

2) N, kg, m and second are consistent units.

$$P_o := 50 \quad m := 17.5 \quad k := 7000 \quad t_d := 0.2 \quad dt := 0.025 \quad t_{\max} := 2$$

$$\omega_n := \sqrt{\frac{k}{m}} \quad T := \frac{2 \cdot \pi}{\omega_n} \quad \omega_n = 20 \quad T = 0.31416$$

```

P(Po,td,dt,tmax) :=
  t ← -dt
  i ← -1
  while t ≤ tmax - dt
    t ← t + dt
    i ← i + 1
    Pi,0 ← t
    Pi,1 ← Po ·  $\frac{t}{t_d}$  if t ≤ td
    Pi,1 ← 0 otherwise
  P

```

	0	1
0	0	0
1	0.025	6.25
2	0.05	12.5
3	0.075	18.75
4	0.1	25
5	0.125	31.25
6	0.15	37.5
7	0.175	43.75
8	0.2	50
9	0.225	0
10	0.25	0
11	0.275	0
12	0.3	0
13	0.325	0
14	0.35	0
15	0.375	0

P(Po,td,dt,tmax) =

Force := P(Po,td,dt,tmax)

Q2) Subroutine which calculates the displacement response using Newmark Algorithm.

```

Newmark(k,m,dt,γ,β,ζ,force,v0,u0) :=
    countert ← rows(force)
    forcev ← force<1>
    time ← force<0>
    ωn ← √(k/m)
    c ← 2 · ζ · m · ωn
    v0 ← v0
    u0,1 ← u0
    u0,0 ← time0
    a0 ← (forcev0 - c · v0 - k · u0,1) / m
    kh ← k + (γ / (β · dt)) · c + (1 / (β · dt2)) · m
    ca ← (1 / (β · dt)) · m + (γ / β) · c
    cb ← (1 / (2 · β)) · m + dt · ((γ / (2 · β)) - 1) · c
    for i ∈ 0 .. countert - 2
        dpi ← forcevi+1 - forcevi + ca · vi + cb · ai
        dui ← dpi / kh
        dvi ← (γ / (β · dt)) · dui - (γ / β) · vi + dt · (1 - (γ / (2 · β))) · ai
        dai ← (1 / (β · dt2)) · dui - (1 / (β · dt)) · vi - (1 / (2 · β)) · ai
        ui+1,0 ← timei+1
        ui+1,1 ← ui,1 + dui
        vi+1 ← vi + dvi
        ai+1 ← ai + dai
    u

```

k : stiffness of the SDOF system.

m : mass of the SDOF system.

dt : Time step.

γ , β : Parameters of Newmark's method.

ζ : Damping ratio.

Force : Matrix which contains the force vector. First column is the time column and second column is the force column.

v0 : initial velocity.

u0 : initial displacement.

A matrix consisting of two columns is the output, first column is the time column and second is the displacement column.

Note : $\gamma = 1/2$, $\beta = 1/4$ represents the average acceleration method and $\gamma = 1/2$, $\beta = 1/6$ represents the linear acceleration method. Linear acceleration method is stable when $dt/T_n < 0.551$ and average acceleration method is stable for any value of dt .

Average acceleration method

$$\gamma := \frac{1}{2} \quad \beta := \frac{1}{4} \quad \zeta := 0 \quad v0 := 0 \quad u0 := 0$$

Newmark(k, m, dt, γ , β , ζ , Force, v0, u0) =

	0	1
0	0	0
1	0.025	0.0000525
2	0.05	0.0003028
3	0.075	0.0009019
4	0.1	0.0019191
5	0.125	0.0033251
6	0.15	0.0049991
7	0.175	0.0067574
8	0.2	0.0083963
9	0.225	0.0092675
10	0.25	0.0083783
11	0.275	0.0055178
12	0.3	0.001359
13	0.325	-0.0031196
14	0.35	-0.0068642
15	0.375	-0.0089937

Displacements are in meters.

Linear acceleration method

$\gamma := \frac{1}{2}$ $\beta := \frac{1}{6}$ $\zeta := 0$ $v0 := 0$ $u0 := 0$

Newmark(k,m,dt,γ,β,ζ,Force,v0,u0) =

	0	1
0	0	0
1	0.025	0.0000357
2	0.05	0.0002771
3	0.075	0.0008806
4	0.1	0.0019156
5	0.125	0.003348
6	0.15	0.0050483
7	0.175	0.0068227
8	0.2	0.0084597
9	0.225	0.0094592
10	0.25	0.0084742
11	0.275	0.0054554
12	0.3	0.0011273
13	0.325	-0.0034713
14	0.35	-0.0072369
15	0.375	-0.0092655

Displacements are in meters.