



For RSA algorithm, we need to generate a public and a private key.

1. Choosing two distinct prime numbers: $p = 6733$, $q = 6073$
2. Computing $n = p \times q = 6733 \times 6073 = 40889509$
3. Computing least common multiple of $(p-1)$ and $(q-1)$: $\text{lcm}(6732, 6072) = 309672$
4. Selecting any number that ensure $1 < e < 123200$ and coprime to 309672 . Then let $e = 7$.
5. Computing d , the modular multiplicative inverse of $e \pmod{\text{lcm}(p-1, q-1)}$. Then $d = 44239$.
6. Now, public key = $\{e, n\} = \{7, 40889509\}$ and private key = $\{d, n\} = \{44239, 40889509\}$
7. For encrypting the message, we can pick the public key. " $message^e \pmod{n}$ " will return us the cipher text.
8. For decrypting the message, we should pick the private key. " $message^d \pmod{n}$ " will return us the plain text.
9. Our hash function returns a hexadecimal value. We need to convert it into decimals so we can do the calculations. Decimal value of "b9a2" is "47522".
10. $47522^7 \pmod{40889509} = 15279871$
11. $434054^{136889} \pmod{2469981} = 47522$
12. This is how RSA algorithm works.

SAMPLE RUN 1)

ID: 29438745367

Prime numbers for source keys: (5501, 4481)

Source public key: {9;24649981}

Source private key: {136889;24649981}

Prime numbers for destination keys: (6733, 6073)

Destination public key: {7;40889509}

Destination private key: {44239;40889509}

```
-----  
Original ID: 29438745367  
-----
```

```
Source Public Key: {9;24649981}
```

```
Source Private Key: {136889;24649981}
```

```
Destination Public Key: {7;40889509}
```

```
Destination Private Key: {44239;40889509}  
-----
```

```
Session Key: 4480919969
```

```
Returned Session Key: 4480919969  
-----
```

```
Original Hashed ID (CRC-16/MODBUS): 0xb9a2
```

```
Computed Hash: 0xb9a2  
-----
```

```
Verified  
-----
```

SAMPLE RUN 2)

ID: 74543222905

Prime numbers for source keys: (5501, 4481)

Source public key: {9;24649981}

Source private key: {136889;24649981}

Prime numbers for destination keys: (6733, 6073)

Destination public key: {7;40889509}

Destination private key: {44239;40889509}

```
-----  
Original ID: 74543222905  
-----
```

```
Source Public Key: {9;24649981}
```

```
Source Private Key: {136889;24649981}
```

```
Destination Public Key: {7;40889509}
```

```
Destination Private Key: {44239;40889509}  
-----
```

```
Session Key: 2376444027
```

```
Returned Session Key: 2376444027  
-----
```

```
Original Hashed ID (CRC-16/MODBUS): 0x7bff
```

```
Computed Hash: 0x7bff  
-----
```

```
Verified  
-----
```

For the first 2 samples, e value in RSA algorithm is set to 7.

For the next 2 run samples, we decreased the value of e in RSA algorithm to 3, for making it run faster.

SAMPLE RUN 3)

ID: 29438745367

Prime numbers for source keys: (4507, 3491)

Source public key: {7;15733937}

Source private key: {2246563;15733937}

Prime numbers for destination keys: (5737, 5077)

Destination public key: {5;29126749}

Destination private key: {1455797;29126749}

```
-----  
Original ID: 29438745367  
-----  
Source Public Key: {7;15733937}  
Source Private Key: {2246563;15733937}  
Destination Public Key: {5;29126749}  
Destination Private Key: {1455797;29126749}  
-----  
Session Key: 3126343501  
Returned Session Key: 3126343501  
-----  
Original Hashed ID (CRC-16/MODBUS): 0xb9a2  
Computed Hash: 0xb9a2  
-----  
Verified  
-----
```

SAMPLE RUN 4)

ID: 74543222905

Prime numbers for source keys: (4507, 3491)

Source public key: {7;15733937}

Source private key: {2246563;15733937}

Prime numbers for destination keys: (5737, 5077)

Destination public key: {5;29126749}

Destination private key: {1455797;29126749}

```
-----  
Original ID: 74543222905  
-----  
Source Public Key: {7;15733937}  
Source Private Key: {2246563;15733937}  
Destination Public Key: {5;29126749}  
Destination Private Key: {1455797;29126749}  
-----  
Session Key: 2408629342  
Returned Session Key: 2408629342  
-----  
Original Hashed ID (CRC-16/MODBUS): 0x7bff  
Computed Hash: 0x7bff  
-----  
Verified  
-----
```