

**RULES**

1. The answers of the exercises will be posted on our website at 17:00 PM on 04.01.2013: www2.ce.metu.edu.tr/~ce305 .
2. This is the **version 7.0**. In case there are any corrections for this exercise, we will post an updated version on our website. You can follow the changes in the exercises by the **Version History** section below.

Version History

V7.0 Exercise is released.

1. The following equation can be used to model the deflection of a sailboat mast subject to a wind force:

$$\frac{d^2 y}{dz^2} = \frac{f(z)}{2EI} (L - z)^2$$

where $f(z)$ is the wind force, E is the modulus of elasticity, L is mast length, and I is the moment of inertia. Note that the force varies with height according to:

$$f(z) = \frac{200z}{5+z} e^{-2z/30}$$

Calculate the deflection if $y = 0$ and $\frac{dy}{dz} = 0$ at $z = 0$ using Heun's (one-cyle, non-iterative) method along the length of mast.

Use a step size of 0.5 m, parameter values of $L=30$ m, $E=1.25 \cdot 10^8$ Pa and $I=0.05$ kg.m² for your computation.

Hints:

- You should use a system of ordinary differential equations approach.
- Do not make any changes in units.

2. Consider the boundary value problem;

$$\frac{d^2 x}{dt^2} + 3 \frac{dx}{dt} + 4x(t) = 0 \text{ with } x(0.5) = 3 \text{ and } x(2.5) = -2$$

Find $x(1.0)$, $x(1.5)$ and $x(2.0)$ using $O(h^2)$ finite difference formula. Note that $h=0.5$.