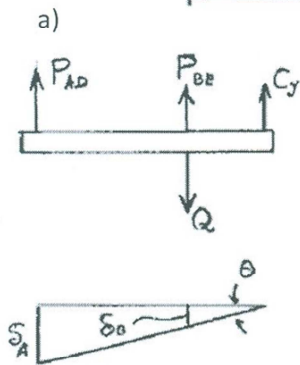


The rigid bar ABC is supported by two links, AD and BE, of uniform 37.5 mm x 6 mm rectangular cross section and made of mild steel with  $E = 200$  GPa. The magnitude of the force  $Q$  applied at B is 260 kN. Knowing that  $a = 0.64$  m, determine,

- The value of the normal stress in each link
- The deflection of point B



Statics:  $\sum M_C = 0 \quad 0.640(Q - P_{BE}) - 2.64 P_{AD} = 0$

Deformation:  $\delta_A = 2.64 \theta, \quad \delta_B = a\theta = 0.640 \theta$

Elastic Analysis:

$$A = (37.5)(6) = 225 \text{ mm}^2 = 225 \times 10^{-6} \text{ m}^2$$

$$P_{AD} = \frac{EA}{L_{AD}} \delta_A = \frac{(200 \times 10^9)(225 \times 10^{-6})}{1.7} \delta_A = 26.47 \times 10^6 \delta_A$$

$$= (26.47 \times 10^6)(2.64 \theta) = 69.88 \times 10^6 \theta$$

$$\sigma_{AD} = \frac{P_{AD}}{A} = 310.6 \times 10^7 \theta$$

$$P_{BE} = \frac{EA}{L_{BE}} \delta_B = \frac{(200 \times 10^9)(225 \times 10^{-6})}{1.0} \delta_B = 45 \times 10^6 \delta_B$$

$$= (45 \times 10^6)(0.640 \theta) = 28.80 \times 10^6 \theta$$

From Statics  $Q = P_{BE} + \frac{2.64}{0.640} P_{AD} = P_{BE} + 4.125 P_{AD}$

$$= [28.80 \times 10^6 + (4.125)(69.88 \times 10^6)] \theta = 317.06 \times 10^6 \theta$$

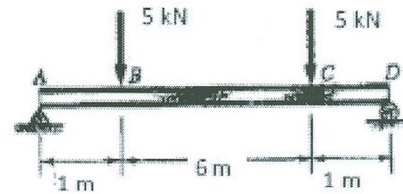
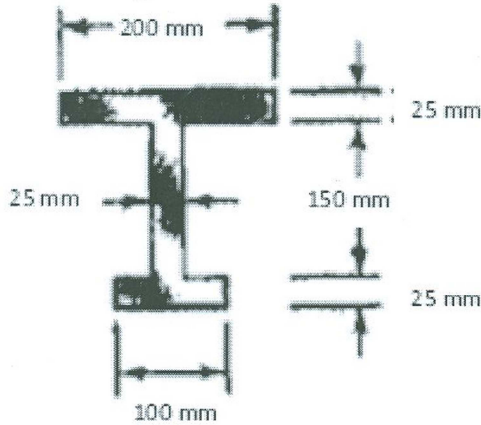
$$260000 \text{ N} = 317.06 \times 10^6 \theta \Rightarrow \theta = 820.03 \times 10^{-6}$$

$$P_{AD} = 69.88 \times 10^6 \theta = 57304 \text{ N} = 57.31 \text{ kN} \quad \sigma_{AD} = \frac{P_{AD}}{A_{AD}} = \frac{57304}{225} = 254.68 \text{ MPa}$$

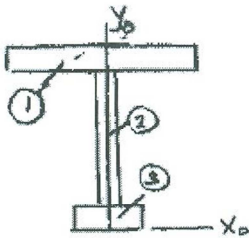
$$P_{BE} = 28.80 \times 10^6 \theta = 23617 \text{ N} = 23.617 \text{ kN} \quad \sigma_{BE} = \frac{P_{BE}}{A_{BE}} = \frac{23617}{225} = 104.96 \text{ MPa}$$

$$\text{b) } \delta_B = \frac{P_{BE} L_{BE}}{E A_{BE}} = \frac{23617 \times 1000}{200 \times 10^3 \times 225} = 0.542 \text{ mm}$$

2-



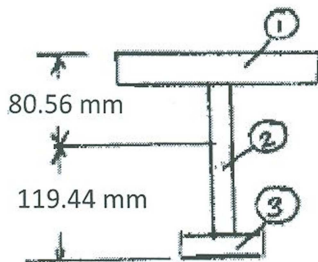
Two vertical forces are applied to a beam of the cross section shown above. Determine the maximum tensile and compressive stresses in portion BC of the beam.



	A	$\bar{y}_o$	$A\bar{y}_o$
①	5000	187.5	937500
②	3750	100	375000
③	2500	12.5	31250
$\Sigma$	11250		1343750

$$Y_o = 1343750 / 11250 = 119.44 \text{ mm}$$

Neutral axis lies 119.44 mm above the base



$$I_1 = \frac{1}{12} b_1 h_1^3 + A_1 (d_1)^2 = \frac{1}{12} \times (200) \times (25)^3 + 5000 \times (168.06)^2$$

$$= 23421234.67 \text{ mm}^4$$

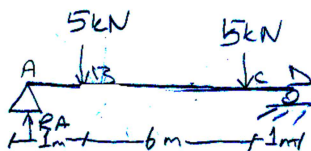
$$I_2 = \frac{1}{12} b_2 h_2^3 + A_2 (d_2)^2 = \frac{1}{12} \times (25) \times (150)^3 + 3750 \times (19.44)^2$$

$$= 8448426 \text{ mm}^4$$

$$I_3 = \frac{1}{12} b_3 h_3^3 + A_3 (d_3)^2 = \frac{1}{12} \times (100) \times (25)^3 + 2500 \times (106.94)^2$$

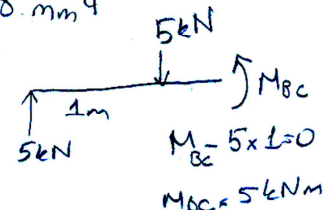
$$= 28720617.33 \text{ mm}^4$$

$$I = I_1 + I_2 + I_3 = 60590278 \text{ mm}^4$$



$$\sum M_D = 0 \quad 8R_A - 5 \times 7 - 5 \times 1 = 0$$

$$R_A = 5 \text{ kN}$$



$$M_{BC} = 5 \text{ kNm}$$

$$\Rightarrow (\sigma_{\max})_{\text{comp}} = \frac{M_{BC} y_{\text{top}}}{I} = \frac{-5 \times 10^6 \times 80.56}{60590278} = -6.85 \text{ MPa}$$

$$(\sigma_{\max})_{\text{tens}} = \frac{M_{BC} y_{\text{bot}}}{I} = \frac{-5 \times 10^6 \times (-119.44)}{60590278} = 9.86 \text{ MPa}$$