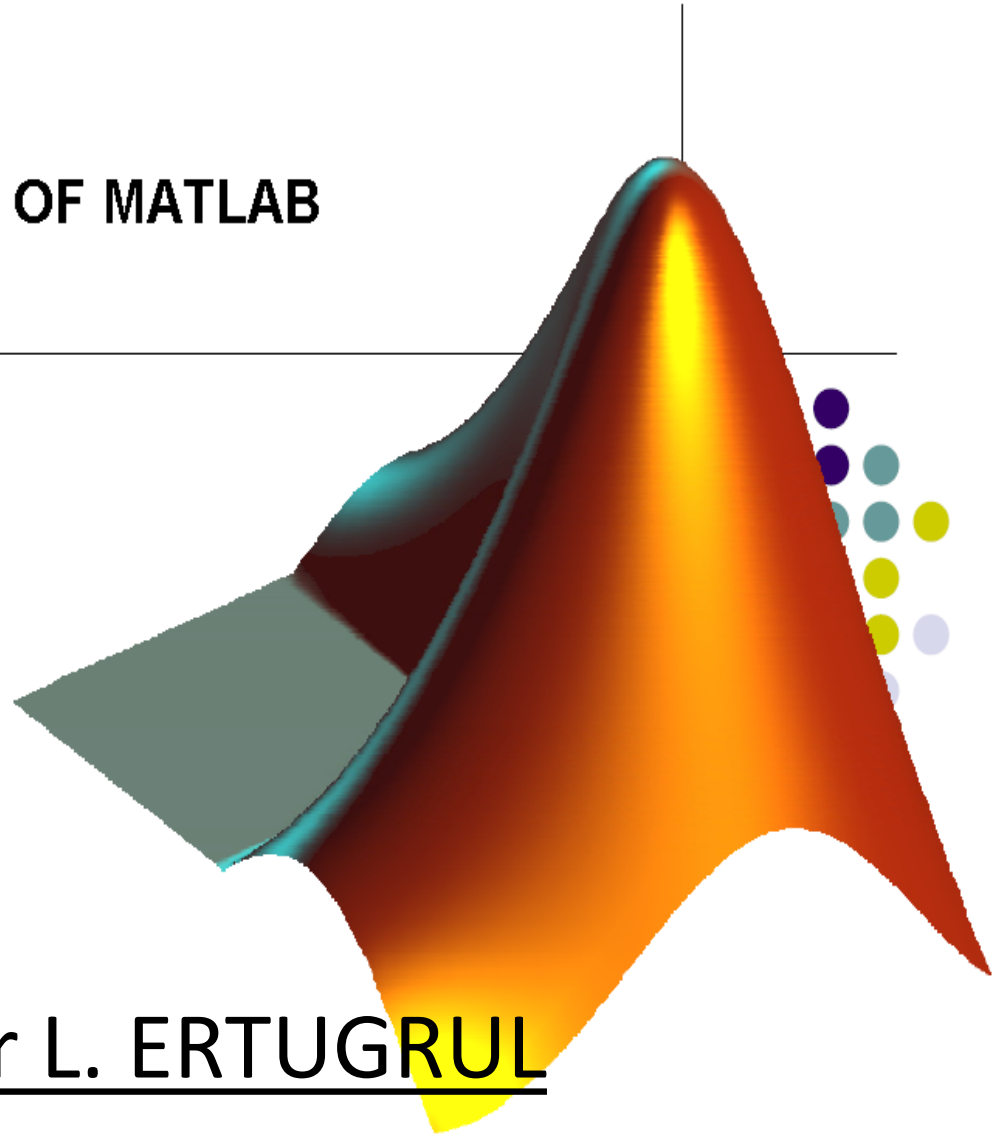


FUNDAMENTALS OF MATLAB

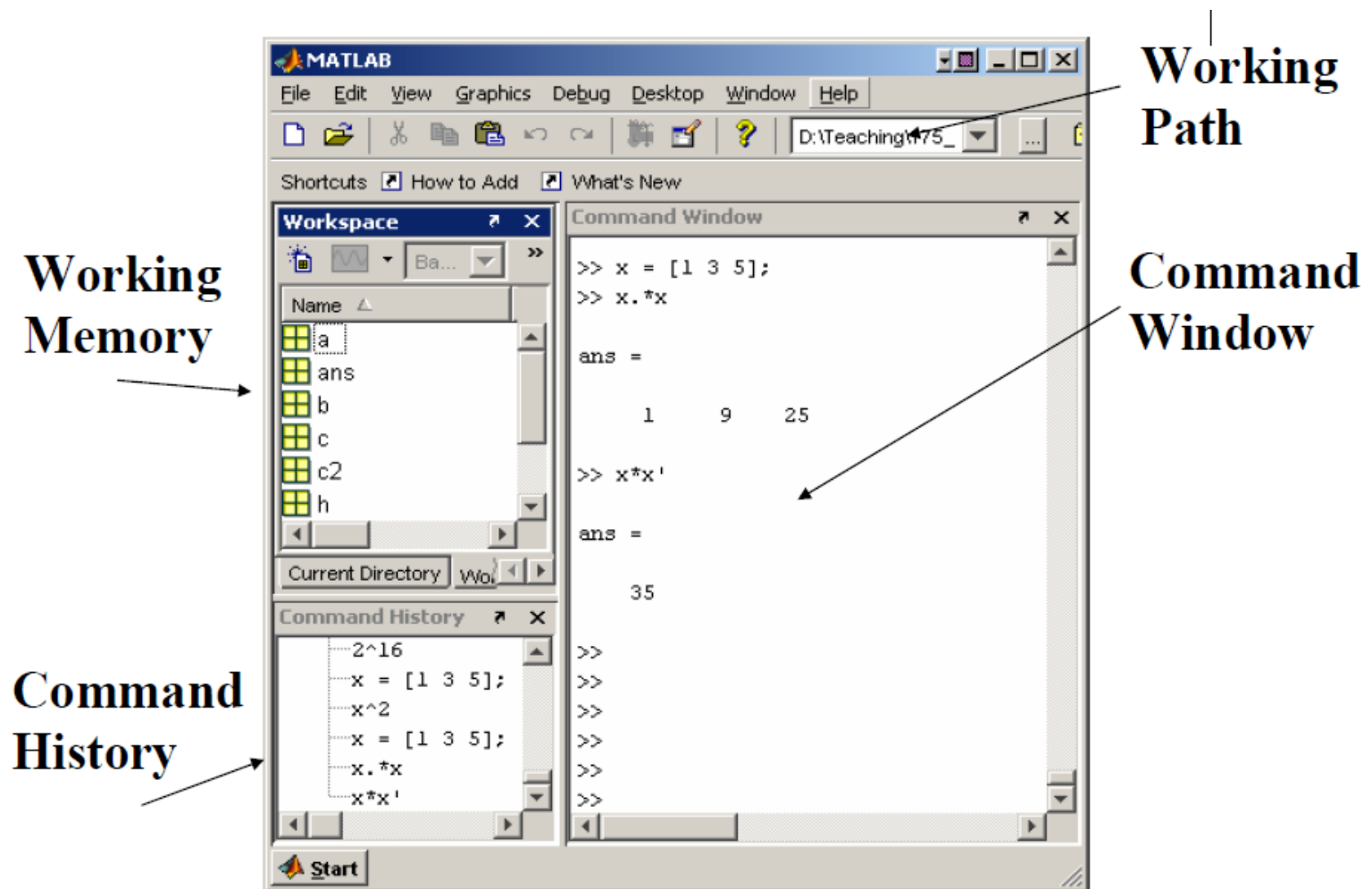


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OUTLINE

- Vectors and vector operations
- Matrix and matrix operations
- Simple plotting
- 2D-3D Plotting capabilities of MATLAB

MATLAB GUI



Vectors in MATLAB

This command creates a row vector

```
a = [1 2 3]
```

```
a =
```

1

2

3

Vectors in MATLAB

```
b = [1; 2; 3]
```

```
b =  
    1  
    2  
    3
```

Vectors in MATLAB

Command **length** returns the number of components of a vector

```
length(a)
```

```
ans =  
     3
```

Vectors in MATLAB

The *dot operator*. plays a specific role in MATLAB. It is used for the componentwise application of the operator that follows the dot operator

```
a.*a
```

```
ans =
```

```
1
```

```
4
```

```
9
```

Vectors in MATLAB

The *dot operator*. plays a specific role in MATLAB. It is used for the componentwise application of the operator that follows the dot operator

```
a.^2
```

```
ans =
```

```
1
```

```
4
```

```
9
```


Vectors and vector operations

Componentwise division of vectors **a** and **b** can be accomplished by using the *backslash operator* `\` together with the dot operator `.`

```
a.\b'
```

```
ans =
```

```
1
```

```
1
```

```
1
```

Vectors and vector operations

$$\mathbf{a} = \mathbf{a}'$$

$$\mathbf{a} =$$

1

2

3

Vectors and vector operations

```
dotprod = a' * b
```

```
dotprod =  
14
```

Vectors and vector operations

The *cross product* of two three-dimensional vectors is calculated using command **cross**.

$$\mathbf{b} = [-2 \ 1 \ 2];$$

Vectors and vector operations

```
b = [-2 1 2];
```

```
cp = cross(a,b)
```

```
cp =  
1      -8      5
```

MATRICE OPERATIONS

$A = [1 \ 2 \ 3; 4 \ 5 \ 6; 7 \ 8 \ 10]$

$A =$

1	2	3
4	5	6
7	8	10

MATRICE OPERATIONS

```
A = [1 2 3;4 5 6;7 8 10]
```

```
A =
```

```
     1     2     3  
     4     5     6  
     7     8    10
```

```
A(:)
```

```
ans =
```

```
     1  
     4  
     7  
     2  
     5  
     8  
     3  
     6  
    10
```

The *colon operator* `:` stands for *all columns* or *all rows*. For the matrix `A` from the last example the following command

MATRICE OPERATIONS

To delete a row (column) use the *empty vector operator* `[]`

$$A(:, 2) = []$$

$$A =$$

$$\begin{bmatrix} 1 & 3 \\ 4 & 6 \\ 7 & 10 \end{bmatrix}$$

MATRICE OPERATIONS

Second column of the matrix **A** is now deleted. To insert a row (column),
creating matrices and vectors

$$\mathbf{A} = [\mathbf{A}(:, 1) \quad [2 \ 5 \ 8]^\top \quad \mathbf{A}(:, 2)]$$

$$\mathbf{A} =$$

$$\begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 10 \end{array}$$

MATRICE OPERATIONS

$A = [1 \ 2 \ 3; 4 \ 5 \ 6; 7 \ 8 \ 10]$

$A =$

1	2	3
4	5	6
7	8	10

MATRICE OPERATIONS

Note that the *semicolon operator* ; separates the rows. To extract a submatrix **B** consisting of rows 1 and 3 and columns 1 and 2 of the matrix **A** do the following

$$\mathbf{B} = \mathbf{A}([1 \ 3], [1 \ 2])$$

$$\mathbf{B} =$$

$$\begin{array}{cc} 1 & 2 \\ 7 & 8 \end{array}$$

MATRICE OPERATIONS

To interchange rows 1 and 3 of **A** use the vector of row indices together with the colon operator

$$C = A([3 \ 2 \ 1], :)$$

C =

7	8	10
4	5	6
1	2	3

MATRICE OPERATIONS

$$A * A$$

MATRICE OPERATIONS

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{bmatrix} ;$$

MATRICE OPERATIONS

$A * A$

“??? Error using ==> *
Inner matrix dimensions must agree.

generates an error message.

Solving systems of linear equations by matrix operations

$$8x_1 + x_2 + 6x_3 = 7.5$$

$$3x_1 + 5x_2 + 7x_3 = 4$$

$$4x_1 + 9x_2 + 2x_3 = 12$$

Solving equations

```
A=[8,1,6;3,5,7;4,9,2];
```

```
B=[7.5,4,12]'
```

```
X=A\b (you should  
use left slash)
```

Or

```
X=linsolve(A,B)
```

Inverse of a matrix

MATLAB function `inv` is used to compute the inverse matrix.

Let the matrix `A` be defined as follows

```
A = [1 2 3;4 5 6;7 8 10]
```

```
A =
```

1	2	3
4	5	6
7	8	10

Inverse of a matrix

```
B = inv(A)
```

```
B =  
-0.6667    -1.3333    1.0000  
-0.6667     3.6667   -2.0000  
 1.0000    -2.0000    1.0000
```

Verify that B is the inverse of A!!

```
A*B
```

```
ans =  
 1.0000         0    -0.0000  
         0    1.0000         0  
         0         0    1.0000
```

In a similar way one can check that $B*A = I$.

Basic plotting

```
x = 0:pi/40:4*pi;  
plot(x, sin(x))
```

`title('text')` writes the text as a title at the top of the graph.

`xlabel('horizontal')` labels the x -axis.

`ylabel('vertical')` labels the y -axis.

Basic plotting

```
plot(x, y, '--')
```

```
plot(x, y, 'o')
```

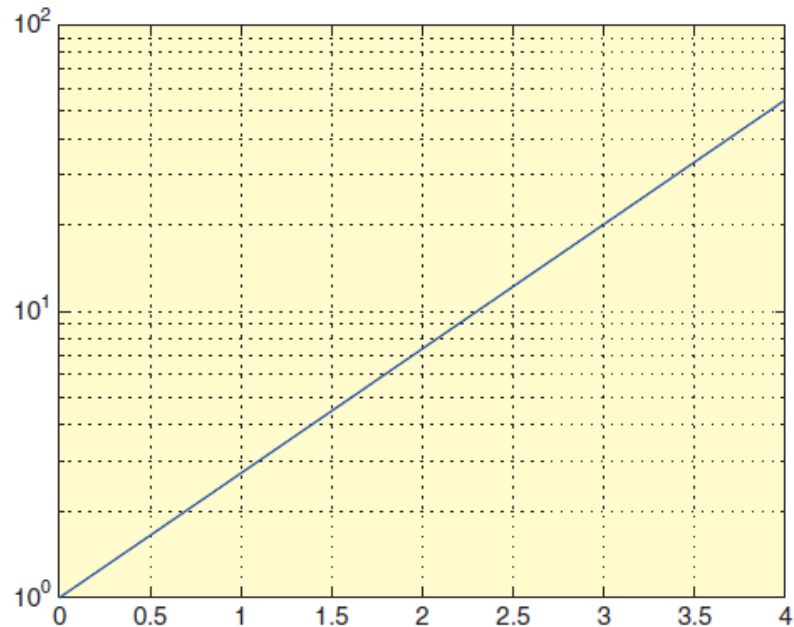
Basic plotting

```
plot(x, sin(x), x, cos(x), 'om--')
```

```
axis( [xmin, xmax, ymin, ymax] )
```

Basic plotting

```
x = 0:0.01:4;  
semilogy(x, exp(x)), grid
```



Simple 3D mesh plotting

$$z = x^2 - y^2.$$

$$0 \leq x \leq 5, \quad 0 \leq y \leq 5.$$

Set up the grid in x-y space

```
[x y] = meshgrid(0:5);
```

```
[x y] = meshgrid(0:0.25:5);
```

You can set up the grid in x-y space with a fine mesh

Simple 3D mesh plotting

$$z = x^2 - y^2 \quad 0 \leq x \leq 5, \quad 0 \leq y \leq 5.$$

Define surface in x-y-z space in MATLAB

$$z = x.^2 - y.^2$$

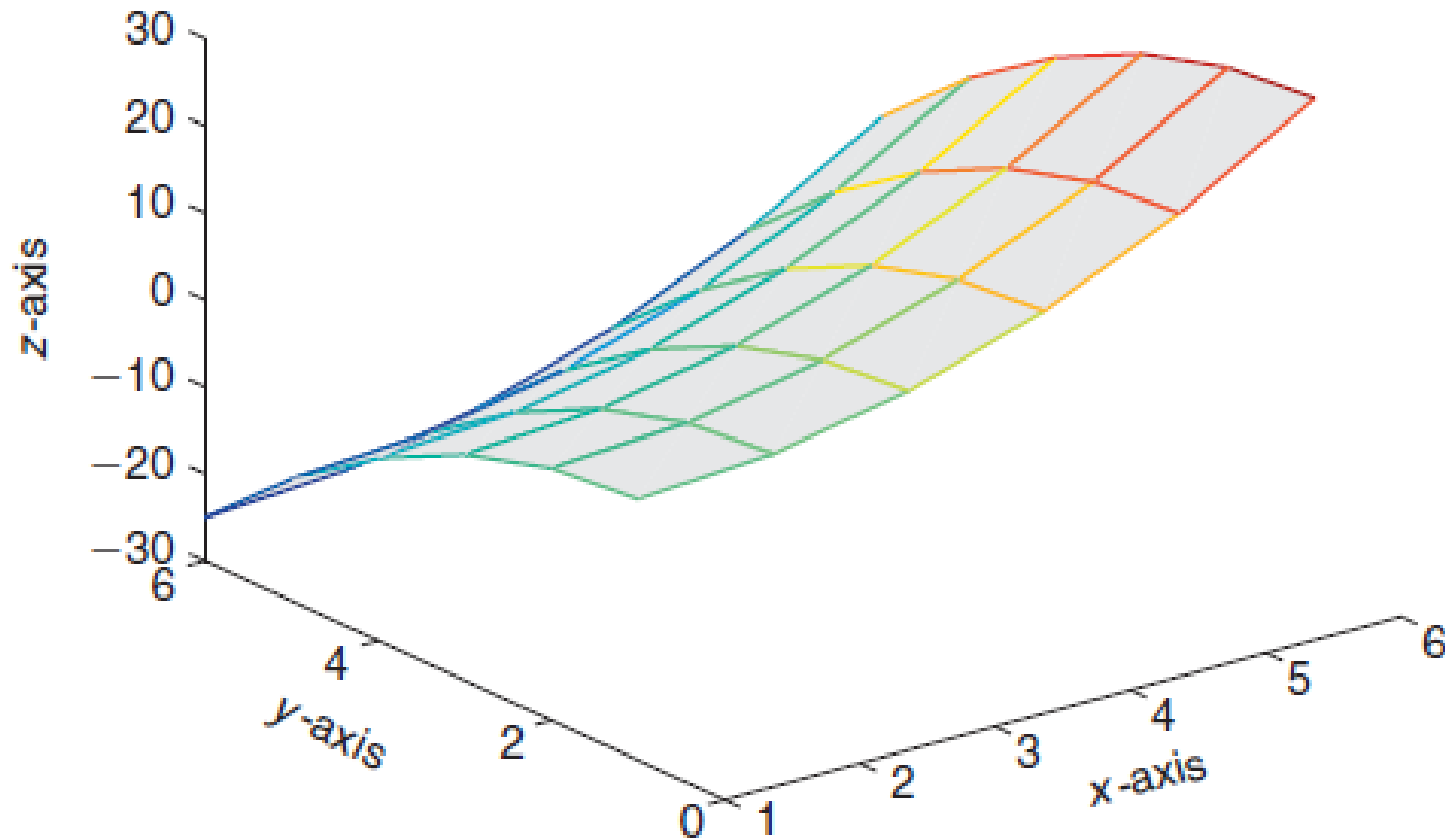
`mesh(z)`

`[x y] = meshgrid(0:0.25:5);`

You can set up the grid in x-y space with a fine mesh

Simple 3D mesh plotting

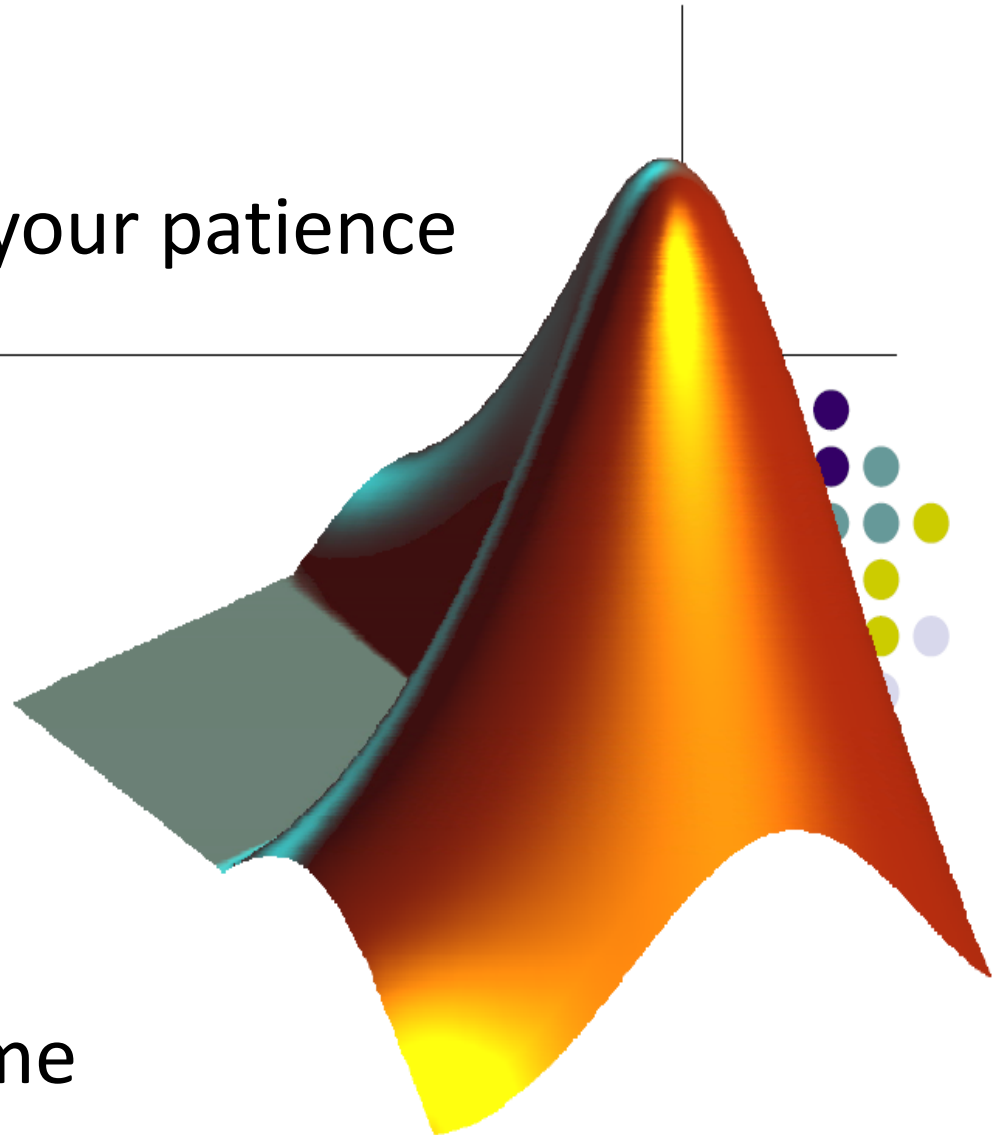
$$z = x^2 - y^2 \quad 0 \leq x \leq 5, \quad 0 \leq y \leq 5.$$



```
[x y] = meshgrid(0:0.25:5);
```

You can set up the grid in x-y space with a fine mesh

Thank you for your patience



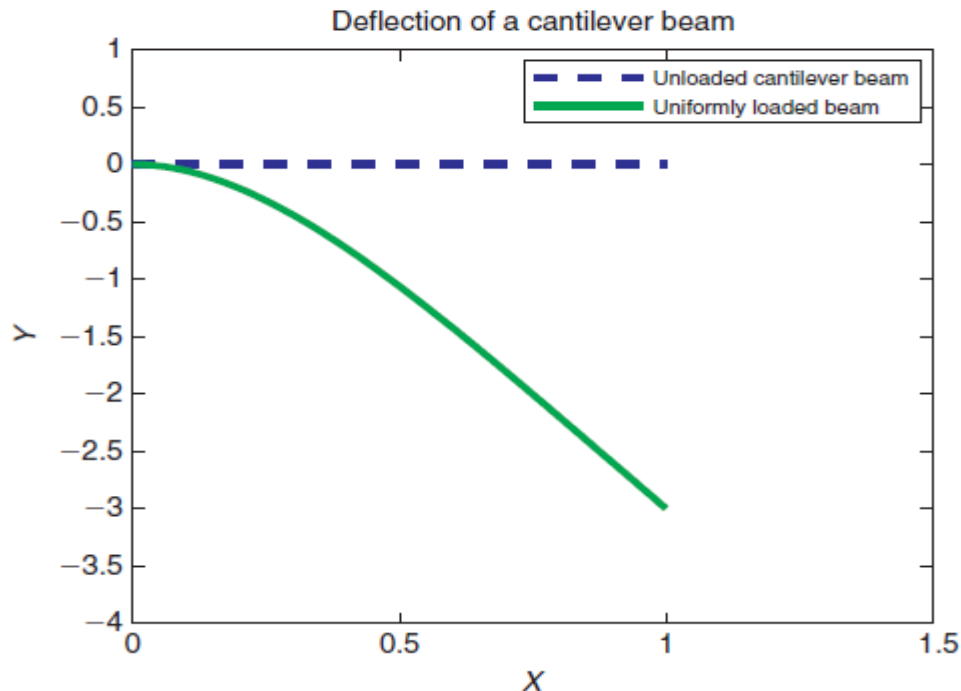
Questions welcome

TASK 1

CANTILEVER BEAM

For a uniformly loaded span of a cantilever beam attached to a wall at $x = 0$ with the free end at $x = L$, the formula for the vertical displacement from $y = 0$ under the loaded condition, with y the coordinate in the direction opposite that of the load, can be written as follows:

$$Y = \frac{y 24EI}{wL^4} = -(X^4 - 4X^3 + 6X^2),$$



Task 2

$$M = \begin{pmatrix} 1 & 0 & 0 \\ 0 & j & 1 \\ j & j+1 & -3 \end{pmatrix},$$

1. Expand the matrix M to a 6×6 matrix V of the form

$$V = \begin{pmatrix} M & M \\ M & M \end{pmatrix}.$$

2. Delete row 2 and column 3 from the matrix V (reduced matrix V_{23}).
3. Create a new vector z_4 from row 4 of the matrix V .
4. Modify the entry $V(4, 2)$ in the matrix V to $j + 5$.

Task 3

Calculate the values of the signal (function)

$$s(t) = \sin(2\pi 5t) \cos(2\pi 3t) + e^{-0.1t}$$

for a time vector of times between 0 and 10 with a step size of 0.1.