



1. Write a MATLAB code for the following function, which takes an input, x and returns the result.

$$f(x) = \frac{1}{x} - 0.5$$

2. Write a MATLAB code that calculates n^{th} derivative of the $f(x)$, which takes two arguments: n and x .

3. Write a MATLAB code that uses Taylor series expansion to approximate $f(x)$ from $x_i=3$ with $h=0.5$. Calculate the value of the function at $x_{i+1}=3.5$ with relative true error less than 0.0005 where;

$$x_{i+1} = x_i + h$$

$$f(x_{i+1}) = f(x_i) + f'(x_i) \cdot h + \frac{f''(x_i)}{2!} \cdot h^2 + \frac{f'''(x_i)}{3!} \cdot h^3 + \dots + \frac{f^{(n)}(x_i)}{n!} \cdot h^n + R_n$$

$$\varepsilon_{RT} = \left| \frac{f_{\text{exact}} - f_{\text{approximate}}}{f_{\text{exact}}} \right| \leq 0.0005$$