

# **CE 300 SUMMER PRACTISE INTRODUCTION TO MATLAB**

## **MATLAB TOOLBOXES**

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# WHAT IS A MATLAB TOOLBOX?

Toolboxes are libraries of extra routines.

## **Example Toolboxes Civil Engineers Use:**

- Aerospace Toolbox
- Curve Fitting Toolbox
- Financial Toolbox
- Image Processing Toolbox
- Mapping Toolbox
- Optimization Toolbox
- Paralle Computing Toolbox
- Signal Processing Toolbox
- Statistics Toolbox
- Symbolic Math Toolbox
- System Identification Toolbox
- Simulink



# OUTLINE

- Symbolic Math Toolbox
- Curve Fitting Toolbox
- Statistics Toolbox

## OBJECTIVE:

Introduce you 3 toolboxes of MATLAB.

Get familiar with the basics of these toolboxes.



# SYMBOLIC MATH TOOLBOX

- Perform symbolic computations.
- Basic tasks:
  - Differentiation
  - Integration
  - Linear algebra
  - Simplification
  - Equation solving
- You can access from Matlab Command Line or from MuPAD Notebook.



# SYMBOLIC TOOLBOX BASICS

- **`x=sym('x')`** defines x as a symbolic object
- **`x=sym('w','x','y','z')`** defines w,x,y,z as symbolic objects
- **`syms w x y z`**
- **`a=sym(3/5)`** a is defined as a symbolic object and assigned to 3/5.
- **`M=[w x; y z]`** M is a symbolic matrix since w,x,y,z are symbolic objects.
- **`f=5*x^2+3*x-2`** By assigning different values to x, you can obtain the corresponding values of f by: **`eval(f)`**

OR

**`subs(f, 1)`** Substitutes 1 as x in f.

```
>> syms x
>> f=5*x^2+3*x-2;
>> x=1;
>> eval(f)

ans =

     6

>> x=2;
>> eval(f)

ans =

    24

>> subs(f,1)

ans =

     6

>> |
```

# SYMBOLIC EXPRESSIONS

Given a function  $f(x)$

- **simplify(f)** Simplifies the symbolic expression
- **expand(f)** Groups similar terms, multiplies parenthesis to rewrite a polynomial in a standard form
- **factor(f)** Shows the polynomial roots

```
>> syms x
>> f=(x+3)*(x^2+5*x+2)+(x^2+1)*(x+3)
>> expand(f)

ans =

2*x^3 + 11*x^2 + 18*x + 9

>> factor(f)

ans =

(2*x + 3)*(x + 3)*(x + 1)

>>
```



# DIFFERENTIATION AND INTEGRATION

**diff** and **int** are the two functions used for differentiation and integration, respectively.

```
>> syms x
>> f=atan(x);
>> diff(f)

ans =

1/(x^2 + 1)

>> syms y
>> f=sin(x)*exp(2*y);
>> diff(f,y)

ans =

2*exp(2*y)*sin(x)

>> |
```

Differentiate f  
with respect to y

```
>> syms x
>> f=x^2+x+3;
>> y=int(f)
```

y =

```
(x*(2*x^2 + 3*x + 18))/6
```

```
>> expand(y)
```

ans =

```
x^3/3 + x^2/2 + 3*x
```

```
>> syms y
>> f=x^4+y^3;
>> int(f,y)
```

ans =

```
x^4*y + y^4/4
```

```
>> int(f,y,1,10)
```

ans =

```
9*x^4 + 9999/4
```

```
>> |
```

INDEFINITE  
INTEGRAL  
Integrate f with  
respect to y

DEFINITE  
INTEGRAL  
Integrate f  
with respect to  
y between 1  
and 10.

# EQUATION SOLVING & PLOTTING

**solve** is used to obtain the solution of system equations.

```
>> syms x x1 x2 x3
>> eq='x^2-6*x-7';
>> solve(eq)

ans =

-1
7

>> eq1='x1+2*x2+2*x3=0';
>> eq2='2*x1+3*x2+4*x3=1';
>> eq3='-x1+x2+x3=-6';
>> sol=solve(eq1,eq2,eq3);
>> sol.x1

ans =

4

>> sol.x2

ans =

-1

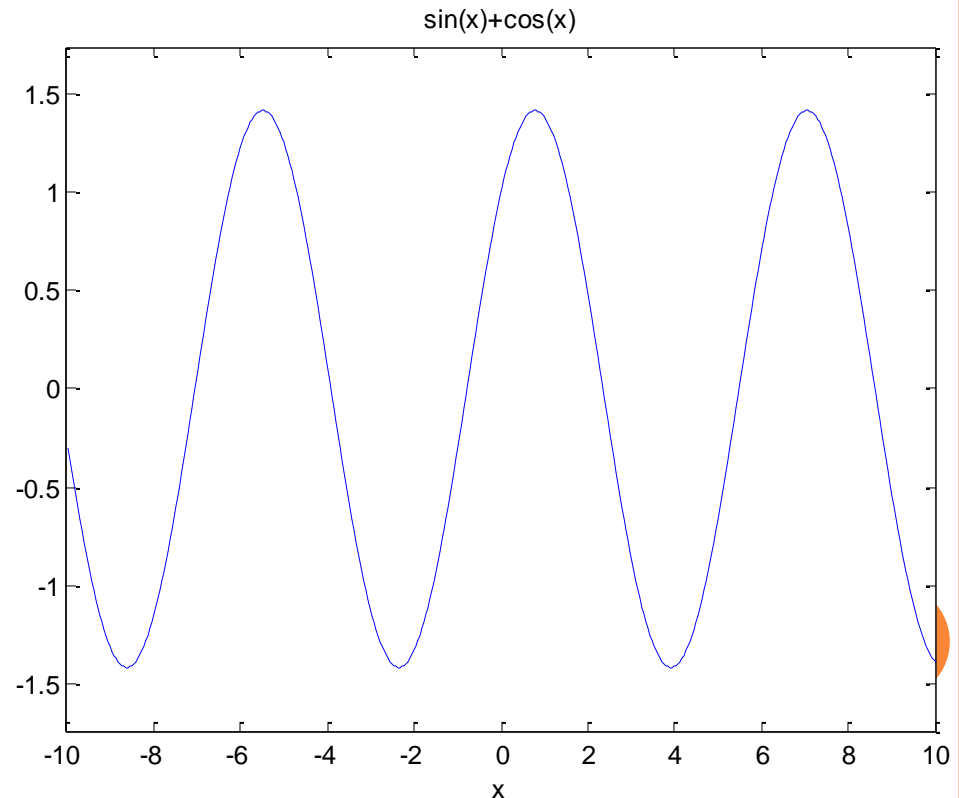
>> sol.x3

ans =

-1
```

**ezplot** is used to obtain simple plots of equations.

```
>> syms x
>> f='sin(x)+cos(x)';
>> ezplot(f, [-10,10]);
>>
```

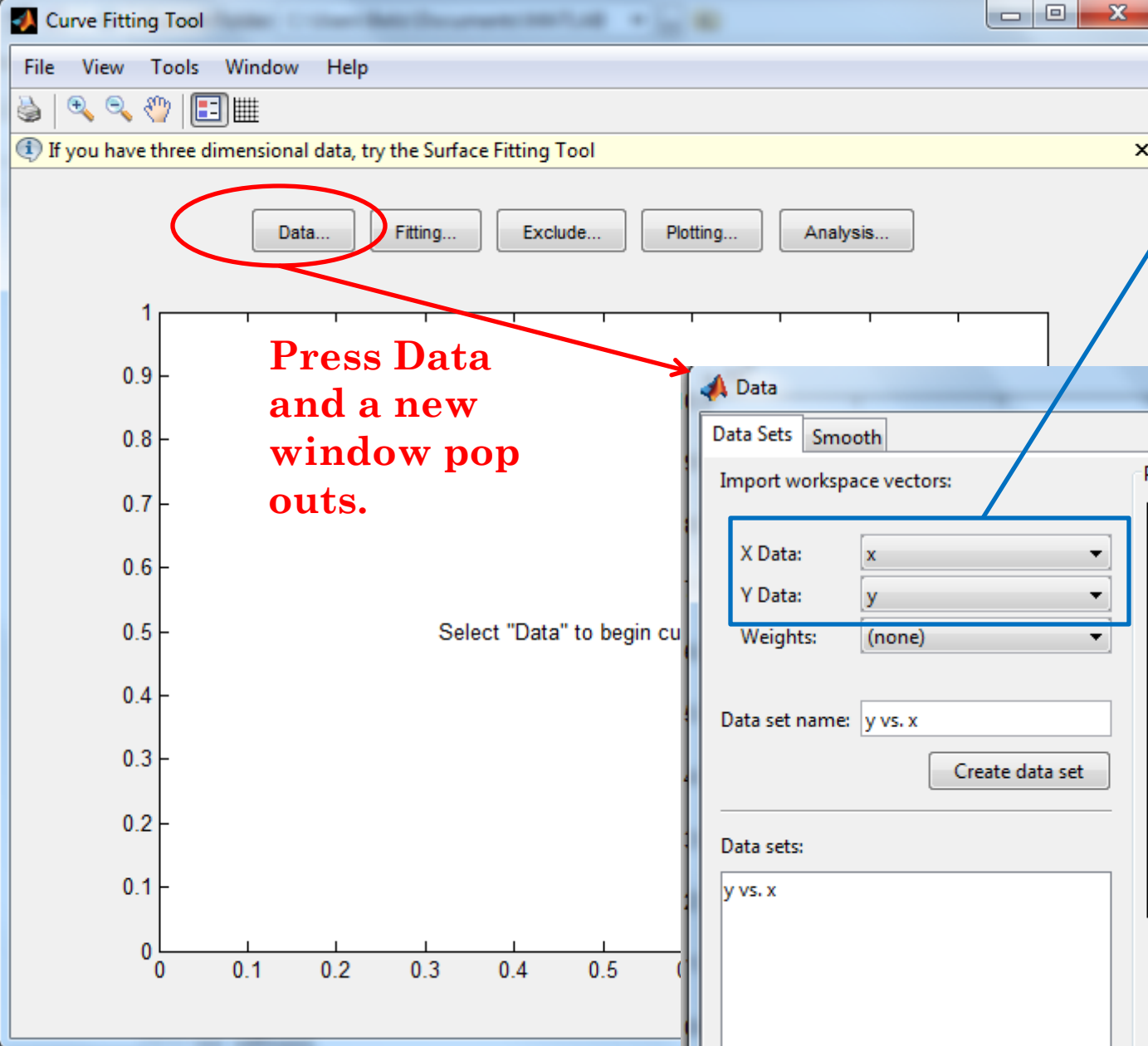




# CURVE FITTING TOOLBOX

- Fitting methods for linear least squares, nonlinear least squares, weighted least squares, constrained least squares, and robust fitting are available
- Data and fit statistics to assist you in analyzing your models
- In the command window, type:
  - **cftool** to open Curve Fitting Toolbox
  - **sftool** to open Surface Fitting Toolbox
- We will work on Curve Fitting Toolbox.





**Press Data  
and a new  
window pops  
out.**

**Select x and y  
variables on  
which a curve  
will be fitted and  
press create  
data set.**

Data

Data Sets Smooth

Import workspace vectors:

X Data: x

Y Data: y

Weights: (none)

Data set name: y vs. x

Create data set

Data sets:

y vs. x

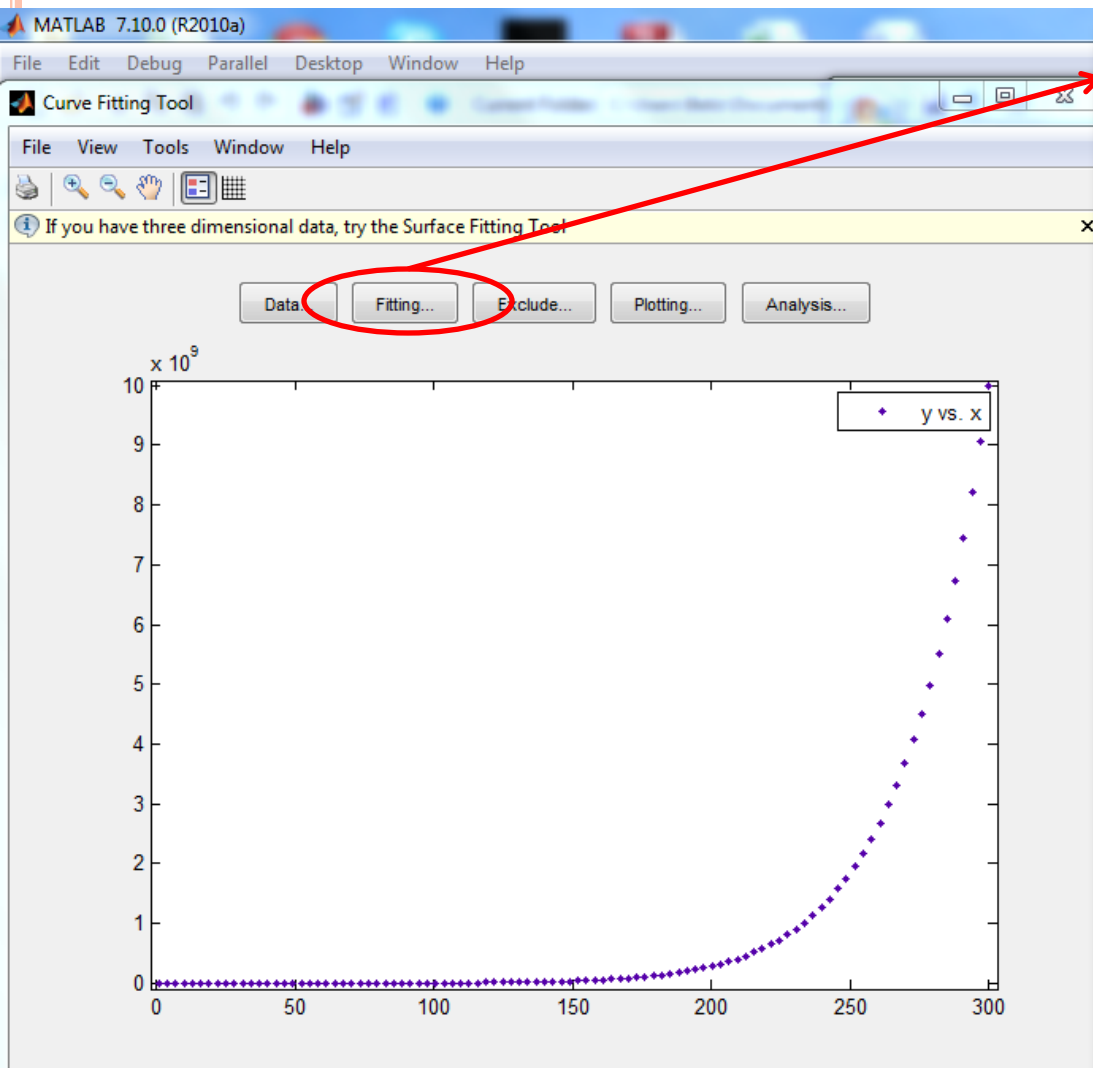
View Rename Delete

Preview

Close Help

After having created the data set, press  
Fitting button.

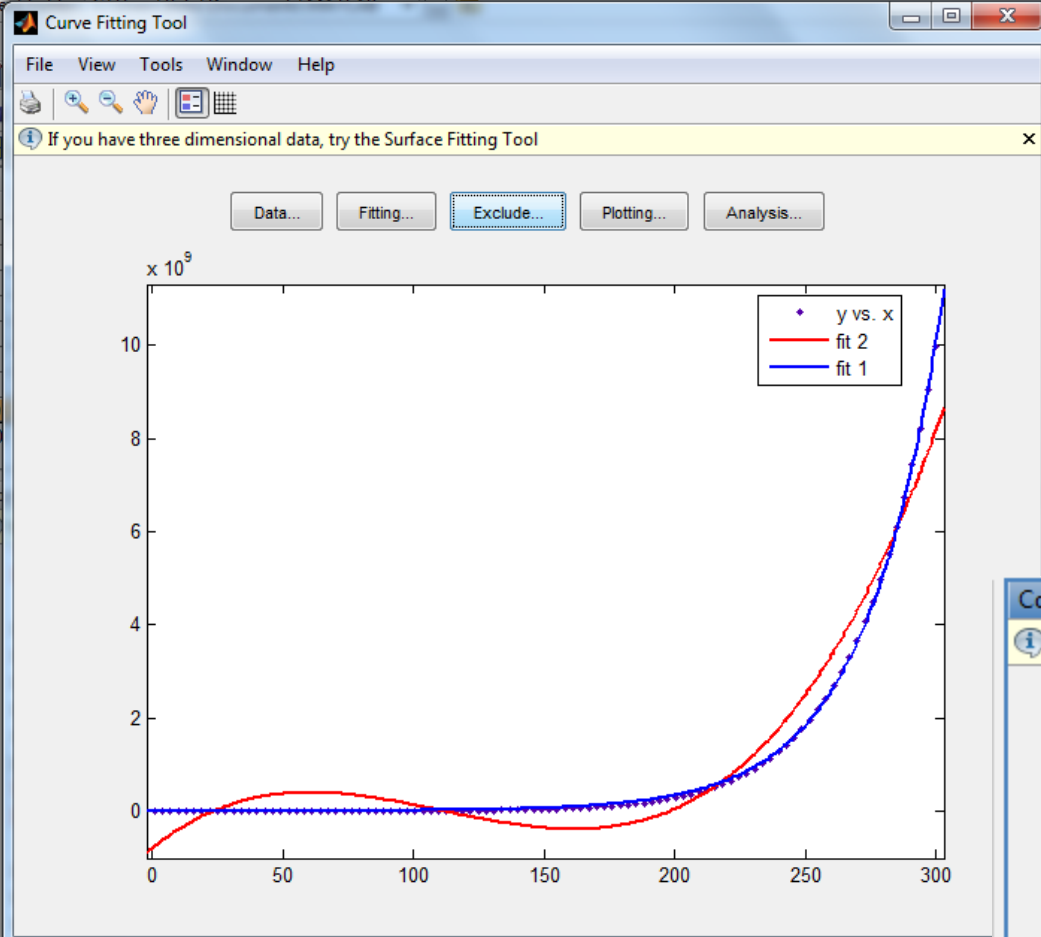
Select the  
type of fit.



The image shows the 'Fit Editor' dialog box. The 'Type of fit' dropdown menu is open, showing a list of fit types: Polynomial, Fourier, Gaussian, Interpolant, Polynomial (highlighted), Power, Rational, Smoothing Spline, and Sum of Sin Functions. A purple arrow points from the text 'Select the type of fit.' to the 'Polynomial' option. The 'Fit name' is 'fit 1' and the 'Data set' is 'y vs. x'. The 'Exclusion rule' is '(none)'. The 'Center and scale X data' checkbox is unchecked. The 'Fit options...' button is visible. The 'Results' section contains the text: 'Click "Apply" to save the changes to the fit.' The 'Table of Fits' section shows a table with columns: Fit name, Data set, Equation name, SSE, and R-... The table contains one row: fit 1, (none), (none), NaN, NaN. The 'Save to workspace...' button is highlighted with an orange circle, and an orange arrow points from the text 'You can save the details of the fitted curve to the workspace.' to it.

Fit name	Data set	Equation name	SSE	R-...
fit 1	(none)	(none)	NaN	NaN

You can save the details of the fitted  
curve to the workspace.



- In the curve fitting tool, you can visualize the fitted models with respect to the dataset.

- You can see the properties of the fitted plot from the command window.

```

Command Window
New to MATLAB? Watch this Video, see Demos, or read Getting Started.

>> fittedmodel1

fittedmodel1 =

General model Gauss1:
fittedmodel1(x) = a1*exp(-(x-b1)/c1)^2)
Coefficients (with 95% confidence bounds):
    a1 = 1.912e+032  (-2.389e+037, 2.389e+037)
    b1 = -4.296e+004  (-7.72e+007, 7.711e+007)
    c1 =          5153  (-4.617e+006, 4.627e+006)

>> fittedmodel2

fittedmodel2 =

General model Exp1:
fittedmodel2(x) = a*exp(b*x)
Coefficients (with 95% confidence bounds):
    a = 3.701e+005  (3.481e+005, 3.921e+005)
    b = 0.03405  (0.03384, 0.03426)
fx >>

```

# CURVE FITTING FROM THE COMMAND LINE

## ○ `options = fitoptions('Method',method)`

Method	The fitting method. A complete list of supported fitting methods is given below. The default is 'None'.	
	'NearestInterpolant'	Nearest neighbor interpolation
	'LinearInterpolant'	Linear interpolation
	'PchipInterpolant'	Piecewise cubic Hermite interpolation (curves only)
	'CubicSplineInterpolant'	Cubic spline interpolation
	'BiharmonicInterpolant'	Biharmonic surface interpolation
	'SmoothingSpline'	Smoothing spline
	'LowessFit'	Lowess smoothing (surfaces only)
	'LinearLeastSquares'	Linear least squares
	'NonlinearLeastSquares'	Nonlinear least squares

## ○ `ffun = fitype(libname)`

## ○ `ffun = fitype(expr)`



```
>> g = fitype('a*x^2+b*x+c','coeff',{'a','b','c'})
```

```
g =
```

```
General model:
```

```
g(a,b,c,x) = a*x^2+b*x+c
```

```
>> |
```

libname	Description
'poly1'	Linear polynomial curve
'poly11'	Linear polynomial surface
'poly2'	Quadratic polynomial curve
'linearinterp'	Piecewise linear interpolation
'cubicinterp'	Piecewise cubic interpolation
'smoothingspline'	Smoothing spline (curve)
'lowess'	Local linear regression (surface)

# CURVE FITTING FROM THE COMMAND LINE

- **[fitobject, gof] = fit(x,y,fitType)** fits the data in x and y with the library model, anonymous function or fittype object specified by fitType.
- It returns the goodness-of-fit statistics to the structure gof which are summarized in the below table.

Field	Value
sse	Sum of squares due to error
R2	Coefficient of determination
adjustedR2	Degree-of-freedom adjusted coefficient of determination
stdError	Root mean squared error (standard error)



# STATISTICS TOOLBOX

- Aim is to assess and understand data
- Functions for modeling data, analyzing historical trends, simulating systems, developing statistical algorithms.

## Key Features

- Data organization and management
- Descriptive statistics
- Statistical plotting and data visualization
- Probability distributions
- Analysis of variance (ANOVA)
- Linear and nonlinear modeling
- Multivariate statistics
- Design of Experiments (DOE)
- Hypothesis testing
- Statistical Process Control (SPC)



# MEASURE OF CENTRAL TENDENCY

Function Name	Description
<a href="#"><u>geomean</u></a>	Geometric mean
<a href="#"><u>harmmean</u></a>	Harmonic mean
<a href="#"><u>mean</u></a>	Arithmetic average
<a href="#"><u>median</u></a>	50th percentile
<a href="#"><u>mode</u></a>	Most frequent value
<a href="#"><u>trimmean</u></a>	Trimmed mean

## **Note that;**

**mean(x)** is the average of the data x

**median(x)** is the middle value of the data x sorted by value

**mode (x)** is the most common value in the dataset x





# STATISTICAL ANALYSIS

```
>> a=[1 2 3;1 3 4;2 2 5]
```

```
a =
```

1	2	3
1	3	4
2	2	5

```
>> mean(a)
```

```
ans =
```

1.3333	2.3333	4.0000
--------	--------	--------

```
>> median(a)
```

```
ans =
```

1	2	4
---	---	---

```
>> mode(a)
```

```
ans =
```

1	2	3
---	---	---



# MEASURES OF SCALE (MAXIMUM AND MINIMUM)

**max** (x): find the largest value in x

**[y,k]=max**(x): find y and k that are the maximum value of x, indices of first maximum.

**max**(x,y): compares x and y and report the minimum

**min**(x): find the smallest value in x

**[y,k]=min**(x): find y and k that are the minimum value of x, indices of first minimum.

**min**(x,y): compares x and y and report the minimum



# STATISTICAL ANALYSIS

```
>> a=[1 2 3;4 5 6;7 8 9];  
b=[7 8 9;1 2 3;4 5 6];
```

```
|>> max(a)
```

```
>> [y,k]=max(a)
```

```
>> min(a,b)
```

```
|>> max(1,5)
```



# MEASURES OF SCALE (SUM AND PRODUCT)

**sum** ( $x$ ): sum of elements

**prod** ( $x$ ): product of elements

**cumsum** ( $x$ ): cumulative sum of elements

**cumprod** ( $x$ ): cumulative product of the elements



# STATISTICAL ANALYSIS

```
>> A=[1 2 3;4 5 6;7 8 9];
```

```
>> sum(A)
```

```
ans =
```

```
12    15    18
```

```
>> prod(A)
```

```
ans =
```

```
28    80   162
```

```
>> cumsum(A)
```

```
ans =
```

```
1     2     3
5     7     9
12    15    18
```

```
>> cumprod(A)
```

```
ans =
```

```
1     2     3
4    10    18
28   80   162
```



# MEASURE OF DISPERSION

Function Name	Description
<a href="#"><u>iqr</u></a>	Interquartile range
<a href="#"><u>mad</u></a>	Mean absolute deviation
<a href="#"><u>moment</u></a>	Central moment of all orders
<a href="#"><u>range</u></a>	Range
<a href="#"><u>std</u></a>	Standard deviation
<a href="#"><u>var</u></a>	Variance

**Note that;**

*standard deviation* shows how much variation there is from the data average

*variance* shows how far a set of numbers are spread out from each other.



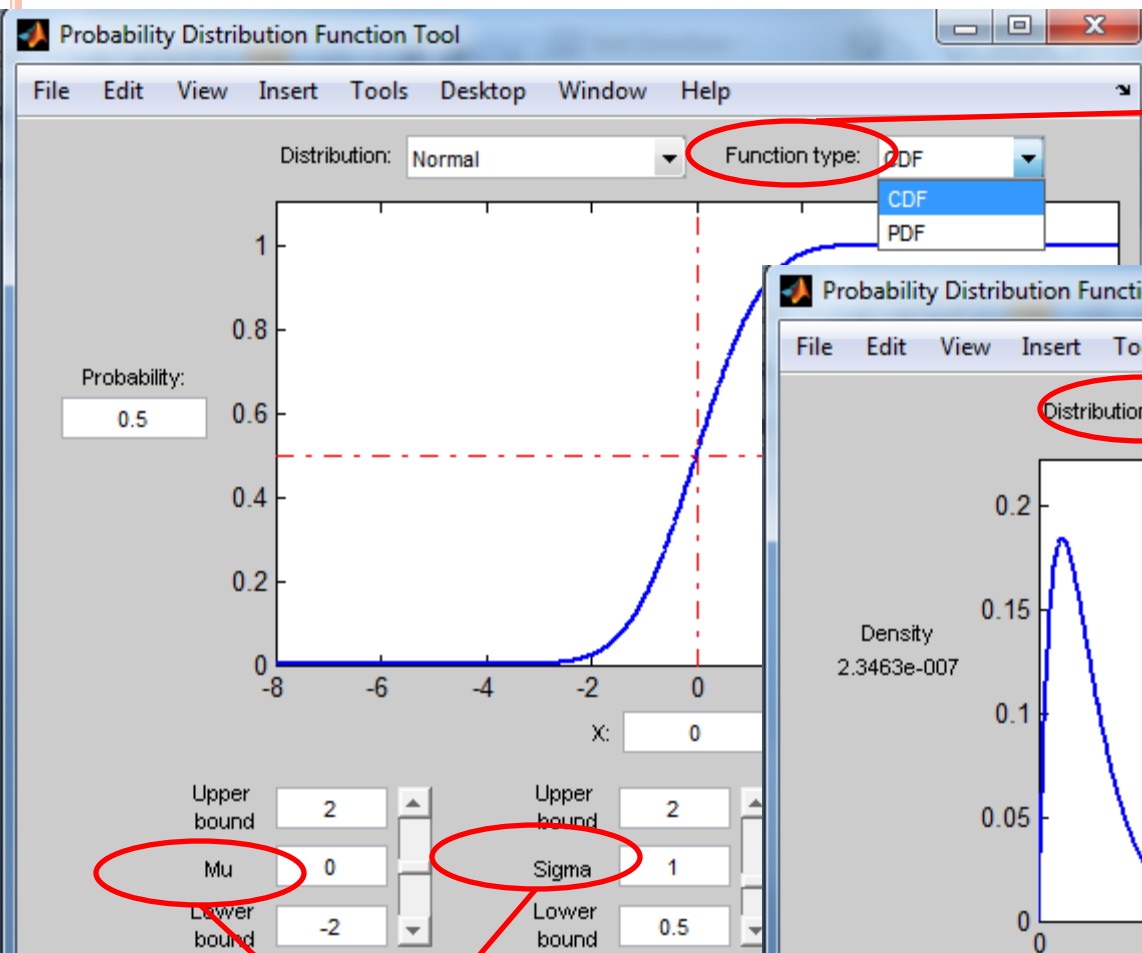
# RANDOM NUMBER GENERATION

- **randn([m n])** returns an  $m \times n$  matrix containing numbers that obey standard normal distribution
- **lognrnd(mu,sigma,m,n)** returns an  $m \times n$  matrix containing numbers that obey lognormal distribution that have  $\mu$  and  $\sigma$  as the mean and stdev of the corresponding normal dist.



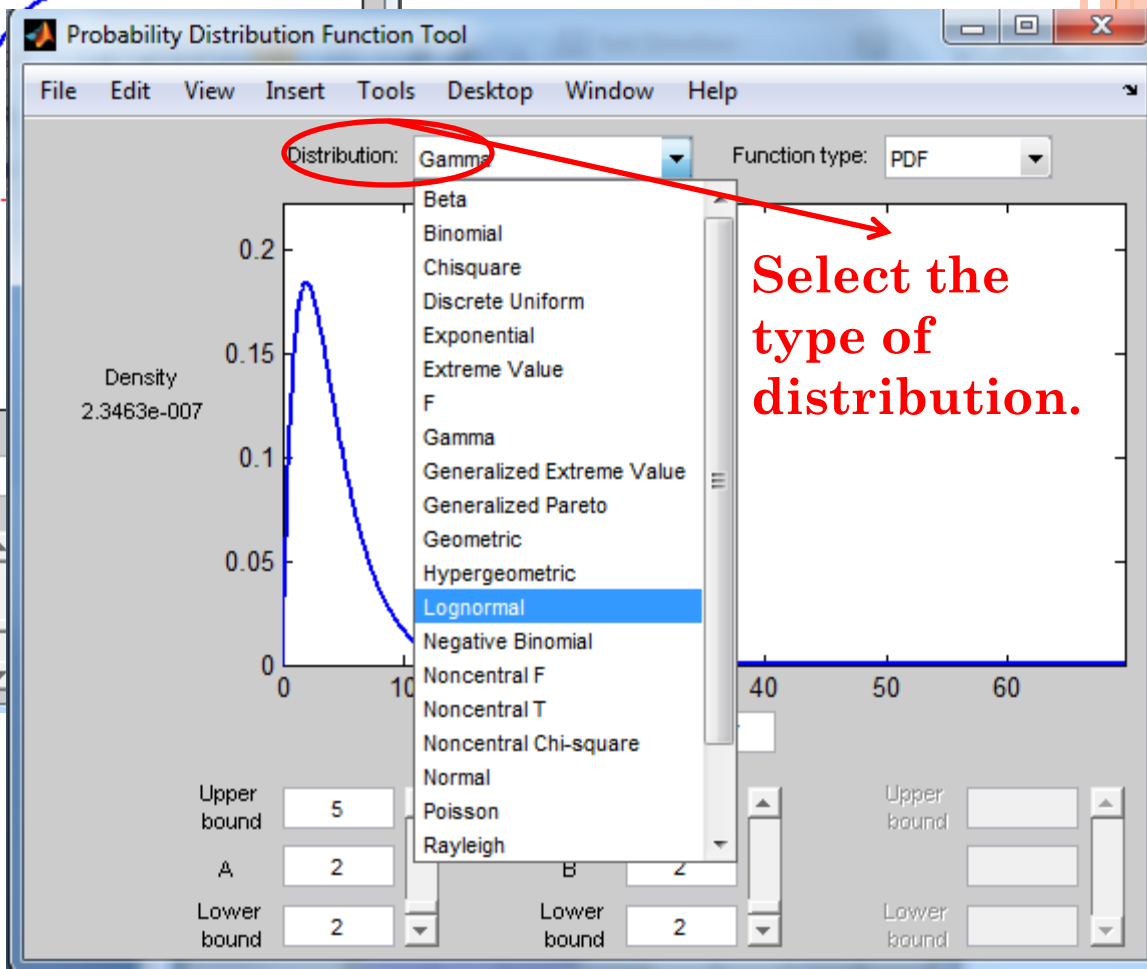
# PROBABILITY DISTRIBUTION

- Type **disttool** to the command window



$\mu$  and  $\sigma$ , which are the identifiers of a distribution are defined.

You can select the function type, either a PDF or a CDF.



Select the type of distribution.



# QUESTIONS??

