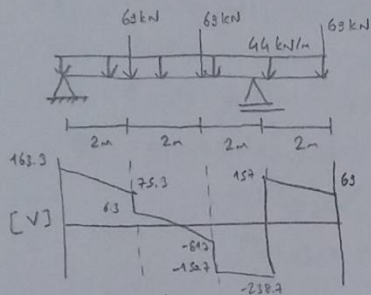


# CE382 - Reinforced Concrete Fundamentals

## Homework 5

1)



$$p = 1.4 \times 15 + 1.6 \times 30 = 69 \text{ kN}$$

$$q = 1.4 \times 20 + 1.6 \times 10 = 44 \text{ kN/m}$$

$$f_{cd} = 27 \text{ MPa}$$

$$f_{ctd} = 1.47 \text{ MPa}$$

$$f_{yd} = 365 \text{ MPa} = f_{ywd}$$

direct support

$$V_d = 163.3 - (44 \times (\frac{0.4}{2} + 0.46)) = 134.3 \text{ kN}$$

indirect support

$$V_d = 238.7 - (44 \times \frac{0.35}{2}) = 231 \text{ kN}$$

$$V_{max} = 0.22 \times 27 \times 350 \times 500 = 1039.5 \text{ kN}$$

$$V_d < V_{max} \quad \checkmark$$

$$V_{cr} = 0.65 \times 1.47 \times 350 \times 460 = 154 \text{ kN}$$

$$V_{cr} < V_d$$

$$\min \frac{A_{sw}}{s} = 0.3 \times \frac{1.82}{365} \times 350 = 0.52$$

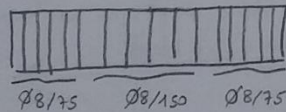
$$V_d = V_c + V_w$$

$$231 = 0.8 \times 154 + V_w$$

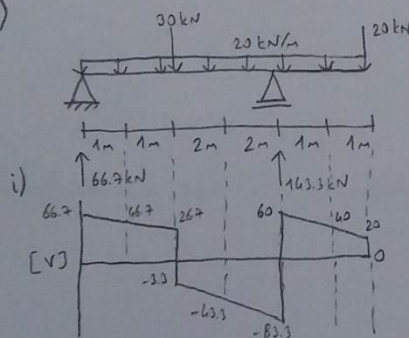
$$107.8 \times 10^3 = \frac{A_{sw}}{s} \times 365 \times 460 \quad \frac{A_{sw}}{s} = 0.64 > \min \frac{A_{sw}}{s}$$

$$\text{use } \phi 8 \quad A_s = 50 \text{ mm}^2 \quad A_{sw} = 2 \times 50 = 100 \text{ mm}^2$$

$$s = \frac{100}{0.64} = 156 \text{ mm} < \frac{d}{2} = 230 \text{ mm}$$



2)



ii)

$$\tau = \frac{VQ}{It}$$

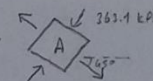
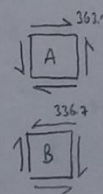
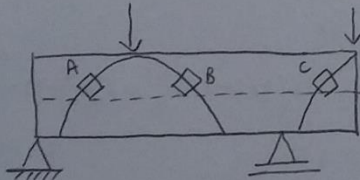
$$Q = 275 \times 350 \times \frac{275}{2} = 13.2 \times 10^6 \text{ mm}^3$$

$$I_x = \frac{1}{2} \times 350 \times 350^3 = 4.85 \times 10^9 \text{ mm}^4$$

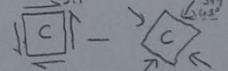
$$\tau_A = \frac{(46.7 \times 10^3) (13.2 \times 10^6)}{(4.85 \times 10^9) (0.35)} = 363.1 \text{ kPa}$$

$$\tau_B = \frac{(-43.3 \times 10^3) (13.2 \times 10^6)}{(4.85 \times 10^9) (0.35)} = -336.7 \text{ kPa}$$

iii)



$$\tau_c = 341 \text{ kPa}$$



3) Column  $350 \times 400 \text{ mm}$

$$f_{cd} = 17 \text{ MPa}$$

$$f_{ctd} = 1.2 \text{ MPa}$$

$$(U_p)_1 = 2 \times (350 + 240) + 2 \times (400 + 240) = 2460 \text{ mm}$$

$$(U_p)_2 = (350 + 240) + 2 \times (400 + 120 + 250) = 2130 \text{ mm}$$

$$V_{pc} = \gamma \cdot f_{ctd} \cdot U_p \cdot d = 1.0 \times 1.2 \times 2130 \times \frac{240}{1000} = 613.4 \text{ kN}$$

$$V_d = 1200 - 800 - 15 \times (0.77 \times 0.53) = 333.2 \text{ kN}$$

$$V_{pc} > V_d \quad \checkmark$$