# Middle East Technical University Department of Mechanical Engineering

## ME 310 – Numerical Methods Fall 2014

## Study Problems - 3\*

Assigned on 27.11.2014
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\*Will not be collected/graded.

1. Employ the following methods to find the maximum of the function given as,

$$f(x) = -x^4 - 2x^3 - 8x^2 - 5x + 48$$

- a) Parabolic Interpolation with  $x_0 = -2$ ,  $x_1 = -1$ ,  $x_2 = 1$  and 4 iterations. Employ new point selection sequence as in the secant method.
- b) Newton's method with initial guess of  $x_0 = -1$  and  $\varepsilon_s = 1\%$

#### [Adapted from Applied Numerical Methods for Engineers, Steven Chapra]

- 2. Use least-squares regression to fit
  - a) a straight line
  - b) a power equation
  - c) a saturation-growth-rate equation
  - d) a parabola

To the given data below and decide whether any one of the curve fits is superior to others. Justify your reasoning.

| X | 5  | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
|---|----|----|----|----|----|----|----|----|----|----|
| у | 17 | 24 | 31 | 33 | 37 | 37 | 40 | 40 | 42 | 41 |

### [Adapted from Applied Numerical Methods for Engineers, Steven Chapra]

#### 3. Given the data

| х    | 1.6 | 2 | 2.5 | 3.2 | 4 | 4.5 |
|------|-----|---|-----|-----|---|-----|
| f(x) | 2   | 8 | 14  | 15  | 8 | 2   |

Calculate f(2.8) using Newton's interpolating polynomials of order 1 through 3. Compute the finite divided differences as in Fig. 18.5 of the textbook.

[Adapted from Applied Numerical Methods for Engineers, Steven Chapra]