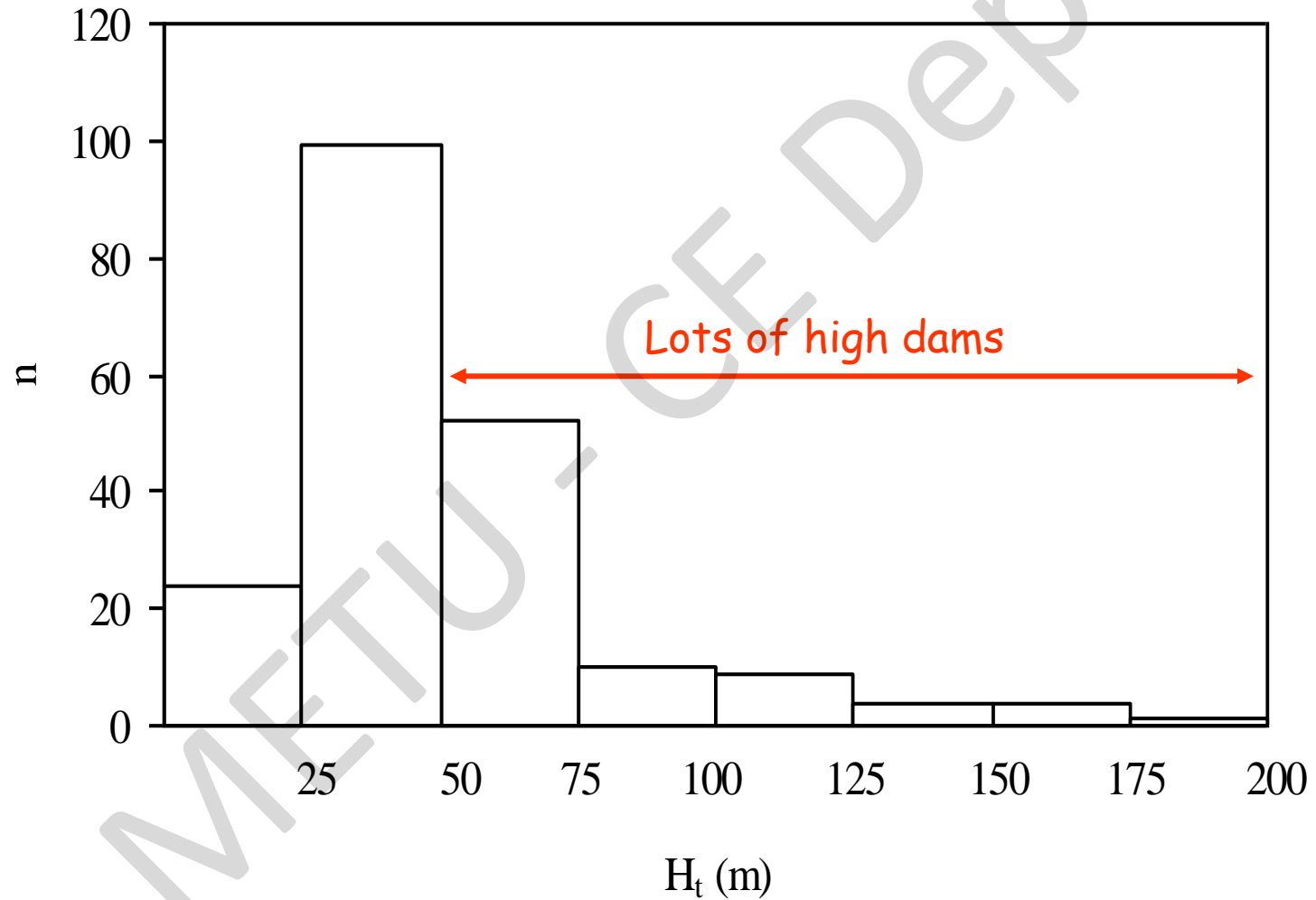
④ Small Dam:  
 $H_f < 10$  m

④ High Dam  
 $H_t > 50$  m



$V$  = reservoir storage  
 $L$  = crest length

## Dams in Turkey



## Parts of dams:

- @ Body
- @ Reservoir
- @ Spillway
- @ Water intake
- @ Diversion facilities
- @ Others

Hydropower station

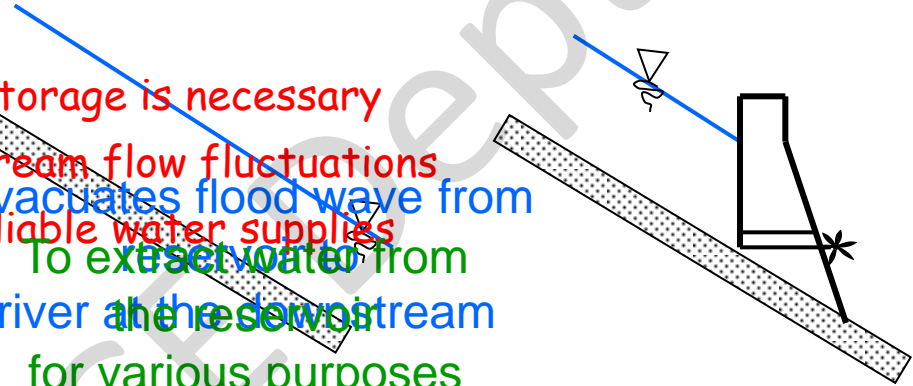
Site installations

Roads

Locks

Fish ladders

Reservoir storage is necessary  
to regulate stream flow fluctuations  
& develop reliable water supplies  
Evacuates flood wave from  
river and the reservoir  
To extract water from  
river and the reservoir  
for various purposes

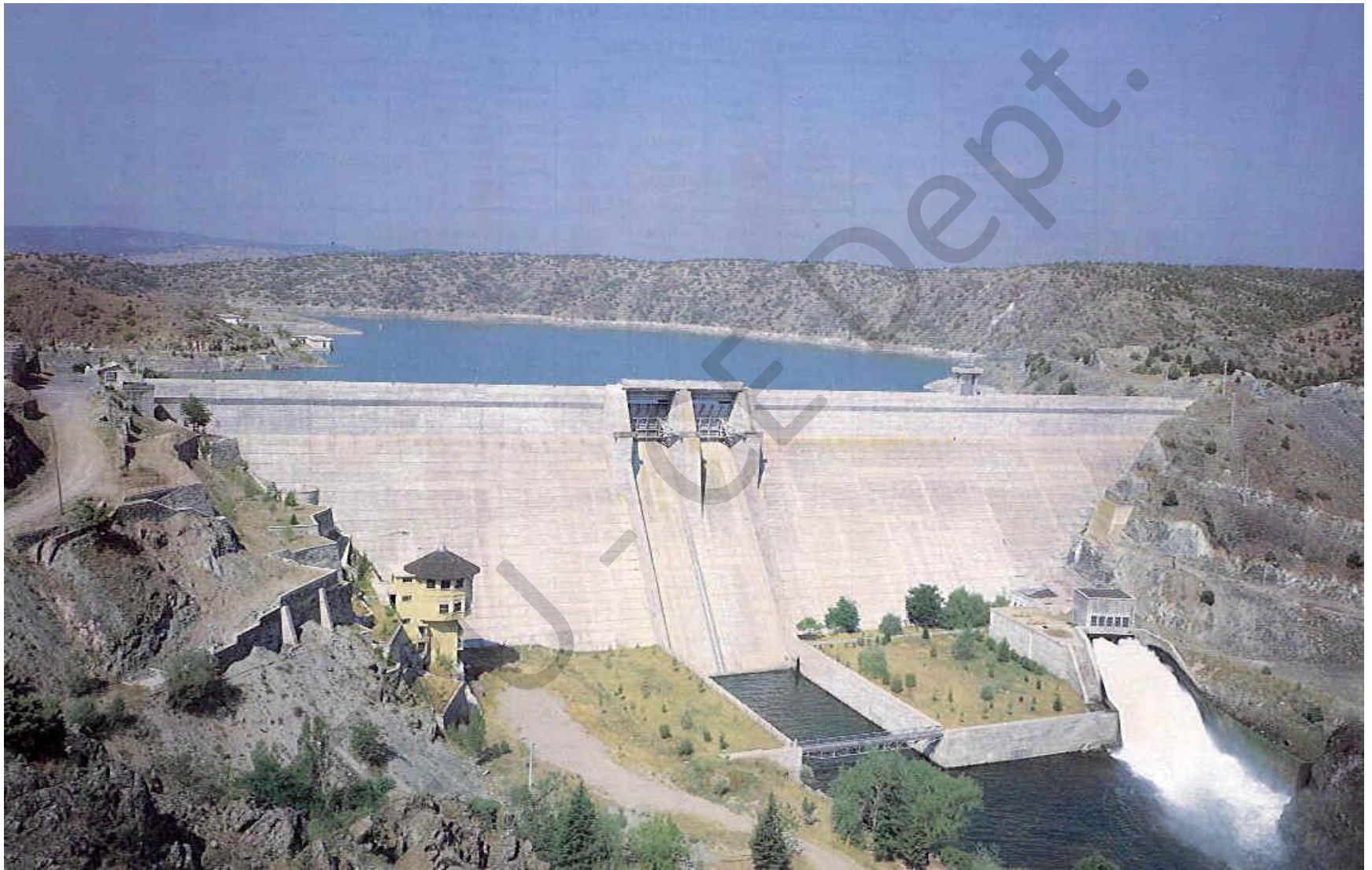


# Classification of dams

## a) GRAVITY DAMS

- ☀ Concrete gravity
- ☀ Prestressed concrete
- ☀ Roller compacted concrete (RCC)
- ☀ Hardfill - most recent type  
Ex: Cindere Dam





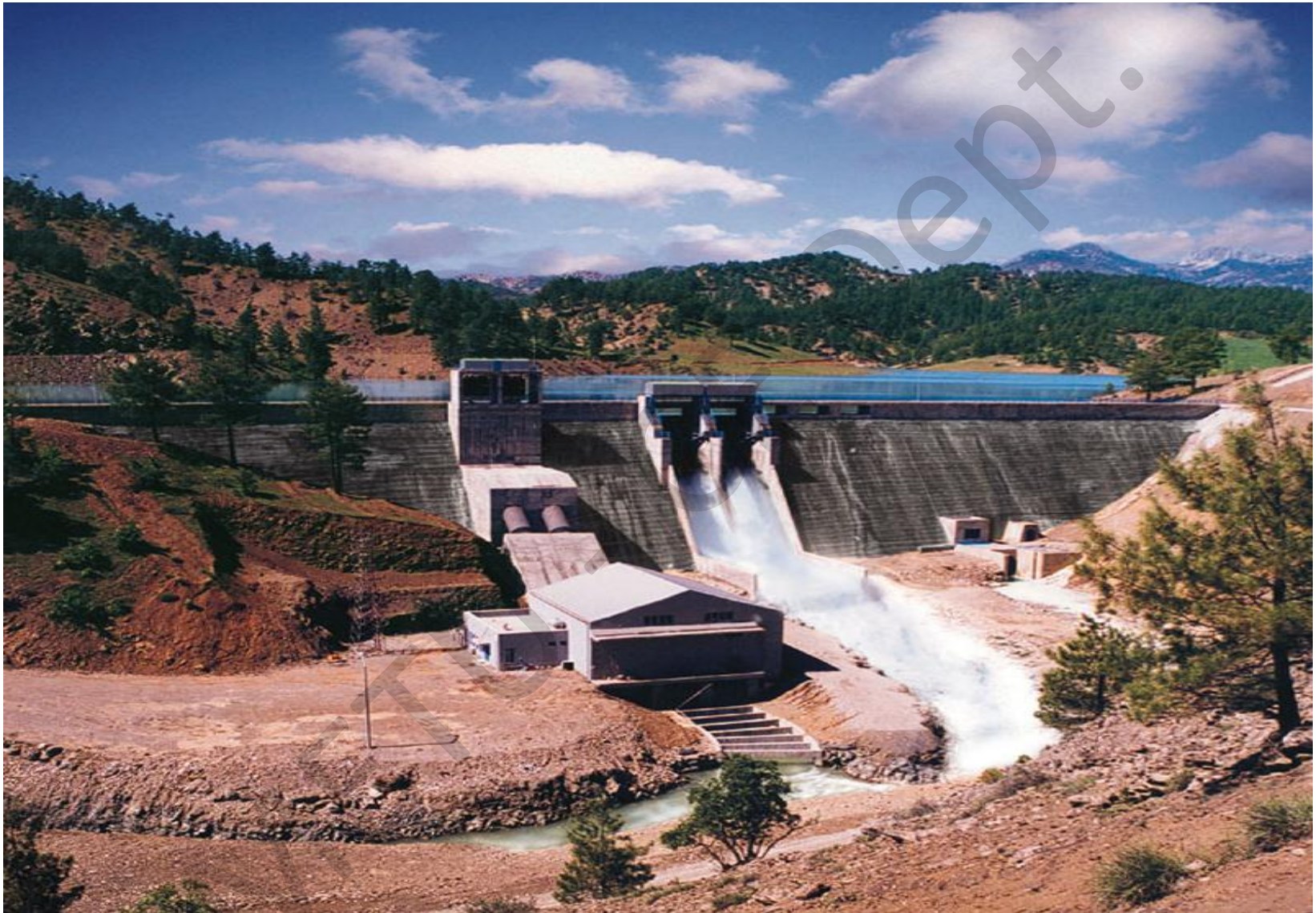
Porsuk Dam (Concrete Gravity) on Porsuk River





Sarıyar Dam (Concrete Gravity) on Sakarya River





Suğatı Dam (Roller Compacted Concrete, RCC)  
on Güredin (Ceyhan) River

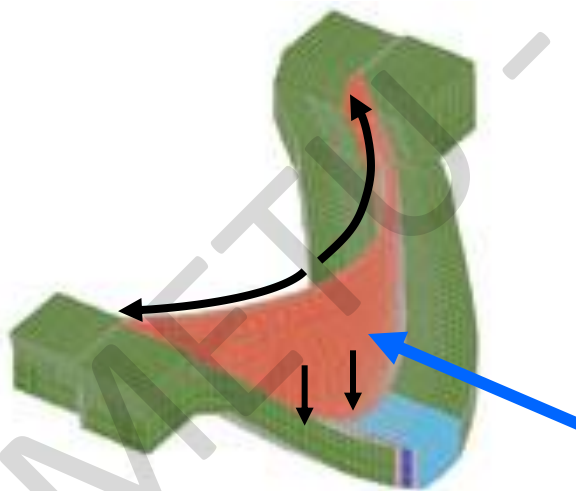




Suçatı Dam (Roller Compacted Concrete, RCC)  
on Güredin (Ceyhan) River

## b) ARCH DAMS

- ✱ Constant-angle arch
- ✱ Constant-center arch
- ✱ Variable-angle, variable center arch



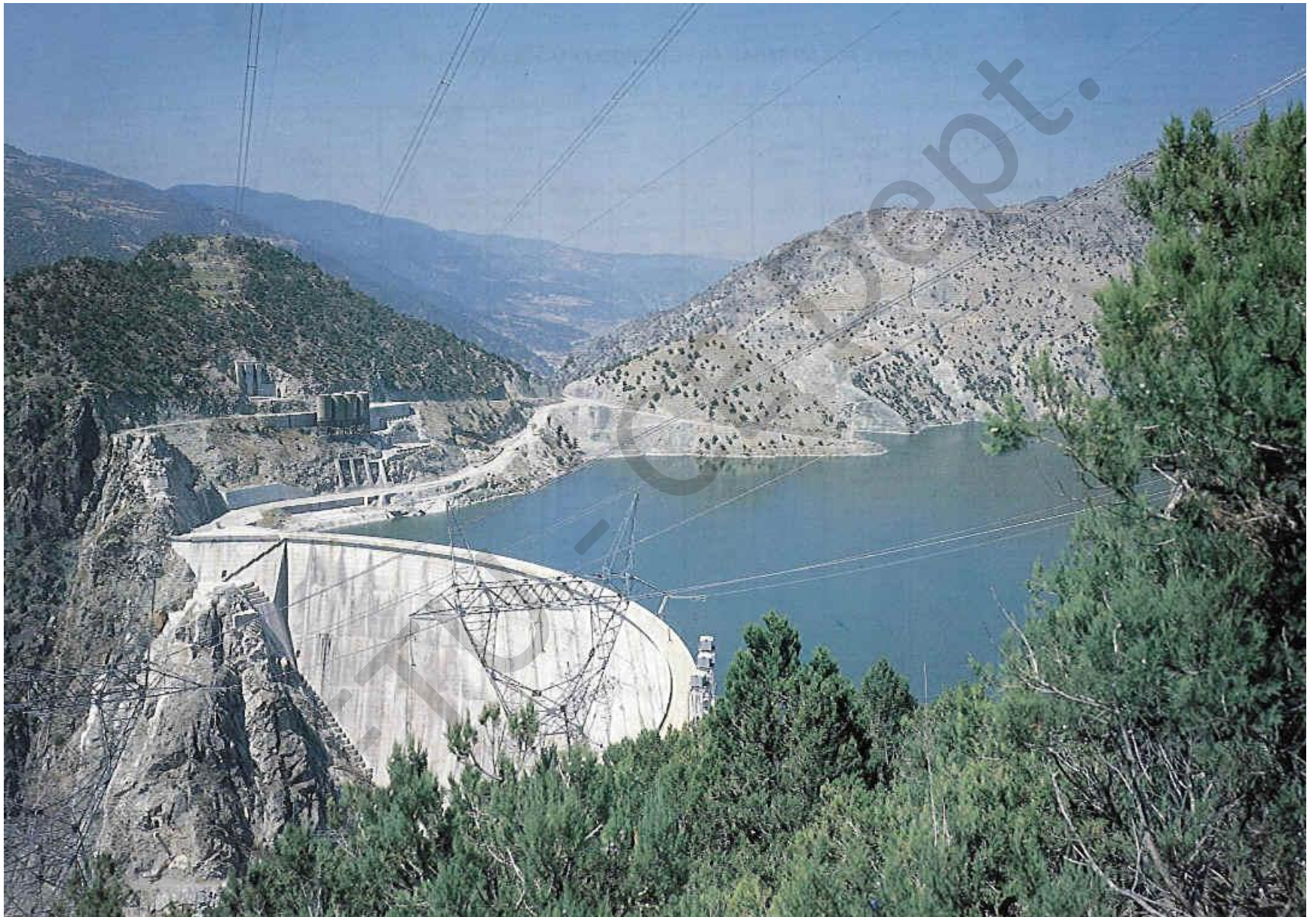
[http://www.minstroy.com/images/proekti/caknkov\\_kamak/stenata.jpg](http://www.minstroy.com/images/proekti/caknkov_kamak/stenata.jpg)

Most of the forces are  
transferred to  
the sides/slopes of the valley



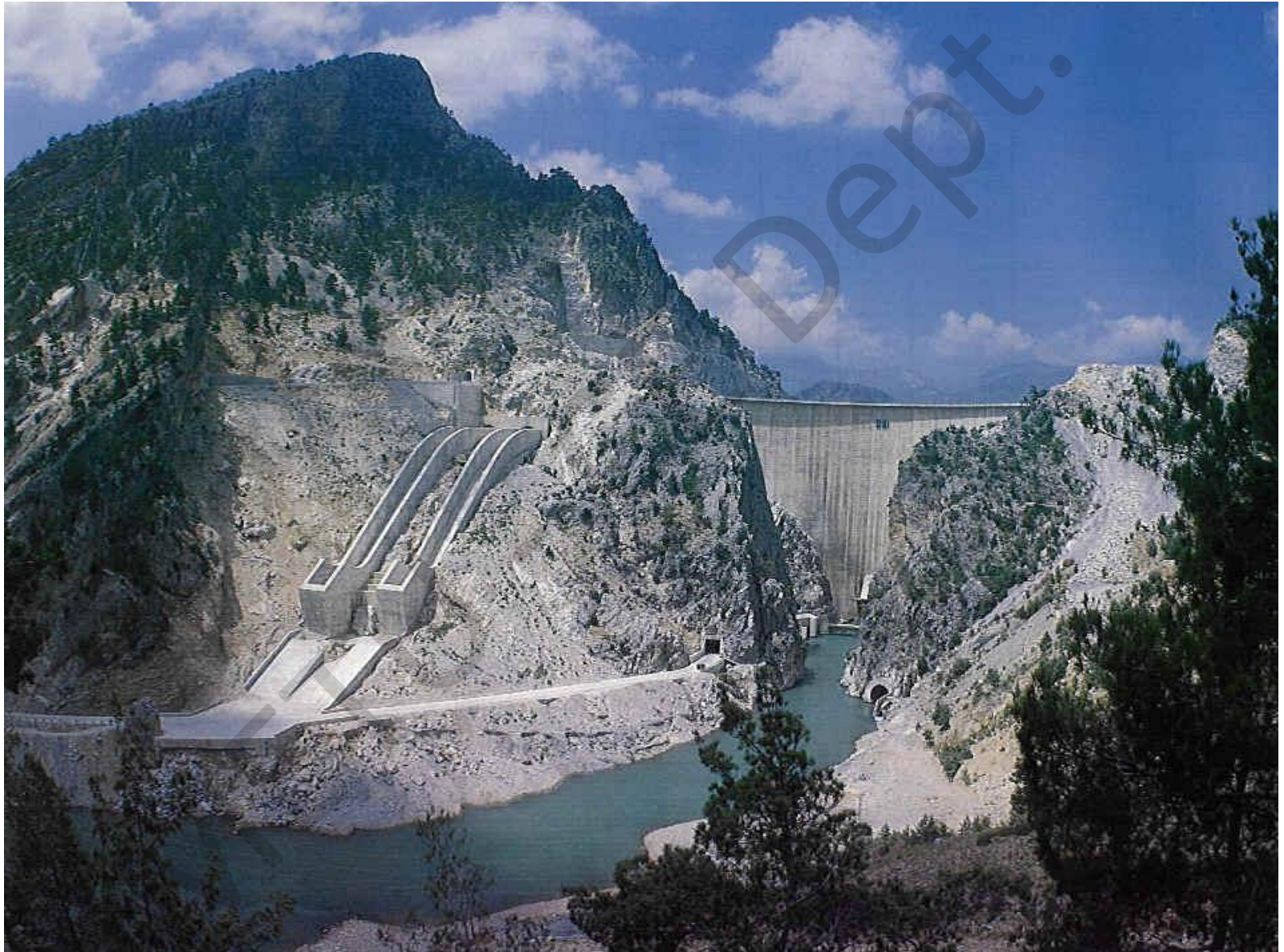
Sides of the valley  
need to be strong





Gökçekaya Dam (Arch) on Sakarya River





Oymapınar Dam (Arch) on Manavgat River





Karakaya Dam (Arch-Gravity) on Fırat River

## b) BUTRESS DAMS

- ✱ Flat-slab buttress
- ✱ Multiple-arch buttress



Elmalı II Dam (Flat-Slab Buttress) on Çavuşbaşı River

## d) EMBANKMENT (FILL) DAMS - composed of earth material at the dam site

- ⊙ Earth-fill (>50% of fill is soil)
  - ✱ Simple embankment
  - ✱ Zoned embankment
  - ✱ Diaphragm-type embankment
- ⊙ Rock-fill (>50% of fill is of rock)
  - ✱ Impermeable-face
  - ✱ Impermeable earth-core



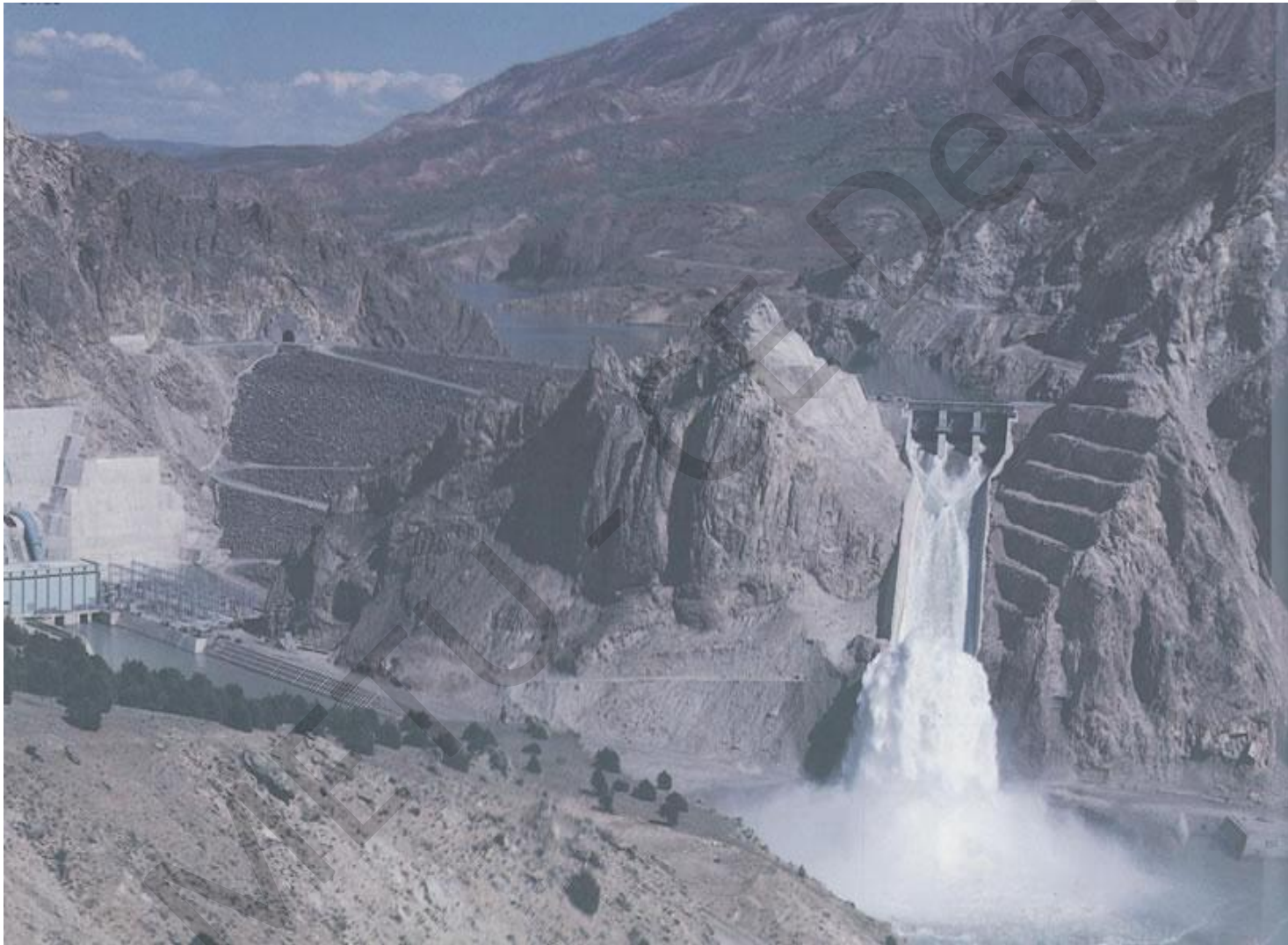


Atatürk Dam (Rockfill) on Fırat River





Hasan Uğurlu Dam (Rockfill) on Yeşilırmak

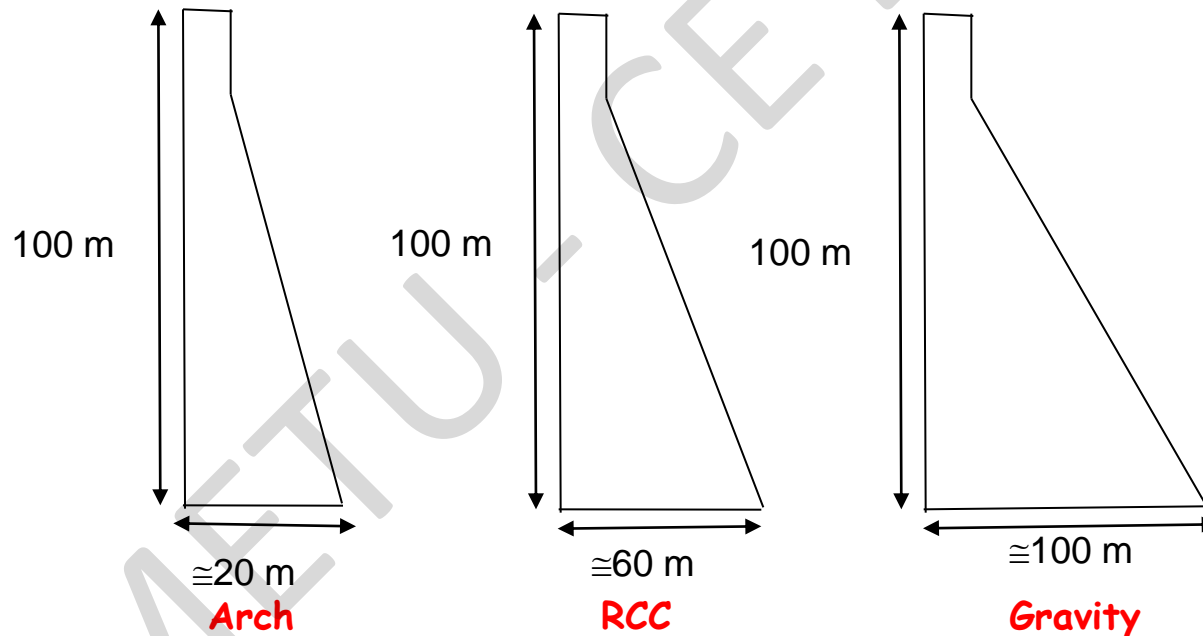


Kılıçkaya Dam (Rockfill) on Kelkit River



# Comparison of dams according to $V_b$

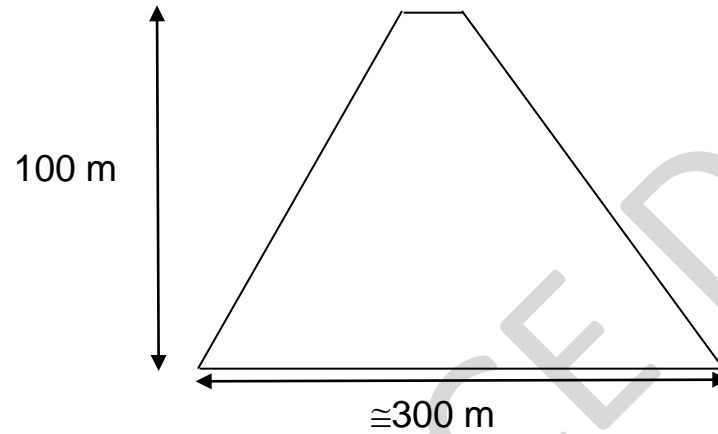
## Concrete dams



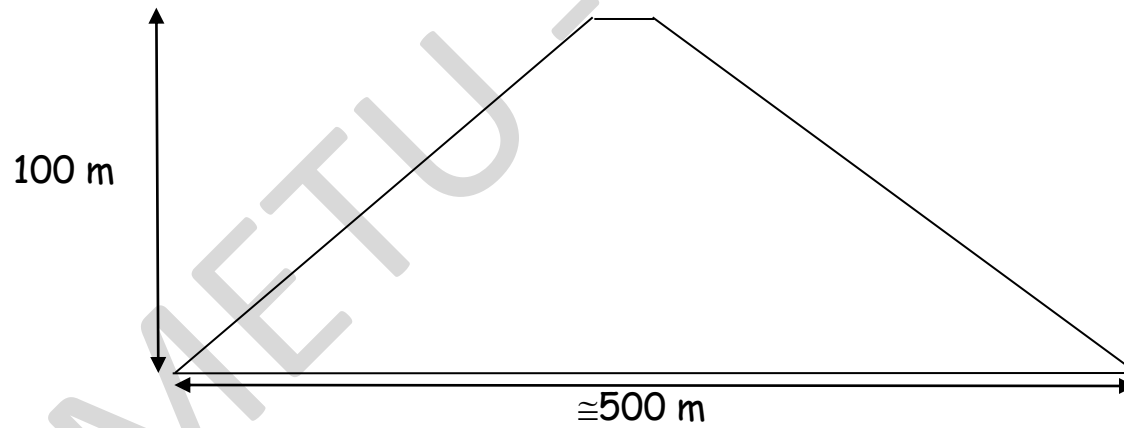
less economic in terms of  
material required



# Fill dams



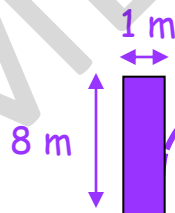
Rockfill



Earthfill

## Comparison of some dams

Dam	Type	$H_f$ (m)	$V_b$ ( $\times 10^6$ m <sup>3</sup> )
Boyabat	Gravity	193	2.3
Berke	Arch	186	0.74
Atatürk	Rockfill	166	84.5



1x8 m<sup>2</sup> wall along Turkey's border!

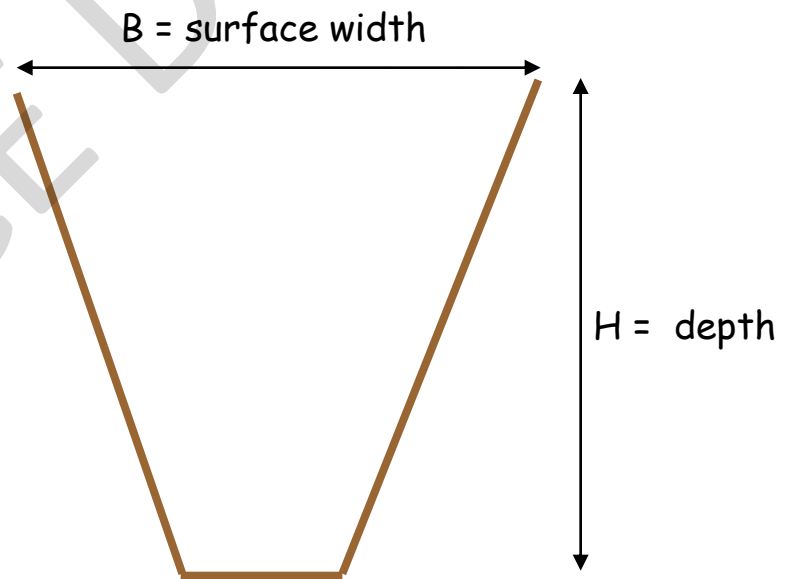
Shape of valley → Type of dam

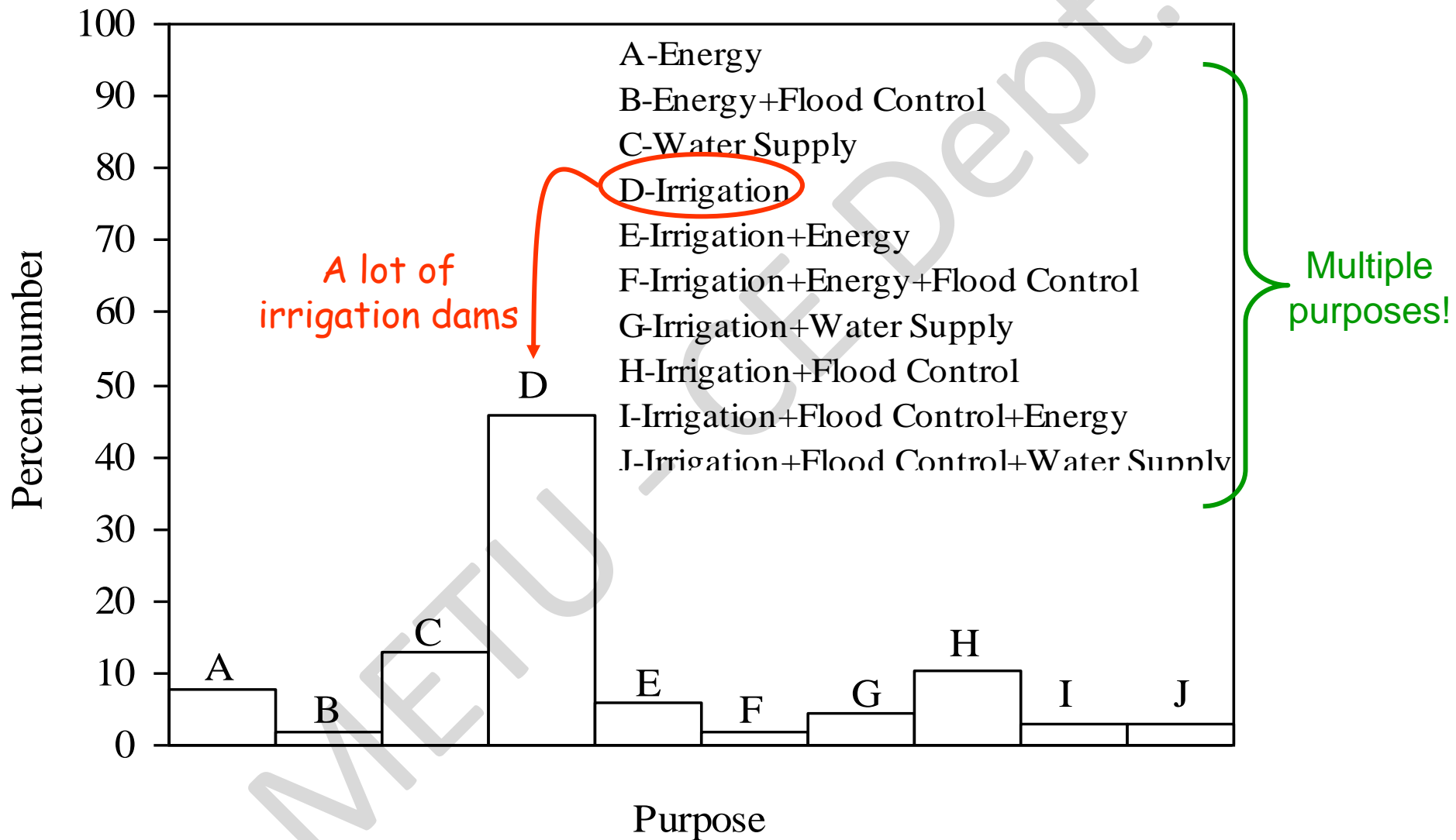
$B/H < 3$ , gorge

$3 \leq B/H \leq 6$ , narrow canyon

$B/H > 6$ , wide valley

Characterized the valley → dam type

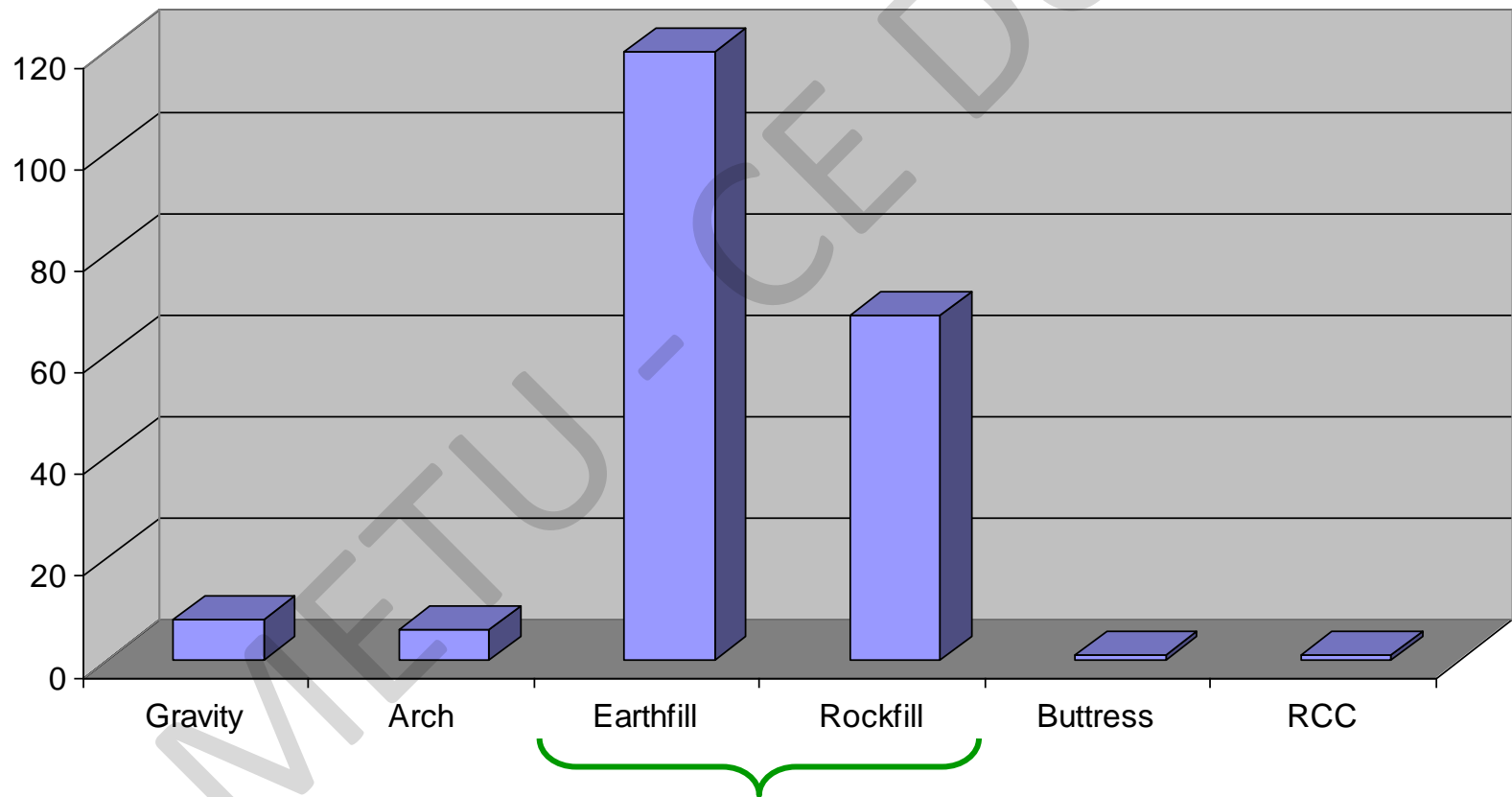






# Statistical values on Turkish Dams (As of 2002)

Number of dams under operation: 204



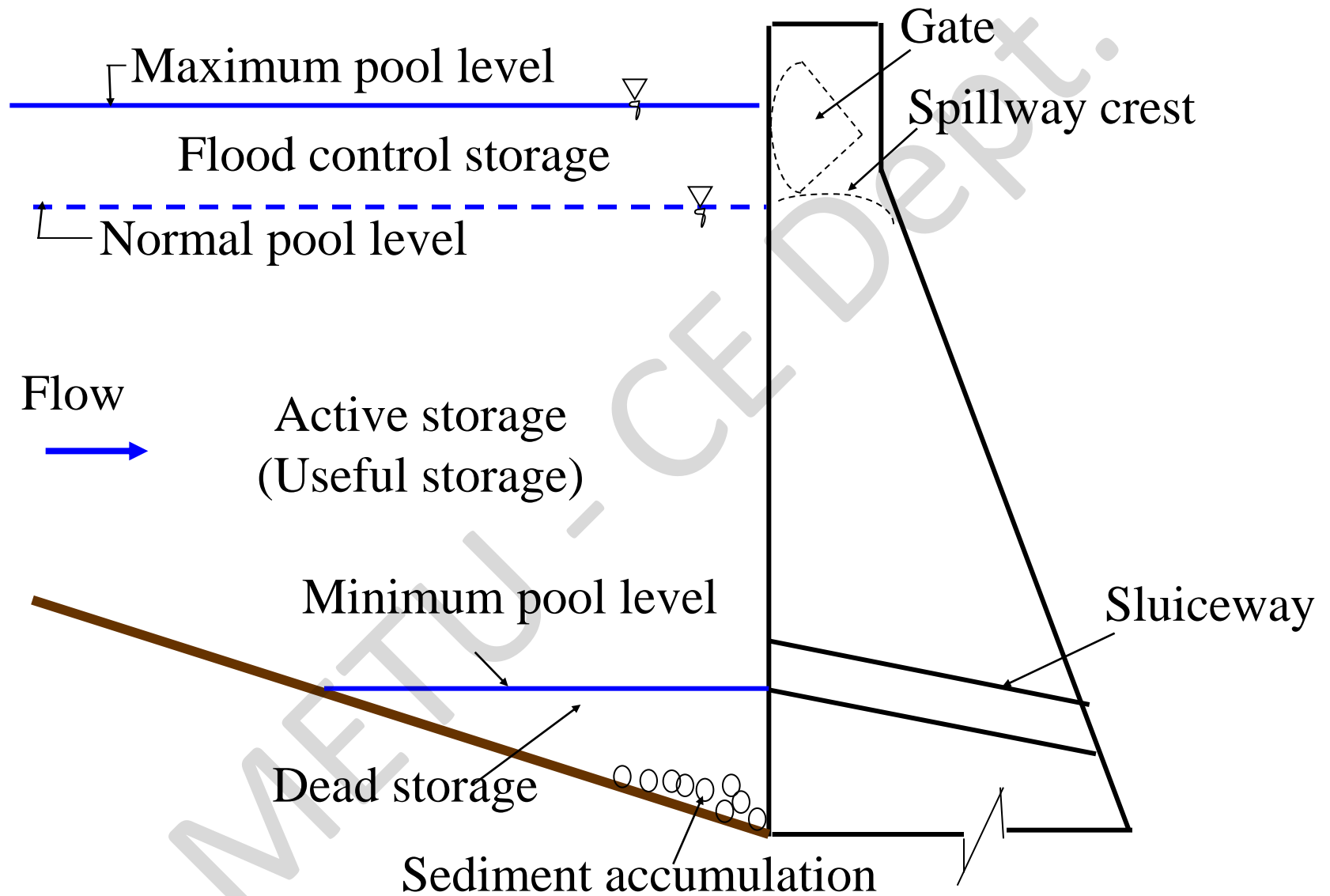
Most of the dams are fill type!



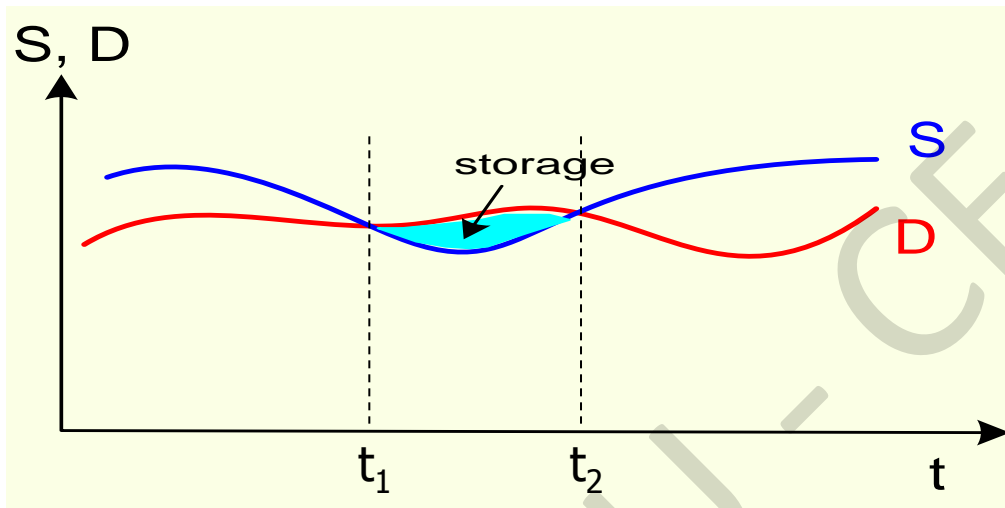
Hasan Uğurlu Dam



**Çamlıdere Dam's  
water intake**

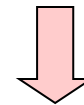


# Reservoir Capacity Determination



S : Supply  
D : Demand  
 $\Sigma S \geq \Sigma D$

Sometimes  $S < D$



Storage is necessary

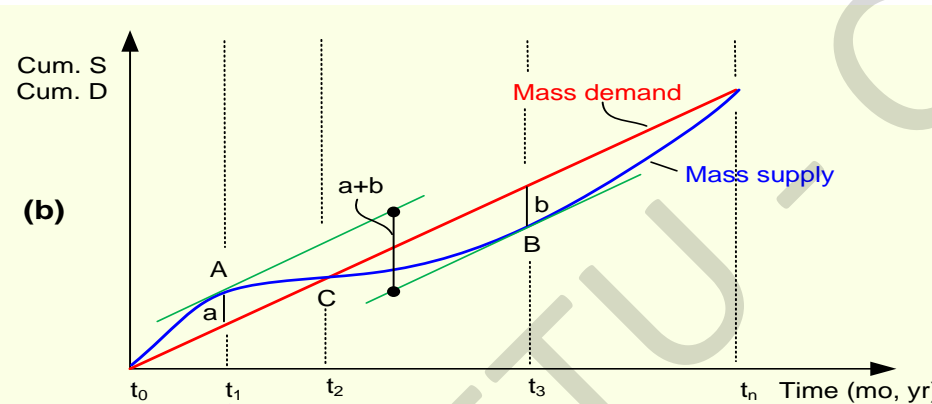
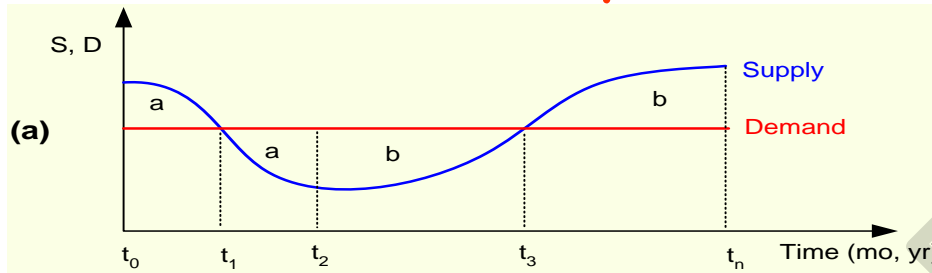
Critical period =  $[t_1, t_2]$

$$\text{Storage} = \int_{t_1}^{t_2} (D - S) dt$$



# Reservoir Capacity Determination

## Mass curve analysis



From  $t_0$  to  $t_1$  reservoir will store a amount of water.  
 Discharge  $S$  at  $t_1 =$  Discharge  $D$  at  $t_1$   
 From  $t_1$  to  $t_2$  the stored amount  $a$  will be used.  
 At  $t_2$  reservoir will be empty.  
 From  $t_2$  to  $t_3$  there will be  $b$  amount of shortage of water.  
 At  $t_3$  the reservoir will start to fill again.  
 At  $t_n$  the reservoir will store  $b$  amount of water.

$$\Sigma S = \Sigma D$$

$S$ : varying  
 $D$ : constant

$$\begin{aligned} t_0 - t_1 &\rightarrow S > D \rightarrow (a) \\ t_1 - t_2 &\rightarrow S < D \rightarrow (a) \\ t_2 - t_3 &\rightarrow S < D \rightarrow (b) \\ t_3 - t_n &\rightarrow S > D \rightarrow (b) \end{aligned} \quad \left. \vphantom{\begin{aligned} t_0 - t_1 &\rightarrow S > D \rightarrow (a) \\ t_1 - t_2 &\rightarrow S < D \rightarrow (a) \\ t_2 - t_3 &\rightarrow S < D \rightarrow (b) \\ t_3 - t_n &\rightarrow S > D \rightarrow (b) \end{aligned}} \right\} (a+b)$$

Critical period =  $[t_1, t_3]$

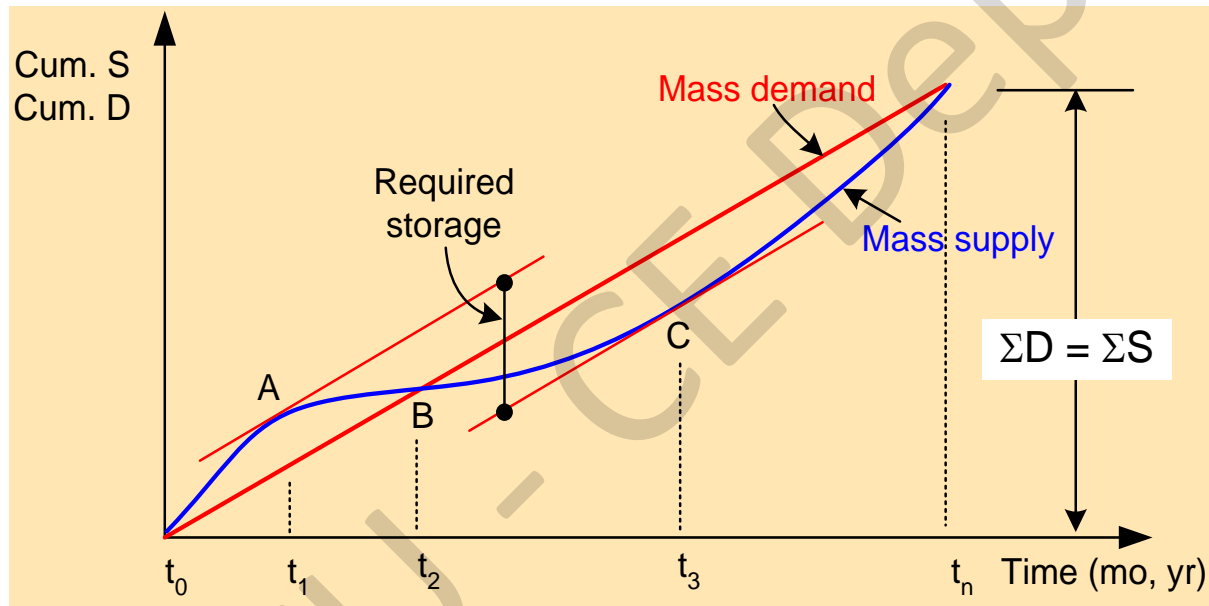
Required storage =  $a + b$

$$\text{Storage} = \int_{t_1}^{t_3} (D - S) dt$$



from second year on  
 there will not be  
 any shortage

# Reservoir Capacity Determination



100 % regulation ( $\Sigma S = \Sigma D$ )

**Example 11** Determine the capacity of storage reservoir with given monthly flows using mass curve analysis. Assume yield is equal to average flow. Also find the monthly contents of the reservoir and monthly changes in the reservoir volume.

a) Tabular solution:

Month	$S_t$ ( $10^6 \text{ m}^3$ )	$D_t$ ( $10^6 \text{ m}^3$ )	$\Sigma S_t$ ( $10^6 \text{ m}^3$ )	$\Sigma D_t$ ( $10^6 \text{ m}^3$ )	$\Sigma S_t - \Sigma D_t$ ( $10^6 \text{ m}^3$ )	Change in res.vol. ( $10^6 \text{ m}^3$ )	Res. content ( $10^6 \text{ m}^3$ )
1	2	3	4	5	6	7	8
Oct.	2,3	5,5	2,3	5,5	- 3,2	-3.2	2.1
Nov.	3,8	5,5	6,1	11,0	- 4,9	-1.7	0.4
Dec.	5,1	5,5	11,2	16,5	- 5,3 *	-0.4	0
Jan.	7,1	5,5	18,3	22,0	- 3,7	1.6	1.6
Feb.	8,2	5,5	26,5	27,5	- 1,0	2.7	4.3
March	11,5	5,5	38,0	33,0	5,0	6	10.3
April	7,2	5,5	45,2	38,5	6,7	1.7	12
May	11,8	5,5	57,0	44,0	13,0 *	6.3	18.3
June	3,5	5,5	60,5	49,5	11,0	-2	16.3
July	1,5	5,5	62,0	55,0	7,0	-4	12.3
Aug.	2,2	5,5	64,2	60,5	3,7	-3.3	9
Sep.	1,8	5,5	66,0	66,0	0,0	-3.7	5.3
S	66	66					

given

$$66/12 = 5.5$$

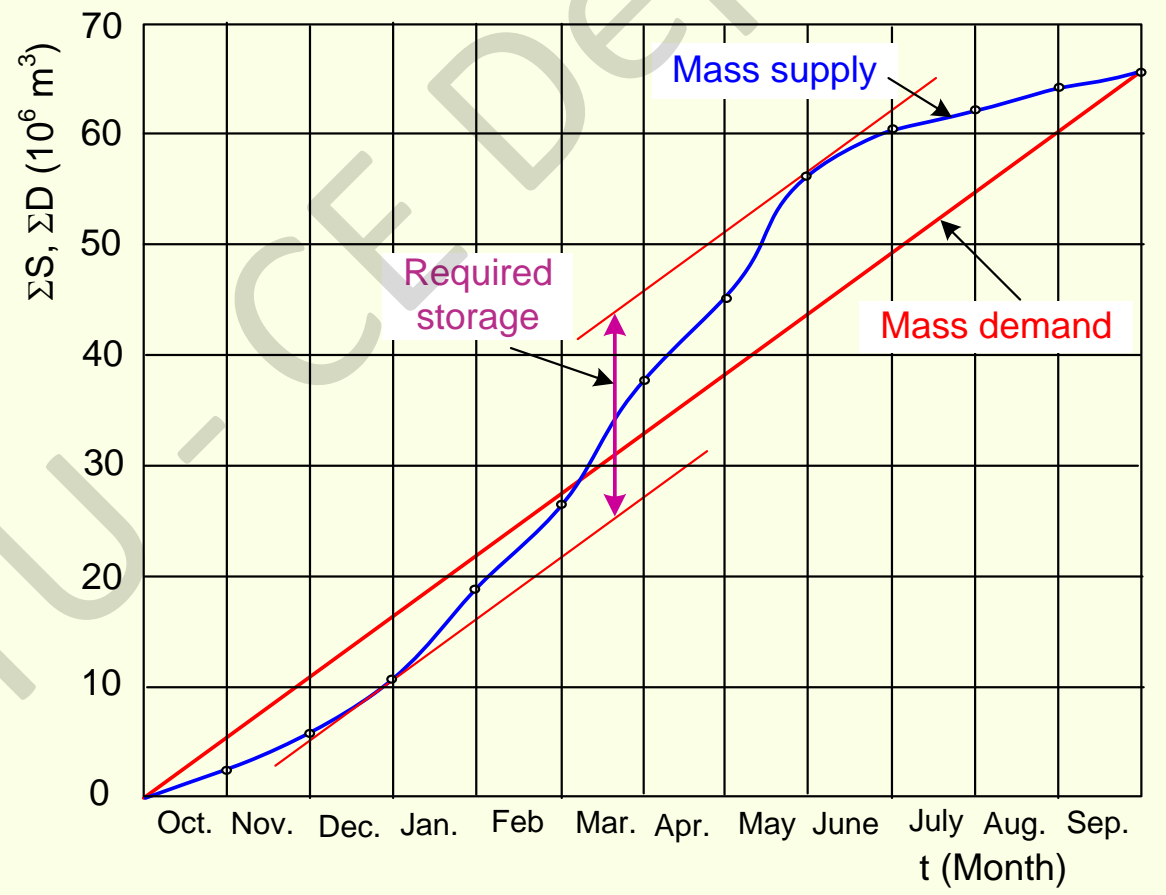
$$S = 5.3 + 13.0 = 18.3 \times 10^6 \text{ m}^3$$

(sum of highest negative and highest positive values in column 6)



## b) Graphical solution

Month	$\Sigma S_t$ ( $10^6 \text{ m}^3$ )	$\Sigma D_t$ ( $10^6 \text{ m}^3$ )
(1)	(2)	(3)
Oct.	2,3	5,5
Nov.	6,1	11,0
Dec.	11,2	16,5
Jan.	18,3	22,0
Feb.	26,5	27,5
March	38,0	33,0
April	45,2	38,5
May	57,0	44,0
June	60,5	49,5
July	62,0	55,0
Aug.	64,2	60,5
Sep.	66,0	66,0



$$S = 18.3 \cdot 10^6 \text{ m}^3$$

## Some examples - people impacted from dam projects in Turkey

	KEBAN	KARAKAYA	ATATÜRK
# of people directly and indirectly impacted	46167	45000	50000
# of families resettled	159	250	344
# of villages impacted	126	105	142 + 1 district

Ref: TRCOLD (1999). Dam Engineering in Turkey, Turkish National Committee On Large Dams, Ankara.

## Planning of dams:

- ④ Reconnaissance surveys  $\Rightarrow$  eliminate infeasible alternatives
- ④ Feasibility study  $\Rightarrow$  select the best dam type & site
  - ✱ Economical &
  - ✱ Technical feasibility
- ④ Planning study  $\Rightarrow$  design the selected alternative
  - ✱ Final design
  - ✱ Operational policy
  - ✱ Management requirements, etc.



## Feasibility study:

- @ estimation of water demand,  $D \rightarrow \text{HARD!}$
  - @ determination of water potential,  $S \rightarrow \text{HARD!}$
  - @ optimal plans,  $D \Leftrightarrow S \rightarrow \text{VERY IMPORTANT}$ 
    - ✱ For ex: If  $D \gg S$  then a large reservoir is required
  - @ determination of dam site
  - @ determination of dam type
  - @ project design  $\rightarrow \text{DIMENSIONS}$
- ✱ foundation conditions
  - ✱ availability of material
  - ✱ spillway type
  - ✱ earthquake zone, etc.

# Feasibility study-Determination of dam site

- @ topography
- @ geologic formation → effect foundation
- @ flood hazard → storage capacity should be sufficient
- @ spillway location & possibilities
- @ climate
- @ diversion facilities
- @ sediment problem → impacts lifetime of the project
- @ water quality → upstream reaches of river are preferable for dams
- @ transportation facilities → locations that require min. cost for road construction
- @ right of way cost → relocation of too many people is NOT GOOD (istimlak bedeli)

narrow valley  
with rock abutments → arch dams

low rolling hills → fill dams

Tf large flood evacuation  
In a rainy climate, construction of an earthfill dam is not easy thus a rockfill dam is preferable

NOT good location for a dam  
due to sedimentation prob.  
construction

# Feasibility study-Project design

## @ Hydrologic design

- ✱ determination of maximum design lake elevation
- ✱ determination of spillway capacity
- ✱ determination of crest elevation of the dam

## @ Hydraulic design

- ✱ determination of static and dynamic loads
- ✱ design of spillway and energy dissipating facilities
- ✱ design of outlet works

## @ Structural design

- ✱ determination of stress distributions
- ✱ determination of required reinforcement
- ✱ structural checks for the body, spillway, and outlet works

Dam break scenarios!





St. Francis Dam (California, USA) → arch dam  
collapsed during a heavy flood (1928)



14 lives  
+  
1 billion \$  
lost

Teton Dam (Idaho, USA) → earhfill dam  
collapsed due to seepage (1976)  
it was 1 year old when collapsed

1. Reconnaissance surveys
2. Feasibility

### 3. Planning study:

- @ topographic surveys → reservoir area-elevation-volume curves are determined
- @ foundation studies → are carried out for seepage, permeability, grouting, etc.
- @ details on materials & constructional facilities → quantity of mat'ls req'd, # and type of construction equipment, etc.
- @ hydrologic study → measurement of rainfall, discharge, temp., etc., a stream-gauging station is established.
- @ reservoir operation study → performed periodically

# Construction of dams

a) evaluation of time schedule & required equipment

- ✱ Coordination of various companies

b) diversion of river flow

- ✱ To provide a dry area for construction

c) foundation treatment

- ✱ Less deformation
- ✱ ↓ permeability & seepage
- ✱ ↑ shearing strength
- ✱ Slope stability for side hills

- ❖ Concrete & rock-fill dams should be adapted for hard formations like rock & granite
- ❖ Earth-fill dams can be chosen for most type of foundation conditions.

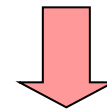
d) formation of dam body



## a) Time schedule & equipment:

- ⌚ map of dam site: 1/500 - 1/5000
- ⌚ the approximate quantities of work
  - ✱ excavation
  - ✱ concrete pouring
  - ✱ filling
  - ✱ explosions
  - ✱ grouting
- ⌚ diversion facilities
- ⌚ urgency of work  $\Rightarrow$  national project !

Various structural units of a dam may be constructed by different companies



coordination is  
**IMPORTANT**

## b) Diversion of river flow

- ⌚ diversion by side tunnel or channel
  - ☀ tunnel - preferable for narrow & stiff valley
  - ☀ channel - preferable for wide valley
- ⌚ two-stage diversion

# A diversion facility is composed of:

## @ a conduit

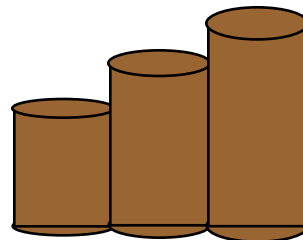
- ✱ a tunnel of a diameter of  $D_{\min} = 3 \text{ m}$  → so that a small truck can fit in
- ✱ a lined trapezoidal channel

## @ upstream and downstream cofferdams

- ✱ embankment
  - homogeneous fill
  - zoned fill

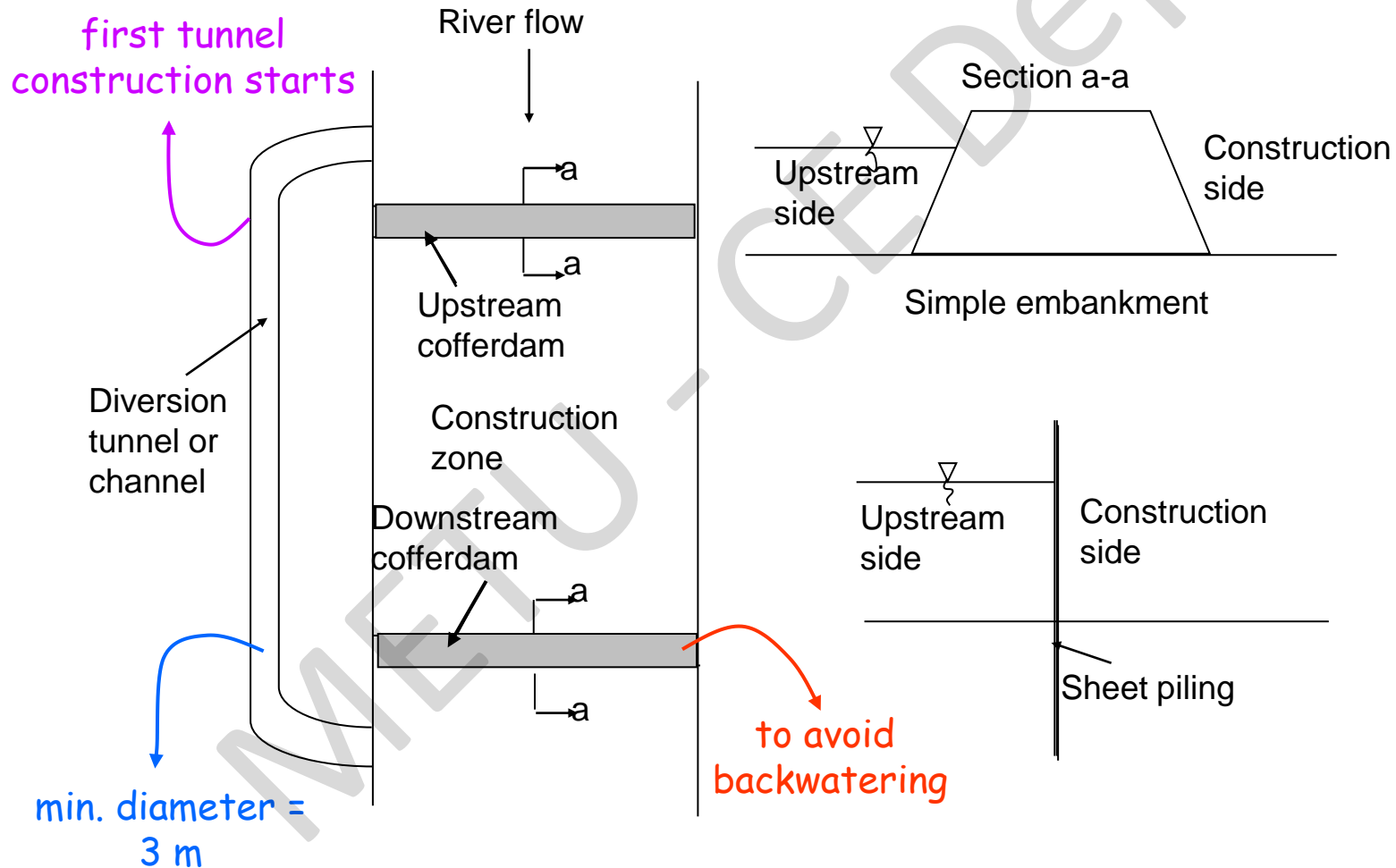
✱ sheet pile

✱ cellular



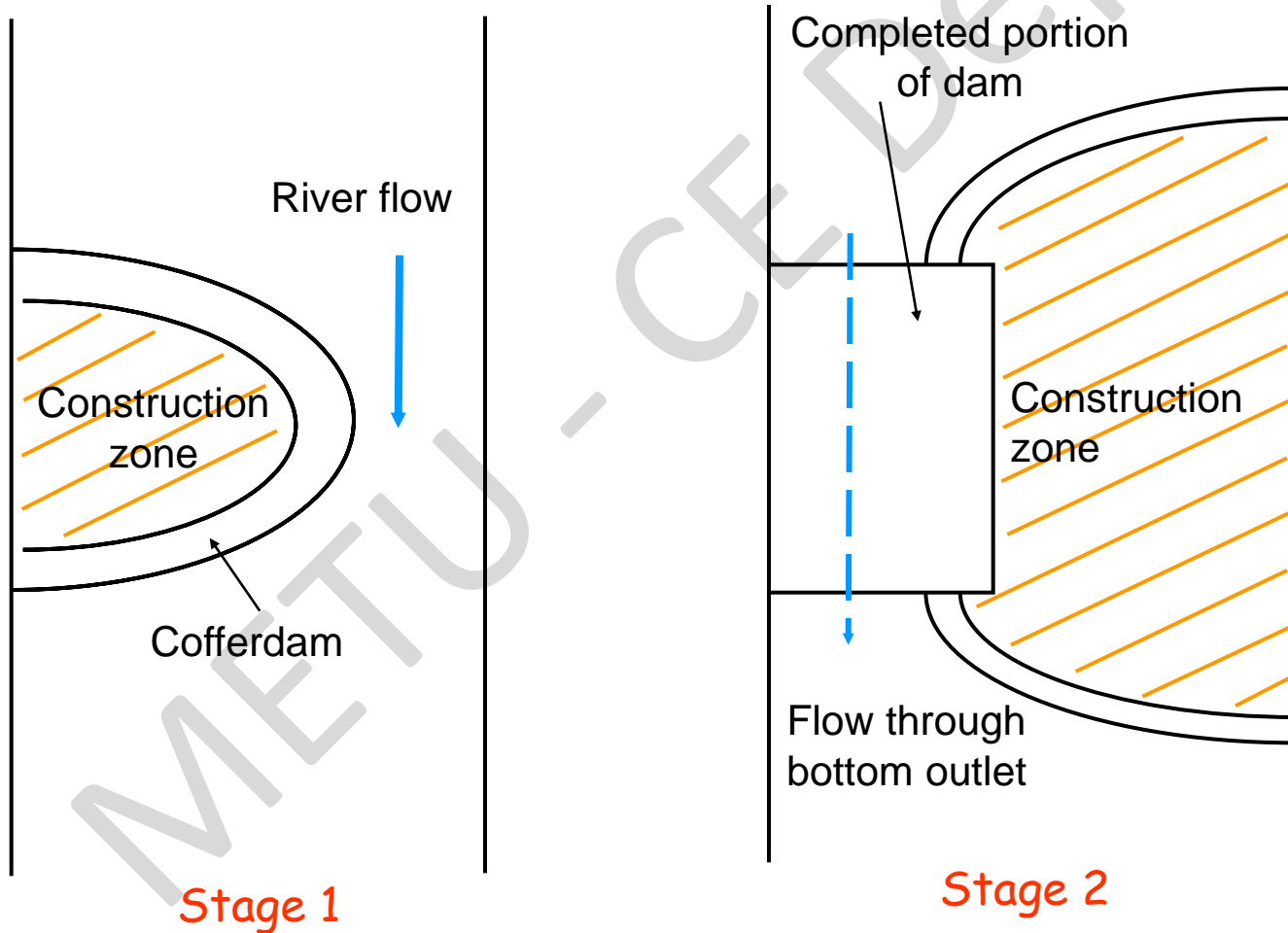
containers filled with earth material

# Diversion by side tunnel or channel





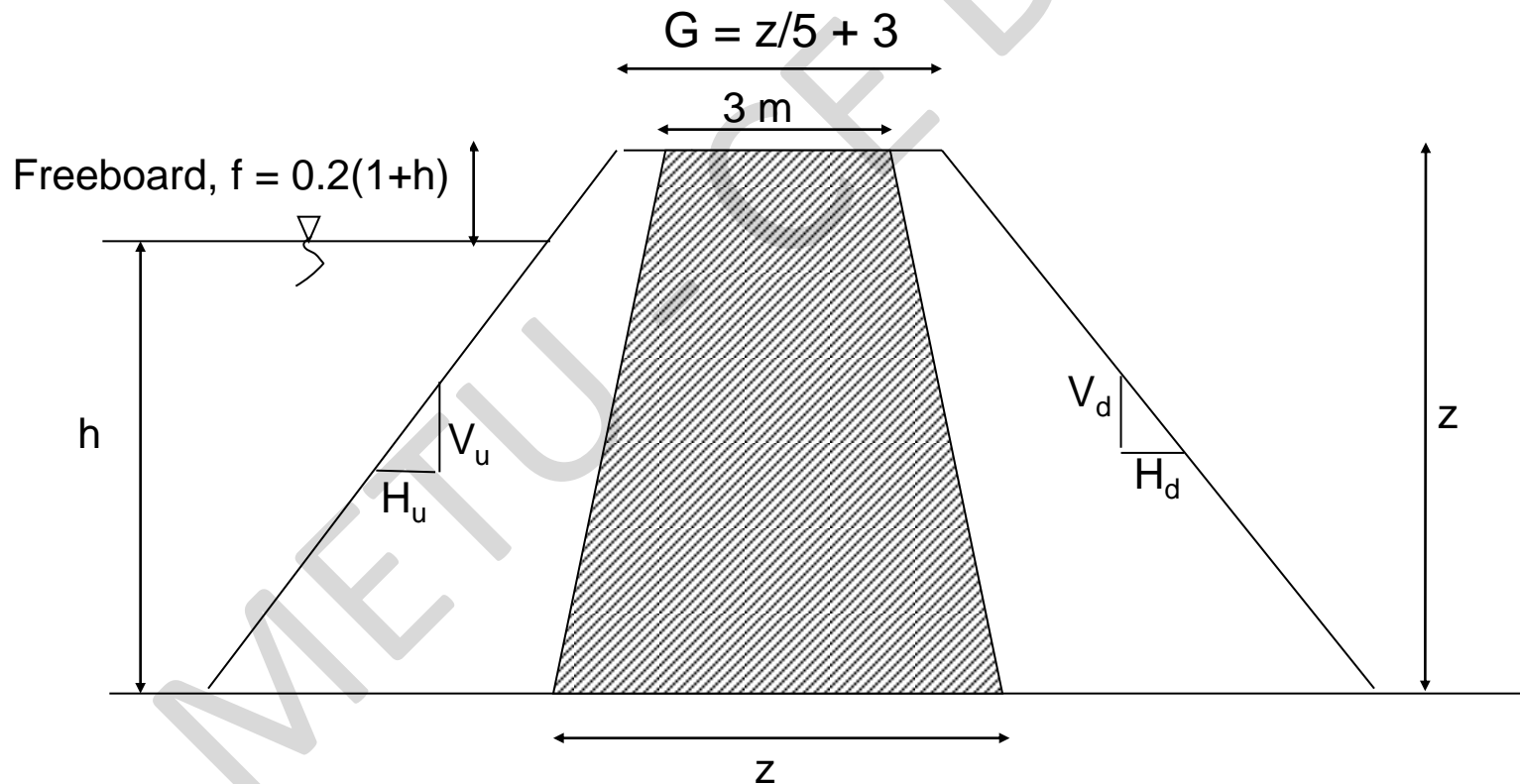
## Two-stage diversion - practiced especially in wide valleys good for concrete dams



# Earth cofferdam on impervious foundation

Generally designed for 20 yr flood

should be constructed  
during low flow season



## c) Foundation treatment

- @ the foundation must be excavated to solid rock before any concrete is poured.
- @ after excavation the cavities or faults in the underlying strata are sealed with concrete or grout.

### a) Clearing:

- ✱ leveling of reservoir site → dam will fill evenly
- ✱ stripping of dam site → increase shear resistance
- ✱ removal of organic material and wastes → avoid taste & odor and also to avoid increase of porosity in embankment dams

# Foundation treatment

## b) Grouting operation:

Grout mix → cement, water & aggregate

Grout mix is injected under pressure (so that the mix will reach deeper regions)

- ✱ to increase the foundation bearing capacity
- ✱ to reduce foundation porosity
- ✱ to solidify the formation underlying the dam & the reservoir

## c) Relief drainage:

- ✱ use of proper drainage facility, e.g. downstream wells



## d) Formation of dam body

- a) **Concrete dams**
- are built of mainly plain concrete to take compressive stresses
  - their own weight resists the forces exerted on them

- @ concrete is poured in isolated blocks of
- \* 1.5 m high
  - \* 15 m long

- @ Care: Minimize heat generation!
- shrinkage  $\Rightarrow$  cracking

- $\Downarrow$
- \* reduced bearing capacity !
  - \* increased seepage !
- $\therefore$  Use of low-heat cement

**Hydration:** process by which cement reacts with water

↓  
Heat is generated

↓  
During dissipation of this heat in long term, the concrete **cools & shrinks**

↓  
May cause cracks

↓  
To meet crack control requirements, placement of concrete is done using monoliths

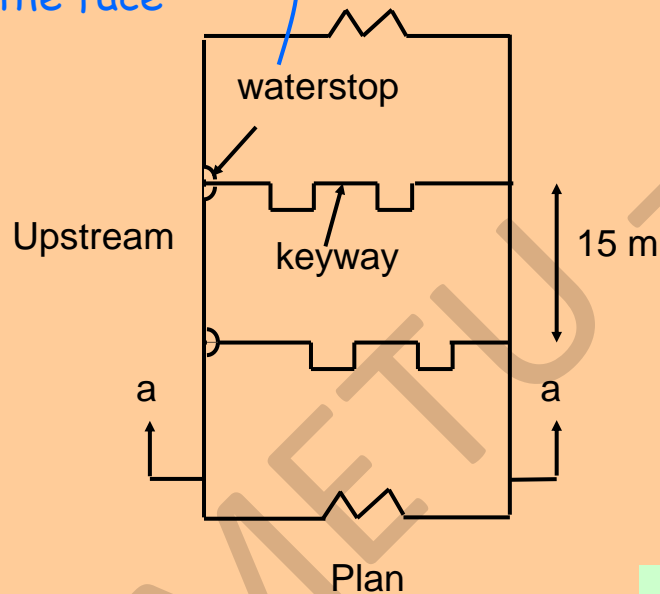
↓  
Individual monoliths are separated by **contraction joints**

## @ Placement technique: **key-trench formation**

- \* foundation

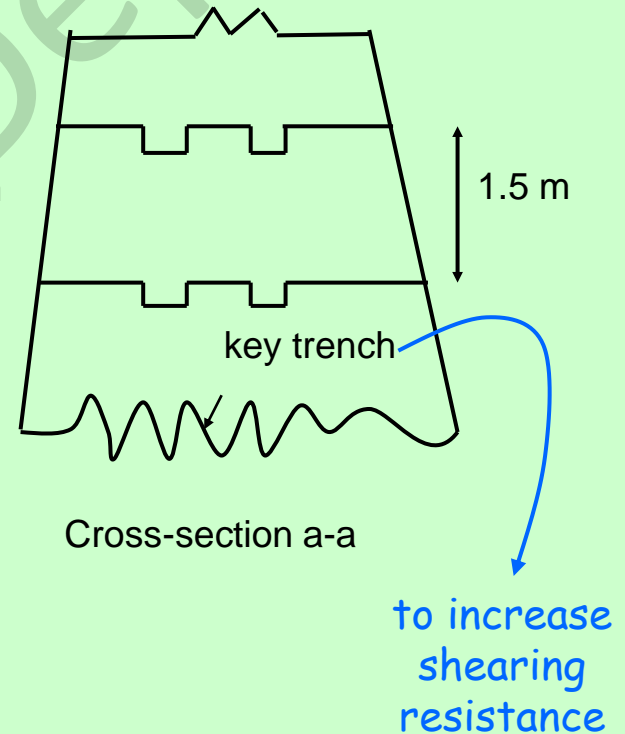
- \* body

used to decrease  
water seepage  
through the face



Not to scale

Upstream



## @ contraction joints

- \* control of internal (temperature) stresses !

## @ Painting lateral surfaces causes elimination of adherence of adjacent blocks

Concrete is a brittle material & is susceptible to cracking due to its low tensile strength



## @ Implementation of

- \* Waterstops } stresses due to shrinkage & seepage control
- \* Inspection galleries } temperature drop in mass concrete,
- \* Internal drainage facilities } concrete dams are built as assemblages of monoliths separated by contraction joints

## b) Prestressed concrete dams: (tension + compression)

- ② prefabricated elements of pre-tensioned bars  
prestressing elements minimize the tensile stresses in the concrete

## c) RCC dams: (compression)

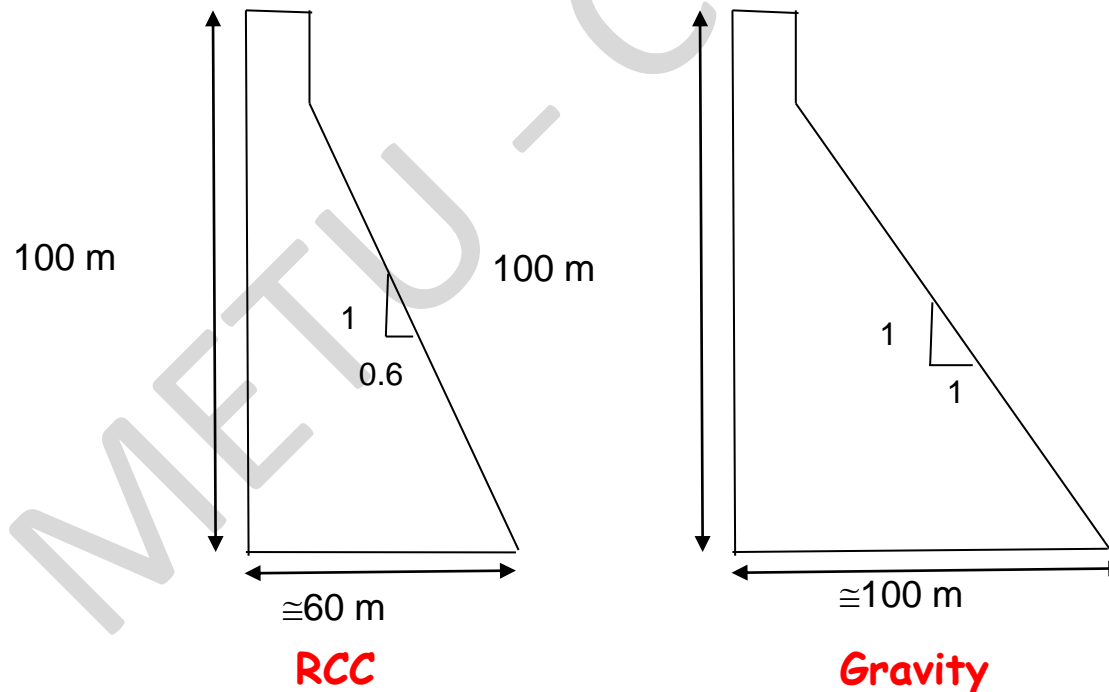
- ② Preparation of a rather dry mix composed of
  - \* limited cement → decreases cost
  - \* fine & coarse aggregate → coarse agg. from explosions
  - \* fly ash → reduces generation of heat during settling of concrete  
→ less shrinkage & cracking
  - \* limited water → dry mix
- ② Pouring this mix in  $\approx 20 - 45$  cm layers
- ② Compaction of layers by static or vibrating rollers



# Advantages of RCC over Conventional Concrete Gravity:

## @ Economical

- ☀ use of coarse aggregate and limited cement
- ☀ specific weight of RCC is high  $\rightarrow$  less volume of concrete required wrt conventional concrete gravity dam



- @ Greatly reduced heat generation during setting (fly ash)



minimized shrinkage problem



no need for vertical contraction joints

- @ Shorter construction duration than other types !

## c2) Recent developments: Hardfill dams

- ✱ Requires symmetrical cross-section → more stable but more material thus more expensive
- ✱ Very little or no binding material is used thus cheaper

## d) Earth fill dams - more than 50% earth material

### @ Placement of fill material composed of

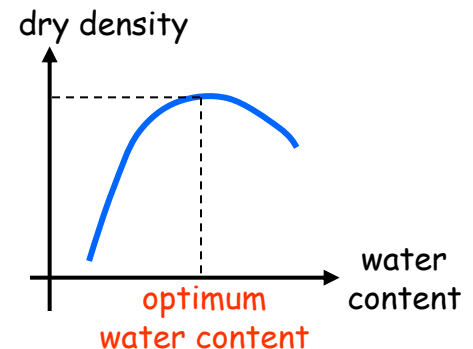
- ☀ non-organic soil → decay causes porosity to increase
- ☀ non-plastic to low-plasticity soil → to avoid deformation

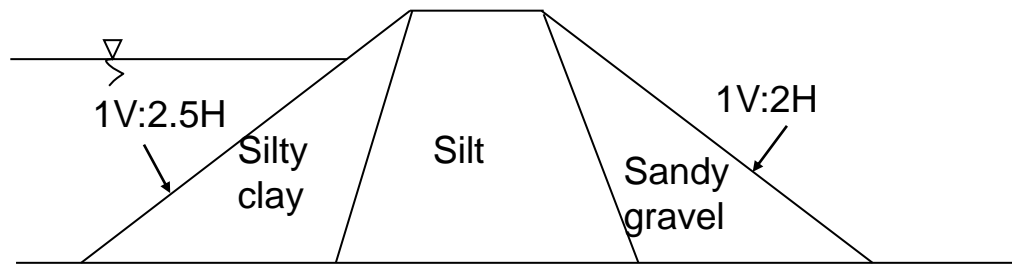
### @ Compaction of layers of $\approx 50$ cm using sheep-foot rollers (fine aggregate) or vibrating rollers (coarse aggregate)

- ☀ to increase compressive & shear strength and
- ☀ to decrease voids

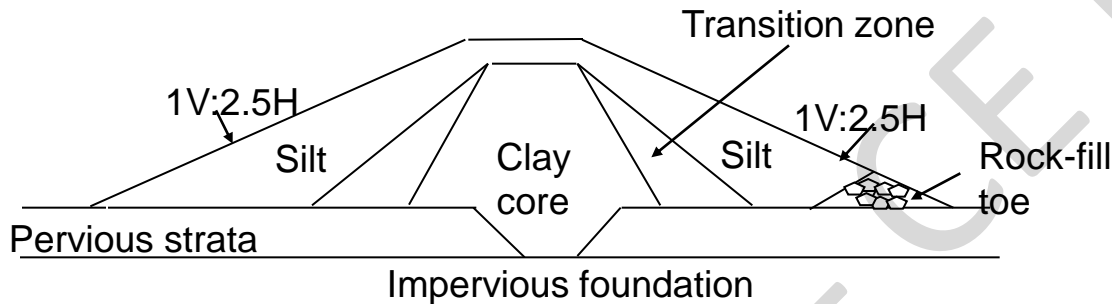
### @ Compaction under optimum moisture content

→ To obtain max. dry density for a desired compaction

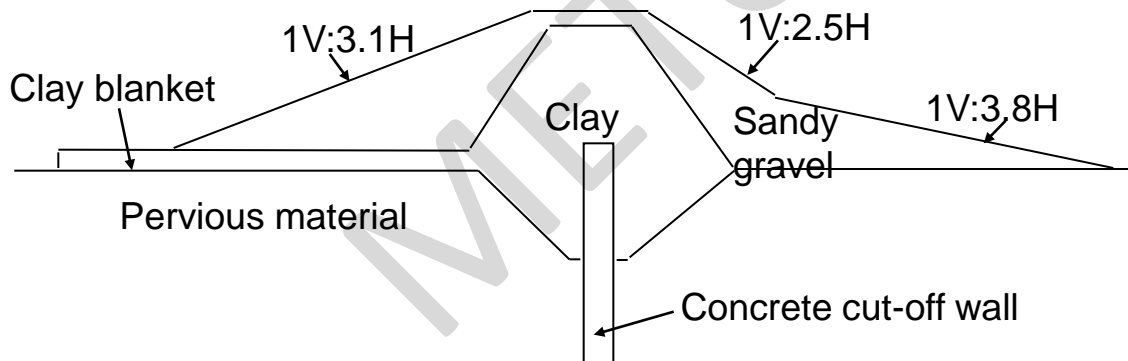




(a) Simple zoned embankment



(b) Earth dam with core extending to impervious foundation



(c) Earth dam on pervious foundation

- ☀ mass of the dam that will make it
- ☀ clay ← low permeability
- ☀ gravel particles can be introduced into clay core to increase the shear strength of the core
- ☀ erosion protection at the **UPSTREAM FACE**



# Slope stability

- ⊙ choose proper side slopes for no sliding
- ⊙ take proper slope-protection remedies:
  - ☀ **Upstream face:** protect against wave induced erosion
    - ▣ use rock/rip-rap or concrete
    - ▣ rip rap → to decrease water erosion by dissipating the energy of the waves
  - ☀ **Downstream face:** protect against wind/rainfall erosion
    - ▣ use grass, but not trees since big rooted plants increase seepage

## e) Rock-fill dams - more than 50% is rock

- @ Formation of core and filter is similar to earth-fill dam!
- @ Compaction of saturated rock → better than just dumping because compaction provides better interlocking
- @ **PROBLEM:** Subject to considerable settlement ← dam is heavy



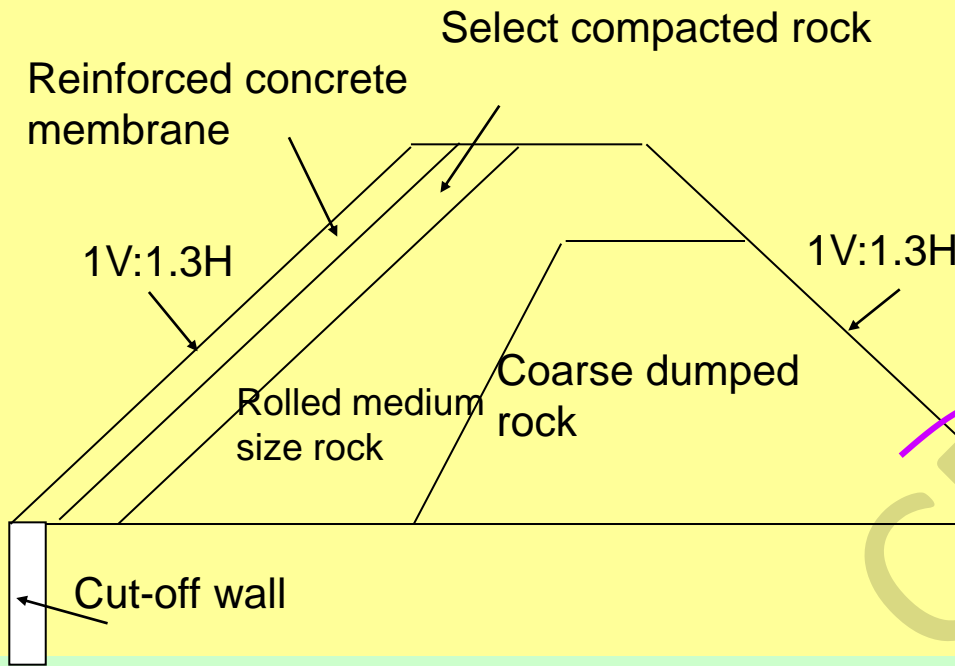
Cracking of membrane



periodic repair

## e) Rock-fill dams - more than 50% is rock

- ⌚ Steeper side slopes than earth-fill dam → less material
- ⌚ Rigid foundation conditions are required!
- ⌚ Speedy construction, easy to increase crest elevation
  - ✱ in a rainy region rock-fill may be preferable
- ⌚ Normally cheaper than a concrete gravity dam if proper material and equipment are available

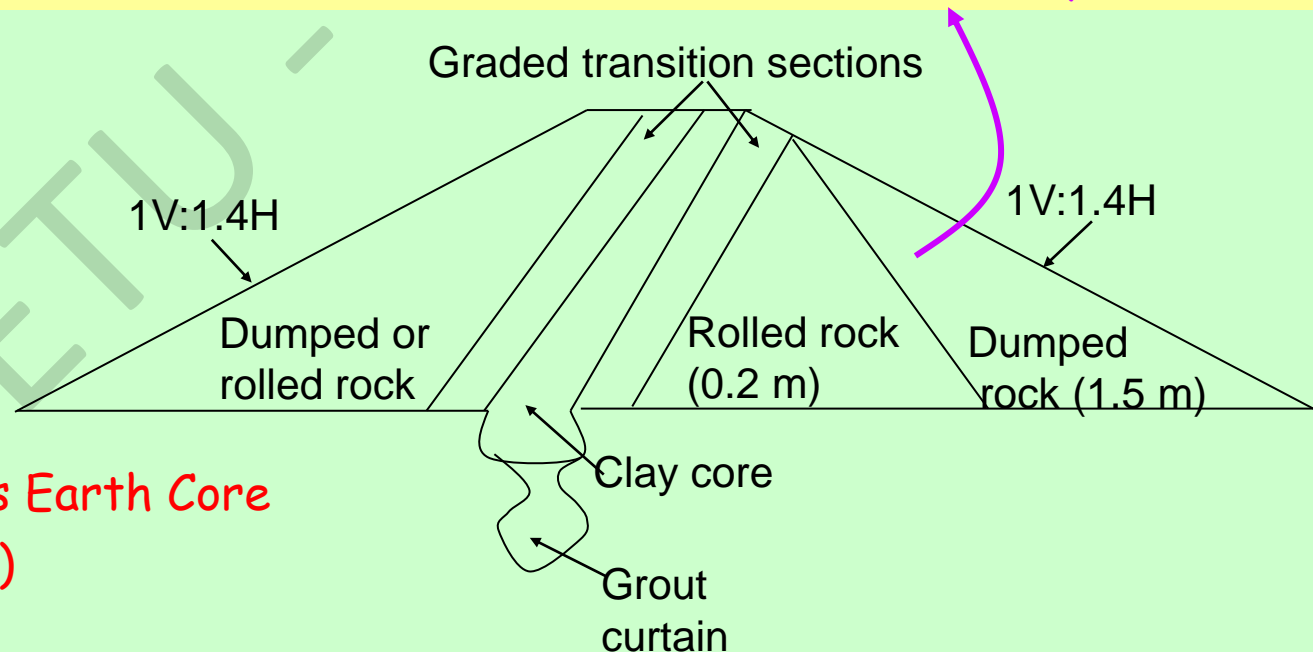


To control seepage through rock-fill dams:

a) **Impervious Face**  
(R/C Membrane, Asphalt Facing, etc.)

*dumped rock to increase weight of the dam (to increase stability)*

b) **Impervious Earth Core**  
(Conventional)



Concrete gravity dams → Proportioned such that its own weight resists the forces exerted upon it

Gravity load satisfies the stability  
(its own weight)

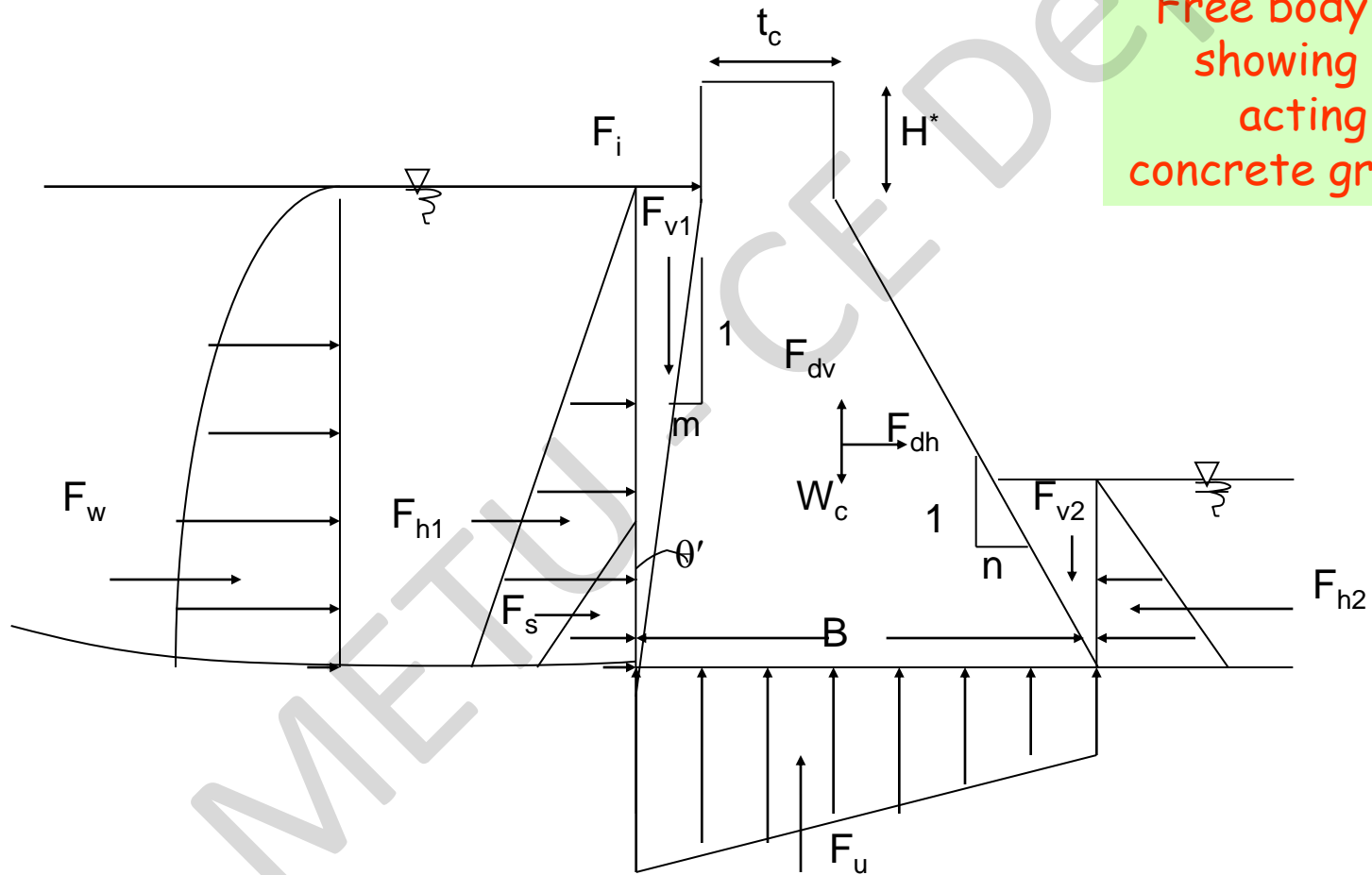
Designed to

- ⊙ take compressive stresses only
- ⊙ be safe under all loading conditions against
  - ✱ overturning
  - ✱ shear and sliding
  - ✱ stresses in the body and at foundation

dimensions are chosen  
s.t. only compressive  
stresses develop under  
all loading conditions.



## Forces acting on a concrete gravity dam



Free body diagram  
showing forces  
acting on a  
concrete gravity dam

- Weight of dam - acts at center of gravity of the dam

$$W_c = \gamma_c V$$

specific weight of concrete

body volume

- Hydrostatic forces

$$F_{h1} = \frac{1}{2} \gamma h_1^2$$

$$F_{v1} = \frac{1}{2} \gamma m h_1^2$$

- Uplift force

$$F_u = \left[ h_2 + \frac{\phi}{2} (h_1 - h_2) \right] B \gamma$$

uplift reduction coefficient

Ex: If uplift forces reduction is 40%  
due to installation of drains, then  
 $\phi = 1 - 0.4 = 0.6$

- ⊙ Lateral earth force - acts at  $h_s/3$  above reservoir bottom

$$F_s = \frac{1}{2} \gamma_s h_s^2 K_a$$

active earth pressure coeff.

specific weight of sediment

- ⊙ Earthquake force on the dam body - acts at center of gravity of the dam

$$F_{dh} = k_h W_c \quad F_{dv} = k_v W_c$$

earthquake coeff.s

- ⊙ Dynamic force in the reservoir - acts at a distance  $0.412h_1$  above reservoir bed

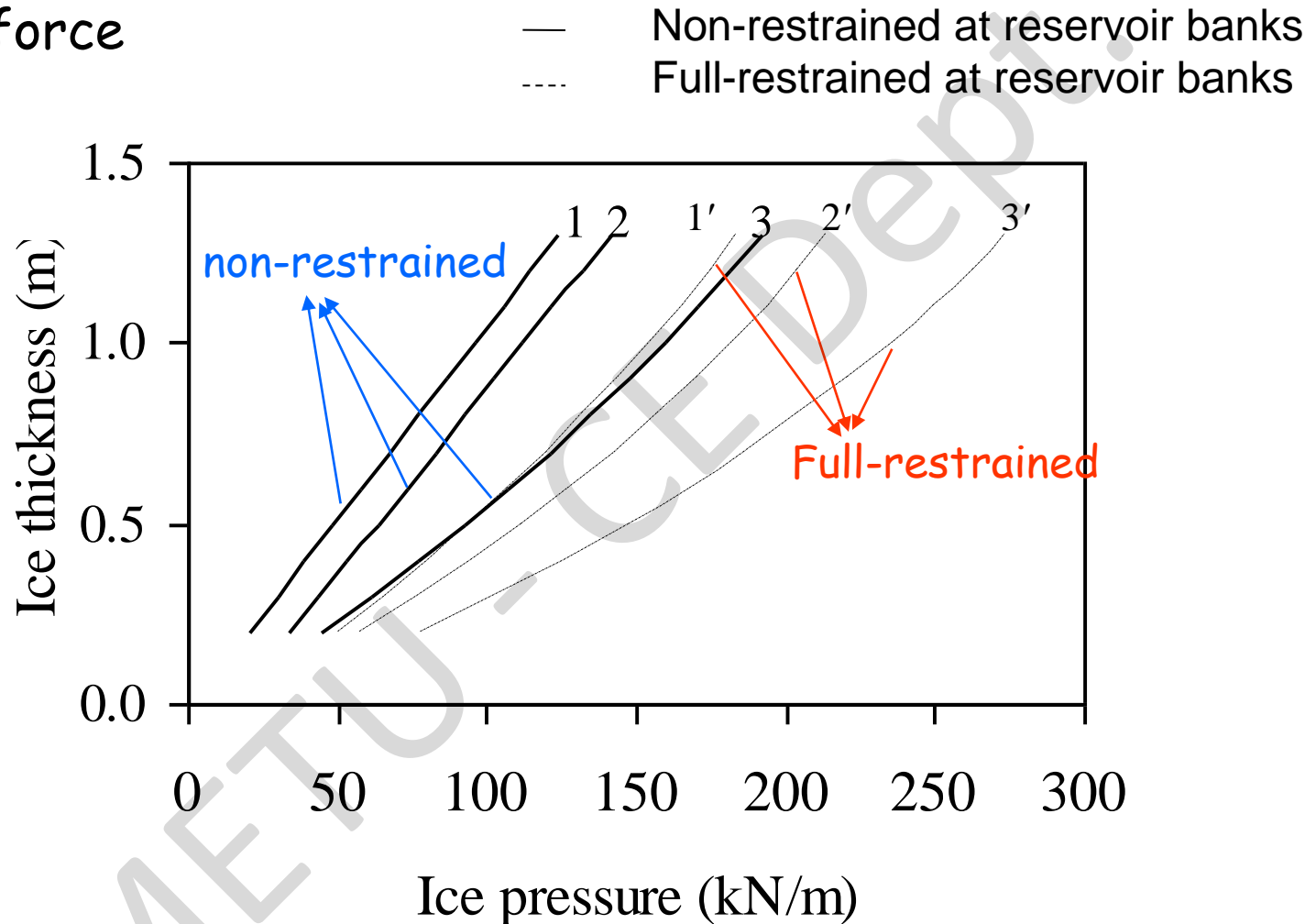
Full case

Empty case

$$F_w = 0.726 C k \gamma h_1^2$$

$$C = 0.7 \left( 1 - \frac{\theta'}{90} \right)$$

## @ Ice force

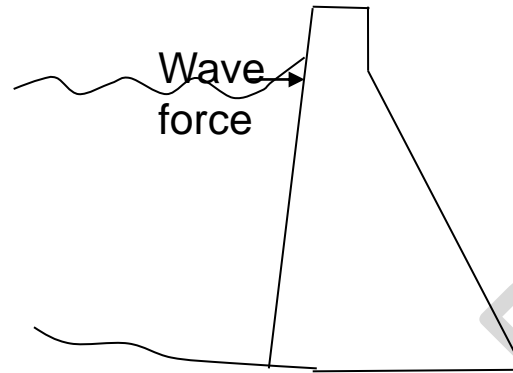


1- Temperature rising at  $2.8^{\circ}/\text{hr}$

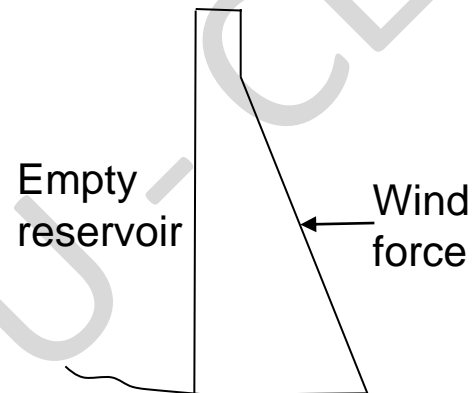
2- Temperature rising at  $5.6^{\circ}/\text{hr}$

3- Temperature rising at  $8.4^{\circ}/\text{hr}$

## @ Wave forces



## @ Wind forces



## @ Dynamic forces on spillways, $\Sigma F = \rho Q \Delta u$

$Q$  = flow rate over spillway  
 $\Delta u$  = change in velocity  
 $\rho$  = density of water



# Loading combinations

Stability analysis are conducted for various loading conditions & dam must prove its safety under all loading conditons.

## 1) Usual loading

- ④ hydrostatic forces at normal operating level ( $F_h$ ,  $F_v$ )
- ④ uplift force ( $F_u$ )
- ④ temperature stresses
- ④ dead loads ( $W_c$ )
- ④ ice load ( $F_i$ )
- ④ silt load ( $F_s$ )

## 2) Unusual Loading - flood condition

- ⌚ hydrostatic forces at full upstream level ( $F_h, F_v$ )
- ⌚ uplift force ( $F_u$ )
- ⌚ temperature stresses
- ⌚ dead loads ( $W_c$ )
- ⌚ silt load ( $F_s$ )

## 3) Extreme or Severe Loading

- ⌚ forces in usual loading + earthquake forces

# Requirements for stability

A dam may fail by

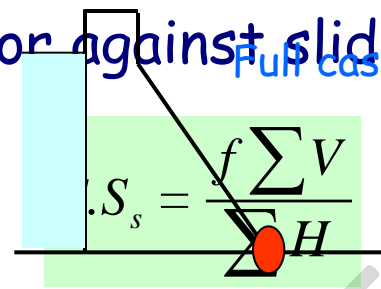
- ④ Overturning
  - Rotation about the toe
- ④ Sliding
  - Sliding over a horizontal plane
- ④ Combined shear and sliding
  - Failure of the material
- ④ Stresses

@ Safety factor against overturning:

$$F.S_o = \frac{\sum M_r}{\sum M_o}$$

→ Total resisting moment about the toe  
→ Total overturning moment about the toe

@ Safety factor against sliding:



$$F.S_s = \frac{f \sum V}{\sum H}$$

$f$  = coefficient of friction  
 $\sum V$  = sum of vertical forces  
 $\sum H$  = sum of horizontal forces

for empty case take  
moments wrt the toe

for empty case take  
moments wrt the heel

@ Safety factor against shear-sliding:

$$F.S_{ss} = \frac{f \sum V + r A \tau_s}{\sum H}$$

sliding      shear

$A$  = area of the shear plane  
 $\tau_s$  = shear strength of concrete  
 $r$  = factor to express the max. allowable average shear stress

## @ Stresses:

$$\sigma = \frac{\sum V}{A} \pm \frac{Mc}{I}$$

normal stress

bending stress

vertical normal stress

net moment about the center of base

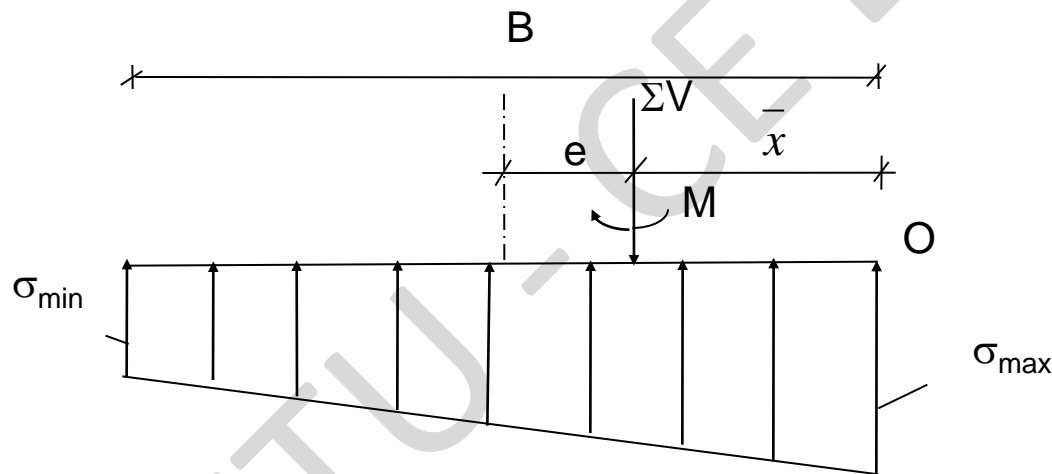
$$M = \sum Ve$$

$$e = \frac{B}{2} - \bar{x}$$

$$c = \frac{B}{2}$$

$$I = \frac{B^3}{12}$$

moment of inertia



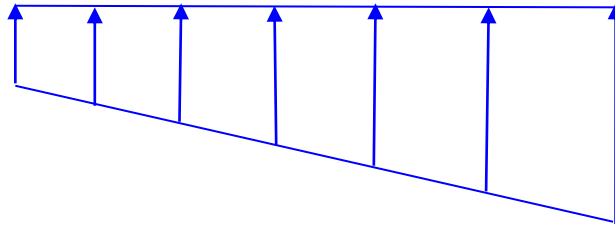
minimum normal stress per unit width

$$\sigma_{\min} = \frac{\sum V}{B} - \frac{\sum V * e * B/2}{B^3/12} = \frac{\sum V}{B} \left( 1 - \frac{6e}{B} \right) \geq 0$$

in order to obtain compressive stresses the min. pressure should be  $\geq 0$

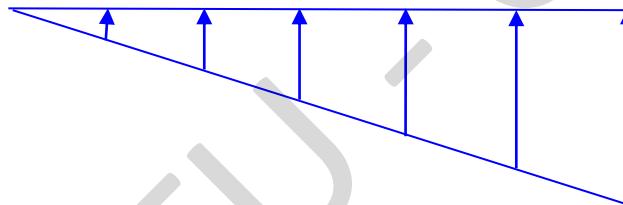


@  $e < B/6 \Rightarrow$  Compression

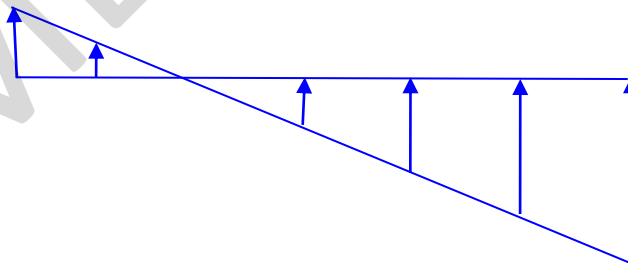


$$\frac{\sum V}{B} \geq 0 \quad \text{or} \quad 1 - \frac{6e}{B} \geq 0$$
$$1 \geq \frac{6e}{B}$$
$$\frac{B}{6} \geq e$$

@  $e = B/6 \Rightarrow$  Triangular distribution



@  $e > B/6 \Rightarrow$  Tension ( $\sigma_t \approx (5-10)\%$  of  $\sigma_{ac}$ )



Tensile strength is approximately  
5-10% of the compressive strength

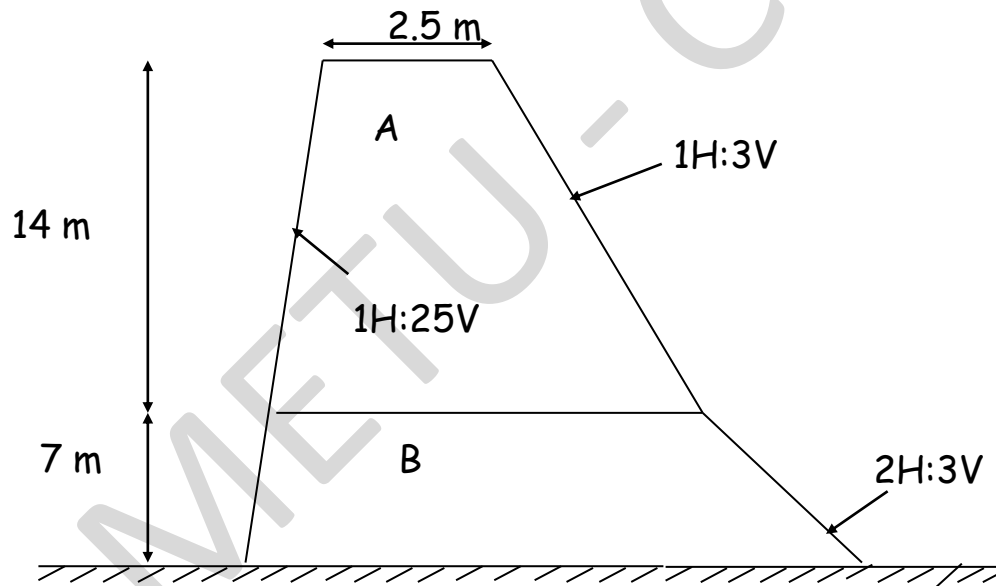
# Safety criteria

Loading	$F.S_s$	$F.S_o$	$F.S_{ss}$	$\sigma_{max}$	
Usual	$\geq 1.5$	$\geq 2.0$	$\geq 3.0$	$\leq \sigma_c/3.0$	$\leq \sigma_f/4.0$
Unusual	$\geq 1.2$	$\geq 1.5$	$\geq 2.0$	$\leq \sigma_c/2.0$	$\leq \sigma_f/2.7$
Extreme	$> 1.0$	$\geq 1.2$	$\geq 1.0$	$\leq \sigma_c$	$\leq \sigma_f/1.3$

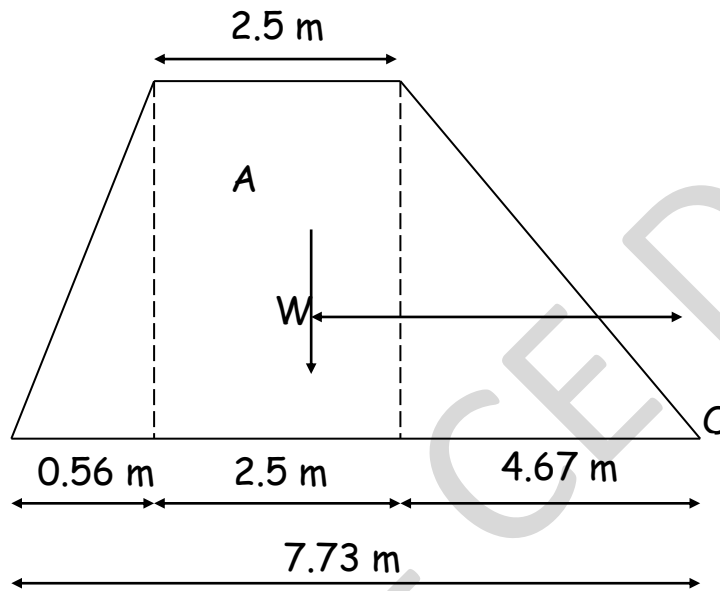
compressive strenght  
of concrete

compressive strenght  
of foundation

**Example 12** A cross-section of a concrete gravity dam is shown in Figure 3.42. Analyze the stability of block A for full and empty upstream reservoir cases, separately. Ignore earthquake, silt, and ice forces. Specific weights of concrete and water are  $23 \text{ kN/m}^3$  and  $10 \text{ kN/m}^3$ , respectively. Compressive and shear strengths of concrete are  $35000 \text{ kN/m}^2$ , and  $6000 \text{ kN/m}^2$ , respectively. The coefficient of friction between concrete blocks is 0.65. There is no tailwater in the downstream. Required safety factors can be taken as those of a usual loading.



a) Empty reservoir case: Free-body diagram for block A is shown below



In case of empty upstream reservoir, since there is no horizontal force acting on block A, such as earthquake force, the block will be infinitely safe against sliding and overturning. However, the stresses in concrete should be checked. The weight of the block is

$$W = (0.5 \times 0.56 + 2.5 + 0.5 \times 4.67) \times 14 \times 23 = 1647.03 \text{ kN/m.}$$

Point of application of  $W$  with respect to point  $O$  in Figure 3.43 is computed as

$\bar{x} = 4.72$  m. The eccentricity of  $W$  around the center of the base is

$$e = 4.72 - \frac{7.73}{2} = 0.86\text{m}$$

Since  $e = 0.86 \text{ m} < B/6 = 1.29$ , compressive stresses develop at the base of block A. Values of  $c$  and  $I$  are as follows:

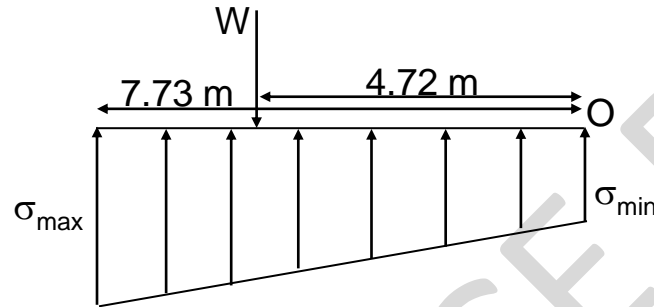
$$c = 7.73 / 2 = 3.87 \text{ m and } I = (7.73)^3 / 12 = 38.49 \text{ m}^3$$

$$M = W * e = 1647.03 * 0.86 = 1416.4 \text{ kN.m /m.}$$

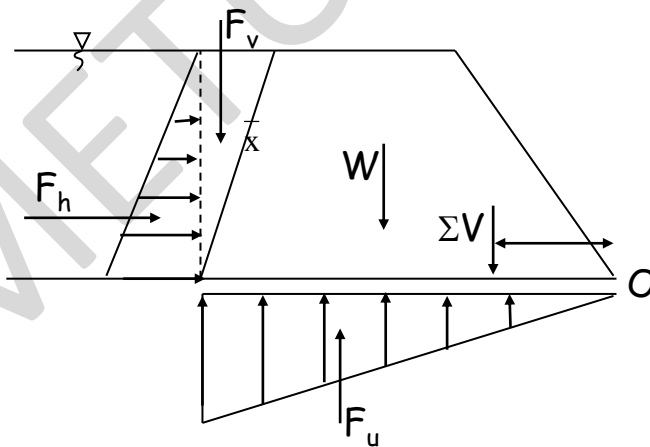
$$\sigma = \frac{1647.03}{7.73} \pm \frac{1416.4 * 3.87}{38.49} = 213.07 \pm 142.41$$



$\sigma_{\max} = 355.48 \text{ kN/m}^2 \ll 35000 \text{ kN/m}^2$ . For usual loading,  $\sigma_{\max} < \sigma_c/3 = 11166.7 \text{ kN/m}^2$  and  $\sigma_{\min} = 70.66 \text{ kN/m}^2 > 0$ , O.K. So, block A is safe for empty reservoir case. Note that the major principle compressive stresses at the upstream and downstream faces are also acceptable. A linear stress distribution is assumed at the base



b) Full reservoir case: For a conservative approach, it is assumed that water might seep through joints and possible cracks in the concrete and exert internal hydrostatic pressures. Therefore, uplift pressures in the dam body should be considered at any level below the reservoir water surface. A free-body diagram is shown



$$F_h = 0.5 \cdot 10 \cdot (14)^2 = 980 \text{ kN/m}$$

$$F_v = 0.5 \cdot 14 \cdot 0.56 \cdot 10 = 39.2 \text{ kN/m}$$

$$F_u = 0.5 \cdot 10 \cdot 14 \cdot 7.73 = 541.1 \text{ kN/m.}$$

Overtaking moments about the toe:

$$\Sigma M_o = 980 \cdot (14/3) + 541.1 \cdot (2/3) \cdot 7.73 = 7361.8 \text{ kN.M/m}$$

Resisting moments about the toe:

$$\Sigma M_r = 1647.03 \cdot 4.72 + 39.2 \cdot 7.54 = 8069.55 \text{ kN.m/m.}$$

$$F.S_o = \frac{\Sigma M_r}{\Sigma M_o} = \frac{8069.55}{7361.8} = 1.1 < 2.0 \quad \text{NOT O.K.}$$

$$\Sigma V = W + F_v - F_u = 1647.03 + 39.2 - 541.1 = 1145.13 \text{ kN/m.}$$

$$\Sigma H = F_h = 980 \text{ kN/m.}$$

$$F.S_{ss} = \frac{0.65 \cdot 1145.13 + 0.33 \cdot 7.73 \cdot 6000}{980} = 16.4 > 3.0 \quad \text{O.K.}$$

$F.S_s = 0.76 < 1.5$ , NOT O.K. Net moment:

$$\Sigma M = \Sigma M_r - \Sigma M_o = 707.75 \text{ kN.m/m.}$$

Point of application of  $\Sigma V$  with respect to toe:

$$\bar{x} = \frac{\Sigma M}{\Sigma V} = \frac{707.75}{1145.13} = 0.62m \quad e = \frac{7.73}{2} - 0.62 = 3.25m$$

$$e > 7.73 / 6 \text{ (tension)}$$

$$M = \Sigma V.e = 1145.13 * 3.25 = 3721.7 \text{ kN.m/m.}$$

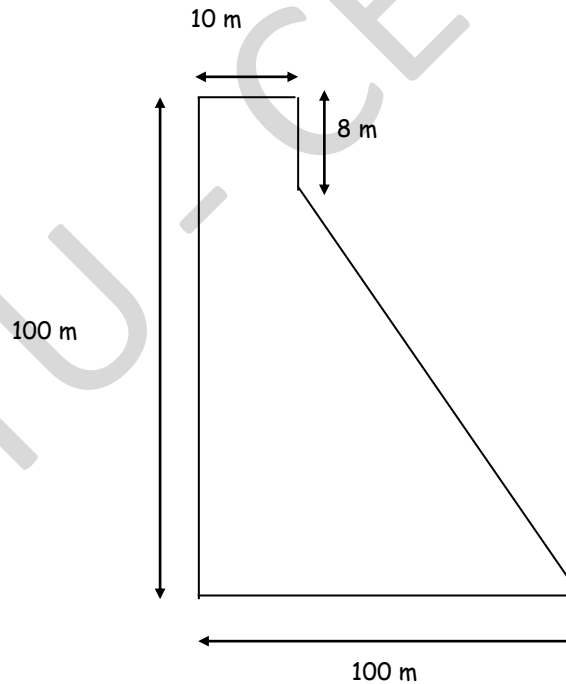
$$\sigma = \frac{1145.13}{7.73} \pm \frac{3721.7 * 3.87}{38.49} = 148.14 \pm 374.2$$

$$\sigma_{\max} = 522.34 \text{ kN/m}^2 < 11166.7 \text{ kN/m}^2, \sigma_{\min} = -226.06 \text{ kN/m}^2 < 0, \sigma_{\min} < \sigma_t, \text{ O.K.}$$

where  $\sigma_t$  is the tensile strength. Block A, and hence the dam, is not stable when the reservoir is full. Dimensions may be increased or measures may be taken to reduce the uplift force.

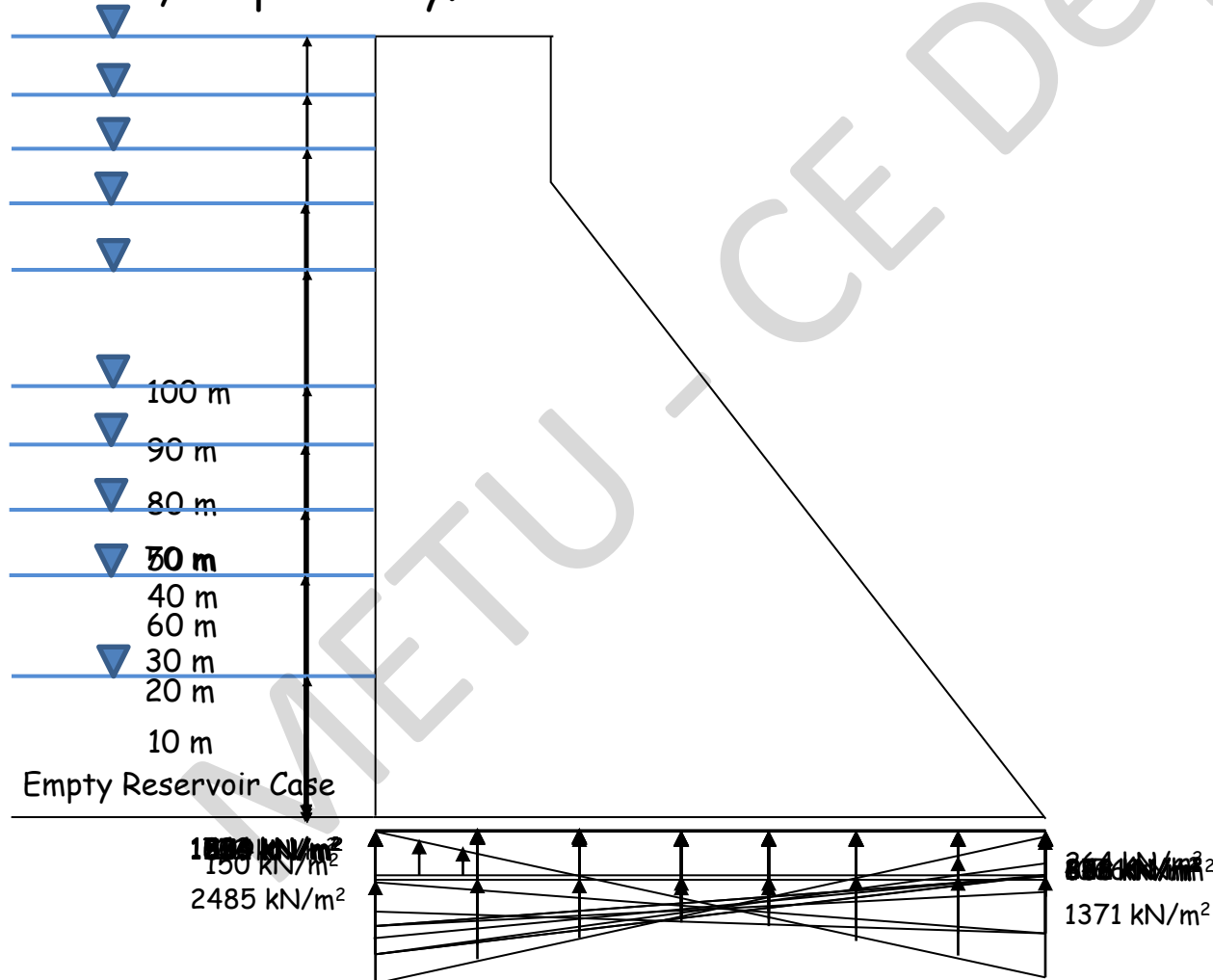
## Example 13

By carrying out a stability analysis of the concrete gravity dam shown in the figure, determine the variation of safety factors and stresses at the foundation level for various operating depths of the reservoir. Ignore silt and ice forces. Take  $k_h=k_v=0.1$ ,  $f=0.7$ ,  $\gamma_{\text{con}}=24 \text{ kN/m}^3$ ,  $\gamma=10 \text{ kN/m}^3$ ,  $\tau_s=6 \text{ MPa}$ ,  $\sigma_c=25 \text{ MPa}$ ,  $\sigma_f = 90 \text{ MPa}$ , and  $\phi = 1.0$ . The required safety factors can be taken as those of the extreme loading case.

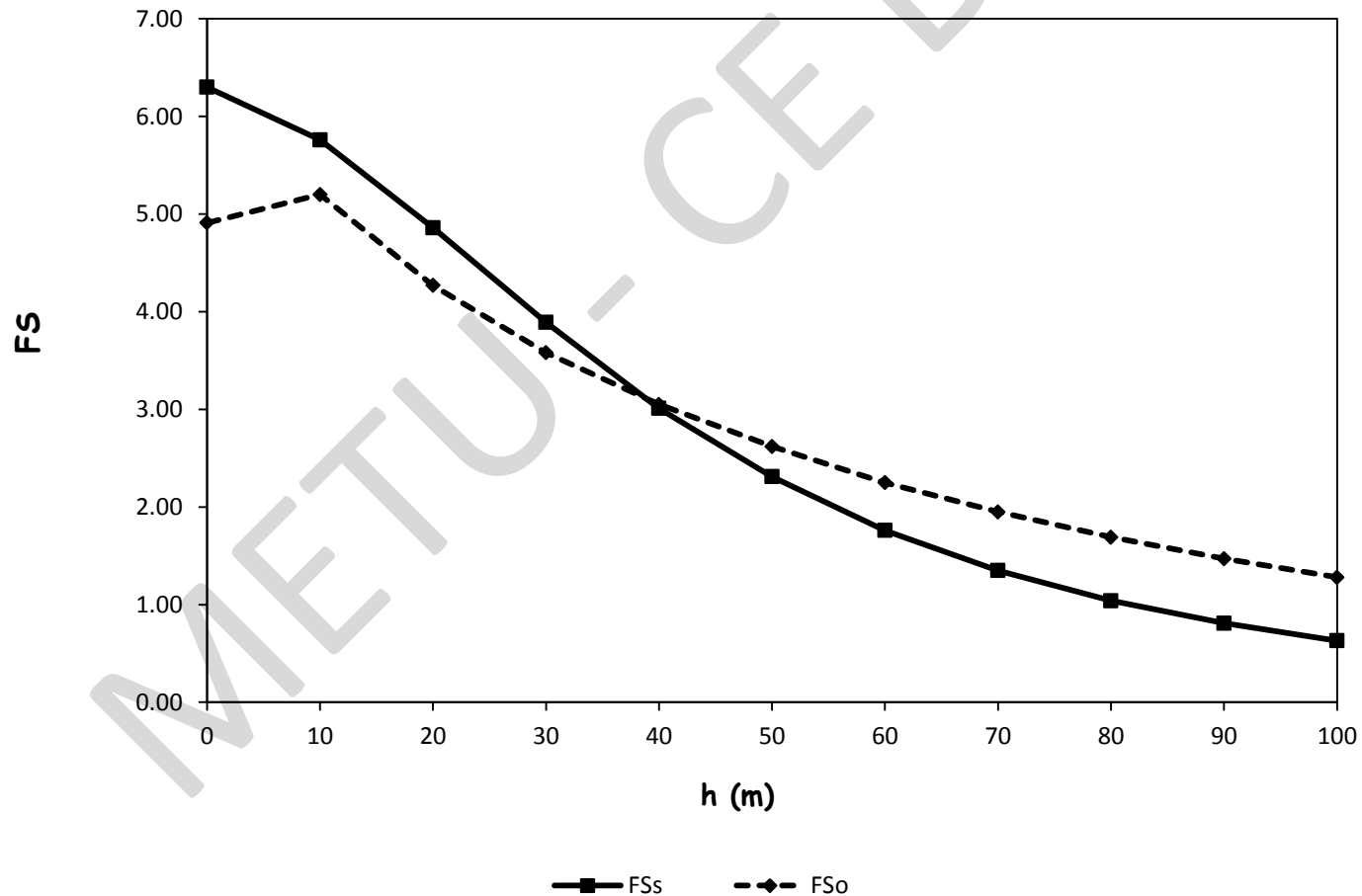


# Solution

The results of the analysis are given in the following animation for various water depths. In the computations, moments are taken with respect to the toe and heel for the cases with water in the upstream and empty reservoir, respectively.



The variation of water depth in the reservoir causes significant changes in the overall stability. The stress distribution at the foundation level was shown in the previous slide. Assuming that the safety criterion for extreme loading is also applicable for this example, the dam is found safe for  $h \leq 80$  m.



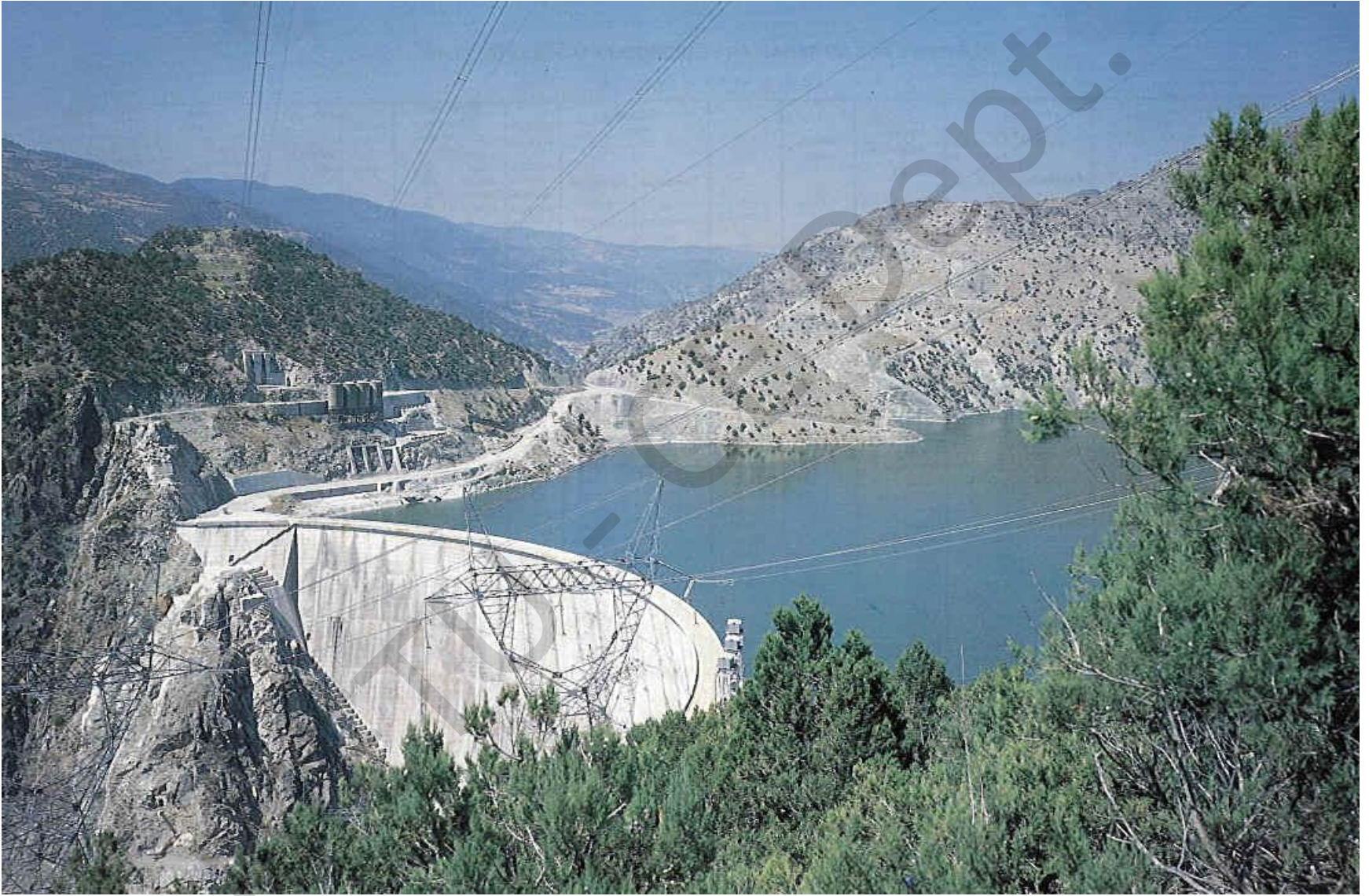


# Arch dams

Stability is based on

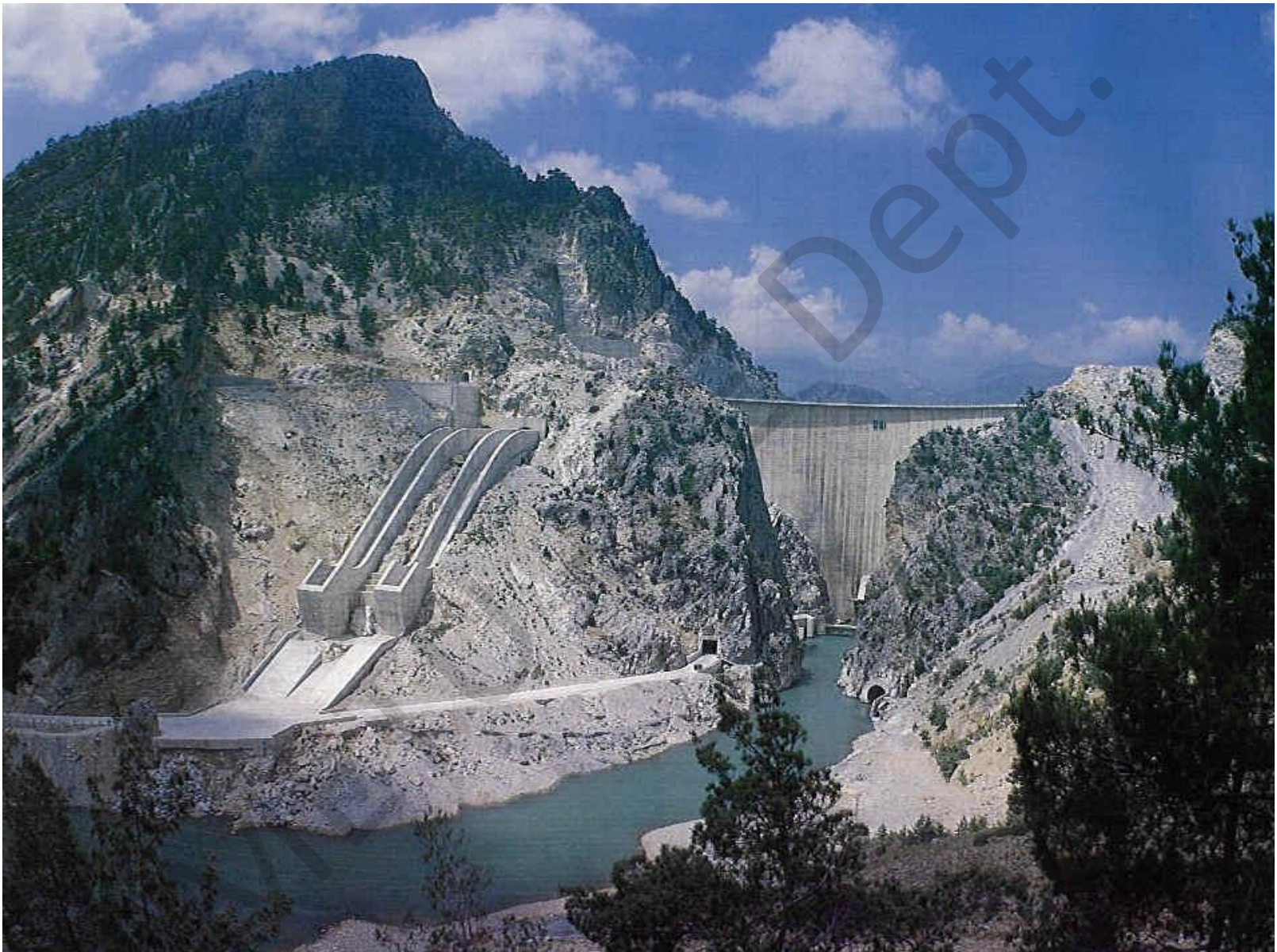
- ✱ its self weight &
- ✱ ability to transmit water load to valley walls by arch action

- ② Thin slender structures curved in plan
- ② They are usually suited to valleys where the valley width to height ratio,  $B/H < 6.0$ .
- ② Water thrust is transmitted partially
  - ✱ by arch action to the sides - Stiff side formation &
  - ✱ by cantilever action to the foundation - Stiff foundation is required



Gökçekaya Dam on Sakarya River





Oymapınar Dam on Manavgat River

- ② From structures and construction view points, an arch dam is composed of series of
  - ✱ horizontal beams
  - ✱ vertical cantilevers
- ② Construction technique is similar to
  - ✱ temperature stresses are pronounced
  - ✱ uplift force is small  
(since base width is small)

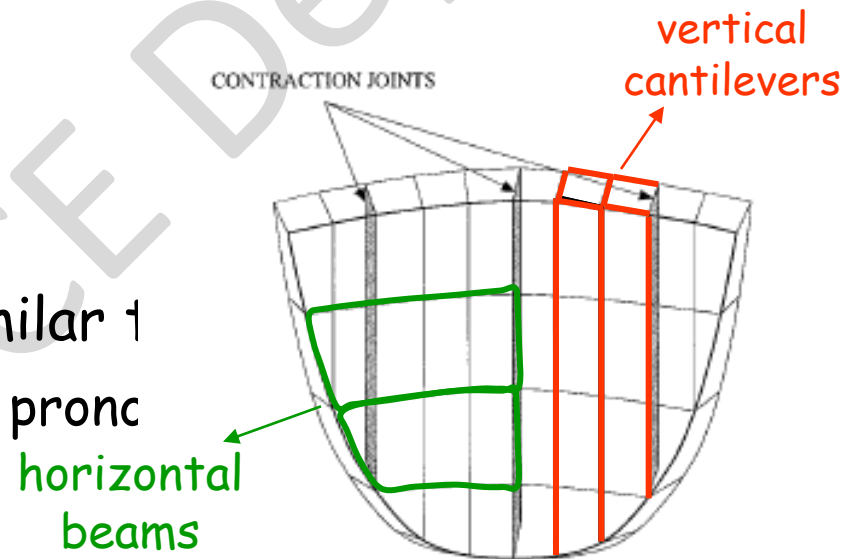


Figure 1. Vertical contraction joints in an arch dam

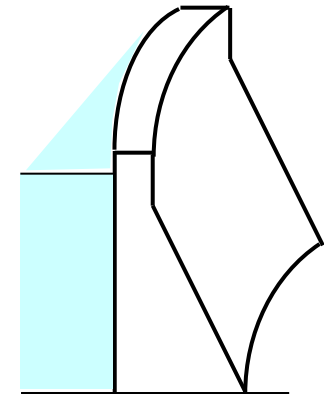
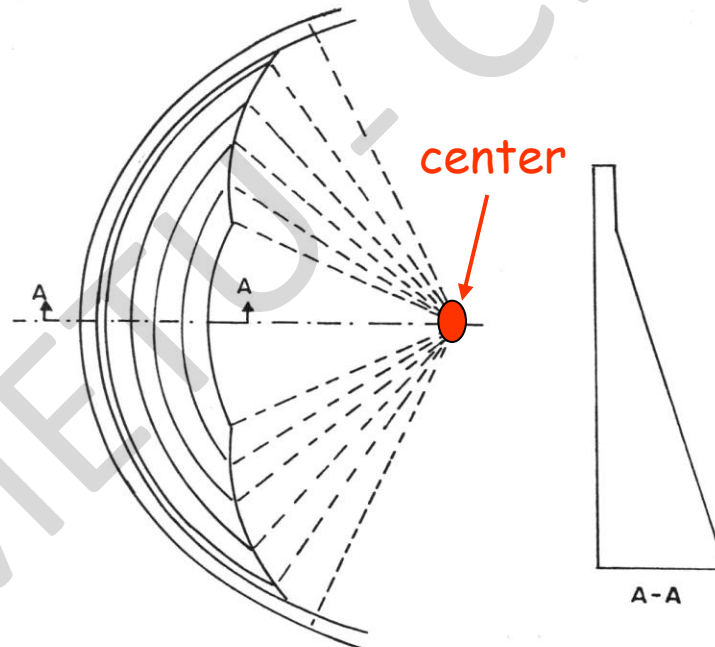
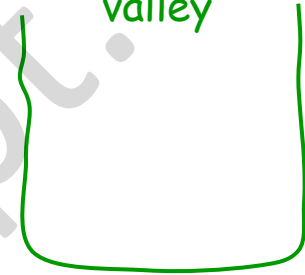
D. T. LAU, B. NORUZIAAN AND A. G. RAZAQPUR

## Types of arch dams:

### A) Constant-center (variable angle):

- ⊙ U-shaped valley
- ⊙ dams of medium height

U-shaped valley



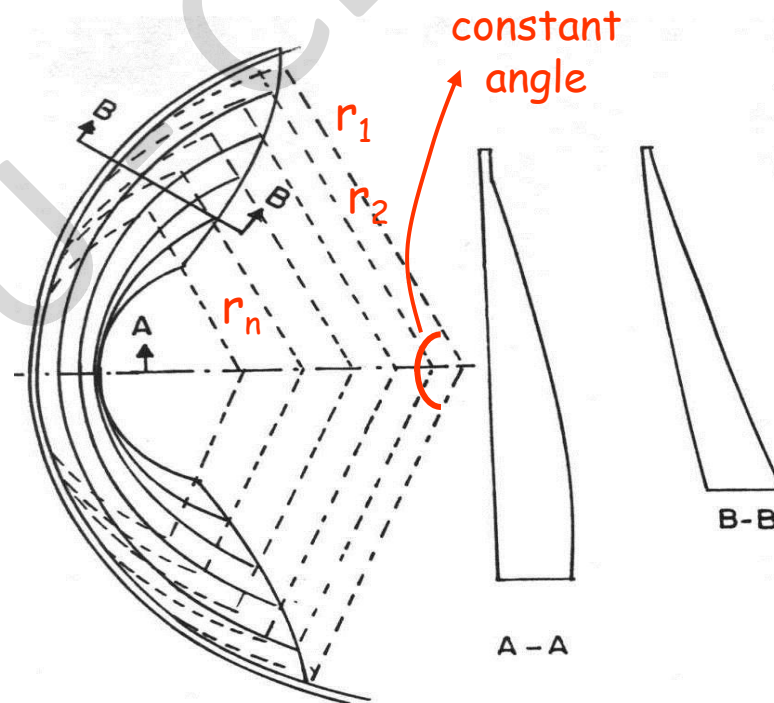
## B) Variable-center (constant angle)

- ⊙ V-shaped valleys
- ⊙ Radius decreases with depth. So arching action is more pronounced at low depths.
- ⊙ Thinner than constant-center dams. So they are more elastic and safer

radius of arch ↓ es  
with depth



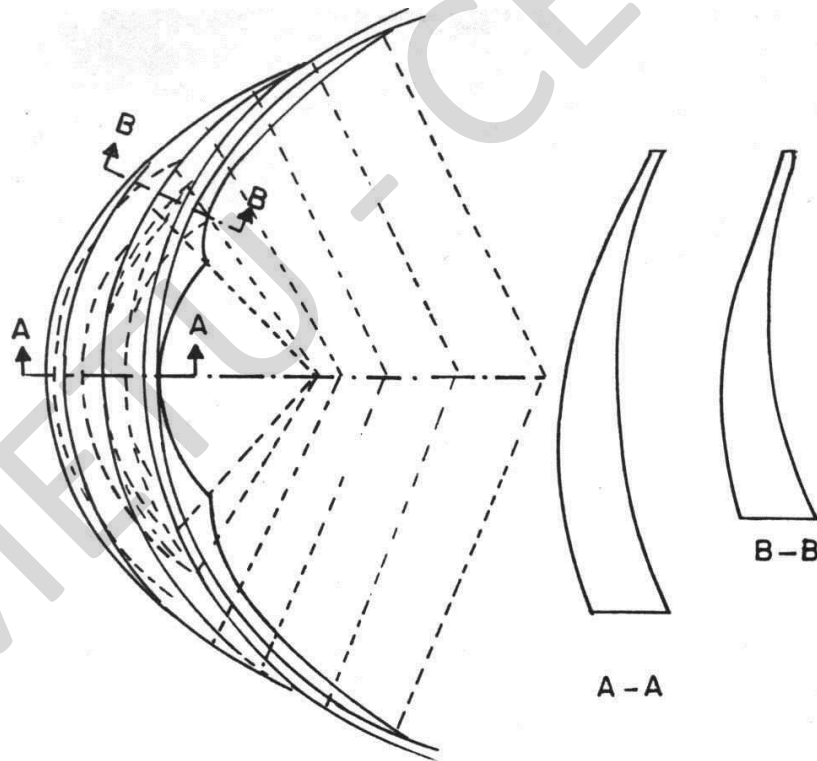
arching action is  
more pronounced  
at low depths





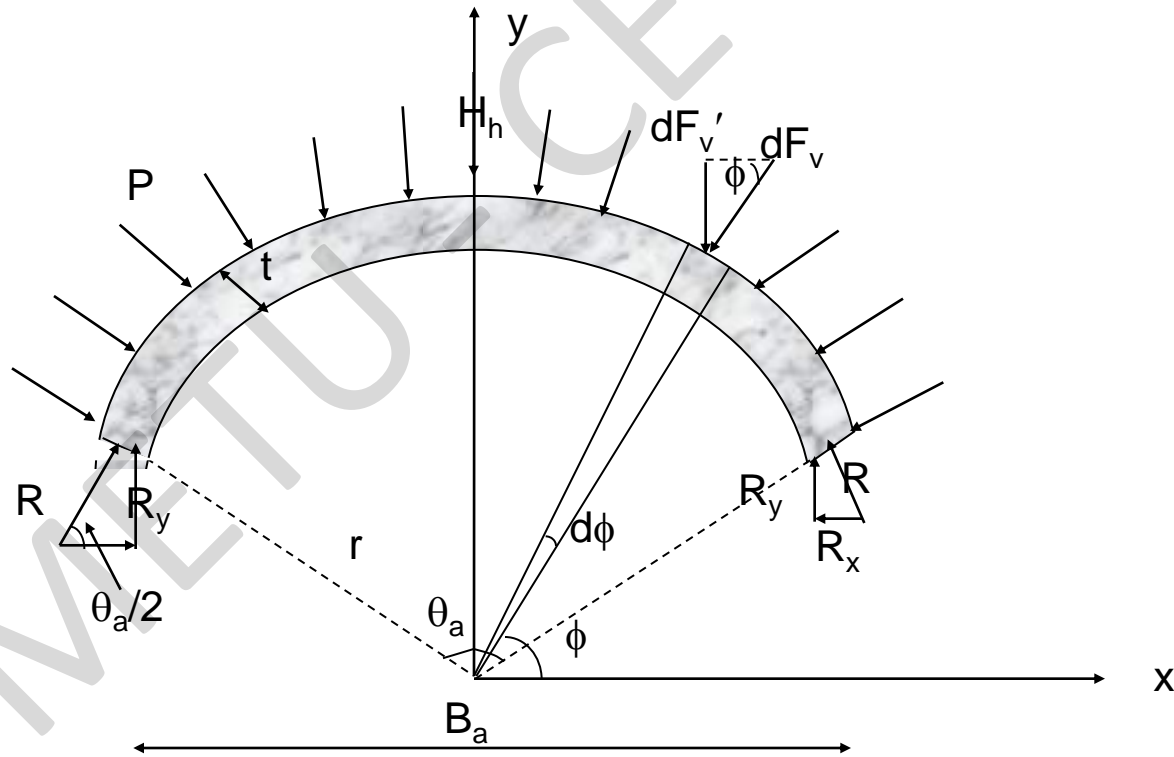
### C) Variable-center, variable-angle arch dams:

- ⊗ Combination of two types described above.
- ⊗ Load distribution in vertical direction governs the cross-sectional shape of the dam.



# Simplified design - arch rib analysis: determination of thickness at any elevation for an arch dam whose crest elevation is already determined

**Assumption:** water thrust induced by hydrostatic pressure is taken by **ARCH ACTION ONLY**



$$dF_v = p(r d\Phi) \xrightarrow[\text{Horizontal component}]{\text{Horizontal component}} dF'_v = p(r d\Phi) \sin \Phi$$

$$H_h = 2 \int_{\left(\frac{\pi}{2} - \frac{\theta_a}{2}\right)}^{\frac{\pi}{2}} \gamma h r \sin \phi d\phi = -2\gamma h r \left( \cos\left(\frac{\pi}{2}\right) - \cos\left(\frac{\pi}{2} - \frac{\theta_a}{2}\right) \right) = 2\gamma h r \sin \frac{\theta_a}{2}$$

$$p = \gamma h$$

$$H_h = 2R_y \quad R_y = R \sin\left(\frac{\theta_a}{2}\right)$$

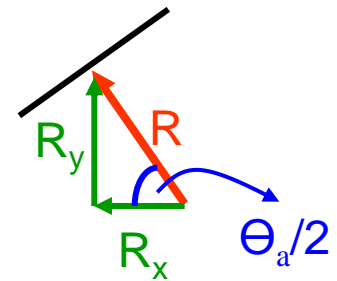
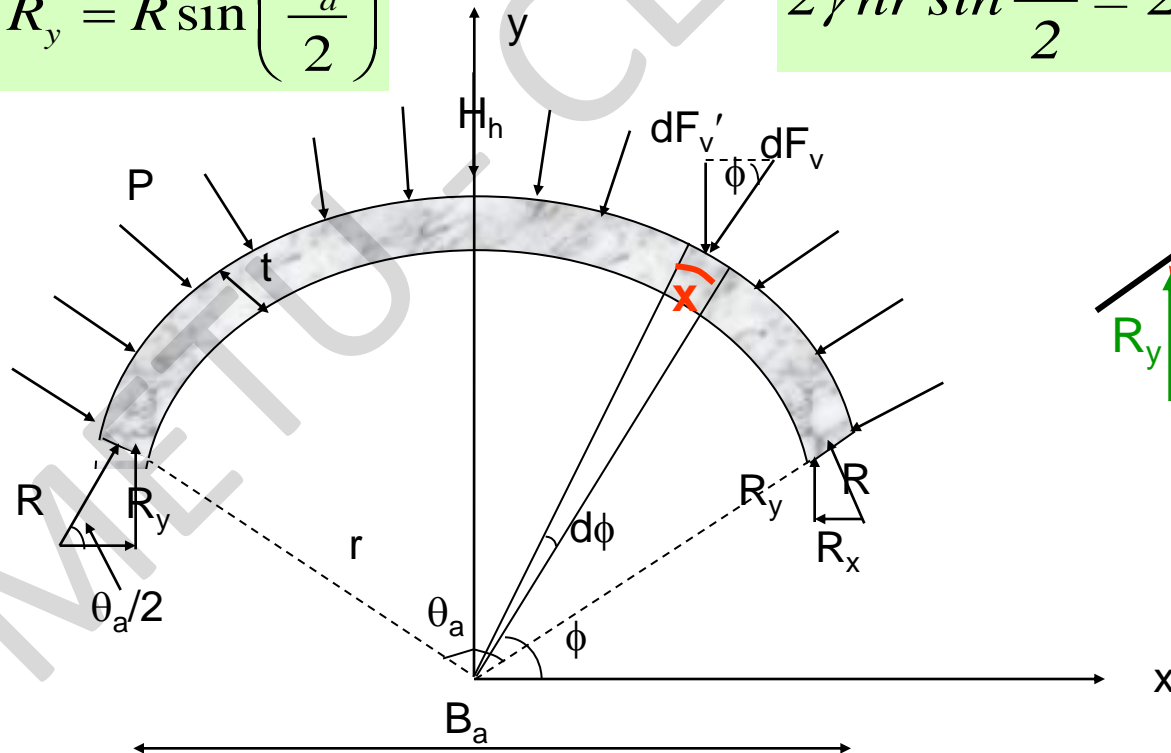
$$2\gamma h r \sin \frac{\theta_a}{2} = 2R \sin \frac{\theta_a}{2}$$

$$\frac{2\pi}{d\Phi} \quad \frac{2\pi r}{x}$$

$$x = r d\Phi$$

$$F = pA$$

$$dF_v = p(r d\Phi)1$$



$$R = \gamma h r$$

$$t \ll r$$

if  $t \ll r \rightarrow$  avr. compressive stress in the rib  $\approx$  max. compressive stress in the rib

$$\sigma_{all} \approx \frac{R}{t} = \frac{\gamma h r}{t}$$

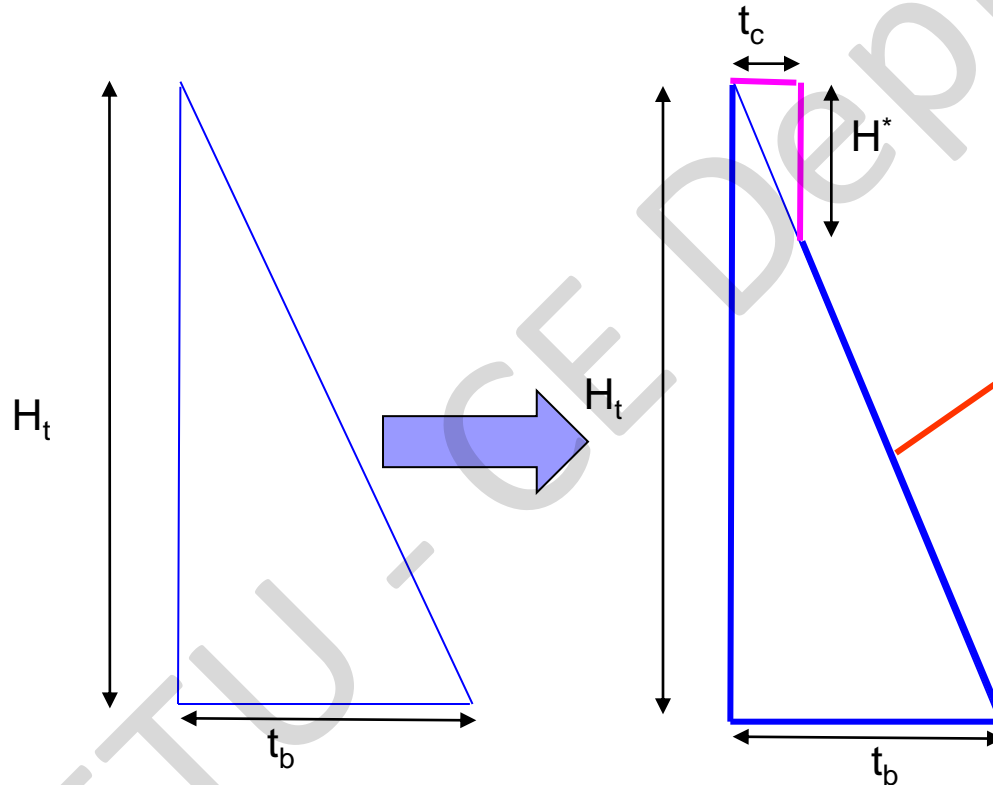
$$t = \frac{\gamma h r}{\sigma_{all}}$$

allowable working stress for concrete in compression

$$V = L t$$

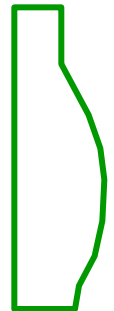
$$V = \frac{\gamma h}{\sigma_{all}} r^2 \theta_a$$

$V$  = volume of concrete per unit height



x-section for U-shaped valley  
 $t = f(h)$

x-section for V-shaped valley  
 $t = f(h^2)$

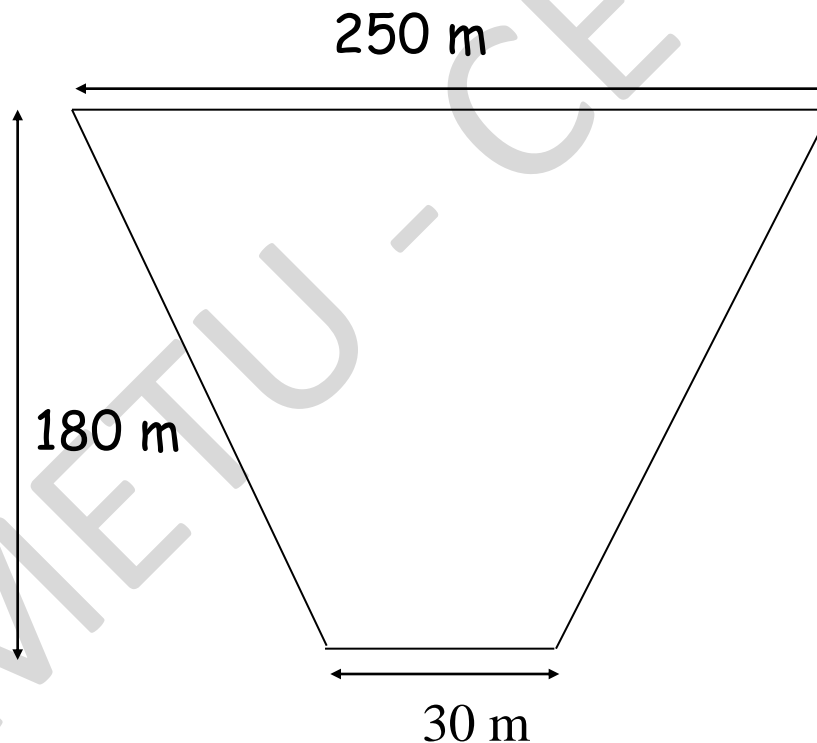


Optimum  $\theta_a = 133^\circ 34'$

In practice,  $\theta_a = 100^\circ$  to  $140^\circ$

## Example 14

- Using the simplified arch rib analysis, design an arch dam 180 m high for a trapezoidal canyon shown below, Upstream face is vertical. Thickness at the crest is 3 m. Take  $\sigma_{all} = 4000 \text{ kN/m}^2$  and  $\theta_a = 120^\circ$ .



# Solution

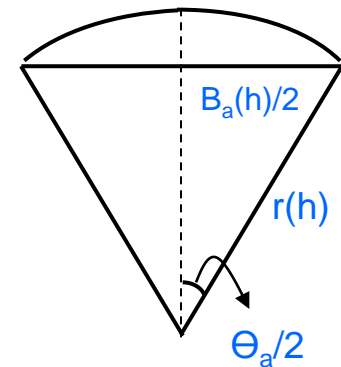
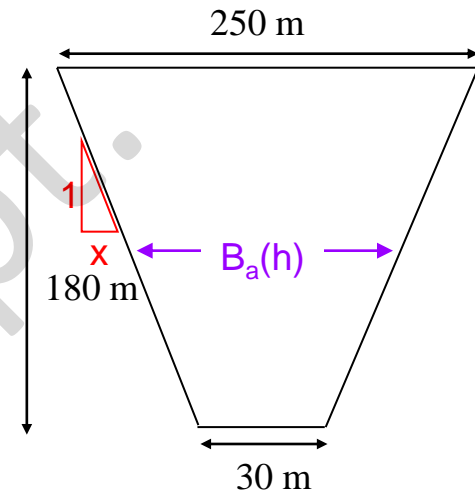
$$B_a(h) = 250 - 1.222h$$

$$r(h) = \frac{B_a(h)}{2 \sin \frac{\theta_a}{2}} = 0.577 B_a(h) = 144.25 - 0.705h$$

$$t = \frac{\gamma h r(h)}{\sigma_{all}} = \frac{\gamma (144.25h - 0.705h^2)}{\sigma_{all}}$$

$$\frac{180}{1} = \frac{(250-30)/2}{x}$$

$$x = 0.611$$





Maximum thickness is obtained from  $\rightarrow dt/dh = 0$

$$\frac{dt}{dh} = \frac{\gamma}{\sigma_{all}} (144.25 - 1.41h) = 0 \rightarrow h_{max} = 102.3m$$

$$t = \frac{\gamma hr(h)}{\sigma_{all}} = \frac{\gamma(144.25h - 0.705h^2)}{\sigma_{all}}$$

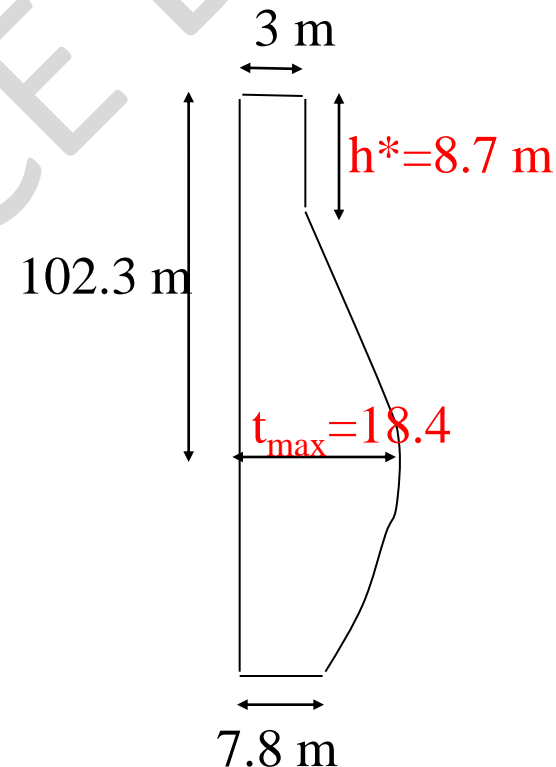
$$t_{max} = \frac{10(144.25 \times 102.3 - 0.705(102.3)^2)}{4000}$$

$$t_{max} = 18.4 \text{ m}$$

$$t = \frac{\gamma hr(h)}{\sigma_{all}} = \frac{\gamma(144.25h - 0.705h^2)}{\sigma_{all}}$$

$$3 = \frac{10(144.25 \times h^* - 0.705(h^*)^2)}{4000}$$

$$h^* = 8.7 \text{ m}$$



④ A constant-angle arch dam is preferable since volume is less!

- ✱ It requires less concrete than a constant-center dam
- ✱ However, its formwork is more difficult

### Constructional details:

- ④ Foundation must be excavated to solid rock
- ④ Abutments should be stripped to join the dam at right angle to the line of thrust to prevent sliding of the dam
- ④ Grouting is usually required at the foundation
- ④ Excessive care for constructional quality!

## Characteristics of dams

Dam Type	Foundation Conditions	Construction Materials
earth-fill	every type	non-organic, non-plastic all soils
rock-fill	hard sandy, gravely or rock	rock and clay
concrete gravity	rock foundation	concrete
arch	rock foundation and abutments	concrete
buttress	rock foundation	plain/reinforced concrete

Dam Type	Construction Conditions	Critical Factor
earth-fill	earth construction equipment needed; average workmanship	overtopping, settlement, excessive seepage, sliding of slopes, earthquake
rock-fill	earth construction equipment needed; average workmanship	overtopping, settlement, excessive seepage, sliding of slopes, earthquake
concrete gravity	concrete mixing plants; skilled workmanship	sliding, settlement, overturning, earthquake
arch	concrete mixing plants; skilled workmanship	sliding, settlement, overturning, earthquake, sliding on abutments
buttress	concrete mixing plants; skilled workmanship	settlement, overturning, earthquake

# Dam safety and rehabilitation

## Possible causes of dam failure (break):

- ⌚ Inadequate spillway capacity
- ⌚ Piping & settlement due to fault movement
- ⌚ Improper protection, stability failure

## Remedies:

- ⌚ Proper design
- ⌚ Use of sound and proper material
- ⌚ Proper construction
- ⌚ Surveillance and continuous monitoring

proper design  
&  
construction  
+  
continuous inspection  
&  
monitoring

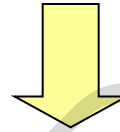
# Indicators of problems

- ⊙ large horizontal and vertical movements of crest,
- ⊙ tilting of the roadway along the crest,
- ⊙ deformation of embankment slopes
- ⊙ higher than usual pore water pressures in embankment dams,
  - ✱ settlement
  - ✱ crest may be tilted due to differential settlement
- ⊙ unusual seepage at the toe or edges of an embankment dam,
- ⊙ seepage flows not decreasing with low flow conditions,
- ⊙ turbid outflows through the embankment,
- ⊙ tilting of the spillway crest,
  - piezometers placed in earth-fill dams indicate the locus of line of saturation which indicates the degree of seepage thru the embankment
- ⊙ increased leakage into inspection galleries in concrete dams, etc.



## Monitoring:

most of the problems  
are due to excessive seepage



- ⊙ Placement of piezometers in earthfill dams
  - ✱ pore water pressure
  - ✱ locus of line of saturation → indicates seepage
- ⊙ Placement of strain gages and stress meters in inspection galleries in concrete dams

## Rehabilitation:

- ⌚ Further grouting after construction  $\Rightarrow$  earth-fill dams
- ⌚ Enlarged toe drain  $\Rightarrow$  embankment dams
- ⌚ Placement of
  - ✱ cutoff wall
  - ✱ impermeable blanket } Embankment dams
- ⌚ Supporting measures against slope failure
  - rip-rap
  - grass
  - concrete blocks/slabs
- ⌚ Handling downstream scour holes after floods



Now spillways !

METU - CE Dept.